2010 Paper 4 Question 4

Computer Graphics and Image Processing

(a) Homogeneous coordinates are often used to represent transformations in 3D:

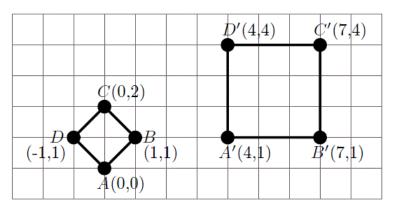
$$\begin{bmatrix} x'_H \\ y'_H \\ z'_H \\ w'_H \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & b_1 \\ a_{21} & a_{22} & a_{23} & b_2 \\ a_{31} & a_{32} & a_{33} & b_3 \\ c_1 & c_2 & c_3 & d \end{bmatrix} \begin{bmatrix} x_H \\ y_H \\ z_H \\ w_H \end{bmatrix}$$

- (i) Explain how to convert standard 3D coordinates, (x, y, z), to homogeneous coordinates, and how to convert homogeneous coordinates to standard 3D coordinates. [2 marks]
- (*ii*) Describe the types of transformations provided by each of the four blocks of coefficients in the matrix $(a_{11} \dots a_{33}, b_1 \dots b_3, c_1 \dots c_3 \text{ and } d)$. [5 marks]
- (*iii*) Explain what transformation is produced by each of the following matrices:

Γ1	0	0	ך 0	Γ1	0	p	-p(1+r) ך
0	1	0	0	0	1	q	$\begin{array}{c c} -q(1+r) \\ -r(1+r) \end{array}$
0	0	1	0	0	0	1+r	-r(1+r)
L0	0	1	0				-r

[5 marks]

(b) Consider the following figure:



- (i) Give a matrix, or product of matrices, that will transform the square ABCD into the rectangle A'B'C'D'. [5 marks]
- (*ii*) Show what happens if the same transformation is applied to A'B'C'D'. [3 marks]