

2 Foundations of Computer Science (LCP)

- (a) Write brief notes on programming with lazy lists in ML. Your answer should include the definition of a polymorphic type of infinite lazy lists, a function to return the tail of a lazy list, a function to create the infinite list of all positive integers, and an apply-to-all functional analogous to the list functional `map`. [6 marks]

- (b) Write a function `diag` that takes a lazy list of lazy lists,

$$\begin{aligned} & [[z_{11}, z_{12}, z_{13}, \dots], \\ & [z_{21}, z_{22}, z_{23}, \dots], \\ & [z_{31}, z_{32}, z_{33}, \dots], \dots] \end{aligned} \quad (*)$$

and returns the diagonal, namely the lazy list $[z_{11}, z_{22}, z_{33}, \dots]$. [3 marks]

- (c) Write a function that takes two lazy lists $[x_1, x_2, x_3, \dots]$ and $[y_1, y_2, y_3, \dots]$ and a function `f` of two arguments; it should return a lazy list of lazy lists like (*) above, with $z_{ij} = f x_i y_j$. [3 marks]

- (d) Write a function that converts a lazy list of lazy lists like (*) above to a lazy list whose elements are all of the z_{ij} , enumerated in some order. [8 marks]