



## Advanced Graphics and Image Processing

# High dynamic range and tone mapping

## Part 1/2 – context, the need for tone-mapping

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# Cornell Box: need for tone-mapping in graphics

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Rendering



Photograph

# Real-world scenes are more challenging

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- ▶ The match could not be achieved if the light source in the top of the box was visible
- ▶ The display could not reproduce the right level of brightness

# Dynamic range



Luminance  
↓  
 $\frac{\max L}{\min L}$   
↑  
(for SNR>3)

# Dynamic range (contrast)

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- ▶ As ratio:

$$C = \frac{L_{\max}}{L_{\min}}$$

- ▶ Usually written as C:1, for example 1000:1.

- ▶ As “orders of magnitude”  
or log10 units:

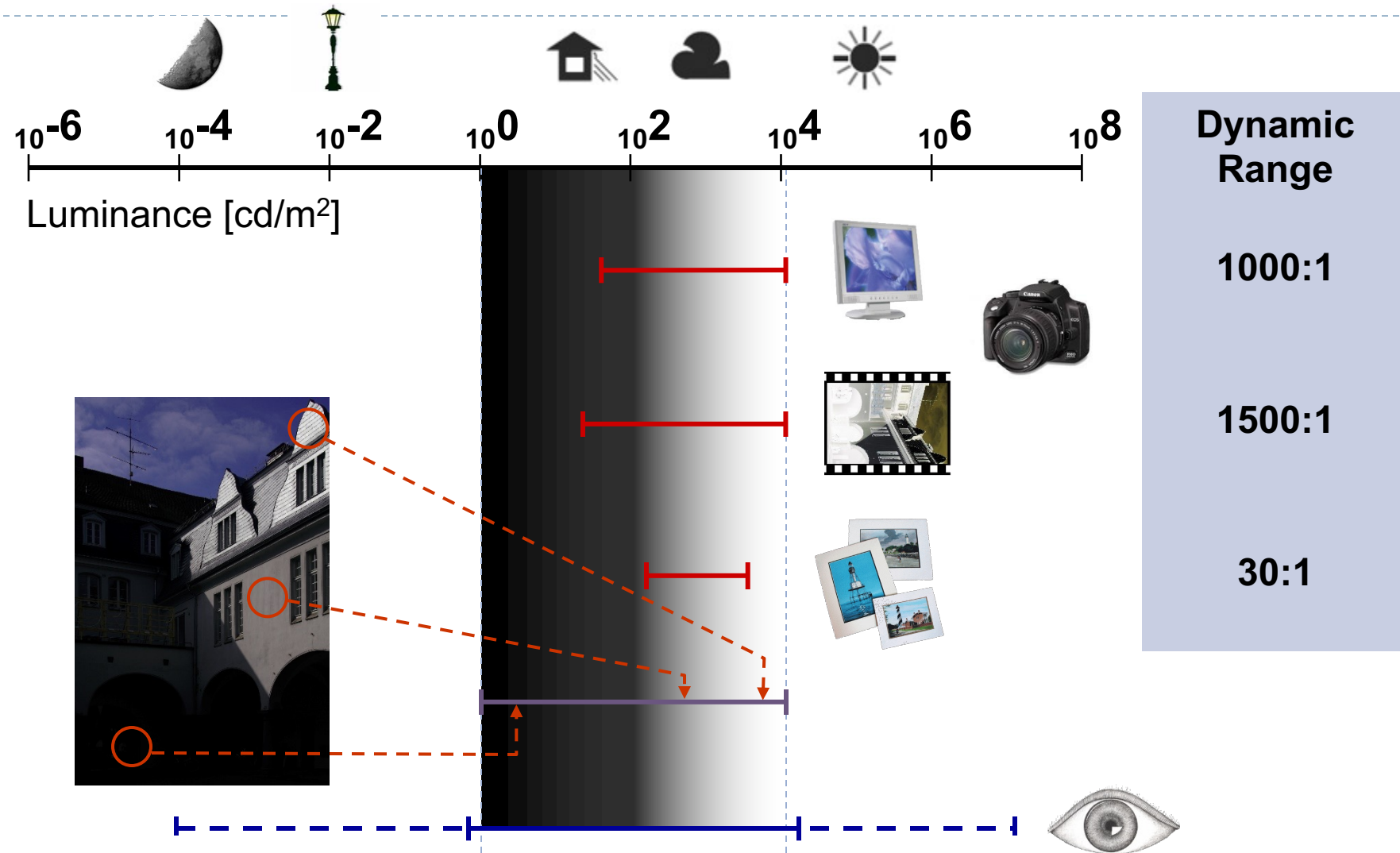
$$C_{10} = \log_{10} \frac{L_{\max}}{L_{\min}}$$

- ▶ As stops:

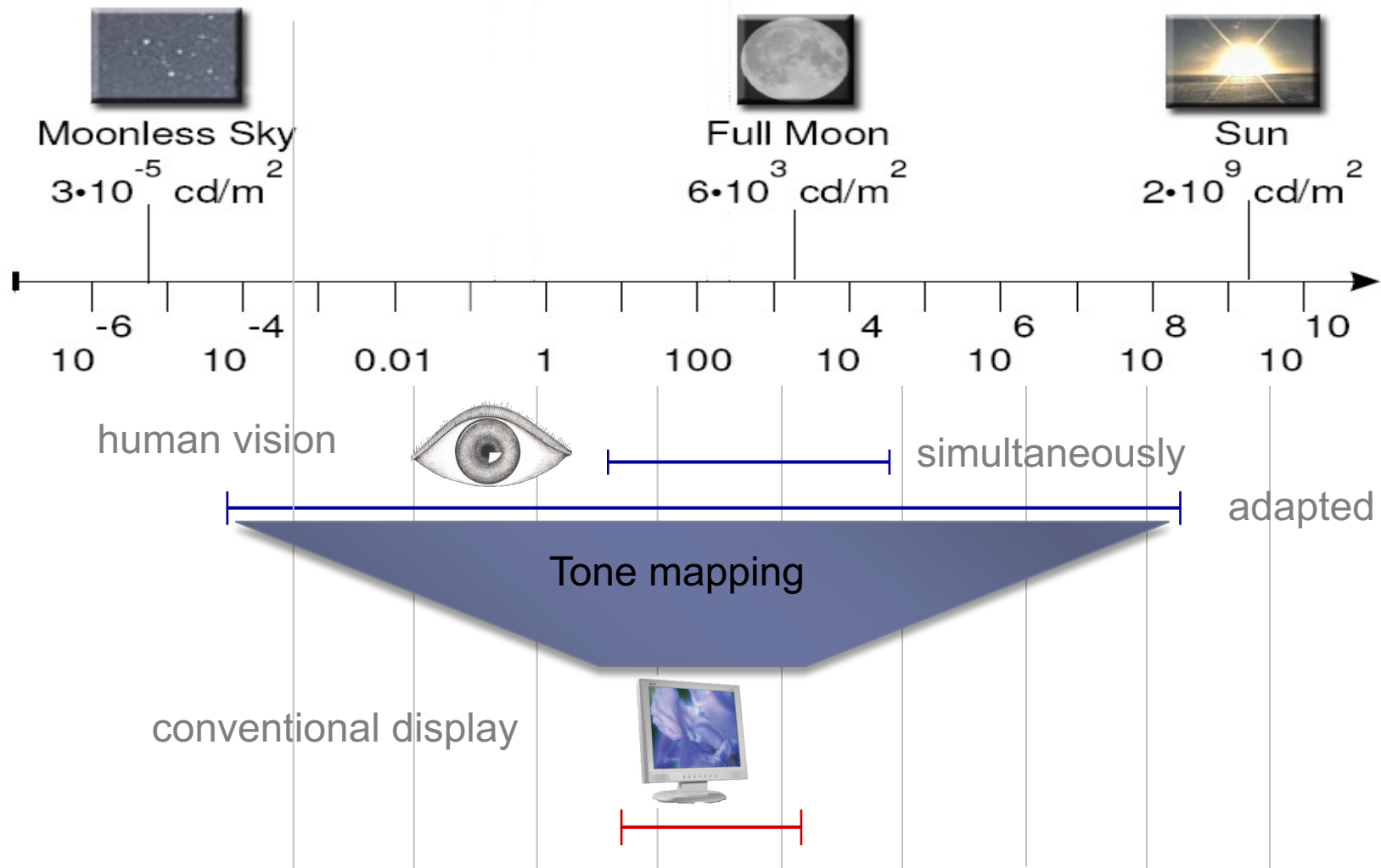
$$C_2 = \log_2 \frac{L_{\max}}{L_{\min}}$$

