Hardware/Software Co-Design using Functional Languages

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Abstract. In previous work we have developed and prototyped a silicon compiler which translates a functional language (SAFL) into hardware. Here we present a SAFL-level program transformation which: (i) partitions a specification into hardware and software parts and (ii) generates a specialised architecture to execute the software part. The architecture consists of a number of interconnected heterogeneous processors. Our method allows a large design space to be explored by systematically transforming a single SAFL specification to investigate different points on the area-time spectrum.

1 Introduction

In [12] we introduced a hardware description language, SAFL (Statically Allocated Functional Language), and sketched its translation to hardware. An optimising silicon compiler for SAFL targetting hierarchical RTL Verilog has been implemented [18] and tested on a number of designs, including a small commercial processor¹. SAFL is a first-order functional language with an ML [10] style syntax. We argue the case for functional languages over (say) Occam on the grounds of easier and more powerful program analysis, transformation and manipulation techniques. The essential features of SAFL can briefly be summarised as follows:

- programs are a sequence of function definitions;
- functions can call other defined functions but recursive calls must be tail-recursive². (Section 2.5 addresses the exact technical restrictions.)

¹ The instruction set of Cambridge Consultants XAP processor was implemented (see www.camcon.co.uk). We did not include the SIF instruction.

 $^{^2}$ Section 2.6.3 shows how this restriction can be removed by mapping general recursive functions into software.

This allows our SAFL silicon compiler to:

- compile SAFL in a resource-aware manner. That is we map each function definition into a single hardware-level resource; functions which are called more than once become shared resources³.
- synthesise highly parallel hardware—referential transparency allows one to evaluate all subexpressions in parallel.
- statically allocate the storage (e.g. registers and memories) required by a SAFL program.

The SAFL language is designed to facilitate source-to-source transformation. Whereas traditional "black-box" synthesis systems synthesise hardware according to user-supplied constraints, our approach is to select a particular implementation by applying transformation rules to the SAFL source as a pre-compilation phase. We have shown that applying fold/unfold transformations [4] to SAFL specifications allows one to explore various time-area tradeoffs at the hardware level [12, 13]. The purpose of this paper is to demonstrate how hardware/software partitioning can be seen as a source-to-source transformation at the SAFL level thus providing a formal framework in which to investigate hardware/software codesign. In fact we go one step further than traditional co-design since as well as partitioning a specification into hardware and software parts our transformation procedure can also synthesise an architecture tailored specifically for executing the software part. This architecture consists of any number of interconnected heterogeneous processors. There are a number of advantages to our approach:

- Synthesising an architecture specifically to execute a known piece of software can offer significant advantages over a fixed architecture [17].
- The ability to synthesise multiple processors allows a wide range of areatime tradeoffs to be explored. Not only does hardware/software partitioning affect the area-time position of the final design, but the number of processors synthesised to execute the software part is also significant: increasing the number of processors pushes the area up whilst potentially reducing execution time (as the processors can operate in parallel).
- Resource-awareness allows a SAFL specification to represent shared resources.
 This increases the power of our partitioning transformation since, for example, multiple processors can access the same hardware resource (see Figure 1 for an example).

1.1 A brief overview of the SAFL language

SAFL is a language of first order recurrence equations; a user program consists of a sequence of function definitions:

fun
$$f_1(\vec{x}) = e_1$$
; ...; fun $f_n(\vec{x}) = e_n$

³ All sharing issues are handled automatically by our silicon compiler: arbiters are inserted where necessary to protect shared resources and data-validity analysis is performed facilitating the generation of efficient inter-resource interface logic [18].

Programs have a distinguished function, main, (usually f_n) which represents an external world interface—at the hardware level it accepts values on an input port and may later produce a value on an output port. The abstract syntax of SAFL expressions, e, is as follows (we abbreviate tuples (e_1, \ldots, e_k) as \vec{e} and similarly (x_1, \ldots, x_k) as \vec{x}):

```
- variables: x; constants: c;
- user function calls: f(\vec{e});
- primitive function calls: a(\vec{e})—where a ranges over primitive operators (e.g. +, -, <=, && etc.);
- conditionals: e_1 ? e_2 : e_3; and
- let bindings: let \vec{x} = \vec{e} in e_0 end
```

See Figures 3 and 4 for concrete examples of SAFL code.

