

Compiler Construction

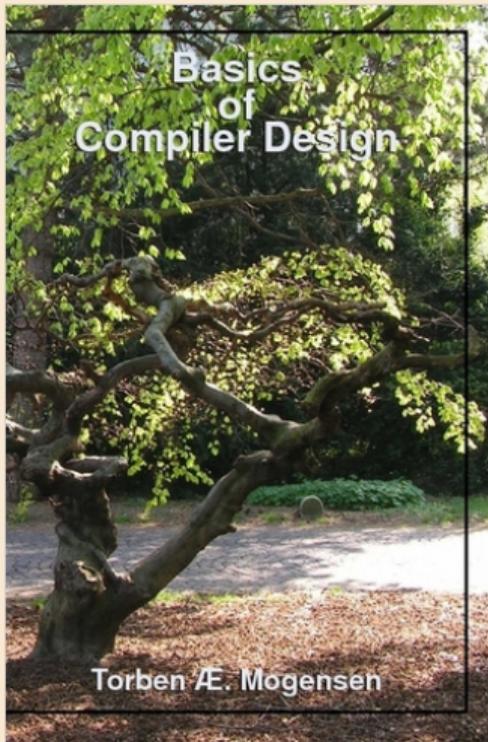
Lecture 16



Bootstrapping

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Chapter 13 of

Basics of Compiler Design

Torben Ægidius Mogensen

<http://hjemmesider.diku.dk/~torbenm/Basics/>

Notation

Notation: programs, interpreters, machines

Notation



Examples

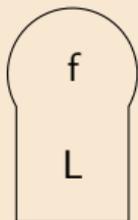
Compiling compilers

Full bootstrap

Verified compilation

Trusting trust

A program



Computes function f
written in language L

An interpreter



Interprets language $L2$
written in language $L1$

A machine



Executes code
in language L

Notation



Examples

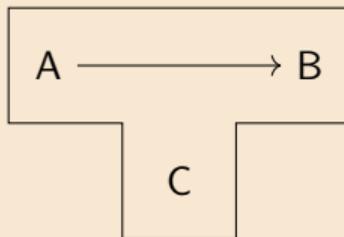
Compiling
compilers

Full
bootstrap

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compilation

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trust

A compiler



Translates language A into language B
Written in language C

Examples

Executing programs

Notation

Examples

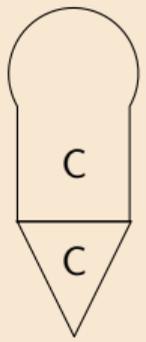
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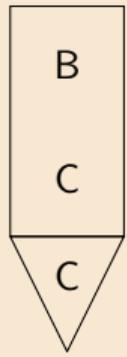
Trusting trust

To execute a program



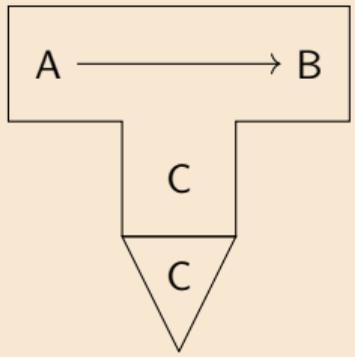
we run it on a machine

To execute an interpreter



we run it on a machine

To execute a compiler



we run it on a machine

Interpreting a program

Notation

Examples

Compiling
compilers

Full
bootstrap

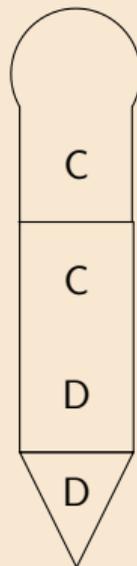
Verified
compilation

Trusting
trust

Run a program
written in language C

on an interpreter for C
written in language D

on a D machine



(Note: the languages must match)

