## COMPUTER SCIENCE TRIPOS Part Ib - 2023 - Paper 4

## 4 Prolog (ijl20)

In your answers ensure each relation has a comment giving a declarative reading of its behaviour. Avoid unnecessary use of cut and do not use extra-logical relations such as findall, assertz and not $(\backslash+)$. Built-in library relations should not be assumed. The Prolog operator in $A \backslash=B$, meaning $A$ will not unify with $B$, may be used.
(a) Explain Prolog's process of unification. What situation would an occurs check guard against?
(b) Assume node(Left, Right) and leaf (Name, Value) compound terms are used to represent trees such as:


Define a relation lookup(+Tree,?Name,?Value) which finds the value(s) associated with a given name in trees of the above form.
[3 marks]
(c) Given a list of atoms, L1, define a relation rle(+L1,?L2) which runlength encodes L1 into L2. For example, rle([a,a,b,c,a,a,a],L) should succeed with $\mathrm{L}=[2 * \mathrm{a}, 1 * \mathrm{~b}, 1 * \mathrm{c}, 3 * \mathrm{a}]$. Giving reasons, indicate for your answer whether a query $\operatorname{rle}(\mathrm{L},[2 * \mathrm{a}, 1 * \mathrm{~b}, 1 * \mathrm{c}, 3 * \mathrm{a}]$ ) would succeed with $\mathrm{L}=[\mathrm{a}, \mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{a}, \mathrm{a}, \mathrm{a}]$.
(d) Complementary to rle/2, define a relation rld(+L1,? 2 ) which decodes a run-length-encoded list L1 as defined in part (c) into L2.
(e) The Prolog relations below, given a query alter_list([2,4,6], L), will succeed with $L=[a, a, b]$. Use an additional difference-list argument to accumulate the execution path through the Prolog clauses. Number the clauses 1 to 4 such that alter_list ([2, 4, 6],L,Path-[]) will succeed with the sequence of clauses as a list of integers in Path, i.e. with $\mathrm{L}=[\mathrm{a}, \mathrm{a}, \mathrm{b}]$ and Path $=[4,1,4,1,4,2,3]$.

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change(N,a) :- N < 5.
change(N,b) :- N >= 5.
alter_list([],[]).
alter_list([H1|T1],[H2|T2]) :- change(H1,H2), alter_list(T1,T2).
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