One stop is doubling  
of halving the amount of light

# High dynamic range (HDR)



# Tone-mapping problem





# Why do we need tone mapping?

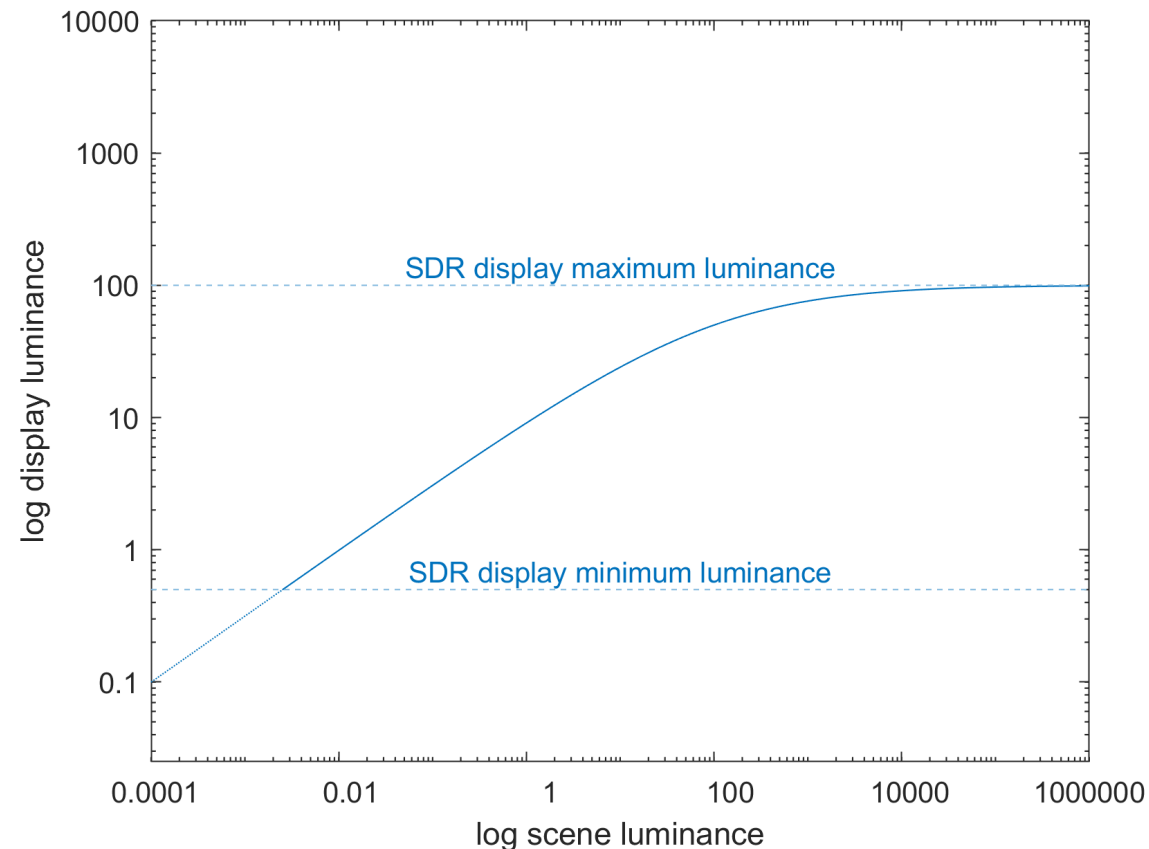
- ▶ To **reduce dynamic range**
- ▶ To **customize the look**
  - ▶ colour grading
- ▶ To **simulate human vision**
  - ▶ for example night vision
- ▶ To adapt displayed images to a **display and viewing conditions**
- ▶ To make rendered images look **more realistic**
- ▶ To map from **scene- to display-referred** colours
- ▶ Different tone mapping operators achieve different goals





# From scene- to display-referred colours

- ▶ The primary purpose of tone mapping is to transform an image from *scene-referred* to *display-referred* colours



# Tone-mapping in rendering

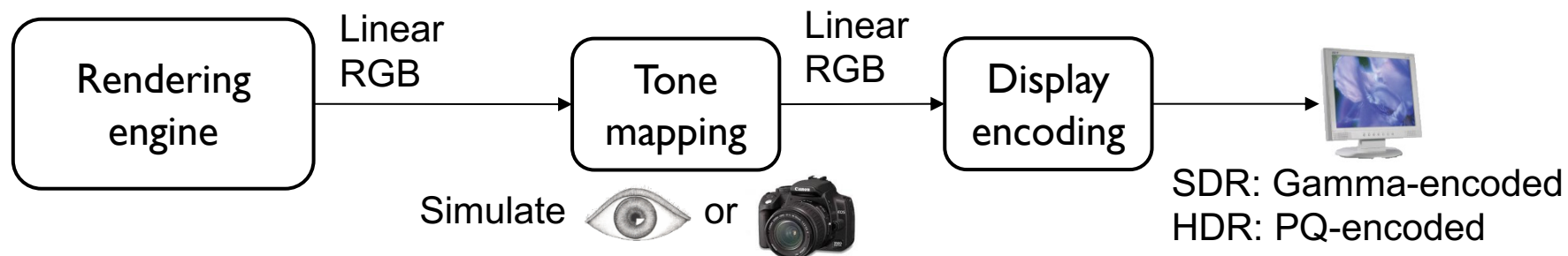
- ▶ Any physically-based rendering requires tone-mapping
- ▶ “HDR rendering” in games is pseudo-physically-based rendering
- ▶ Goal: to simulate a camera or the eye
- ▶ Greatly enhances realism

LDR illumination  
No tone-mapping

HDR illumination  
Tone-mapping



Half-Life 2: Lost coast



# Basic tone-mapping and display coding

- ▶ The simplest form of tone-mapping is the exposure/brightness adjustment:

$$R_d = \frac{R_s}{L_{white}}$$

Diagram annotations:

- Display-referred red value (points to  $R_d$ )
- Scene-referred (points to  $R_s$ )
- Scene-referred luminance of white (points to  $L_{white}$ )

- ▶ R for red, the same for green and blue
- ▶ No contrast compression, only for a moderate dynamic range

- ▶ The simplest form of display coding is the “gamma”

$$R' = (R_d)^{\frac{1}{\gamma}}$$

Diagram annotations:

- Prime (') denotes a gamma-corrected value (points to  $R'$ )
- Typically  $\gamma=2.2$  (points to  $\gamma$ )

- ▶ For SDR displays only

UNIVERSITY OF  
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COMPUTER LABORATORY



**Advanced Graphics and Image Processing**

# **High dynamic range and tone mapping**

## **Part 2/2 – tone mapping techniques**

Rafał Mantiuk

*Computer Laboratory, University of Cambridge*

# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Colour transfer
- ▶ Base-detail separation
- ▶ Glare

# Arithmetic of HDR images

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- ▶ How do the basic arithmetic operations

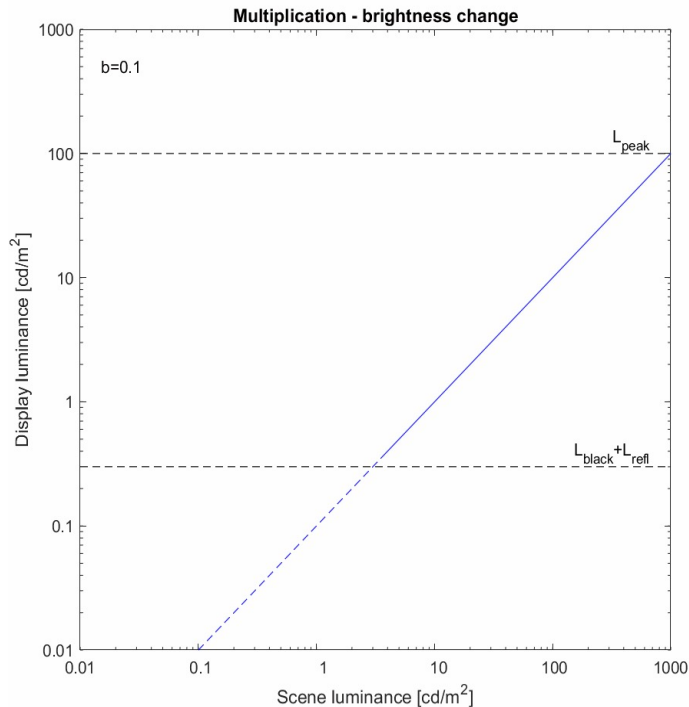
- ▶ Addition
- ▶ Multiplication
- ▶ Power function

affect the appearance of an HDR image?

