

1993 Paper 1 Question 7

State carefully what it means to say that a function has time complexity $O(f(n))$, and give ML definitions for some example `int ->int` functions which have time complexities $O(\log n)$, $O(n)$, $O(n^2)$, $O(n^3)$. In what circumstances can a function have time complexity $O(1)$?

Estimate the time complexities of the functions `f1`, `f2` and `f3` defined below:

```
fun f1 0 = 1
  | f1 n = 1 + f1(n-1);
```

```
fun f2 0 = 1
  | f2 n = f2(n-1) + f1 n;
```

```
fun f3 0 = 1
  | f3 n = f3(n div 7) + f3(5*n div 7) + f1 n;
```