1.2 Comparison with other work

Previous work on compiling declarative specifications to hardware has centred on how functional languages themselves can be used as tools to aid the design of circuits. Sheeran's et al. muFP [19] and Lava [2] systems use functional programming techniques (such as higher order functions) to express concisely the repeating structures that often appear in hardware circuits. In this framework, using different interpretations of primitive functions corresponds to various operations including behavioural simulation and netlist generation. Our approach takes SAFL constructs (rather than gates) as primitive. Although this restricts the class of circuits we can describe to those which satisfy certain high-level properties, it permits high-level analysis and optimisation yielding efficient hardware. (A more detailed comparison of SAFL with other hardware description languages including Verilog, VHDL, ELLA and Lustre can be found in [13]).

Hardware/software co-design is well-studied and many tools have been built to aid the partitioning process [3, 6, 1]. Although these systems differ in their approach to co-design they are similar in so far as partitioning is a "blackbox" phase performed as part of the synthesis process. By making partitioning visible at the source-level we believe our approach to be more flexible—hardware/software co-design is just one of a library of source-to-source transformations which can be applied incrementally to explore a wide range of architectural trade-offs.

The idea of converting a program into a parameterised processor and corresponding instruction memory is not new; Page described a similar transformation [17] within the framework of Handel [16] (a subset of Occam for which a silicon compiler was written). Whereas Page's transformation allowed a designer to synthesise a single parameterised processor, our method allows one to generate a much more general architecture consisting of multiple communicating processors accessing a set of (potentially shared) hardware resources.

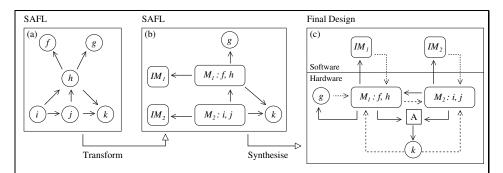
The impact of source-to-source transformation has been investigated in the context of imperative hardware description languages [20, 14]. We argue that

program transformation is a more powerful technique in the SAFL domain for two reasons:

- The functional properties of SAFL allow equational reasoning and hence make a wide range of transformations applicable (as we do not have to worry about side effects).
- The resource-aware properties of SAFL give fold/unfold transformations precise meaning at the design-level (e.g. we know that duplicating a function definition in the source is guaranteed to duplicate the corresponding resource in the generated circuit).

2 Technical Details

The first step in the partitioning transformation is to define a partitioning function, π , specifying which SAFL functions are to be implemented directly in hardware and which are to be mapped to a processor for software execution. Automated partitioning is not the subject of this paper; we assume that π is supplied by the user. For expository purposes we initially describe a transformation where all processors are variants of a stack machine: Section 2.1 describes the operation of the stack machine and Section 2.2 shows how it can be encoded as a SAFL function; a compiler from SAFL to stack code is presented in Section 2.3. In Section 2.6 we generalise our partitioning transformation to a network of heterogenous processors.



Partitioning: (a) shows the call-graph of a SAFL specification, P; (b) shows the call-graph of $\hat{\pi}(P)$, where $\pi = \{(f, M_1), (h, M_1), (i, M_2), (j, M_2)\}$. IM_1 and IM_2 are instruction memory functions (see Section 2.2); (c) shows the structure of the final circuit after compilation. The box marked 'A' represents an arbiter (inserted automatically by the SAFL compiler) protecting shared resource k; the bold arrows represent calls, the dotted arrows represent return values.

Fig. 1. A diagrammatic view of the partitioning transformation

Let \mathcal{M} be the set of processor instances used in the final design. We define a (partial) partitioning function

$$\pi: SAFL \ function \ name
ightharpoonup \mathcal{M}$$

mapping the function definitions in our SAFL specification onto processors in \mathcal{M} . $\pi(f)$ is the processor on which function f is to be implemented. If $f \notin Dom(\pi)$ then we realise f in hardware, otherwise we say that f is located on machine $\pi(f)$. Note that multiple functions can be mapped to the same processor.