- ▶ We work in the luminance space (NOT luma)
- ▶ The same operations can be applied to linear RGB
  - ▶ Or only to luminance and the colour can be transferred



# Multiplication – brightness change



Resulting  
luminance

Input  
luminance

$$T(L_p) = b \cdot L_p$$

Brightness change  
parameter

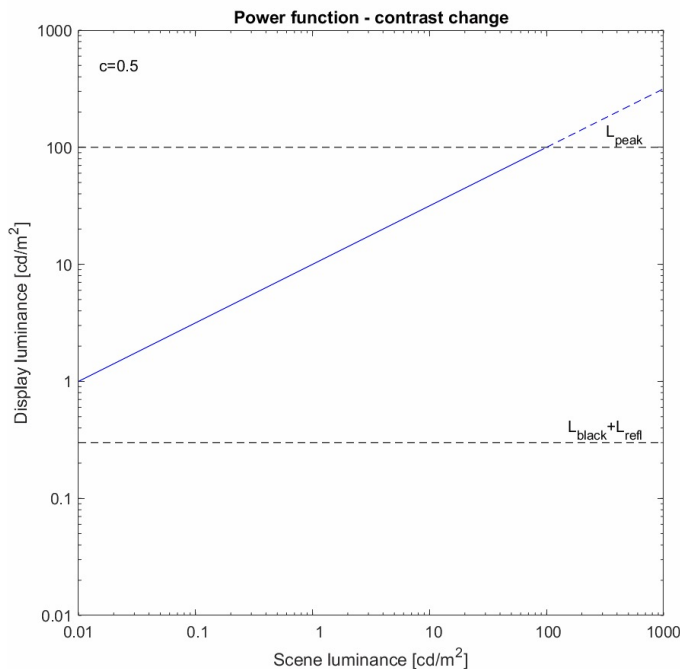
- Multiplication makes the image brighter or darker
- It does not change the dynamic range!

# Power function – contrast change

$$T(L_p) = L_{peak} \left( \frac{L_p}{L_{white}} \right)^c$$

Contrast change  
(gamma)

Luminance to be  
mapped to white

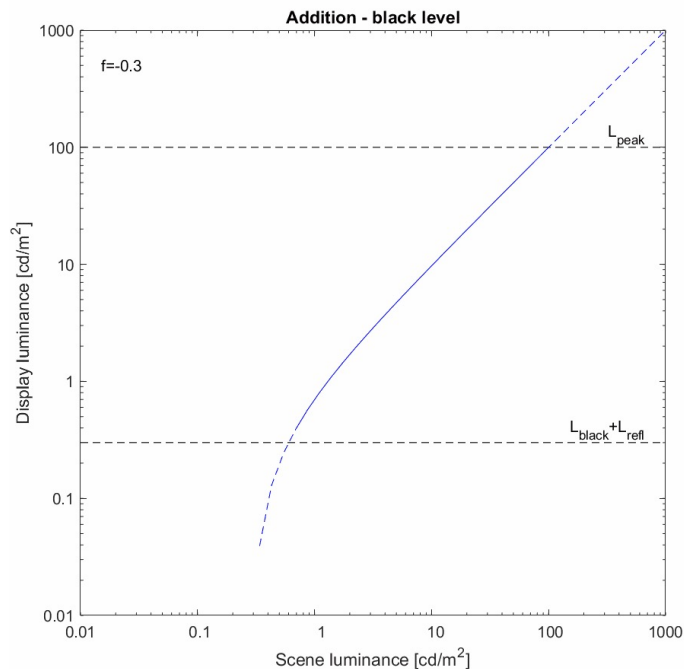


- ▶ Power function stretches or shrinks the dynamic range of an image
- ▶ It is usually performed relative to a reference white colour (and luminance)
- ▶ Side effect: brightness of the dark image part will change
- ▶ Slope on a log-log plot explains contrast change

# Addition – black level

$$T(L_p) = L_p + f$$

Black level  
(flare, fog)



- ▶ Addition elevates black level, adds „fog” to an image
- ▶ It affects mostly darker tones
- ▶ It reduces image dynamic range
- ▶ Subtraction can compensate for ambient light

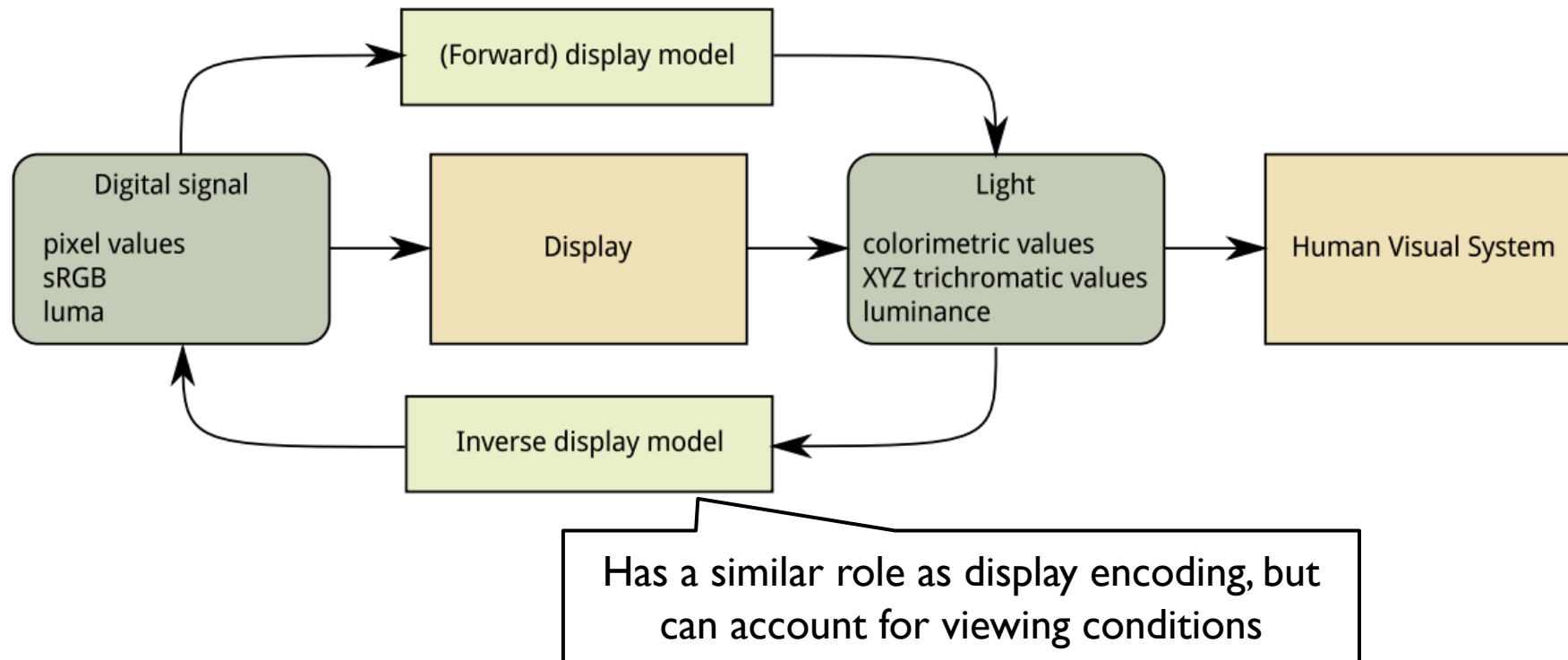
# Techniques

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- ▶ Arithmetic of HDR images
- ▶ **Display model**
- ▶ Tone-curve
- ▶ Colour transfer
- ▶ Base-detail separation
- ▶ Glare

# Display-adaptive tone mapping

- ▶ Tone-mapping can account for the physical model of a display
  - ▶ How a display transforms pixel values into emitted light
  - ▶ Useful for ambient light compensation



# (Forward) Display model (SDR)

## ► GOG: Gain-Offset-Gamma

Luminance

Display peak  
luminance

Gamma

Display  
black level

Screen  
reflections

$$L = (L_{peak} - L_{black})V^\gamma + L_{black} + L_{refl}$$

Gain

Pixel value  
0-1

Offset

Reflectance  
factor (0.01)

$$L_{refl} = \frac{k}{\pi} E_{amb}$$

Ambient illumination  
(in lux)

(\*) assuming a matt screen



# Inverse display model

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Symbols are the same as for the forward display model

$$V = \left( \frac{L - L_{black} - L_{refl}}{L_{peak} - L_{black}} \right)^{(1/\gamma)}$$

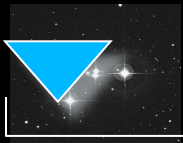
Note: This display model does not address any colour issues. The same equation is applied to red, green and blue colour channels. The assumption is that the display primaries are the same as for the sRGB colour space.