Interpreting a Java program

Notation

Examples

Compiling
compilers

Full
bootstrap

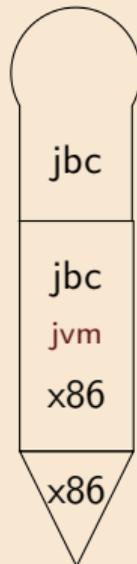
Verified
compilation

Trusting
trust

Run a program
written in Java byte code

on an interpreter for Java byte code
written in x86 code

on a x86 machine



Running a compiler on an interpreter

Notation

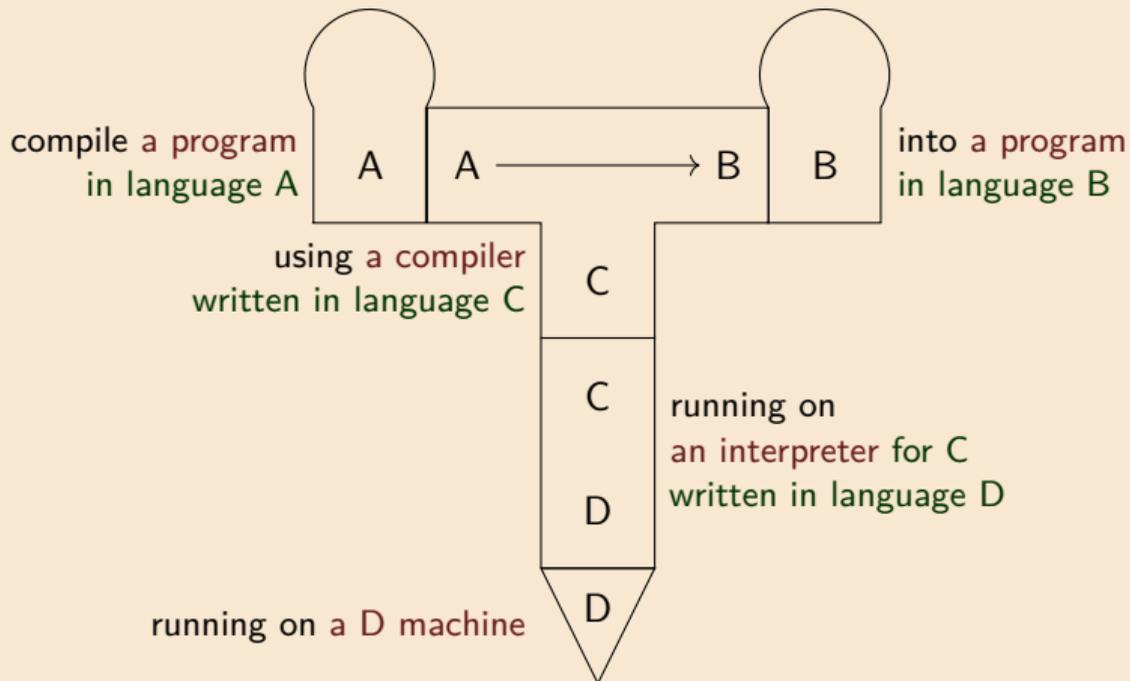
Examples

Compiling compilers

Full bootstrap

Verified compilation

Trusting trust



Running javac on the JVM

Notation

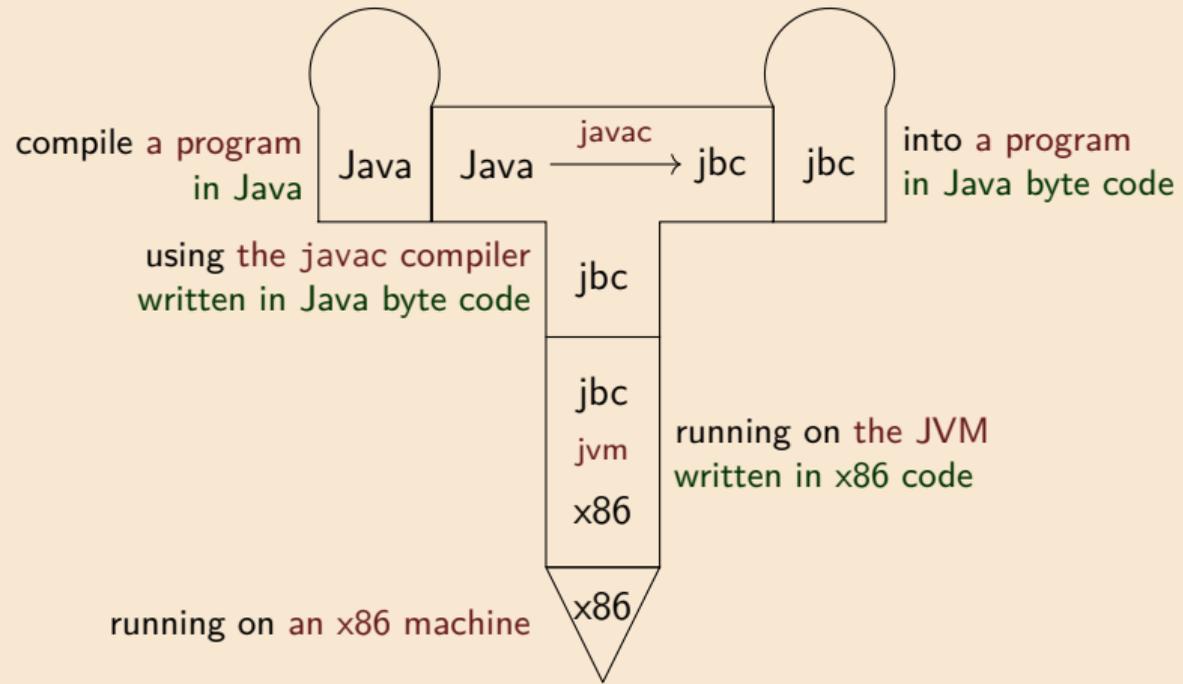
Examples

Compiling compilers

Full bootstrap

Verified compilation

Trusting trust



Ahead-of-time compilation for Java

Notation

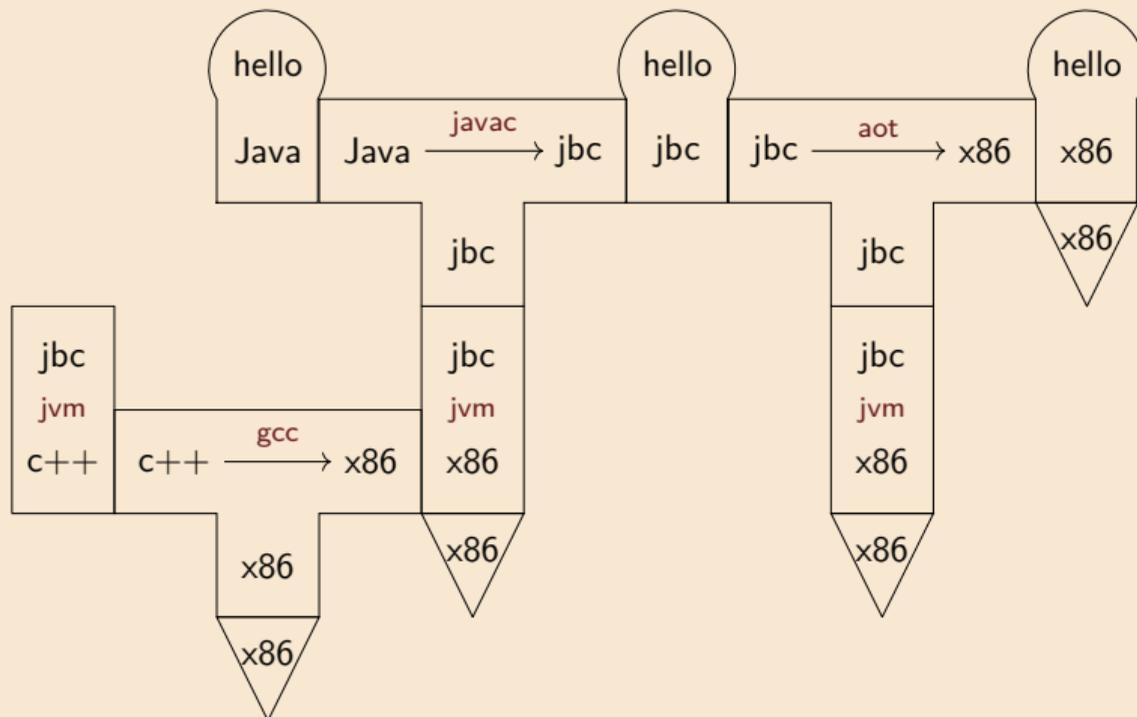
Examples

Compiling compilers

Full bootstrap

Verified compilation

Trusting trust



Thanks to David Greaves for the example

Compiling compilers



Notation

Examples

Compiling
compilers

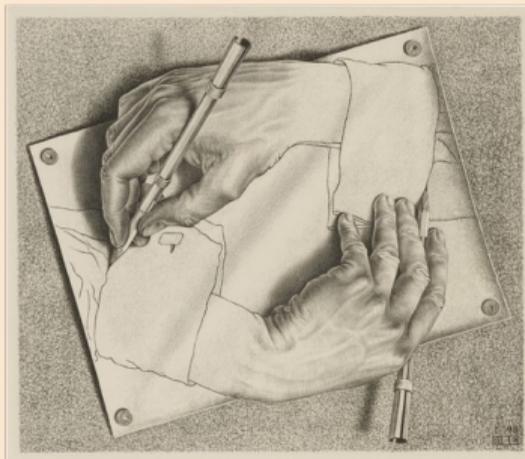


Full
bootstrap

Verified
compilation