We extend π to a transformation function

$$\hat{\pi}: SAFL\ Program \rightarrow SAFL\ Program$$

such that given a SAFL program, P, $\hat{\pi}(P)$ is another SAFL program which respects the partitioning function π . Figure 1 shows the effect of a partitioning transformation, $\hat{\pi}$, where

$$\mathcal{M} = \{M_1, M_2\}; \text{ and }$$

 $\pi = \{(f, M_1), (h, M_1), (i, M_2), (j, M_2)\}$

In this example we see that g and k are implemented in hardware since $g, k \notin Dom(\pi)$. $\hat{\pi}(P)$ contains function definitions: $\mathtt{M_1}$, $\mathtt{M_2}$, $\mathtt{IM_1}$, $\mathtt{IM_2}$, \mathtt{g} and \mathtt{k} where $\mathtt{M_1}$ and $\mathtt{M_2}$ are processor instances and $\mathtt{IM_1}$ and $\mathtt{IM_2}$ are instruction memories (see Section 2.2).

2.1 The Stack Machine Template

Our stack machine can be seen as a cut-down version of both Landin's SECD machine [9] and Cardelli's Functional Abstract Machine [5]. Each instruction has an op-code field and an operand field n. The following instructions are defined:

$\mathtt{PushC}(n)$	push constant n onto the stack
$\mathtt{PushV}(n)$	push variable (from offset n into the current stack)
$\mathtt{PushA}(n)$	push the value of the stack machine's argument a_n (see Sec-
	tion 2.2) to the stack
Squeeze(n)	pop top value; pop next n values; re-push top value
$\mathtt{Return}(n)$	pop result; pop link; pop n arguments; re-push result; branch
	to link
${\tt Call_Int}(n)$	push address of next instruction onto stack and branch to ad-
	$\mathrm{dress}\; n$
Jz(n)	pop a value; if it is zero branch to address n
$\mathtt{Jmp}(n)$	jump to address n
$\mathtt{Alu2}(n)$	pop two values; do 2-operand builtin operation n on them and
	push the result
Halt	terminate the stack machine returning the value on top of the
	stack

We define a family of instructions to allow the stack machine to call external functions:

```
Call_Ext<sub>f</sub> pop each of f's arguments from the stack; invoke the external function f and push the result to the top of the stack.
```

The stack machine template, SMT, is an abstract model of the stack machine parameterised on the code it will have to execute. Given a stack machine program, s, (i.e. a list of stack machine instructions as outlined above) $SMT\langle s\rangle$ is a stack machine instance: a SAFL function encoding a stack machine specialised for executing s. Our notion of a template is similar to a VHDL generic.

2.2 Stack Machine Instances

A stack machine instance, $SM_i \in \mathcal{M}$, is a SAFL function of the form:

```
fun SM_i(a_1, \ldots, a_{n_i}, PC, SP) = \ldots
where n_i = max(\{arity(f) \mid \pi(f) = SM_i\})
```

Arguments PC and SP are used to store the program counter and stack pointer respectively; a_1, \ldots, a_{n_i} are used to receive arguments of functions located on SM_i . Each stack machine instance is associated with an instruction memory function, IM_i of the form:

```
fun IM_i(address) =
case address of 0 => instruction_0
| 1 => instruction_1
... etc.
```

 SM_i calls $IM_i(PC)$ to load instructions for execution.

For example, consider a stack machine instance, $SM_{f,h}$, where we choose to locate functions f (of arity 2) and h (of arity 3). Then $n_{f,h}=3$ yielding signature: $SM_{f,h}(\mathbf{a}_1,\mathbf{a}_2,\mathbf{a}_3,PC,SP)$. $IM_{f,h}$ is an instruction memory containing compiled code for f and h. To compute the value of h(x,y,z) we invoke $SM_{f,h}$ with arguments $\mathbf{a}_1=x$, $\mathbf{a}_2=y$, $\mathbf{a}_3=z$, $PC=ext_h_{entry}$ (h's external entry point—see Section 2.3) and SP=0. Similarly to compute the value of f(x,y) we invoke $SM_{f,h}$ with arguments $\mathbf{a}_1=x$, $\mathbf{a}_2=y$, $\mathbf{a}_3=0$, $PC=ext_f_{entry}$ and SP=0. Note how we pad the \mathbf{a} -arguments with 0's since arity(f)<3.