# Ambient illumination compensation

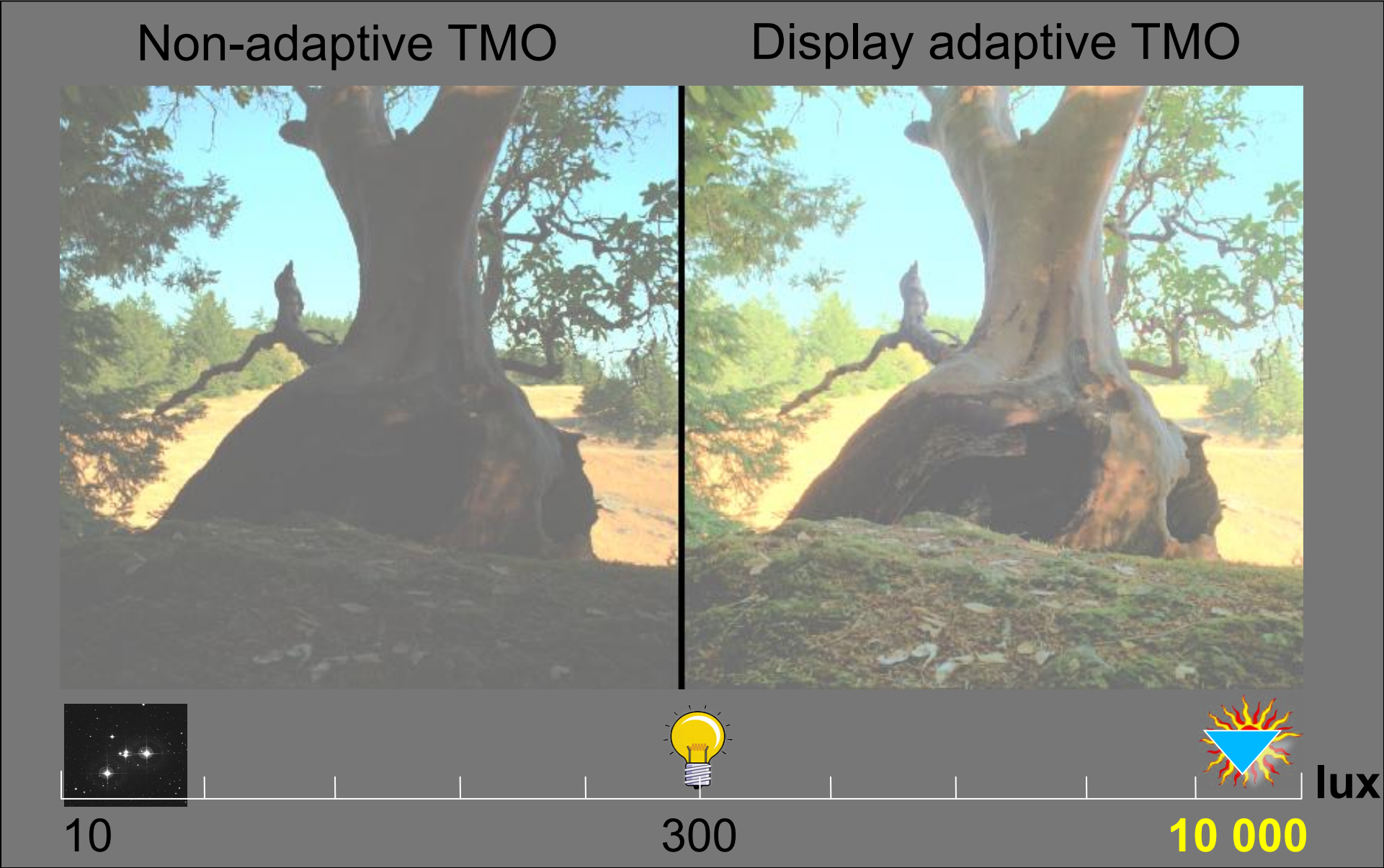
Non-adaptive TMO



Display adaptive TMO



# Ambient illumination compensation



# Example: Ambient light compensation

- ▶ We are looking at the screen in bright light

$$L_{peak} = 100 [cd \cdot m^{-2}]$$

$$k = 0.005$$

Modern screens have  
reflectivity of around 0.5%

$$L_{black} = 0.1 [cd \cdot m^{-2}]$$

$$E_{amb} = 2000 [lux] \quad L_{refl} = \frac{0.005}{\pi} 2000 = 3.183 [cd \cdot m^{-2}]$$

- ▶ We assume that the dynamic of the input is 2.6 ( $\approx 400:1$ )

$$r_{in} = 2.6 \quad r_{out} = \log_{10} \frac{L_{peak}}{L_{black} + L_{refl}} = 1.77$$

- ▶ First, we need to compress contrast to fit the available dynamic range, then compensate for ambient light

$$L_{out} = L_{wp} \left( \frac{L_{in}}{L_{wp}} \right)^{\frac{r_{out}}{r_{in}}} - L_{refl}$$

The resulting value is in luminance,  
must be mapped to display luma /  
gamma corrected values  
(display encoded)

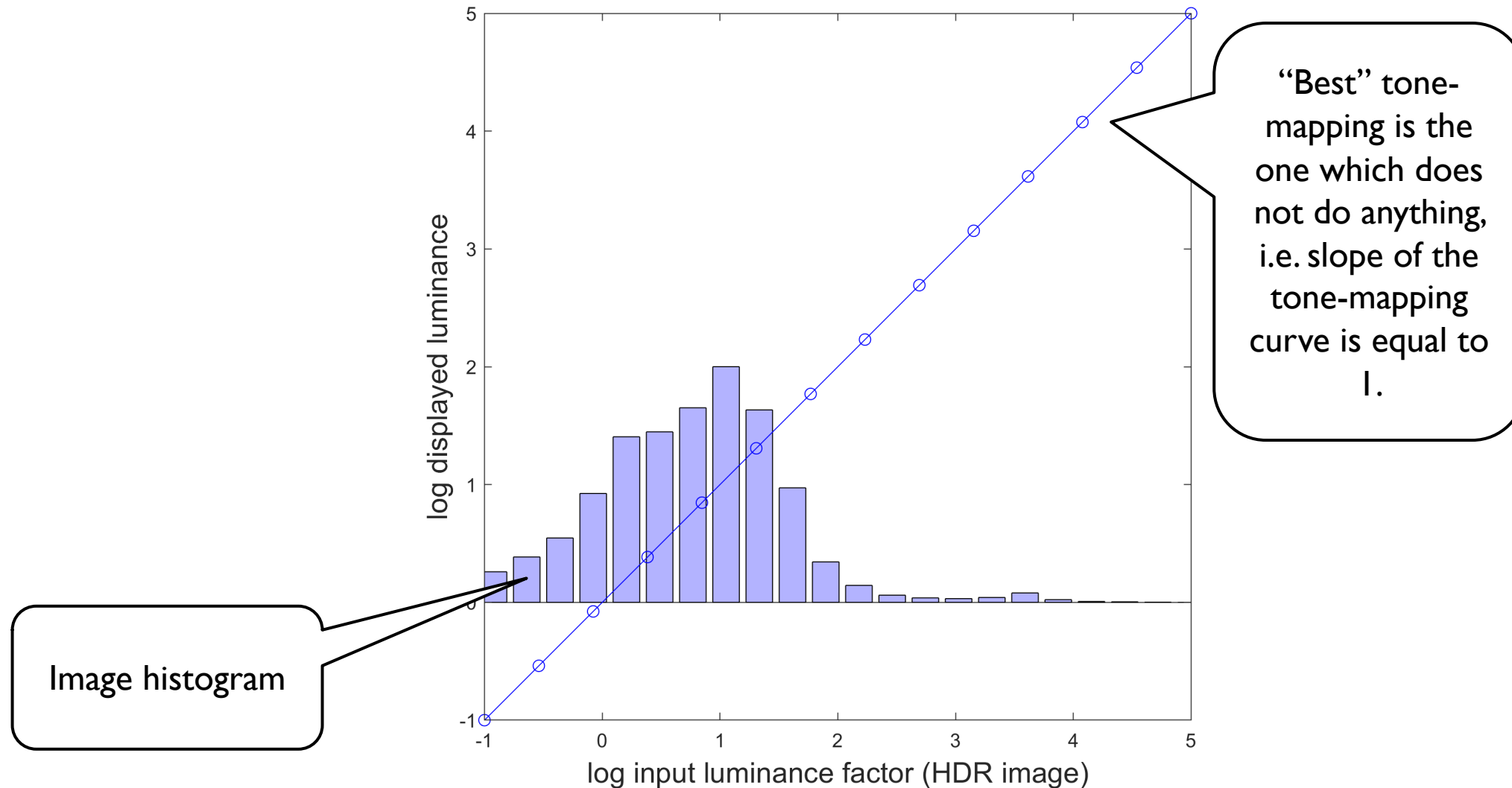
Simplest, but not the  
best tone mapping