Trusting
trust

The OCaml compiler
is written in OCaml



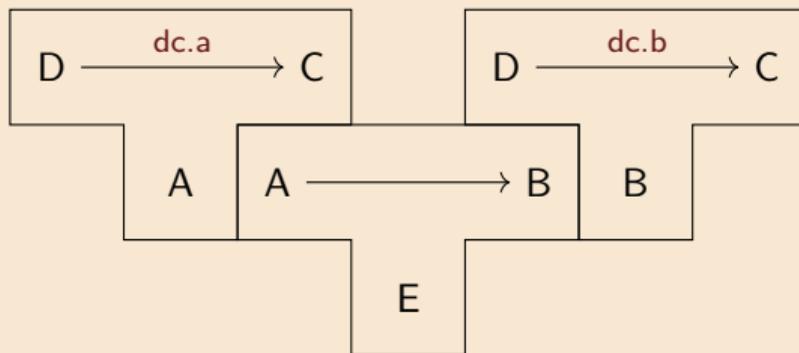
Puzzle: how was the compiler compiled?

Translating translators

Compilers can be translated, just like any other program:

a compiler from **D** to **C**
in language **A**

a compiler from **D** to **C**
in language **B**



compile programs from **A** to **B**

Notation

Examples

Compiling
compilers



Full
bootstrap

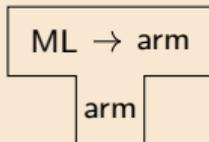
Verified
compilation

Trusting
trust

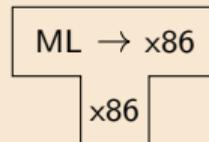
Porting a compiler to a new platform

Notation

We have:
a compiler from ML to arm
that runs on arm



We want:
a compiler from ML to x86
that runs on x86



Examples

Compiling
compilers



Full
bootstrap

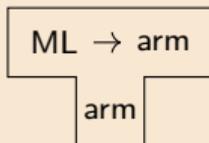
Verified
compilation

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trust

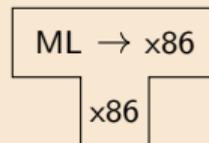
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Examples