The co-design of hardware and software means that instructions and ALU operations are only added to SM_i if they appear in IM_i . Parameterising the stack machine template in this way can considerably reduce the area of the final design since we remove redundant logic in each processor instance.

We can consider many other areas of parameterisation. For example we can adjust the op-code width and assign op-codes to minimise instruction-decoding delay [17]. Figure 4 gives the SAFL code for a 16-bit stack machine instance⁴. An alu2 function, and an example stack machine program which computes triangular numbers is shown in Figure 3.

⁴ Approximately 2000 2-input equivalent gates when compiled using the SAFL silicon compiler. For simplicity we consider a simple stack machine with no Call_Ext instructions.

2.3 Compilation to Stack Code

Figure 2 gives a compilation function from SAFL to stack based code. Although the translation of many SAFL constructs is self-explanatory, the compilation rules for function definition and function call require further explanation:

Compiling Function Definitions

The code generated for function definition

fun
$$f(x_1,\ldots,x_k)=e$$

requires explanation in that we create 2 distinct entry points for f: f_{entry} and ext_-f_{entry} . The internal entry point, f_{entry} , is used when f is invoked internally (i.e. with a Call_Int instruction). The external entry point, ext_-f_{entry} , is used when f is invoked externally (i.e. via a call to $\pi(f)$, the machine on which f is implemented). In this latter case, we simply execute k PushA instructions to push f's arguments onto the stack before jumping to f's internal entry point, f_{entry} .

Compiling Function Calls

Suppose function g is in software $(g \in Dom(\pi))$ and calls function f. The code generated for the call depends on the location of f relative to g. There are three possibilities:

- 1. If f and g are both implemented in software on the same machine $(f \in Dom(\pi) \land \pi(f) = \pi(g))$ then we simply push each of f's arguments to the stack and branch to f's internal entry point with a Call_Int instruction. The Call_Int instruction pushes the return address and jumps to f_{entry} ; the compiled code for f is responsible for popping the arguments and link leaving the return value on the top of the stack.
- 2. If f is implemented in hardware $(f \notin Dom(\pi))$ then we push each of f's arguments to the stack and invoke the hardware resource corresponding to f by means of a Call_Ext_f instruction. The Call_Ext_f instruction pops each of f's arguments, invokes resource f and pushes f's return value to the stack.
- 3. If f and g are both implemented in software but on different machines $(f,g\in Dom(\pi) \land \pi(f) \neq \pi(g))$ then g needs to invoke $\pi(f)$ (the machine on which f is located). We push $\pi(f)$'s arguments to the stack: the arguments for f possibly padded by 0s (see Section 2.2) followed by the program counter PC initialised to ext_f_{entry} and the stack pointer SP initialised to 0. We then invoke $\pi(f)$ using a Call_Ext $\pi(f)$ instruction.

Let σ , be an environment mapping variable names to stack offsets (offset 0 signifies the top of the stack). Let g be the name of the function we are compiling. Then $[\cdot]^g \sigma$ gives an instruction list corresponding to g. (We omit g for readability in the following—it is only used to identify whether a called function is located on the same machine).

We use the notation $\sigma\{x \mapsto n\}$ to represent environment σ extended with x mapping to n. σ^{+n} represents an environment constructed by incrementing all stack offsets in σ by n—i.e. $\sigma^{+n}(x) = \sigma(x) + n$. \emptyset is the empty environment. The infix operator @ appends instruction lists. Repeat(l, n) is $l \ @ \ldots \ @ \ l \ (n \text{ times})$; (this is used to generate instruction sequences to pad argument lists with 0s).

Fig. 2. Compiling SAFL into Stack Code for Execution on a Stack Machine Instance

2.4 The Partitioning Transformation

Having introduced the stack machine (Section 2.1) and the associated compilation function (Section 2.3) the details of the partitioning transformation, $\hat{\pi}$, are as follows:

Let P be the SAFL program we wish to transform using π . Let f be a SAFL function in P with definition d_f of the form

fun
$$f(x_1,\ldots,x_k)=e$$

We construct a partitioned program $\hat{\pi}(P)$ from P as follows:

1. For each function definition $d_f \in P$ to be mapped to hardware (i.e. $f \notin Dom(\pi)$) create a variant in $\hat{\pi}(P)$ which is as d_f but for each call, $g(e_1, \ldots, e_k)$:

If $g \in Dom(\pi)$ then replace the call $g(\vec{e})$ with a call:

$$m(e_1,\ldots,e_k,\underbrace{0,\ldots,0}_{arity(m)-2-k}ext_g_{entry},0)$$

where $m = \pi(g)$, the stack machine instance on which g is located.

- 2. For each $m \in \mathcal{M}$:
 - (a) Compile instruction sequences for functions located on m:

$$Code_m = \{ [\![d_f]\!] \mid \pi(f) = m \}$$

- (b) Generate machine code for m, $MCode_m$, by resolving symbols in $Code_m$, assigning opcodes and converting into binary representation.
- (c) Generate an instruction memory for m by adding a function definition, IM_m , to $\hat{\pi}(P)$ of the form:

```
\begin{array}{ll} \text{fun IM}_m \, (\text{address}) \, = \\ & \text{case address of 0 => instruction\_0} \\ & | \, \, 1 \, = > \, \text{instruction\_1} \\ & \dots \, \, \text{etc.} \end{array}
```

where each instruction j is taken from $MCode_m$.

(d) Generate a stack machine instance, $SMT(Code_m)$ and append it to $\hat{\pi}(P)$.

For each $m \in \mathcal{M}$, $\hat{\pi}(P)$ contains a corresponding processor instance and instruction memory function. When $\hat{\pi}(P)$ is compiled to hardware resource-awareness ensures that each processor definition function becomes a single processor and each instruction memory function becomes a single instruction memory. The remaining functions in $\hat{\pi}(P)$ are mapped to hardware resources as required. Function calls are synthesised into optimised communication paths between the hardware resources (see Figure 1c).

2.5 Validity of Partitioning Functions

This section concerns some fine technical details—it can be skipped on first reading.

We clarify the SAFL restriction on recursion 5 given in the Introduction as follows.

In order for a SAFL program to be valid, all recursive calls, including those calls which form part of mutually-recursive cycle, may only occur in tail-context. Non-recursive calls may appear freely.

This allows storage for SAFL variables to be allocated statically as tail recursion does not require the dynamic allocation of stack frames.

Unfortunately, in general, a partitioning function, π , may transform a valid SAFL program, P, into an invalid SAFL program, $\hat{\pi}(P)$, which does not satisfy the recursion restrictions. For example consider the following program, P_{bad} :

```
fun f(x) = x+1;
fun g(x) = f(x)+2;
fun h(x) = g(x+3);
```

Partitioning P_{bad} with $\pi = \{(f, SM), (h, SM)\}$ yields a new program, $\hat{\pi}(P_{bad})$, of the form:

 $\hat{\pi}(P_{bad})$ has invalid recursion between g and SM. The problem is that the call to SM in the body of g is part of a mutually-recursive cycle and is not in tail-context.

We therefore require a restriction on partitions π to ensure that if P is a valid SAFL program then $\hat{\pi}(P)$ will also be a valid SAFL program. For the purposes of this paper we give the following sufficient condition:

 π is a valid partition with respect to SAFL program, P, iff all cycles occurring the call graph of $\hat{\pi}(P)$ already exist in the call graph of P, with the exception of self-cycles generated by direct tail-recursion.

Thus, in particular, new functions in $\hat{\pi}(P)$ —i.e. stack machines and their instructions memories—must not have mutual recursion with any other functions.

2.6 Extensions

Fine Grained Partitioning We have presented a program transformation to map function definitions to hardware or software, but what if we want to map part of a function definition to hardware and the rest to software? This can be achieved by applying fold/unfold transformations before our partitioning transformation. For example, consider the function

⁵ A more formal presentation can be found in [12].

```
f(x,y) = if x=0 then y
else f(x-1, x*y - 7 + 5*x)
```

If we choose to map f to software our design will contain a processor and associated machine code consisting of a sequence of instructions representing multiply x and y, subtract 7, add 5 times x. However, consider transforming f with a single application of the *fold*-rule [4]:

```
i(x,y) = x*y-7 + 5*x

f(x,y) = if x=0 then y else f(x-1, i(x,y))
```

Now mapping f to software and i to hardware leads to a software representation for f containing fewer instructions and a specialised processor with a x*y-7 + 5*x instruction.

