## 1. Optics


made of tiny controllable mirrors, or with gas bubbles which can reflect light (optionally with wavelength-converters).

## Takes milliseconds to reconfigure.

No buffers.

Inflexible but high capacity.

## QUESTION:

What is the best way to manage an all-optical network?

## 2. Lightpath assignment



Given a graph $G=(V, E),|V|=n$, and a set of colours $C$ :

A lightpath between nodes $s$ and $t$ is a path from $s$ to $t$, with associated colour $c \in C$.

A lightpath assignment is a collection of lightpaths between all pairs of nodes, such that any two lightpaths of the same colour are edge-disjoint.

QUESTION:
Given a graph $G$, what is the smallest number of colours ?=|C| for which there exists a lightpath assigment?

## BOTTLENECK CUTS



This graph requires

$$
?=n_{1} n_{2} / U U^{-1}=33
$$

colours.
Furthermore, one can find a wavelength assignment which uses 33 colours.

For 'real' graphs, this often happens: there is often a bottleneck cut which is tight.

# 3. Optical Packet Networks 



Packets arrive from outside, and are stored in electronic buffers.

From time to time, tunable lasers beam the data Into the optical core network.

QUESTIONS: Packets and circuits? Buffers and multiplexing?

## 1. STATIC

Set up permanent end-to-end lightpaths.
2. PACKET

Send packets in, and hope they don't collide.

## 3. BURST

a. Accumulate a burst of packets;
signal to request a lightpath;
once the request is acknowledged, send the burst;
tear down the lightpath.
b. Accumulate a burst of packets;
at time $t$, send a burst-coming notification;
at time $t+e$, send the burst.
4. TIME-DIVISION-SLOTTED

Signal to the network to say:
'I will send a burst of size $B$ every $T$ seconds'

## 4. Multiplexing

EXAMPLE 1:
Consider a link with ? available wavelengths. Let there be $L$ independent arrival processes,
each a Poisson flow of packets of rate ?,
where the size of each packet is $\operatorname{Exp}(\mu)$.
How large can the total arrival rate be?

## PACKET:

Let packets be immediately assigned a free wavelength, if one is available, and otherwise dropped.
Suppose the system is provisioned so that the probability of a drop is less than $e^{-}$?

SLOT:
For each arrival process:
accumulate packets in a buffer of size $B$,
and every $T$ seconds send out a burst of packets.
Suppose the system is provisioned so that the probability of buffer overflow is less than $e^{-}$?

## CONCLUDE

PACKET shows slightly more multiplexing gain;
SLOT shows much more buffering gain.

## 4. Multiplexing

EXAMPLE 2:
Consider a link with ? available wavelengths. Let there be $L_{2}$ independent arrival processes, each a Poisson flow of packets of rate $L_{1}$ ?, where the size of each packet is 1 . How many wavelengths do we need?

## BURST:

Accumulate packets in a buffer of size $L_{1} B$, and whenever it fills, send out a burst of size $L_{1} B$. Suppose the system is provisioned so that the probability that bursts collide is less than $e^{-}$.

SLOT:
For each arrival process:
accumulate packets in a buffer of size $L_{1} B$, and every $T$ seconds send out a burst of packets.
Suppose the system is provisioned so that the probability of buffer overflow is less than $e^{-}$?

CONCLUDE
BURST benefits from $L_{1}$ multiplexing,
SLOT benefits from $L_{2}$ multiplexing;
SLOT shows much more buffering gain.

## 4. Multiplexing

## CONCLUSION

Networks typically deal with variable input traffic using

- buffers
- multiplexing.

An optical network has

- a flexible (electronic) boundary, where buffers and multiplexing can be exploited
- an inflexible (optical) core, with no buffering and limited multiplexing ability.

This suggests we design the core to work like a circuit-switched (possibly TDM) network.
(Still, packet networks are far easier to manage!)

## 5. Edge-buffers



Suppose the input process is stationary.
Let $A(t)$ be the amount of work arriving in $(0, t)$.
Let $\mu=\mathrm{E} \quad A(t) / t$ and $V(t)=\operatorname{Var} A(t)$.
Suppose the burst-assembler has a buffer of size $B$, and emits a burst every $T$ seconds.

Seek to adaptively set $T$, to ensure that the probability of buffer overflow is small.

Using log P(overflow) ~ -(B- $\mu T)^{2} / 2 V(t)$,
a simple algorithm gives:



