Combinatory Categorial Grammar

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Simple vs. complex category



loday's lecture:	Catego	orial Gramm	ıar	
	John np	$\frac{likes}{(s\backslash np)/np} \\ \frac{s\backslash np}{s}$	Mary np > <	

Discussion



Categorial Grammar: Overview

Complex category

In a CG, all constituents—and in particular the lexical elements are associated with a very specific *category* which define their syntactic behaviour.

Simple phrase-structure rules

A set of universal rules defines how words and other constituents can be combined according to their categories.

Syntax vs. Semantics

Syntactic and semantic descriptions are tightly connected \rightarrow CG is popular amongst logicians and semanticists.

Outline

Ideas of Categorial Grammar

Category Rule Schemata Semantics

Non-local Dependency Constructions

Combinatory Categorial Grammar

Categories

Definition

The set of syntactic categories \mathcal{C} is defined recursively:

- ► Atomic categories: the grammar for each language is assumed to define a finite set of atomic categories, usually s, np, n, pp, ... ∈ C
- Complex categories: if X and Y $\in C$, then X/Y, X\Y $\in C$

Complex categories X/Y or $X\backslash Y$ are functors

- X: a result
- Y: an argument
- /: arguments to the right of the functor
- \blacktriangleright \: arguments to the left of the functor

Complex categories encode subcategorisation	information
intransitive verb: s\np	⊳ walked
transitive verb: (s\np)/np	\triangleright respected
ditransitive verb: ((s\np)/np)/np	⊳ gave

(s np)/np

- ▶ the verb takes a noun phrase to its right, and
- ► another noun phrase to its left to form a sentence.

There is no explicit difference made between phrases and words: An intransitive verb is described in the same way as a verb phrase with an object: s\np.

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Modification

In CG, adjuncts have the following general form: X \X or X/X.

Example

- ► PP nominal: (np\np)/np
- PP verbal: ((s np) (s np))/np

Lexicalization (1)

Lexicalization

In a lexicalized grammar, each element of the grammar contains at least one lexical item (terminal).

• G1: S
$$\rightarrow$$
 SS, S \rightarrow a

► G2: S →
$$a$$
S, S → a

Grammar or Lexicon

In a CG,

- the lexicon specifies the categories that the words of a language can take;
- lexical entries do most of the grammatical work of mapping the strings of the language to their interpretations.

Lexicalization (2)

The Principle of Lexical Head Government

Both bounded and unbounded syntactic dependencies are specified by the lexical syntactic type of their head.

Example

- (1) a. John \vdash np
 - b. *shares* ⊢ np
 - c. $buys \vdash (s \mid np)/np$
 - d. $sleeps \vdash s \setminus np$
 - e. well $\vdash (s \mid np)/(s \mid np)$ s \mid np-like thing.

⊳ *John* is a noun phrase.

- ▷ *shares* is a noun phrase.
- ▷ *buy* is a transitive verb.
- ▷ *sleeps* is an intransitive verb.

> well can modify a

Lexicalization (3)

The Principle of Head Categorial Uniqueness

A single nondisjunctive lexical category for the head of a given construction specifies both the bounded dependencies that arise when its complements are in canonical position and the unbounded dependencies that arise when those complements are displaced under relativization, coordination, and the like.

$\textit{admire} \vdash (s \backslash np) / np$

- (2) a. John admires Mary.
 - b. the man that I believe that John admires.
 - c. I believe that John admires and you believe that he dislikes, the woman in the skinny skirt.

AB categorial grammar (1)

Variants of categorial grammar differ in the rules they allow.

- The system defined by Ajdukiewicz (1935) and Bar-Hillel (1953) forms the basis for all variants of categorial grammar.
- In AB categorial grammar, categories can only combine through function application.