Dealing with Heterogeneous Processors So far we have only considered executing software on a network of stack machines. Although the stack machine is a familiar choice for expository purposes, in a real design one would often prefer to use different architectures. For example, specialised VLIW [8] architectures are a typical choice for data-dominated embedded systems since many operations can be performed in parallel without the overhead of dynamic instruction scheduling. The commercial "Art Designer" tool [1] partitions a C program into hardware and software by constructing a single specialised VLIW processor and compiling code for it. In general, however, designs often consist of multiple communicating processors chosen to reflect various cost and performance constraints. Our framework can be extended to handle a network of heterogeneous processors as follows:

Let Templates be a set of processor templates (c.f. the stack machine template, SMT, in section 2.1).

Let *Compilers* be a set of compilers from SAFL to machine code for processor templates.

As part of the transformation process, the user now specifies two extra functions:

$$\delta: \mathcal{M} \to \mathit{Templates}$$

 $\tau: \mathcal{M} \to \mathit{Compilers}$

 δ maps each processor instance, $m \in \mathcal{M}$, onto a SAFL processor template and τ maps each $m \in \mathcal{M}$ onto an associated compiler. We then modify the transformation procedure described in Section 2.4 to generate a partitioned program, $\hat{\pi}_{\delta,\tau}(P)$ as follows: for each $m \in \mathcal{M}$ we generate machine code, $MCode_m$, using compiler $\tau(m)$; we then use processor template, $MT = \delta(m)$, to generate processor instance $MT\langle MCode_m\rangle$ and append this to $\hat{\pi}_{\delta,\tau}(P)$.

Extending the SAFL Language Recall that the SAFL language specifies that all recursive calls must be in tail-context. Since only tail-recursive calls are

permitted, our silicon compiler is able to statically allocate all the storage needed for a SAFL program.

As an example of these restrictions consider the following definitions of the factorial function:

```
rfact(x) = if x=0 then 1 else x*rfact(x-1)
if act(x,a) = if x=0 then a else if <math>act(x-1,x*a)
```

rfact is not a valid SAFL program since the recursive call is not in a tail-context. However the equivalent tail-recursive factorial function, ifact which uses a second argument to accumulate partial results is a valid SAFL program.

Although one can sometimes transform a non-tail recursive program into an equivalent tail-recursive one, this is not always easy or natural. The transformation of factorial into its tail-recursive equivalent is only possible because multiplication is an associative operator. Thus, in general we require a way of extending SAFL to handle general unrestricted recursion. Our partitioning transformation provides us with one way to do this:

Consider a new language, SAFL+ constructed by removing the recursion restrictions from SAFL. We can use our partitioning transformation to transform SAFL+ to SAFL simply by ensuring that each function definition containing recursion other than in a tail-call context is mapped to software. Note that our compilation function (Figure 2) is already capable of dealing with general recursion without any modification.

3 Conclusions and Further Work

Source-level program transformation of a high level HDL is a powerful technique for exploring a wide range of architectural tradeoffs from an initial specification. The partitioning transformation outlined here is applicable to any hardware description language (e.g. VHDL or Verilog) given suitable compilation functions and associated processor templates. However, we believe that equational reasoning makes program transformation a particularly powerful technique in the SAFL domain.

We are in the process of deploying the techniques outlined here as part of a semi-automated transformation system for SAFL programs. The goal of the project is to develop a framework in which a SAFL program can be systematically transformed to investigate a large number of possible implementations of a single specification. So far we have developed a library of transformations which allow us to represent a wide range of concepts in hardware design including: resource sharing/duplication, static/dynamic scheduling [13] and now hardware/software partitioning. In the future we plan to investigate how partial evaluation techniques [7] can be used to transform a processor definition function and its corresponding instruction memory function into a single unit with hardwired control.