# Techniques

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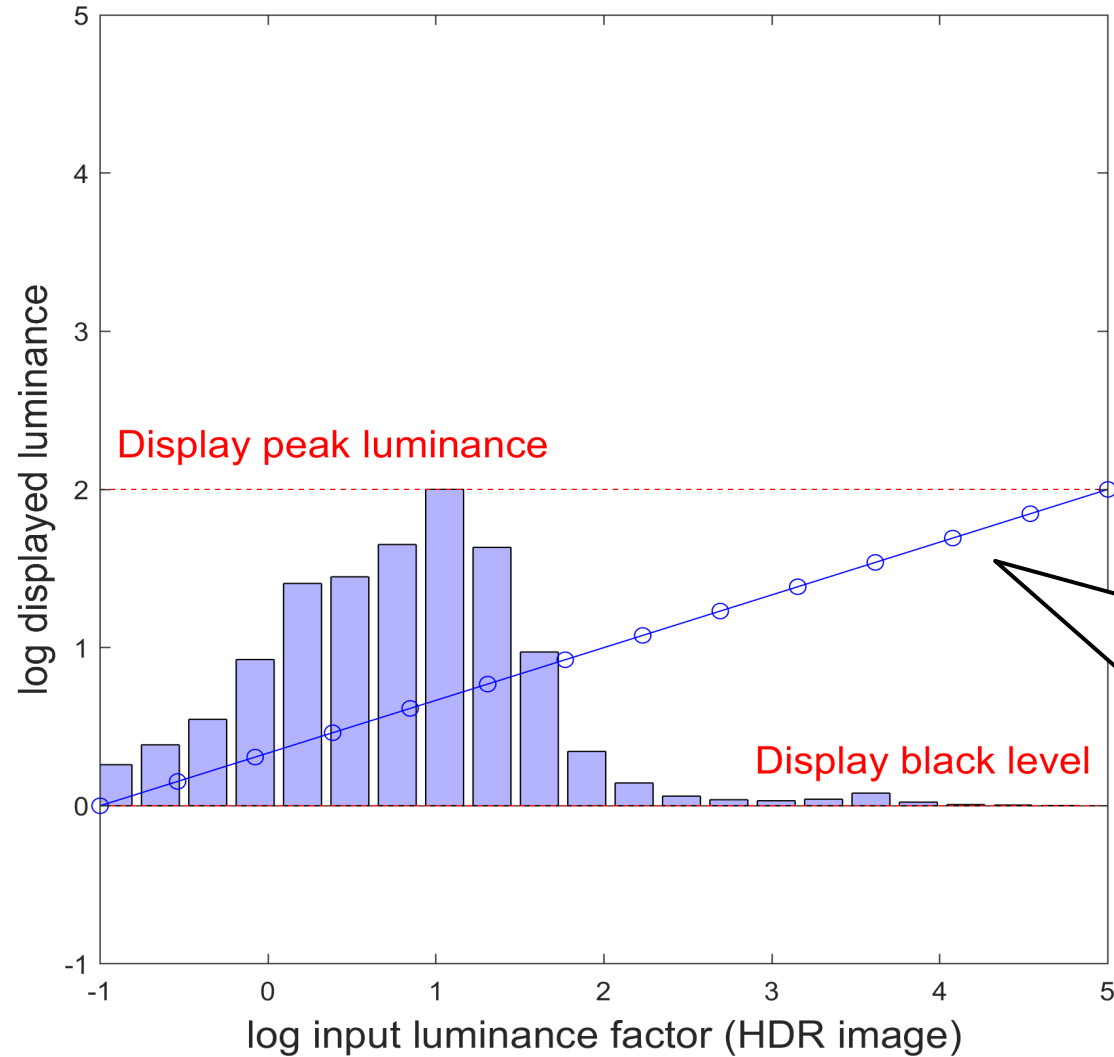
- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ **Tone-curve**
- ▶ Colour transfer
- ▶ Base-detail separation
- ▶ Glare

# Tone-curve



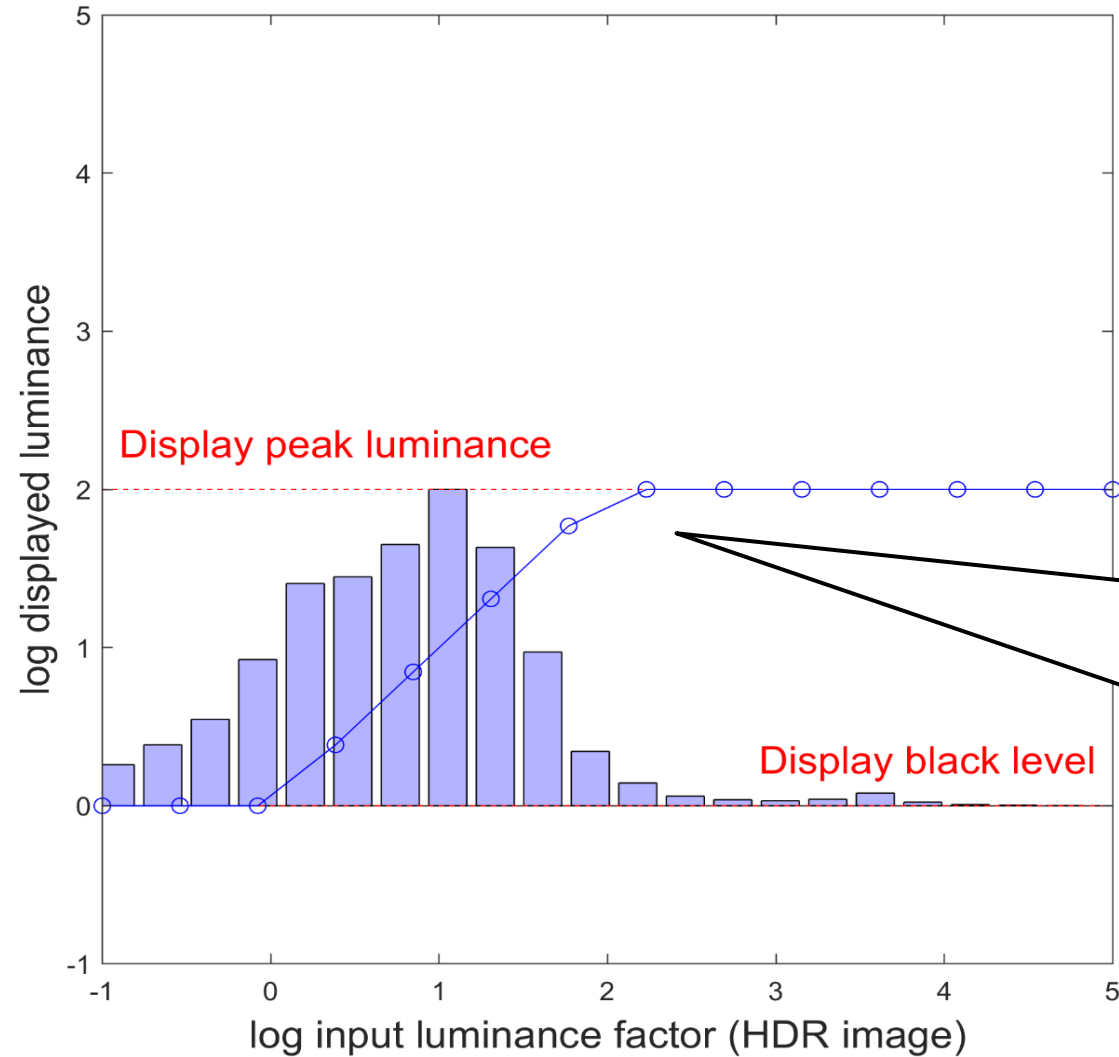


# Tone-curve



But in practice contrast (slope) must be limited due to display limitations.

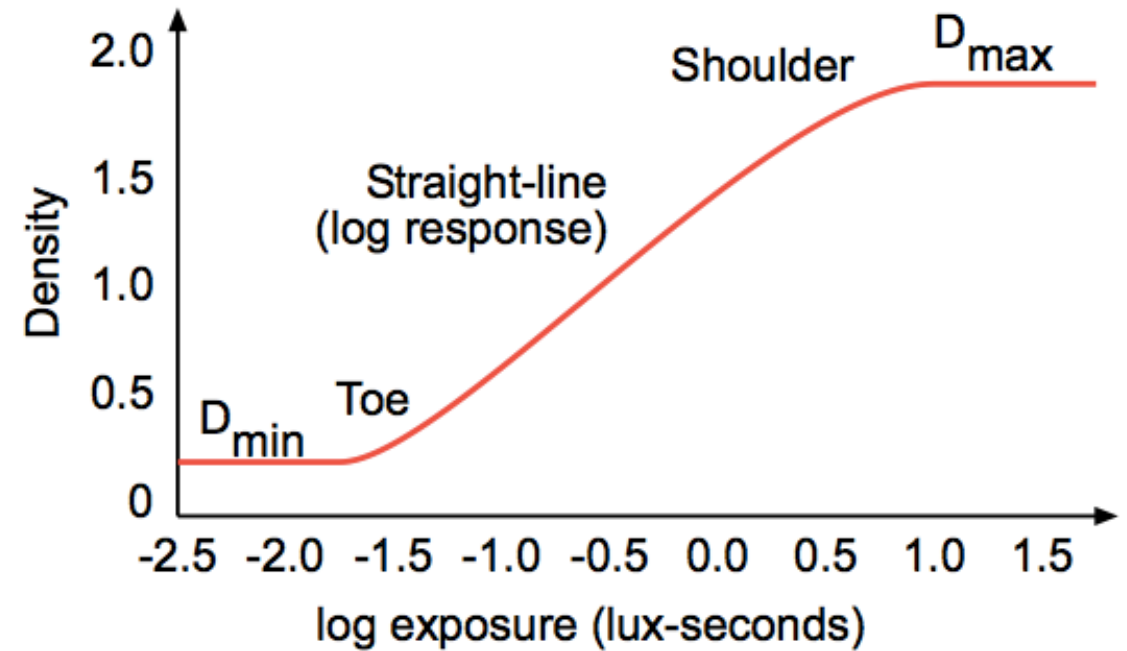
# Tone-curve



Global tone-mapping is a compromise between clipping and contrast compression.