$\begin{array}{c|c} \hline \textbf{Forward application} \\ \hline X/Y & Y & \Rightarrow & X & (>) \end{array} \\ \hline \hline \textbf{Backward application} \\ \hline Y & X \backslash Y & \Rightarrow & X & (<) \end{array}$

AB categorial grammar (2)

Deriving a string

- A string α is grammatical if each word in the string can be assigned a category (as defined by the lexicon) so that the lexical categories of the words in α can be combined (according to the grammar rules) to form a constituent.
- The process of combining constituents in this manner is called a derivation.

Example



Adjuncts

Modification

In CG, adjuncts have the following general form: $X \setminus X$ or X/X.



Not all $X \setminus X$ nor X/X are modifiers.

More examples

$$\frac{\frac{\Re}{\mathsf{np}}}{\underbrace{\frac{\mathsf{s}\backslash\mathsf{np}}{\mathsf{s}\backslash\mathsf{np}}}_{\mathsf{s}\backslash\mathsf{np}}} \frac{\frac{1}{\mathsf{s}\backslash\mathsf{np}}}{\underbrace{\frac{\mathsf{s}\backslash\mathsf{np}}{\mathsf{s}\backslash\mathsf{np}}}} \\ \frac{\mathsf{s}\backslash\mathsf{np}}{\mathsf{s}} < \mathsf{s}$$



Lexicalization (4)

L. Bloomfield, Language

The lexicon is really an appendix of the grammar, a list of basic irregularities. This is all the more evident if meanings are taken into consideration, since the meaning of each morpheme belongs to it by an arbitrary tradition.

CG's view

- If this is the case, nothing in the lexicon is predictable, hence we do not need a theory of the lexicon.
- CG argues that this dichotomy gets in the way of our understanding of how syntax can shape possible lexicons.
 - * Any combinatory difference must be lexically specifiable.



$$\mathbf{buy} \vdash (\mathbf{s} \backslash \mathbf{np_1}) / \mathbf{np_2} : \mathbf{buy} \rightarrow_A \mathbf{np_1} \land \mathbf{buy} \rightarrow_P \mathbf{np_2}$$

- ► Syntactic category: (s\np)/np
- Semantic type (intuitive idea): the np indexed with "2" is the Patient of *buy*; the np indexed with "1" is the Agent of *buy*.

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Using a dependency interpretation					
John buys shares					
np	$(s np_1)/np_2$	np			
	s\np ₁	>			
	S	<			

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Using a dependency interpretation					
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np : john	$\overline{(s\backslashnp_1)/np_2:buy\to_Anp_1\wedgebuy\to_Pnp_2}$	np : shares			
	s\np ₁	>			
	S	<			

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		$s \in Np_1 : buy \to_A np_1 \land buy \to_P sh$	ares			
		S	<			

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	$s: buy \to_A john \land buy \to_P shares$	<			

The principle of type transparency

The principle of Categorial Type Transparency

For a given language, the semantic type of the interpretation together with a number of language-specific directional parameter settings uniquely determines the syntactic category of a category.

The inverse of Type Transparency

For any category, the semantic type is a function of the syntactic type.

The Principle of Combinatory Type Transparency

All syntactic combinatory rules are type-transparent versions of one of a small number simple semantic operations over functions.

CG vs. CFG

- CGs put into the lexicon most of the information that is captured in CFG rules.
- In CGs, all constituents and lexical elements are associated with a syntactic "category."
- In CGs, syntactic information is tightly related to semantic information.

Exam	ple		
S	\rightarrow	NP VP	
VP	\rightarrow	TV NP	
ΤV	\rightarrow	married finds	
marrie	married := $(s np)/np$.		

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Combinatory Categorial Grammar

Local dependencies

A head generally realizes its dependents locally within its head domain

- Arguments:
 - Verbs take arguments: subject, object, complements, ...
 - Heads subcategorize for their arguments
- Adjuncts/Modifiers:
 - adjectives modify nouns,
 - adverbs modify VPs or adjectives,
 - PPs modify NPs or VPs
 - Heads do not subcategorize for their modifiers

These are all local dependencies that can typically be expressed in a CFG.

