

8 Algorithms 1 (jkf21)

- (a) A haulage company uses electric trucks to move goods from one warehouse to another. There are recharging points at the warehouses  $A$  and  $B$ , and at  $n - 1$  intermediate points. The recharging points,  $A = r_0, r_1, \dots, r_n = B$ , are at increasing distances  $d_0 = 0, d_1, d_2, \dots, d_n$  from  $A$ . Trucks can travel for distance  $c$  on a full charge, and the distance between adjacent recharging points is less than  $c$ . To maximise time on the road, the haulage company asks you to find a way of getting from  $A$  to  $B$  that minimises the number of occasions when the trucks have to stop to recharge. Trucks always recharge at  $A$  before setting off. They wish to know which recharging points to use, not only the minimum number of recharges required. You decide to solve the problem using dynamic programming.
- (i) State and explain a formula that expresses an optimal solution in terms of the optimal solutions to subproblems. [5 marks]
- (ii) Devise an algorithm based on dynamic programming to solve the problem and state whether it is top-down or bottom-up. [6 marks]
- (iii) Derive the big-Theta space and time complexities of your approach. [4 marks]
- (b) A friend believes that this optimisation problem can be solved with a greedy algorithm. Are they correct? If so, explain a greedy algorithm. If not, explain why no greedy solution can exist. [5 marks]