Here is an OCaml definition of the Ackermann function, ack:

```ocaml
let rec ack m n =  
    if m = 0 then n+1  
    else if n = 0 then ack (m-1) 1  
    else ack (m-1) (ack m (n-1))
```

(a) You would like to run `ack` on an old system with limited stack space and no support for closures, and decide to rewrite it in stages.

(i) Rewrite the `ack` function to produce a function `ack_cps` in continuation-passing style so that the function

```ocaml
let ack_1 m n = ack_cps m n (fun x -> x)
```

produces the same results as the function `ack`. [5 marks]

(ii) Eliminate higher-order functions from your answer to Part (a)(i) by rewriting `ack_cps` as a function `ack_cps_dfn` in defunctionalized form so that the function

```ocaml
let ack_2 m n = ack_cps_dfn m n ID
```

produces the same results as the function `ack`. [5 marks]

(iii) Convert your answer from Part (a)(ii) to a function `ack_cps_dfn_list` that uses standard lists rather than custom data types [5 marks]

(b) Briefly comment on the way that `ack` and the transformed implementations in Parts (a)(i), (a)(ii) and (a)(iii) use memory, making reference to the stack and heap. [5 marks]