Compiling
compilers

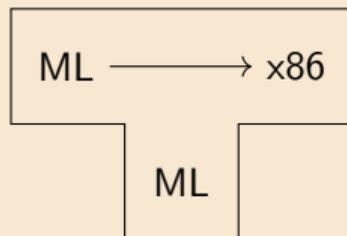


Full
bootstrap

Verified
compilation

Trusting
trust

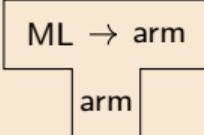
1. write an ML-to-x86 compiler in ML



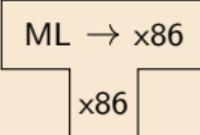
Porting a compiler to a new platform

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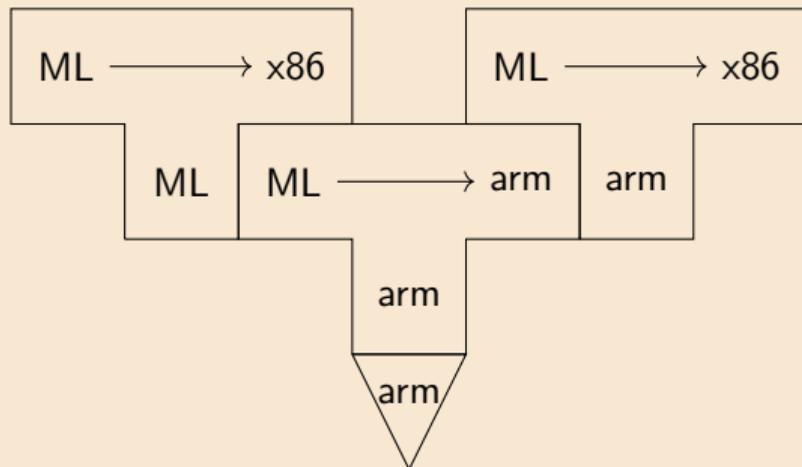
Examples

Compiling
compilers



Full
bootstrap

1. write an ML-to-x86 compiler in ML
2. compile the compiler for arm



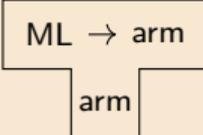
Verified
compilation

Trusting
trust

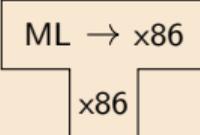
Porting a compiler to a new platform

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Examples

Compiling
compilers

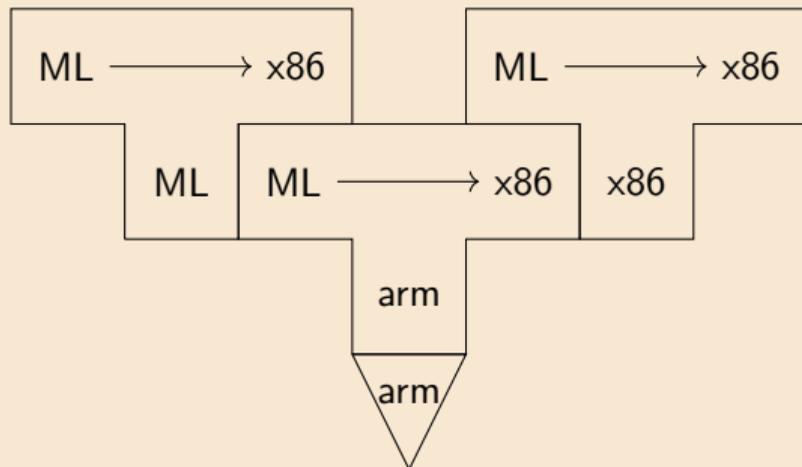


Full
bootstrap

Verified
compilation

Trusting
trust

1. write an ML-to-x86 compiler in ML
2. compile the compiler for arm
3. run the compiler on arm to compile itself



Full bootstrap

Half and full bootstraps

Notation

Examples

Compiling
compilers

Full
bootstrap



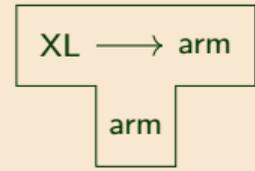
Verified
compilation

Trusting
trust

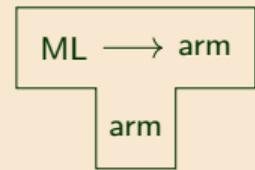
Previous example: *half bootstrap* (needs existing compiler for the language).

New example: *full bootstrap* (no existing ML compiler for the language)

We want:
a compiler from **XL** to arm
that runs on arm



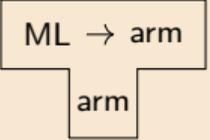
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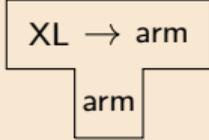
Full bootstrap

Notation

We have:
a compiler from ML to arm
that runs on arm



We want:
a compiler from **XL** to arm
that runs on arm



Examples

Compiling
compilers

Full
bootstrap



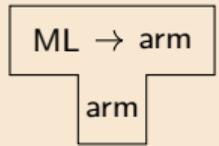
Verified
compilation

Trusting
trust

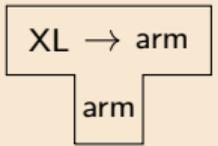
Full bootstrap

Notation

We have:
a compiler from ML to arm
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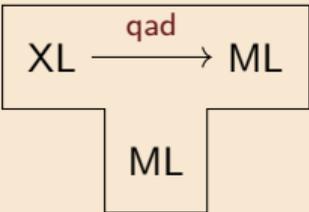
We want:
a compiler from **XL** to arm
that runs on arm



