COMPUTER SCIENCE TRIPOS Part IB – 2024 – Paper 7

5 Formal Models of Language (pjb48)

An intrepid linguist encounters an alien while exploring a remote planet, she documents an alien language that has four sounds, $\Sigma = \{a, e, f, m\}$. The following are examples of the alien's speech and a translation:

$e \ amaf$	nice spaceship
e faem	nice spaceboots
e e amaf	very nice spaceship
e e e faem	extremely nice spaceboots

The linguist hypothesises that Expression 1 matches sound sequences in the alien language.

Expression 1: $e^*(a|e|f|m)(a|e|f|m)^*$

- (a) Describe the strings that are matched by Expression 1. [2 marks]
- (b) Provide a Finite State Automaton that can generate the language defined by Expression 1. [2 marks]

As the linguist continues to explore, she encounters a grumpy alien and documents the following utterances:

fama e amaf	not nice spaceship (unpleasant spaceship)
meaf e e faem	very unpleasant spaceboots
afaf e e e fafa	extremely unpleasant gift

The linguist hypothesises that Expression 2 matches sound sequences in the language.

Expression 2: $w^{-1}e^*w$ where $w \in \Sigma^*$

- (c) Can the linguist draw a Finite State Automaton to generate the language defined by Expression 2? Provide a proof for your answer. [5 marks]
- (d) Provide a grammar that can generate the language defined by Expression 2. [5 marks]

On the far side of the planet, the linguist encounters a new dialect and documents the following utterances:

$amaf \ e \ amaf$	unpleasant spaceship
faem e e faem	very unpleasant spaceboots
mefaem e e e mefaem	extremely unpleasant earthling

- (e) Provide a general expression to match such sound sequences. [1 mark]
- (f) Can you use a Context Free Grammar to generate the language defined by your expression? Provide a proof for your answer. [5 marks]