Center embedding



$\mathsf{VP}{\Rightarrow}\mathsf{V} ~\mathsf{NP} ~\mathsf{NP}$

- (3) a. 我给了那个人一本书
 - b. 我给了站在那儿的那个人一本书
 - c. 我给了站在那儿正在扫二维码的那个人一本书
 - d. 我给了站在那儿正在扫微信二维码买水喝的那个人一本书

Center embedding

常州市发展和改革委员会文件 常发改 [2017] 41 号 市发展改革委关于转发省发展改革委关于转发 国家发展改革委办公厅关于对真抓实干成效 明显地方加大中央预算内投资激励 支持力度的通知的通知的通知

Long-distance dependencies



The distance from the position of the "dislocated" phrase to its "natural home" can be quite far.

wh-question

(4) a. Who do you think _ writes well about human sadness?b. Who do you think the cops are going to believe _?

Long-distance dependencies

Non-local

A syntactic theory needs a mechanism for expressing these *non-local/long-distance/long-range* dependencies.

- How can the non-local relation between a head and such argument be licensed?
- How can their properties be captured?

In Transformational Grammar

Non-local dependencies are analyzed as results of movement.

Wh-movement

Move a wh-phrase to the specifier of CP to check a [+WH] feature in C.

Long-distance dependencies

Long-distance dependencies

Bounded long-distance dependencies:

- Locally mediated dependencies
- Limited distance between the head and argument

Unbounded long-distance dependencies:

Arbitrary distance (within the same sentence)

Bounded dependencies

Raising

(5) He seems to sleep in class.

(Subject/Object) Control

- (6) a. He wants to sleep in class.
 - b. He promises her not to sleep in class.
 - c. She persuades him not to sleep in class.

DP movement



DP movement



No transformation in CG derivation



Control					
She	persuades	him	not to sleep in class		
np	$\overline{((s\backslash np)/(s\backslash np_i))/np_i}$	npj	s∖np _k		
	$(s np)/(s np_i) : i =$	—> =j			
	s\np : slee	$p' \to_A$	him(j=k)		
	S				

Unbounded dependency constructions (UDC)



- (7) a. Who do you think Bob saw?
 - b. Who do you think Bob said he saw?
 - c. Who do you think Bob said he imagined that he saw?

Topicalization

(8) That guy, [I believe Peter told me you thought] you like.

Clefts

(9) It's that guy that I believe Peter told me you thought] you like

Wh-movement



Coordination

Right-node raising

(10) [[she would have bought] and [he might sell]] shares.

Argument-cluster coordination

(11) I give [[you an apple] and [him a pear]].

Gapping

(12) [She likes sushi], and [he sashimi].

Outline

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Combinatory Categorial Grammar: Overview

Extending AB Grammar

- CCG extends AB categorial grammar by a set of rule schemata based on the combinators of combinatory logic.
- CCG facilitates the recovery of the non-local dependencies
 - Syntactically, they allow analyses of extraction and coordinate constructions which use the same lexical categories for the heads of such constructions as in the *canonical case*.
 - Semantically, they guarantee that non-local dependencies fill the same argument slots as local dependencies.
- The weak generative power of AB Grammar and CFG are is equivalent.
- Extra combinatory rules increase the weak generative power to mildly context-sensitivity.

Mark Steedman



- Surface Structure and Interpretation
- The Syntactic Process

Coordination

Simplified coordination rule	9
------------------------------	---

X CONJ
$$X^* \Rightarrow X^*$$

 X, X* and X* are categories of the same type but different interpretations.

Exam	ple				
	Anna	met	and	married	Manny
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n$	<Φ>	<u>_</u>
		s ₈ \np ₉			>
		<			

Semantics

Coordination

Simplified	coordination	rule
------------	--------------	------

X CONJ
$$X^* \Rightarrow X^*$$

- (Φ)
- X, X* and X* are categories of the same type but different interpretations.