Examples

- 1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML

Compiling compilers



Full bootstrap

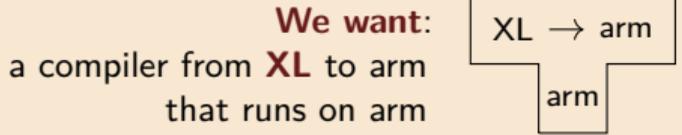
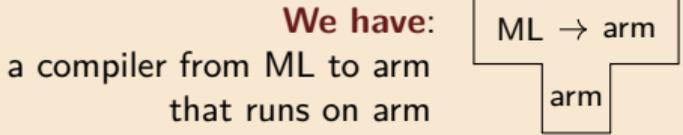


Verified compilation

Trusting trust

Full bootstrap

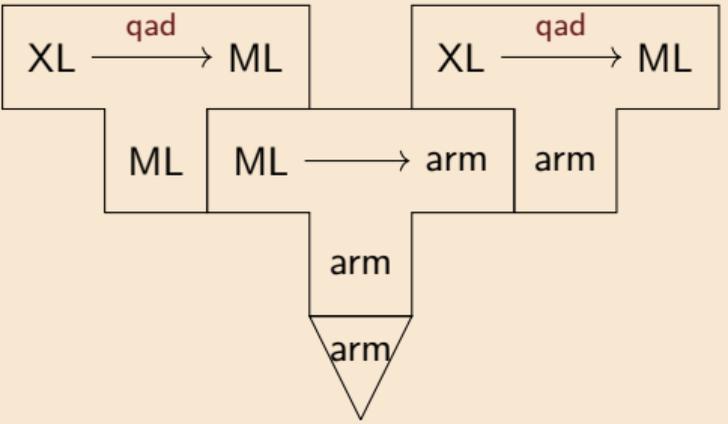
Notation



Examples

1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML

2. compile the QAD compiler for arm



Full bootstrap



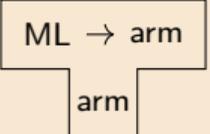
Verified compilation

Trusting trust

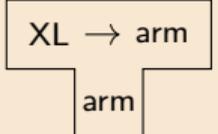
Full bootstrap

Notation

We have: a compiler from ML to arm that runs on arm

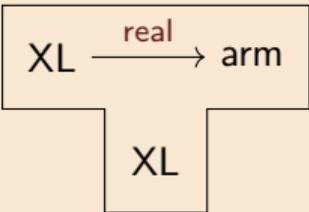


We want: a compiler from **XL** to arm that runs on arm



Examples

1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML
2. compile the QAD compiler for arm
3. Write a real **XL-to-arm** compiler in **XL**



Compiling compilers

Full bootstrap

● ● ○

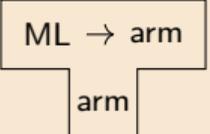
Verified compilation

Trusting trust

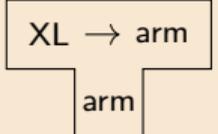
Full bootstrap

Notation

We have: a compiler from ML to arm that runs on arm

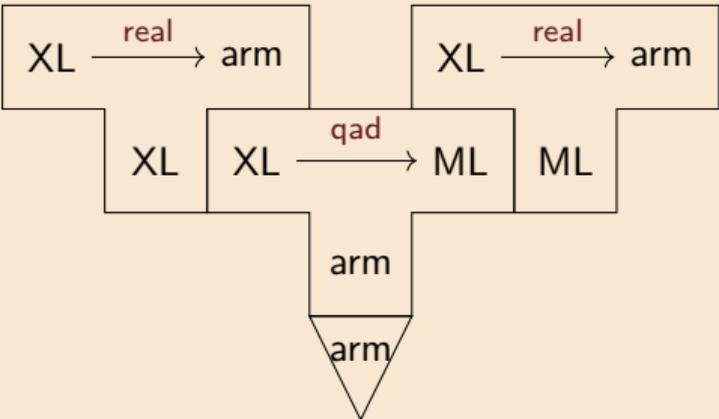


We want: a compiler from **XL** to arm that runs on arm



Examples

1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML
2. compile the QAD compiler for arm
3. Write a real **XL-to-arm** compiler in **XL**
4. Use the QAD compiler to compile the real compiler to ML



Compiling compilers

Full bootstrap



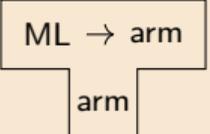
Verified compilation

Trusting trust

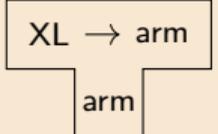
Full bootstrap

Notation

We have: a compiler from ML to arm that runs on arm

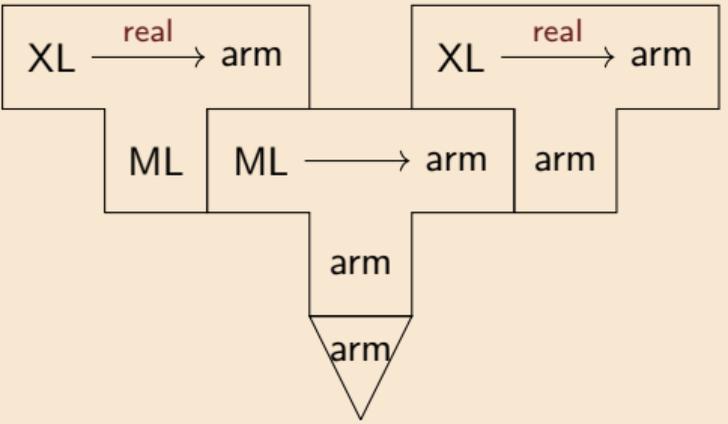


We want: a compiler from **XL** to arm that runs on arm



Examples

1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML
2. compile the QAD compiler for arm
3. Write a real **XL-to-arm** compiler in **XL**
4. Use the QAD compiler to compile the real compiler to ML
5. Compile the resulting ML program to arm