# Sigmoidal tone-curves

- ▶ Very common in digital cameras
  - ▶ Mimic the response of analog film
  - ▶ An analog film has been engineered over many years to produce good tone reproduction
- ▶ Fast to compute



# Sigmoidal tone mapping (a.k.a. Photographic/Reinhard tone mapping)

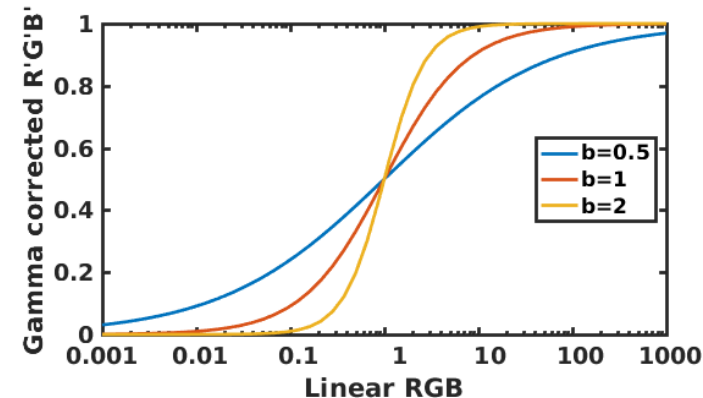
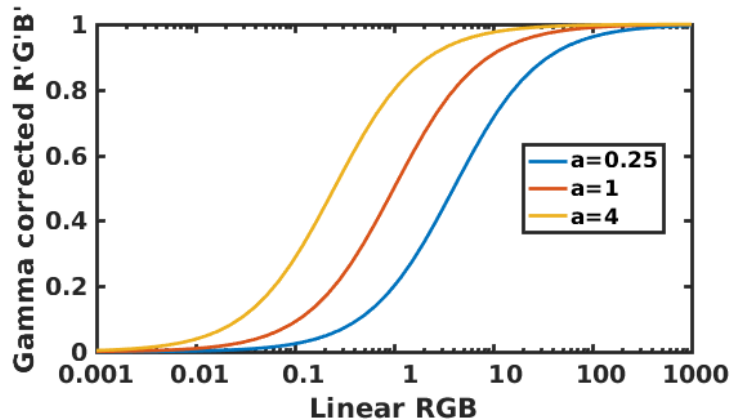
- ▶ Simple formula for a sigmoidal tone-curve:

$$R'(x, y) = \frac{R^b(x, y)}{\left(\frac{L_m}{a}\right)^b + R^b(x, y)}$$

where  $L_m$  is the geometric mean (or mean of logarithms):

$$L_m = \exp\left(\frac{1}{N} \sum_{(x,y)} \ln(L(x, y))\right)$$

and  $L(x, y)$  is the luminance of the pixel  $(x, y)$ .



# Sigmoidal tone mapping example

$a=0.25$



$a=1$



$a=4$



$b=0.5$

$b=1$

$b=2$

# Histogram equalization

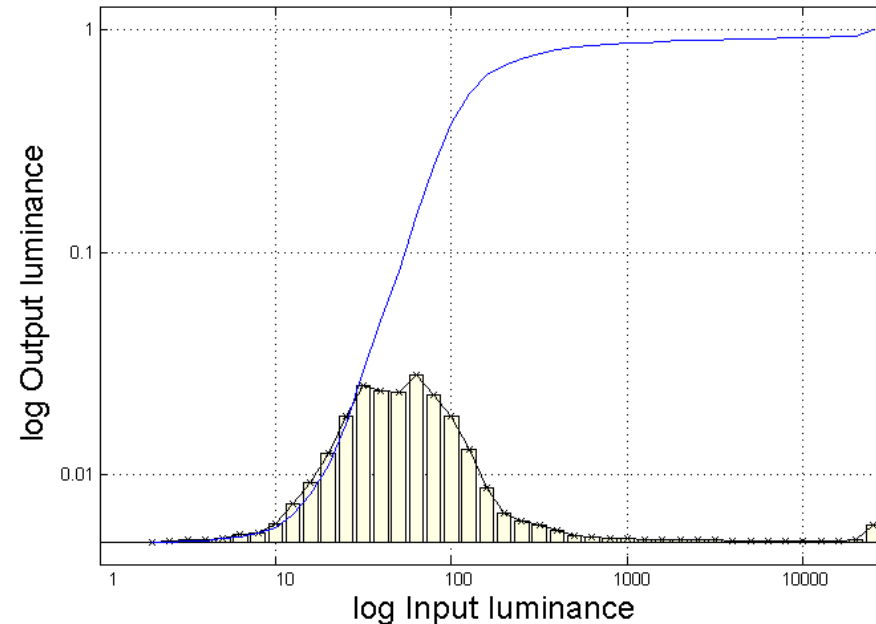
- ▶ 1. Compute normalised cumulative image histogram

$$c(I) = \frac{1}{N} \sum_{i=0}^I h(i) = c(I-1) + \frac{1}{N} h(I)$$

- ▶ For HDR, operate in the log domain
- ▶ 2. Use the cumulative histogram as a tone-mapping function

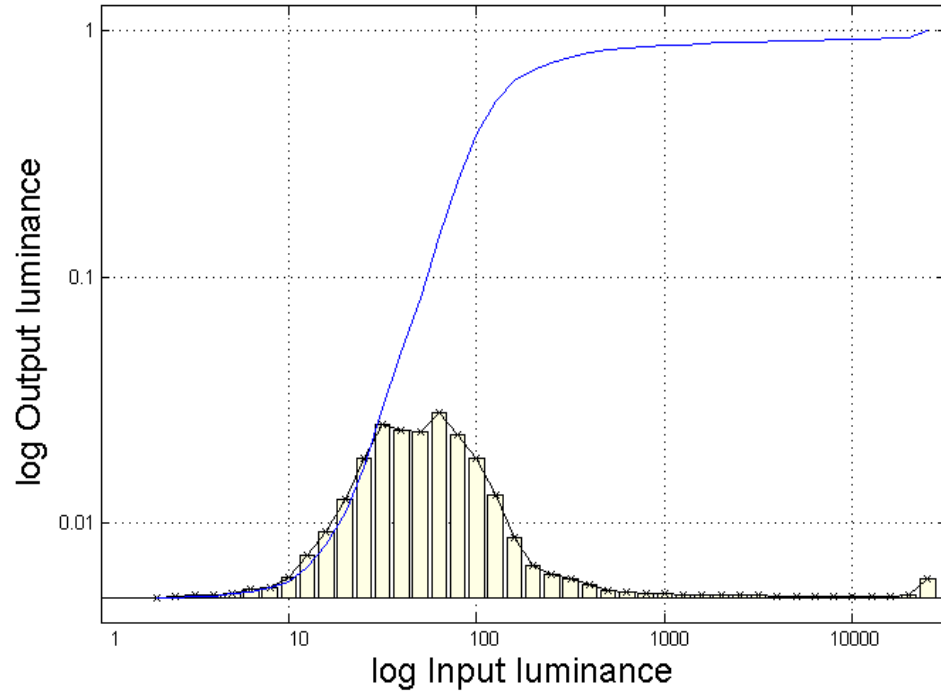
$$Y_{out} = c(Y_{in})$$

- ▶ For HDR, map the log-10 values to the  $[-dr_{out}; 0]$  range
  - ▶ where  $dr_{out}$  is the target dynamic range (of a display)





# Histogram equalization



- ▶ Steepest slope for strongly represented bins
  - ▶ If many pixels have the same value - enhance contrast
  - ▶ Reduce contrast, if few pixels
- ▶ Histogram Equalization distributes contrast distortions relative to the “importance” of a brightness level

# CLAHE: Contrast-Limited Adaptive Histogram Equalization

- ▶ [Pizer et al. Adaptive histogram equalization and its variations. Comput Vision, Graph Image Process 1987], [Larson et al. 1997, IEEE TVCG]

