

Compiler Construction

Lecture 16



Bootstrapping

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Chapter 13 of

Basics of Compiler Design

Torben Ægidius Mogensen

<http://hjemmesider.diku.dk/~torbenm/Basics/>

Notation

Notation: programs, interpreters, machines

Notation



Examples

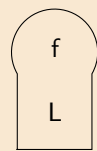
Compiling compilers

Full bootstrap

Verified compilation

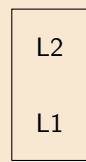
Trusting trust

A program



Computes function f
written in language L

An interpreter



Interprets language $L2$
written in language $L1$

A machine



Executes code
in language L

Notation



Examples

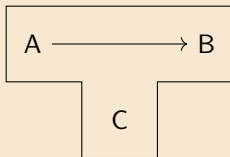
Compiling compilers

Full bootstrap

Verified compilation

Trusting trust

A compiler



Translates language A into language B
Written in language C

Examples

Executing programs

Notation

Examples

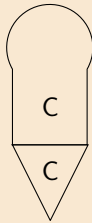
Compiling
compilers

Full
bootstrap

Verified
compilation

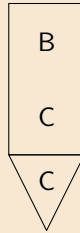
Trusting
trust

To execute a program



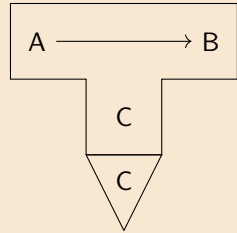
we run it on a machine

To execute an interpreter



we run it on a machine

To execute a compiler



we run it on a machine

Interpreting a program

Notation

Examples

Compiling
compilers

Full
bootstrap

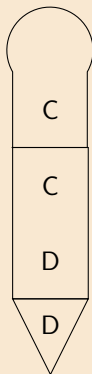
Verified
compilation

Trusting
trust

Run a program
written in language C

on an interpreter for C
written in language D

on a D machine



(Note: the languages must match)