Full bootstrap



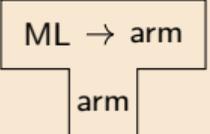
Verified compilation

Trusting trust

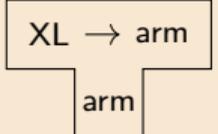
Full bootstrap

Notation

We have: a compiler from ML to arm that runs on arm



We want: a compiler from **XL** to arm that runs on arm



Examples

1. write a quick-and-dirty (QAD) **XL-to-ML** compiler in ML

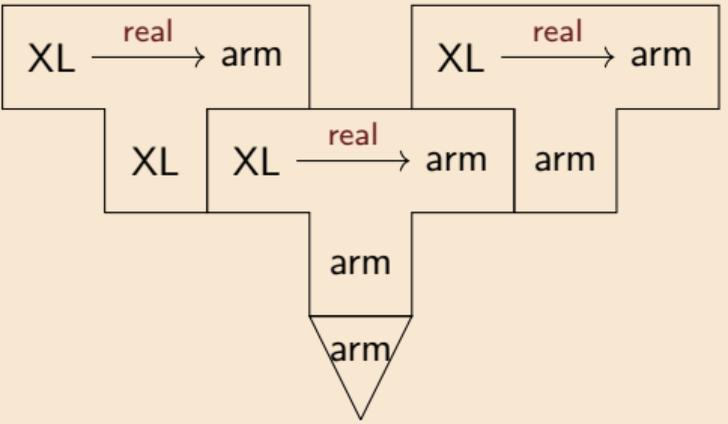
2. compile the QAD compiler for arm

3. Write a real **XL-to-arm** compiler in **XL**

4. Use the QAD compiler to compile the real compiler to ML

5. Compile the resulting ML program to arm

6. Use the generated compiler to compile itself



Compiling compilers

Full bootstrap

● ● ○

Verified compilation

Trusting trust

Notation

Examples

Compiling
compilers

Full
bootstrap



Verified
compilation

Trusting
trust

The *speed* of the quick-and-dirty compiler does not matter much
(We could even use a **quick-and-dirty interpreter** instead)

We don't need to give the quick-and-dirty compiler to users

Once the real compiler works,
we can discard the quick-and-dirty compiler altogether

Verified compilation

New notation: proofs of correctness

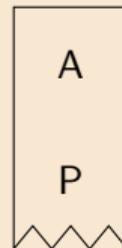
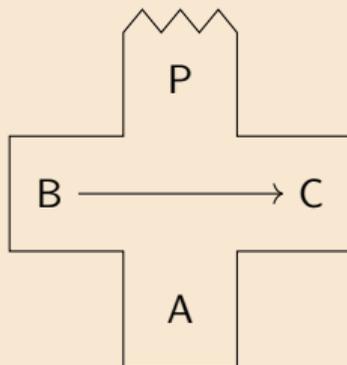
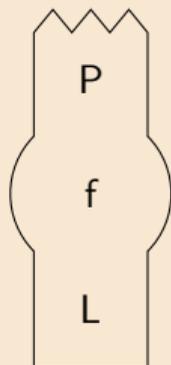
Notation

A verified program

A verified compiler

A proof checker

Examples



Compiling
compilers

Full
bootstrap

Computes function f
written in language L
with a proof in language P

Translates language A into B
written in language C
with a proof in language P

Checks proofs in language P
Written in language A

Verified
compilation



Trusting
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Thanks to Paul D'Souza for the extended notation and the example