Although initial results have been promising, the project is still in its early stages. We are currently investigating ways of extending the SAFL language to

make it more expressive without loosing too many of its mathematical properties. Our current ideas centre around adding synchronous communication and a restricted form of π -calculus [11] style channel passing. We believe that this will allow us to capture the semantics of I/O whilst maintaining the correspondence between high-level function definitions and hardware-level resources.

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References

- 1. The "Art Designer" Tool. See http://www.frontierd.com.
- Bjesse, P., Claessen, K., Sheeran, M. and Singh, S. Lava: Hardware Description in Haskell. Proceedings of the 3rd ACM SIGPLAN International Conference on Functional Programming, 1998.
- Balarin, F., Chiodo, M., Giusto, P., Hsieh, H., Jurecska, A., Lavagno, L., Passerone, C., Sangiovanni-Vincentelli, A., Sentovich, E., Suzuki, K., Tabbara B. Hardware-Software Co-Design of Embedded Systems: The Polis Approach. Kluwer Academic Press, June 1997.
- Burstall, R.M. and Darlington, J. A Transformation System for Developing Recursive Programs, JACM 24(1).
- Cardelli, L. The Functional Abstract Machine. Technical Report TR-107, AT&T Bell Laboratories, April 1983.
- Chou, P., Ortega, R., Borriello, G., The Chinook Hardware/Software Co-Synthesis System. Proceedings of the 8th International Symposium on System Synthesis, 1995.
- Jones, N., Gomard, C. and Sestoft, P. Partial Evaluation and Automatic Program Generation. Published by Prentice Hall (1993); ISBN 0-13-020249-5.
- 8. Hennessy, J., Patterson, D. Computer Architecture A Quantitative Approach. Published by Morgan Kaufmann Publishers, Inc. (1990); ISBN 1-55860-069-8
- Landin, P. The Mechanical Evaluation of Expressions. Computer Journal, Vol. 6, No. 4, 1964, pages 308-320.
- Milner, R., Tofte, M., Harper, R. and MacQueen, D. The Definition of Standard ML (Revised). MIT Press, 1997.
- 11. Milner, R. The Polyadic π -calculus: a tutorial. Technical Report ECS-LFCS-91-180, Laboratory for Foundations of Computer Science, University of Edinburgh, October 1991.
- 12. Mycroft, A. and Sharp, R. A Statically Allocated Parallel Functional Language. Proc. of the International Conference on Automata, Languages and Programming 2000. LNCS Vol. 1853, Springer-Verlag.
- 13. Mycroft, A. and Sharp, R. The FLaSH Project: Resource-Aware Synthesis of Declarative Specifications. Proceedings of The International Workshop on Logic Synthesis 2000. Also available as AT&T Technical Report tr.2000.6 via www.uk.research.att.com