Interpreting a Java program

Notation

Examples

Compiling
compilers

Full
bootstrap

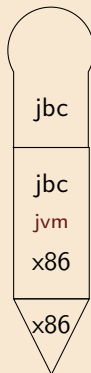
Verified
compilation

Trusting
trust

Run a program
written in Java byte code

on an interpreter for Java byte code
written in x86 code

on a x86 machine



Running a compiler on an interpreter

Notation

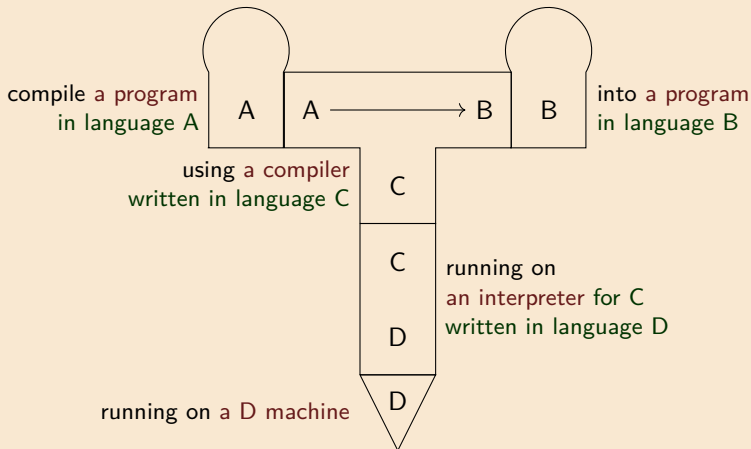
Examples

Compiling
compilers

Full
bootstrap

Verified
compilation

Trusting
trust



Running javac on the JVM

Notation

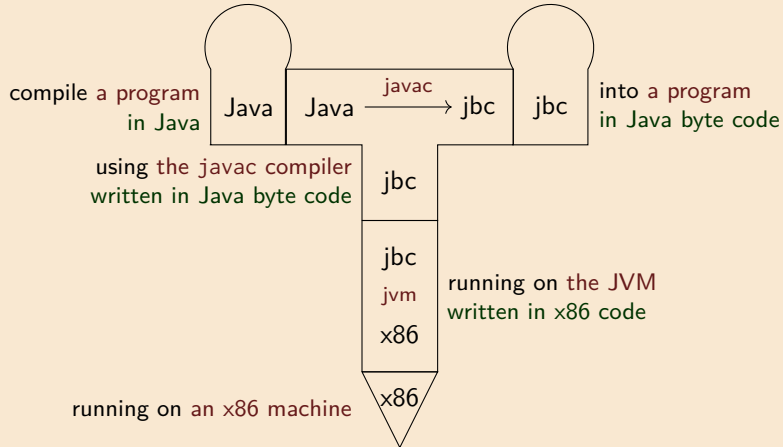
Examples

Compiling
compilers

Full
bootstrap

Verified
compilation

Trusting
trust



Ahead-of-time compilation for Java

Notation

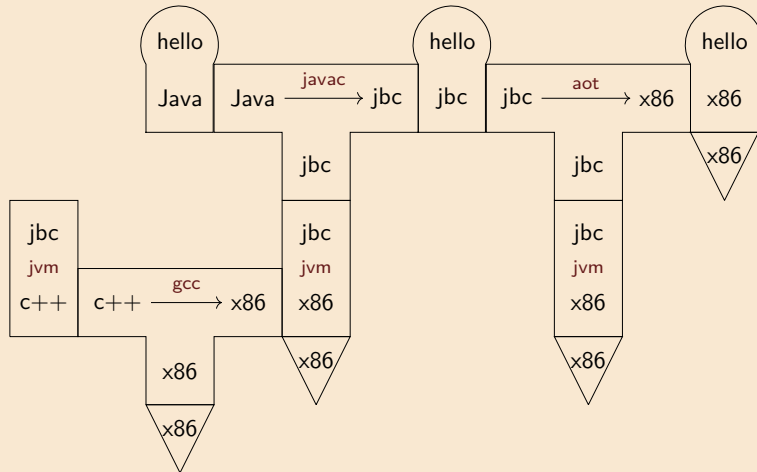
Examples

Compiling
compilers

Full
bootstrap

Verified
compilation

Trusting
trust



Thanks to David Greaves for the example

Compiling compilers



Notation

Examples

Compiling
compilers

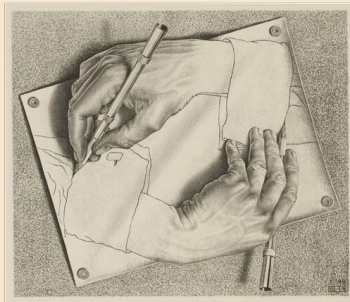


Full
bootstrap

Verified
compilation

Trusting
trust

The OCaml compiler
is written in OCaml



Puzzle: how was the compiler compiled?

Translating translators

Notation

Examples

Compiling
compilers



Full
bootstrap

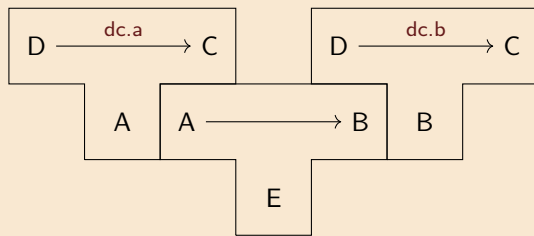
Verified
compilation

Trusting
trust

Compilers can be translated, just like any other program:

a compiler from **D** to **C**
in language **A**

a compiler from **D** to **C**
in language **B**

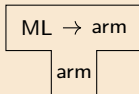


compile programs from **A** to **B**

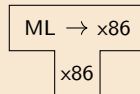
Porting a compiler to a new platform

Notation

We have:
a compiler from ML to arm
that runs on arm



We want:
a compiler from ML to x86
that runs on x86



Examples

Compiling
compilers

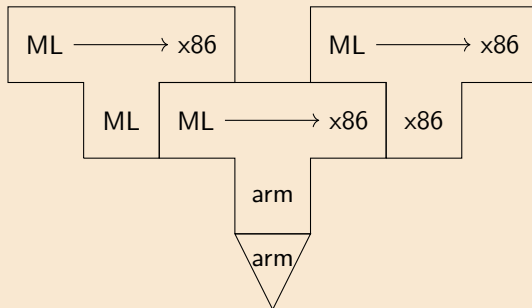


Full
bootstrap

Verified
compilation

Trusting
trust

1. write an ML-to-x86 compiler in ML
2. compile the compiler for arm
3. run the compiler on arm to compile itself



Full bootstrap

Half and full bootstraps

Notation

Examples

Compiling
compilers

Full
bootstrap



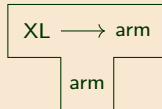
Verified
compilation

Trusting
trust

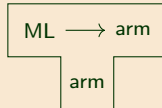
Previous example: *half bootstrap* (needs existing compiler for the language).