Compiling the CakeML verified compiler: $HOL \rightsquigarrow ML$

Notation

The CakeML REPL¹ is written in HOL and compiled to ML code + a proof

Examples

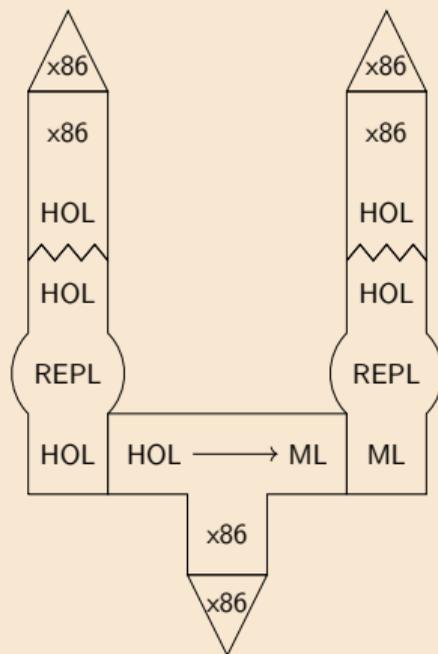
Compiling
compilers

Full
bootstrap

Verified
compilation



Trusting
trust

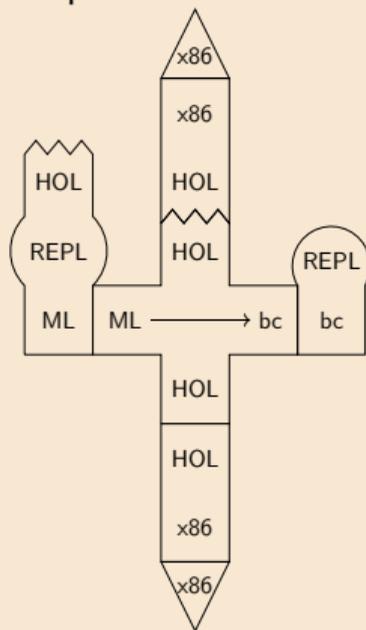


¹ read-eval-print loop

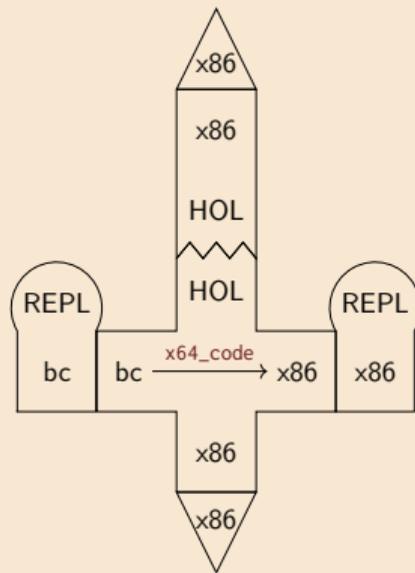
Compiling the CakeML verified compiler: $ML \rightsquigarrow x86$

Notation

Next, the *verified* compiler compiles the REPL to bytecode



Finally, the bytecode is compiled



Theorem (abridged): the x86 REPL behaves according to the original specification

Examples

Compiling compilers

Full bootstrap

Verified compilation



Trusting trust

Trusting trust

Escaping characters

Notation

Aim: modify a compiler to compromise login

Warm up: teach a compiler about vertical tabs

“The cutest program I ever wrote”
– Ken Thompson
(Reflections on Trusting Trust)

Examples

Compiling
compilers

C compilers have code to interpret escape sequences like `\n` in `"Hello, world\n"`:

```
...  
c = next();  
if (c != '\\') return c;  
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
...
```

Full
bootstrap

Q: how can we add support for vertical tabs `\v`?

(Assume the C compiler is bootstrapped.)

Verified
compilation

Trusting
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Teaching the compiler about `\v`

Notation

Step 1: hard-code the ASCII code for `\v` in the compiler source:

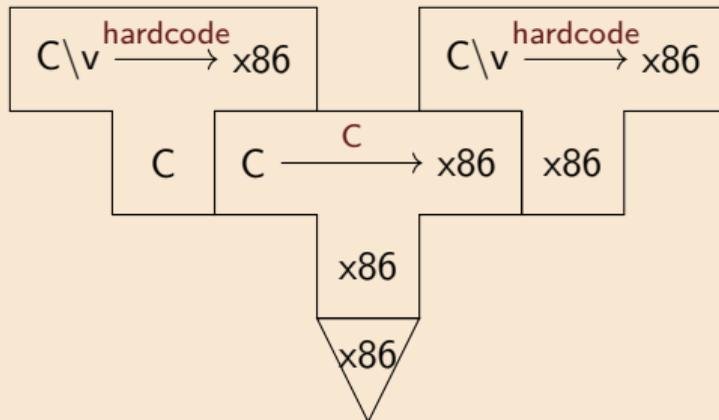
Examples

```
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
if (c == 'v') return 11;  
...
```

Compiling
compilers

Recompile the compiler source using the installed C compiler:

Full
bootstrap



Verified
compilation

Now we have a C compiler that supports `\v` in C programs. Install it.

Trusting
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The compiler has learnt about `\v`

Notation

Step 2: modify the compiler source again to remove the hardcoded constant:

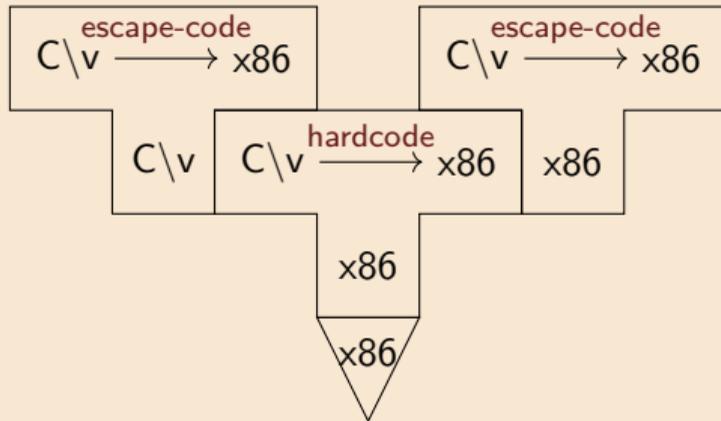
Examples

```
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
if (c == 'v') return '\v';  
...
```

Compiling
compilers

Recompile the modified source using the freshly installed C compiler:

Full
bootstrap



Verified
compilation

The C compiler has learnt to translate `\v` (but there's no record in the source!)