Linear mapping



Histogram equalization

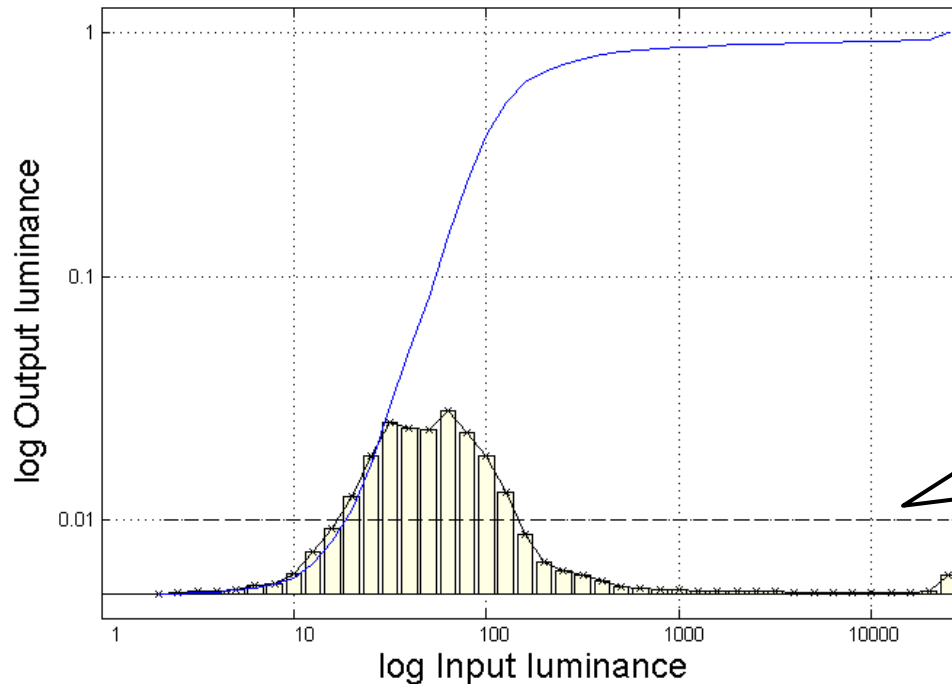


CLAHE



# CLAHE: Contrast-Limited Adaptive Histogram Equalization

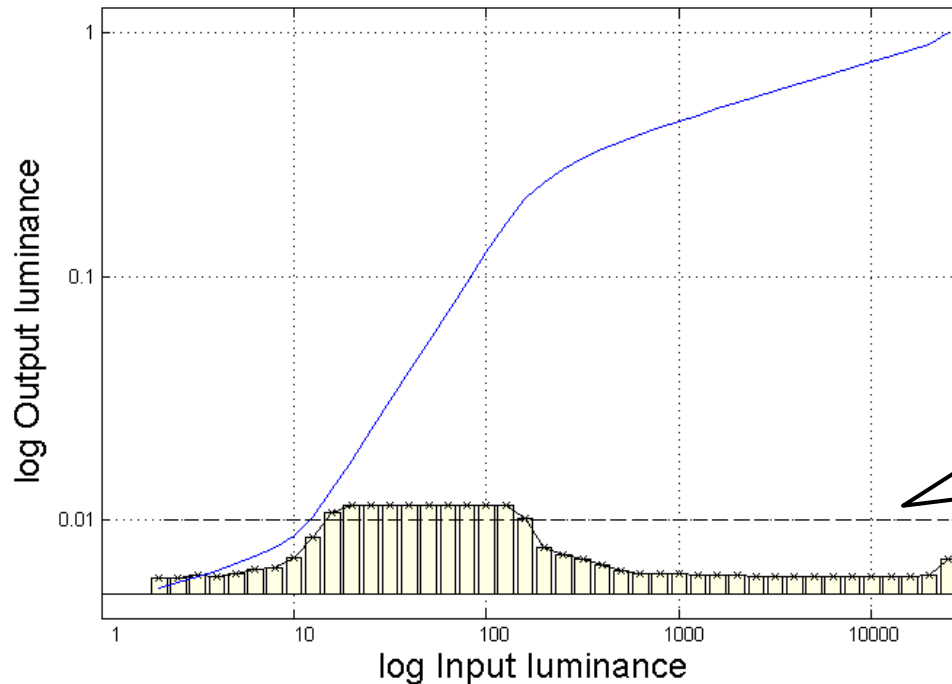
- ▶ Truncate the bins that exceed the ceiling;
- ▶ Distribute the removed counts to all bins;
- ▶ Repeat until converges



Ceiling, based on  
the maximum  
permissible  
contrast

# CLAHE: Contrast-Limited Adaptive Histogram Equalization

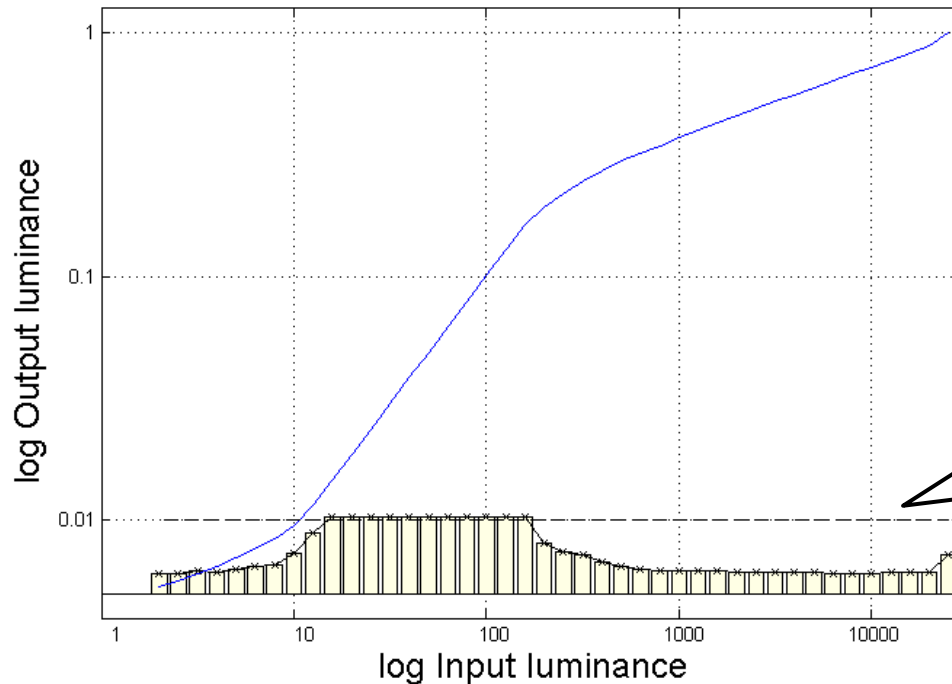
- ▶ Truncate the bins that exceed the ceiling;
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Ceiling, based on  
the maximum  
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# CLAHE: Contrast-Limited Adaptive Histogram Equalization

- ▶ Truncate the bins that exceed the ceiling;
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Ceiling, based on  
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# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ **Colour transfer**
- ▶ Base-detail separation
- ▶ Glare

# Colour transfer in tone-mapping

- ▶ Many tone-mapping operators work on luminance, mean or maximum colour channel value
  - ▶ For speed
  - ▶ To avoid colour artefacts
- ▶ Colours must be transferred later from the original image
- ▶ Colour transfer in the linear RGB colour space:

The diagram illustrates the formula for the output color channel (red),  $R_{out}$ . The formula is  $R_{out} = \left( \frac{R_{in}}{L_{in}} \right)^s \cdot L_{out}$ . A callout box on the left points to  $R_{out}$  and is labeled "Output color channel (red)". A callout box on the right points to the exponent  $s$  and is labeled "Saturation parameter". Another callout box on the right points to  $L_{out}$  and is labeled "Resulting luminance".

$$\text{Output color channel (red)} \rightarrow R_{out} = \left( \frac{R_{in}}{L_{in}} \right)^s \cdot L_{out}$$

Saturation parameter  $s$

Resulting luminance  $L_{out}$

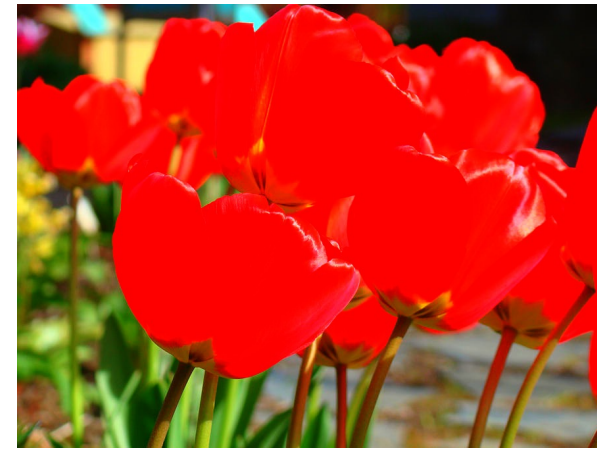
- ▶ The same formula applies to green (G) and blue (B) linear colour values