New example: *full bootstrap* (no existing ML compiler for the language)

We want:
a compiler from **XL** to arm
that runs on arm



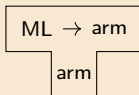
We have:
a compiler from ML to arm
that runs on arm



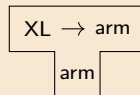
Full bootstrap

Notation

We have:
a compiler from ML to arm
that runs on arm



We want:
a compiler from **XL** to arm
that runs on arm



Examples

1. write a quick-and-dirty (QAD)
XL-to-ML compiler in ML

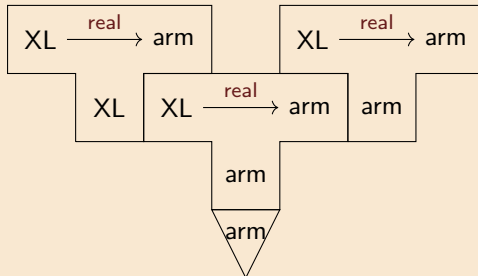
2. compile the QAD compiler for arm

3. Write a real **XL-to-arm** compiler in **XL**

4. Use the QAD compiler to compile
the real compiler to ML

5. Compile the resulting ML program to arm

6. Use the generated compiler to compile itself



Compiling compilers

Full bootstrap



Verified compilation

Trusting trust

Notation

Examples

Compiling
compilers

Full
bootstrap



Verified
compilation

Trusting
trust

The *speed* of the quick-and-dirty compiler does not matter much
(We could even use a **quick-and-dirty interpreter** instead)

We don't need to give the quick-and-dirty compiler to users

Once the real compiler works,
we can discard the quick-and-dirty compiler altogether

Verified compilation

New notation: proofs of correctness

Notation

Examples

Compiling
compilers

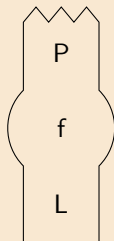
Full
bootstrap

Verified
compilation



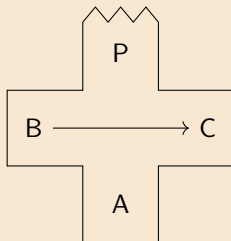
Trusting
trust

A verified program



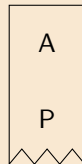
Computes function f
written in language L
with a proof in language P

A verified compiler



Translates language A into B
written in language C
with a proof in language P

A proof checker



Checks proofs in language P
Written in language A

Thanks to Paul D'Souza for the extended notation and the example

Compiling the CakeML verified compiler: $HOL \rightsquigarrow ML$

Notation

The CakeML REPL¹ is written in HOL and compiled to ML code + a proof

Examples

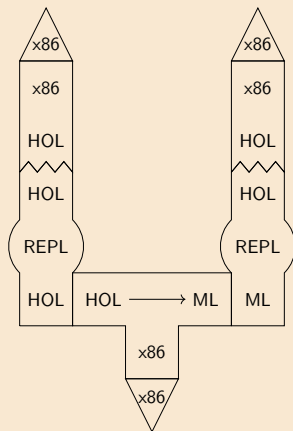
Compiling
compilers

Full
bootstrap

Verified
compilation



Trusting
trust



¹ read-eval-print loop

Compiling the CakeML verified compiler: $ML \rightsquigarrow x86$

Notation

Examples

Compiling
compilers

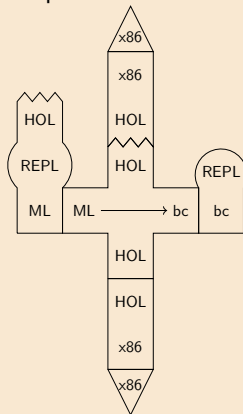
Full
bootstrap

Verified
compilation

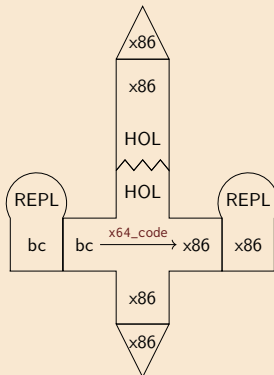


Trusting
trust

Next, the *verified* compiler
compiles the REPL to bytecode



Finally, the bytecode is compiled



Theorem (abridged): the x86 REPL behaves according to the original specification

Trusting trust

Escaping characters

Notation

Examples

Compiling
compilers

Full
bootstrap

Verified
compilation

Trusting
trust



"The cutest program I ever wrote"
– Ken Thompson
(Reflections on Trusting Trust)

Aim: modify a compiler to compromise login

Warm up: teach a compiler about vertical tabs

C compilers have code to interpret escape sequences like `\n` in `"Hello, world\n"`:

```
...  
c = next();  
if (c != '\\') return c;  
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
...
```

Q: how can we add support for vertical tabs `\v`?

(Assume the C compiler is bootstrapped.)

Teaching the compiler about `\v`

Notation

Step 1: hard-code the ASCII code for `\v` in the compiler source:

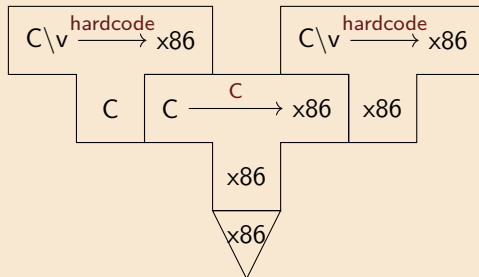
Examples

```
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
if (c == 'v') return 11;  
...
```

Compiling
compilers

Recompile the compiler source using the installed C compiler:

Full
bootstrap



Verified
compilation

Trusting
trust

Now we have a C compiler that supports `\v` in C programs. Install it.