Trusting
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Teaching the compiler to insert backdoors

Notation

Plan: repeat the process to compromise the login command.

Step 1: update the C compiler's code to detect login.c and insert a bug:

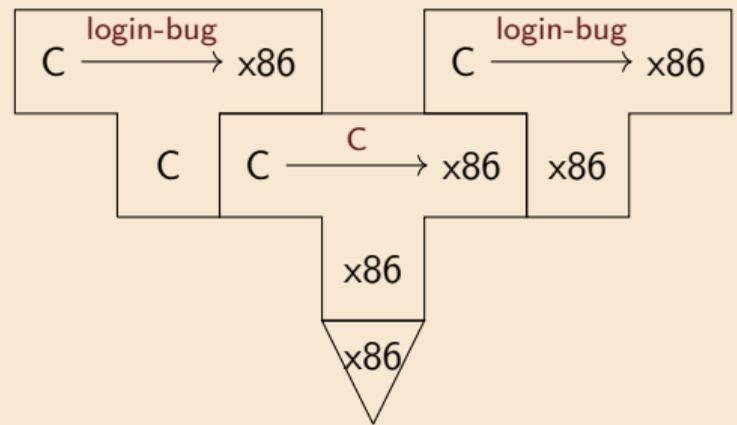
Examples

```
void compile(const char *program) {  
    if (matches(program, "< login code >") {  
        compile("< code for backdoor >");  
    }  
    ...  
}
```

Compiling compilers

Compile and install the new C compiler:

Full bootstrap



Verified compilation

Trusting trust



Notation

Step 2: update the C compiler code to detect compiler.c and insert a 2nd bug:

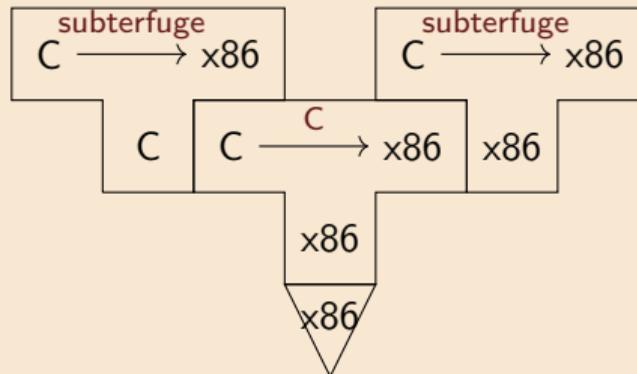
Examples

```
void compile(const char *program) {  
    if (matches(program, "< login code >") {  
        compile("< code for backdoor >");  
    }  
    if (matches(program, "< compiler code >") {  
        compile("< code for miscompilation >");  
    }  
}
```

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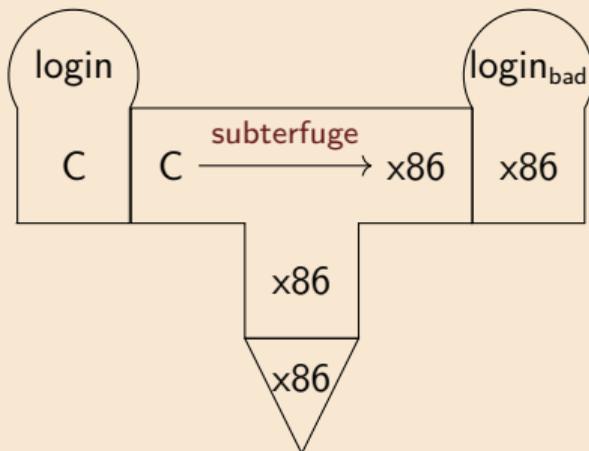
Trusting
trust

Finally: remove the bugs from the compiler source.

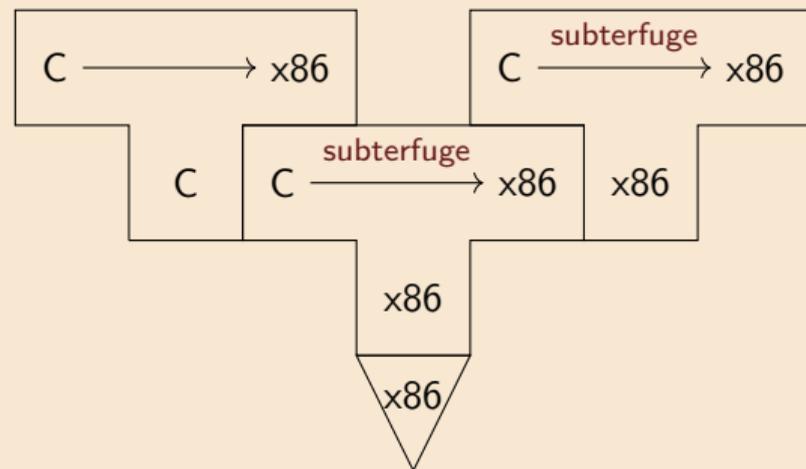
The compiler has learnt to insert backdoors

Notation

The compiler will still miscompile login:



The compiler will now also miscompile the compiler:



Examples

Compiling compilers

Full bootstrap

Verified compilation

The system is **compromised**, with **no trace** in the login or compiler source. We need to *debootstrap* to recover an uncompromised compiler.

Trusting trust