- 14. Nijhar, T., and Brown, A. Source Level Optimisation of VHDL for Behavioural Synthesis. IEE Proceedings on Computers and Digital Techniques, 144, No 1, January 1997, pp1-6.
- 15. O'Donnell, J. Generating Netlists from Executable Circuit Specifications in a Pure Functional Language. In *Functional Programming Glasgow*, Springer-Verlag Workshops in Computing, pages 178-194, 1993.
- 16. Page, I. and Luk, W. Compiling Occam into Field-Programmable Gate Arrays. In Moore and Luk (eds.) FPGAs, pages 271-283. Abingdon EE&CS Books, 1991.
- 17. Page, I. Parameterised Processor Generation. In Moore and Luk (eds.), More FPGAs, pages 225-237. Abingdon EE&CS Books, 1993.
- 18. Sharp, R. and Mycroft, A. The FLaSH Compiler: Efficient Circuits from Functional Specifications. AT&T Technical Report tr.2000.3. Available from www.uk.research.att.com
- 19. Sheeran, M. muFP, a Language for VLSI Design. Proc. ACM Symp. on LISP and Functional Programming, 1984.
- 20. Walker, R. Thomas, D., Behavioral Transformation for Algorithmic Level IC Design. IEEE Transactions on CAD, Vol. 8, No.10, October 1989.

```
(* +-----+
  | SAFL specification of simple stack processor
     Richard Sharp and Alan Mycroft, July 2000
  +-----+ *)
(* ----- *)
fun alu2(op:16, a1:16, a2:16):16 =
  case op of 0 \Rightarrow a1+a2
        ! 1 => a1-a2
        ! 2 => a1&&a2
         ! 3 => a1||a2
         ! 4 => a1^^a2
        ! 16 => a1<a2
        ! 17 => a1>a2
         ! 18 => a1=a2
         ! 19 => a1>=a2
         ! 20 => a1<=a2
        ! 21 => a1<>a2
(* ----- Instruction memory here -----*)
(* The following codes: f(x) = if x then x+f(x-1) else 0;
(* i.e. it computes triangular numbers
fun load_instruction (address:16):24 = case address of
    0 => %00001001000000000000000001 (* pusha 1
                                         *)
   ! 1 => %000001010000000000000011 (*
                                call_int f *)
                               halt
   *)
   ! 3 => %0000001000000000000000001 (* f: pushv 1
                                         *)
   ! 4 => %00000111000000000001100 (* jz l1
                                         *)
                                pushv 1
   *)
                                pushv 2
   *)
                                pushc 1
   ! 7 => %00000010000000000000000001 (*
                                         *)
   alu2 sub
   ! 9 => %000001010000000000000011 (*
                                 call_int f *)
   ! 10=> %000010000000000000000000000 (*
                                 alu2 add *)
   ! 11=> %00000110000000000001101 (*
                                 jmp 12
                                         *)
   ! 12=> %000000100000000000000 (* 11: pushc 0
                                         *)
   *)
default => %101010101010101010101010 (*
                                         *)
external mem_acc (address:16,data:16,write:1):16
inline fun data_read (address:16):16 = mem_acc(address,0,0)
inline fun data_write (address:16,data:16):16 = mem_acc(address,data,1)
```

Fig. 3. The Stack Machine (Part 1 of 2)

```
(* ----- Stack Machine Instance -----*)
fun SMachine (a1:16, PC:16, SP:16):16 =
   let var new_PC : 16 = PC + 1
        var instr : 24 = load_instruction(PC)
var op_code : 8 = instr[23,16]
        var op_rand : 16 = instr[15,0]
var inc_SP : 16 = SP + 1
        var dec_SP : 16 = SP - 1
        case op_code of
              0 => (* halt, returning TOS *)
                        data_read(SP)
            ! 1 => (* push constant operation *)
                        data_write(dec_SP, op_rand);
SMachine (a1, new_PC, dec_SP)
            ! 2 => (* push variable operation *)
                         let var data:16 = data_read(SP+op_rand)
                         in data_write(dec_SP, data);
SMachine (a1, new_PC, dec_SP) end
            ! 9 => (* push a-argument operation *)
                         data_write(dec_SP, a1);
                        SMachine (a1, new_PC, dec_SP)
            ! 3 => (* squeeze operation -- op_rand is how many locals to pop *)
let var new_SP:16 = SP + op_rand
var v:16 = data_read(SP)
                         in data_write(new_SP, v);
                             SMachine (a1, new_PC, new_SP) end
            ! 4 => (* return operation -- op_rand is how many actuals to pop *)
let var new_SP:16 = inc_SP + op_rand
                             var rv:16 = data_read(SP)
                         in let var rl:16 = data_read(inc_SP)
                             in data_write(new_SP, rv);
                                  SMachine (a1, r1, new_SP) end end
            ! 5 => (* call_int operation *)
                         data_write(dec_SP, new_PC);
                        SMachine (a1, op_rand, dec_SP)
            ! 6 => (* jmp (abs) operation *)

SMachine (a1, op_rand, SP)
            ! 7 => (* jz (abs) operation *)
                         let var v:16 = data_read(SP)
                         in SMachine (a1, if v=0 then op_rand else new_PC, inc_SP) end
            ! 8 => (* alu2: binary alu operation -- specified by immediate field *)
                        aluz: binary alu operation -- specified by immedia
let var v2:16 = data_read(SP)
in let var v1:16 = data_read(inc_SP)
in data_write(inc_SP, alu2(op_rand, v1, v2));
SMachine (a1, new_PC, inc_SP) end end
           default =>
                  (* halt, returning Oxffff -- illegal opcode *)
                         %11111111111111111
```

Fig. 4. The Stack Machine (Part 2 of 2)

end