Exam	ple				
	Anna	met	and	married	Manny
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n_1$	<Φ>	~
			>		
			<		

$\frac{\text{Semantics}}{\text{np}_0 = \text{anna', np}_7 = \text{manny'}}$

Coordination

Simplified coordination rule	9
------------------------------	---

X CONJ
$$X^* \Rightarrow X^*$$

Exampl	le				
A	nna	met	and	married	Manny
n	p ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n$	<Φ>	
			>		
			<		

Semantics

 meet'
$$\rightarrow_A$$
 np₂, meet' \rightarrow_P np₃,

Coordination

Simplified coordination rule	9
------------------------------	---

X CONJ
$$X^* \Rightarrow X^*$$

Exam	ple				
	Anna	met	and	married	Manny
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n_1$	p ₁₀	~
			>		
			S 8		<

Semantics
marry'
$$\rightarrow_A np_5$$
, marry' $\rightarrow_P np_6$,

Coordination

Simplified	coordination	rule
------------	--------------	------

X CONJ
$$X^* \Rightarrow X^*$$

Exam	ple				
	Anna	met	and	married	Manny
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n$	<Ψ>	~
			>		
			S 8		<

Semantics

$$s_8 = s_1 = s_4, np_9 = np_2 = np_5, np_{10} = np_3 = np_6$$

Coordination

Simplified coordination rule	9
------------------------------	---

X CONJ
$$X^* \Rightarrow X^*$$

Exam	ple				
	Anna	met	and	married	Manny
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇
		(s ₈	$np_9)/n$	<Φ>	<u>_</u>
			>		
			S ₈		<

$$\frac{\text{Semantics}}{np_{10} = np_{7},}$$

Coordination

Simplified c	oordination rule	è
--------------	------------------	---

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Example							
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np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇			
	(s ₈	$np_9)/n$	<Φ>	<u>_</u>			
		>					
		S8					

$$\frac{\text{Semantics}}{np_0 = np_9,}$$

Coordination

Simplified c	oordination rule	è
--------------	------------------	---

X CONJ
$$X^* \Rightarrow X^*$$

Exam	ple							
	Anna	met	and	married	Manny			
	np ₀	$\overline{(s_1 \backslash np_2)/np_3}$	CONJ	$\overline{(s_4 \setminus np_5)/np_6}$	np ₇			
		(s ₈	$np_9)/n$	<Φ>	<u>_</u>			
		s ₈ \np ₉						
			S ₈		<			

Composition

Forward composition

		V /7			(> D)		
X/Y Y/	$\Sigma \Rightarrow_B$	X/Z			(>B)		
Example	(Abbreviat	ion: vp:	s\np)				
Anna np	$\frac{\textit{met}}{(s\backslash np)/np}$	and CONJ	$\frac{\textit{might}}{(s \setminus np) / vp}$	$\frac{marry}{\sqrt{p/np}} > B$	Manny np		
		(s\np	o)/np	<u>-</u> <Ф>	>		
Semantic	s:		S		<		
 <i>marry</i> ⊢ (s\np₁)/np₂ : s = marry' ∧ marry' →_A np₁ ∧ marry' →_P np₂ <i>might</i> ⊢ (s₁\np₁)/(s₂\np) : may' →_A np₁ ∧ may' →_M s₂ 							

Composition

Generalized forward composition

X/Y	$(Y/Z)/\$_1$	$\Rightarrow_{\mathbf{B}^n}$	$(X/Z)/\$_1$	$(>\mathbf{B}^n)$
-----	--------------	------------------------------	--------------	-------------------



Type raising



Forward composition and type-raising



Maximally incremental left-to-right processing



Backward composition and type-raising

Backward composition					
$Y \backslash Z$	$X \backslash Y$	\Rightarrow_{B}	$X \backslash Z$	(< B)	

Backw	/ard	type	raising				
X ⇒	\mathbf{T}^{*}	$T \setminus (T$	/X)				(< T)
$T \setminus (T /$	X) is	a pai	rametrically	licensed	category	for t	he language.

