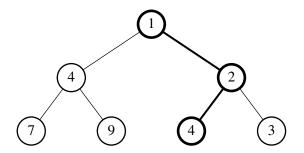
## 2005 Paper 1 Question 6

## Foundations of Computer Science

Consider a datatype of binary trees where both leaves and branches carry labels:

A *path* in a binary tree is a series of labels proceeding from the root to a leaf, as shown in the diagram:



Consider the problem of finding a path in a binary tree such that the integer sum of the labels satisfies a given property. (In the example above, the highlighted path sums to a prime number.)

- (a) Write an ML function find\_path such that find\_path p t returns some path in t whose sum satisfies the boolean-valued function p. If no such path exists, the function should raise an exception.
- (b) Write an ML function all\_paths such that all\_paths p t returns the list of all paths in t whose sums satisfy the boolean-valued function p. [6 marks]
- (c) Write an ML function all\_pathq that is analogous to all\_paths but returns a lazy list of paths. For full credit, your function should find paths upon demand rather than all at once. [Hint: try adding solutions to an accumulating argument.]
  [9 marks]