The compiler has learnt about `\v`

Notation

Step 2: modify the compiler source again to remove the hardcoded constant:

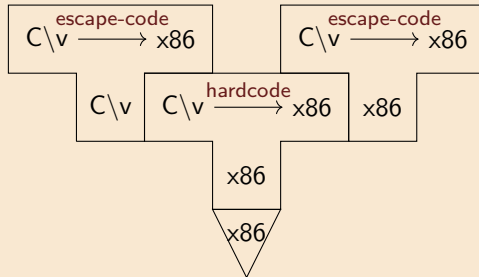
Examples

```
c = next();  
if (c == '\\') return '\\';  
if (c == 'n') return '\n';  
if (c == 'v') return '\v';  
...
```

Compiling
compilers

Recompile the modified source using the freshly installed C compiler:

Full
bootstrap



Verified
compilation

Trusting
trust

The C compiler has learnt to translate `\v` (but there's no record in the source!)

Teaching the compiler to insert backdoors

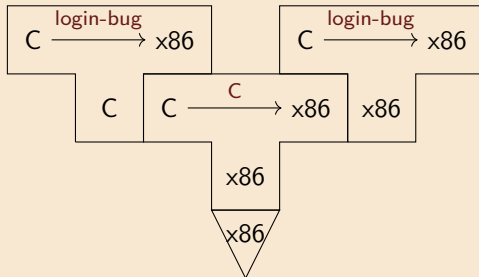
Notation

Plan: repeat the process to compromise the login command.

Step 1: update the C compiler's code to detect login.c and insert a bug:

```
void compile(const char *program) {  
    if (matches(program, "< login code >") {  
        compile("< code for backdoor >");  
    }  
    ...  
}
```

Compile and install the new C compiler:



Examples

Compiling
compilers

Full
bootstrap

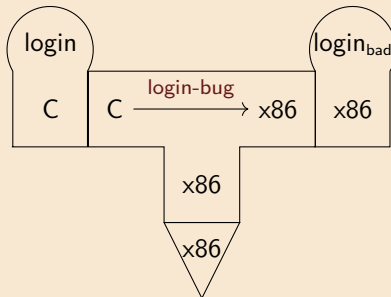
Verified
compilation

Trusting
trust



Notation

Now the compiler will miscompile login:



Problem: people will easily spot the bug in the compiler source.

Trusting
trust



Notation

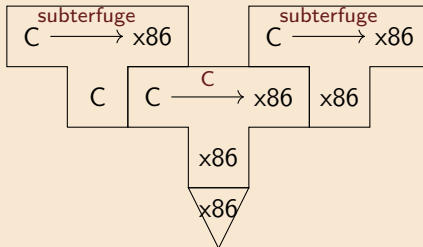
Step 2: update the C compiler code to detect compiler.c and insert a 2nd bug:

Examples

```
void compile(const char *program) {  
    if (matches(program, "< login code >") {  
        compile("< code for backdoor >");  
    }  
    if (matches(program, "< compiler code >") {  
        compile("< code for miscompilation >");  
    }  
}
```

Compiling
compilers

Compile and install the new C compiler:



Finally: remove the bugs from the compiler source.

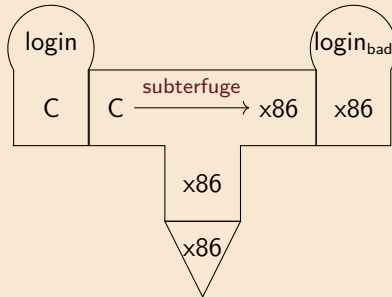
Trusting
trust



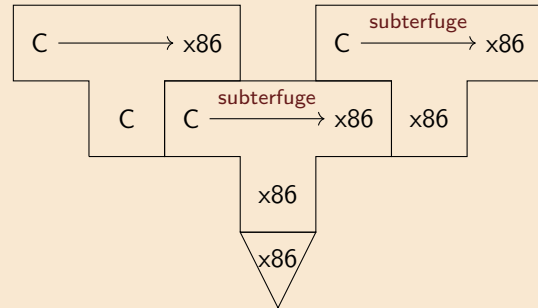
The compiler has learnt to insert backdoors

Notation

The compiler will still miscompile login:



The compiler will now also miscompile the compiler:



The system is **compromised**, with **no trace** in the login or compiler source. We need to *debootstrap* to recover an uncompromised compiler.

Examples

Compiling compilers

Full bootstrap

Verified compilation

Trusting trust