Argument cluster (tv: vp/np, dtv: (vp/np)/np))								
$\frac{give}{dtv}$	$\frac{John}{\frac{tv\backslashdtv}{vp\backslashtv}} \xrightarrow[]{vp\backslashtv}{vp\backslashtv} \overset{an apple}{\underset{vp\backslashdtv}{sp}} \\ \overset{an apple}{\underset{vp\backslashdtv}{sp}} $	and CONJ	$\frac{Mary}{tv \setminus dtv} \stackrel{a flower}{=} \sqrt[]{T}{vp \setminus tv} \\ \hline \\ \hline \\ vp \setminus dtv \\ \hline \\ \hline \\ \hline \\ \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $					
		$vp \backslash dtv$	<Ψ>					
		vp						

Backward crossed substitution



Exa	mple				
	$\frac{which}{(n\backslash n)/(s/np)}$	<i>I will</i> s∕vp	file vp/np	$\frac{without}{\frac{(vp \setminus vp)/vping}{(vp \setminus vp)/}}$	reading vping/np /np
				vp/np	ND X
				s/np	>D
			n\r	1	>

Crossing composition

Forward crossing composition					
$X/Y Y \setminus Z \Rightarrow_{\mathbf{B}} X \setminus Z$					

Backward crossing composition						
Y/Z	$X \setminus Y$	\Rightarrow_{B}	X/Z			

Cross-serial dependency construction								
dat	$\frac{ik}{np_1}$	Cecilia np ₂	de nijlpaarden np ₃	$\frac{zag}{\frac{((s \ np_1) \ np_2) / vp}{((s \ np_1) \ np_2) '}}$	$\frac{voeren}{vp \setminus np_3} \rightarrow B_{\times} \\ 1 \rightarrow 0$			
			(s\np ₁)\np ₂ s\np ₁					
			S		<			

Constraints on combinatory rules

The Principle of Adjacency

Combinatory rules may only apply to finitely many phonologically realized and string-adjacent entities.

The Principle of Consistency

All syntactic combinatory rules must be consistent with the directionality of the principal function.

Principal function: the function among the input functions which determines the range of the result.

Example

$$\blacktriangleright$$
 X\Y
 Y
 \Rightarrow
 X

Constraints on combinatory rules

The Principle of Inheritance

If a category that results from the application of a combinatory rule is a function category, then the slash defining directionality for a given argument in that category will be the same as the one(s) defining directionality for the corresponding argument(s) in the input function(s).

Example

$$\blacktriangleright X/Y \quad Y/Z \quad \Rightarrow \quad X \setminus Z$$

• X/Y CONJ X\Y
$$\Rightarrow$$
 X/Y

Any language is free to restrict combinatory rules to certain categories, or to entirely exclude a given rule type.

LTAG vs. CCG

Lexicalized TAGs are similar to CCGs

For each lexical item the elementary tree(s) which is (are) anchored on that lexical item can be regarded as the (structured) category (categories) associated with that item.



LTAG vs. CCG (cont)

By combining elementary trees with substitution or adjunction, we can assign a structured category (the derived tree) and a functional interpretation to sequences of lexical items even in the cases when the sequence is discontinuous or when it does not define a constituent in the conventional sense.



Summary

- ► Like other CG's, CCG has a transparent syntax-semantics interface. If we know the syntax of a sentence, we also know its meaning.
- CCG has a flexible constituent structure:
 - Simple, unified treatment of extraction and coordination
 - Psycholinguistic motivation: allows incremental processing
- CCG is mildly context-sensitive: CCG can capture crossing dependencies.
- CCG is non-transformational

Reading & homework

▶ §3 The Syntactic Process

Homework

- ▶ 自选10个汉语句子,试用CCG进行分析,并谈谈你对使用CCG分析汉语的感想。
- ▶ 对比你的LTAG和CCG分析,比较两种分析方法的差别