

15 Types (NK)

- (a) Explain what logical connective the product type corresponds to, and what patterns of proof the introduction and elimination forms for products correspond to. [2 marks]
- (b) Explain what a solution for a typing problem $\Gamma \vdash M : ?$ is, and when a solution is principal. [4 marks]
- (c) Give the typing rule for the let-binding form $\text{let } x = M_1 \text{ in } M_2$ in mini-ML with references. [6 marks]
- (d) Do the following programs (for mini-ML with references) have solutions? If so, what is the type of the expression? Justify your answer in each case:
- (i) $\text{let } f = \lambda x (x) \text{ in } (f \text{ true}) :: (f \text{ nil})$ [4 marks]
- (ii) $\text{let } f = \lambda x (x) \text{ in let } g = f f \text{ in } (g \text{ true}) :: (g \text{ nil})$ [4 marks]