# Colour transfer: out-of-gamut problem

- Colours often fall outside the colour gamut when contrast is compressed



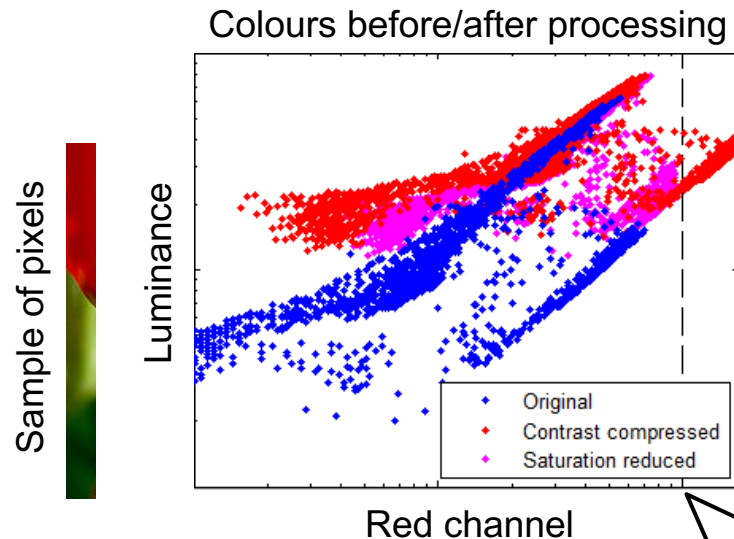
Original image



Contrast reduced ( $s=1$ )



Saturation reduced ( $s=0.6$ )



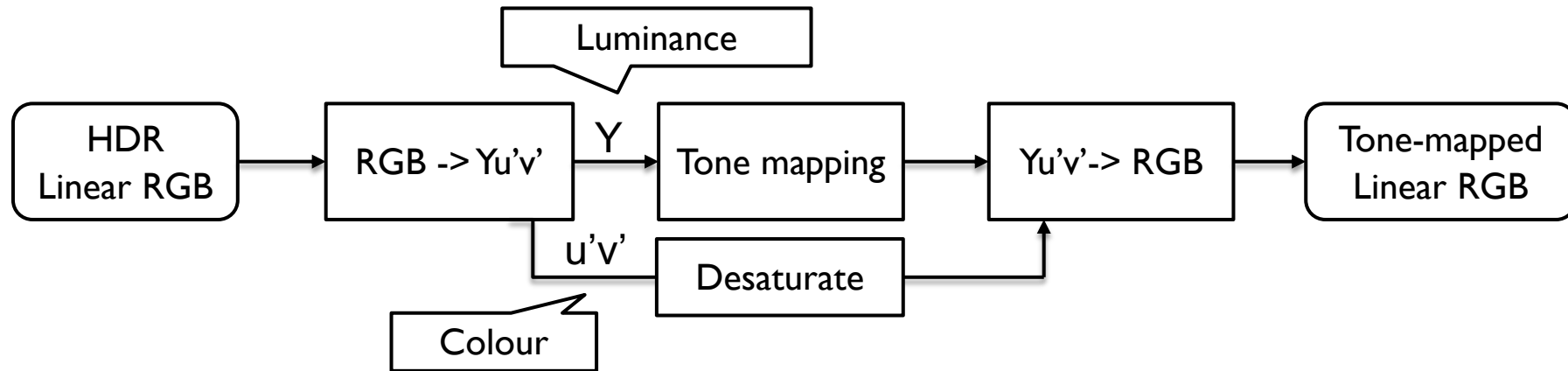
- Reduction in saturation is needed to bring the colors into gamut

Gamut boundary



# Colour transfer: alternative method

- ▶ Colour transfer in linear RGB will alter resulting luminance
- ▶ Colours can be also transferred, and saturation adjusted using CIE  $u'v'$  chromatic coordinates



- ▶ To correct saturation:

$$u'_{out} = (u'_{in} - u'_w) \cdot s + u'_w$$

$$v'_{out} = (v'_{in} - v'_w) \cdot s + v'_w$$

Chroma of the white

$$u'_w = 0.1978$$

$$v'_w = 0.4683$$

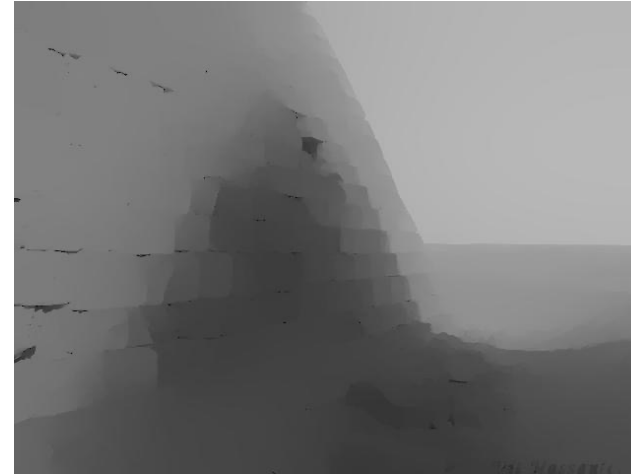
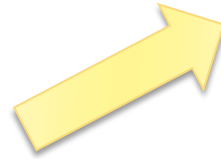
# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Colour transfer
- ▶ Base-detail separation
- ▶ Glare

# Illumination & reflectance separation

Input



Illumination



Reflectance

Image  
linear RGB

$$X_p = I_p R_p$$

Illumination

Reflectance

# Illumination and reflectance

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## Reflectance

- ▶ White  $\approx 90\%$
- ▶ Black  $\approx 3\%$
- ▶ Dynamic range  $< 100:1$
- ▶ Reflectance critical for object & shape detection

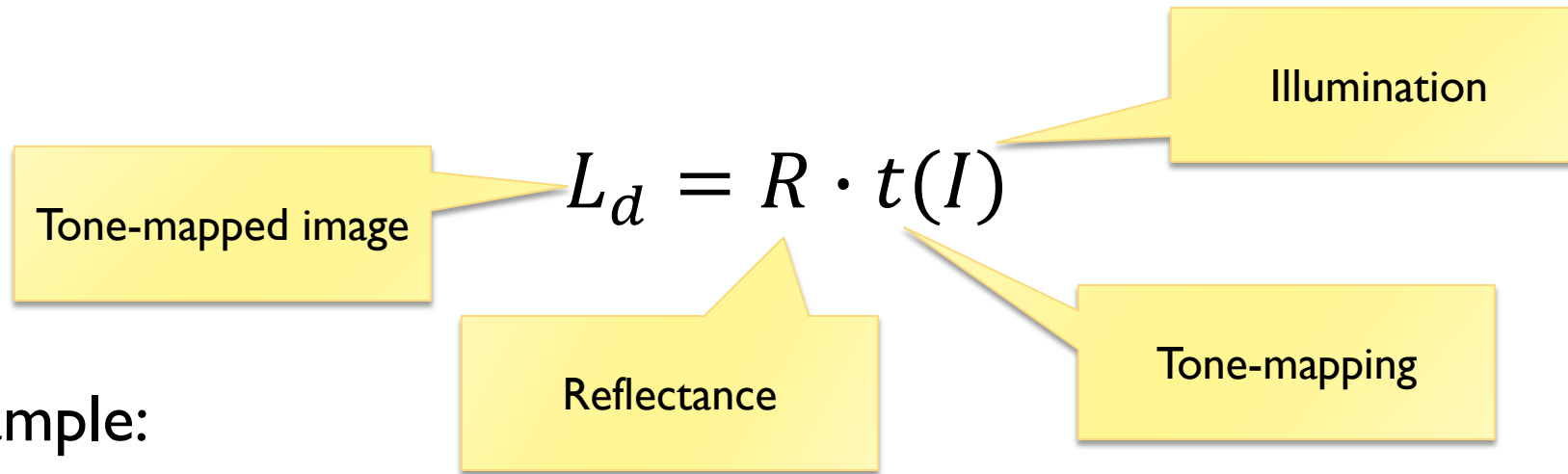
## Illumination

- ▶ Sun  $\approx 10^9 \text{ cd/m}^2$
- ▶ Lowest perceivable luminance  $\approx 10^{-6} \text{ cd/m}^2$
- ▶ Dynamic range 10,000:1 or more
- ▶ Visual system partially discounts illumination

[Tumblin et al. 1999]

# Reflectance & Illumination TMO

- ▶ Hypothesis: *Distortions in reflectance are more apparent than the distortions in illumination*
- ▶ Tone mapping could preserve reflectance but compress illumination



- ▶ for example:

$$L_d = R \cdot (I / L_{white})^c \cdot L_{white}$$

# How to separate the two?

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- ▶ (Incoming) illumination – slowly changing
  - ▶ except very abrupt transitions on shadow boundaries
- ▶ Reflectance – low contrast and high frequency variations



# Gaussian filter

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma_s} e^{\frac{-x^2}{2\sigma_s^2}}$$

- ▶ First order approximation



- ▶ Blurs sharp boundaries
- ▶ Causes halos

Tone mapping  
result





# Bilateral filter

$$I_p \approx \frac{1}{k_s} \sum_{t \in \Omega} f(p-t) g(L_p - L_t) L_p$$

- ▶ Better preserves sharp edges



Tone mapping result

- ▶ Still some blurring on the edges
- ▶ Reflectance is not perfectly separated from illumination near edges



# Weighted-least-squares (WLS) filter

- ▶ Stronger smoothing and still distinct edges



Tone mapping result

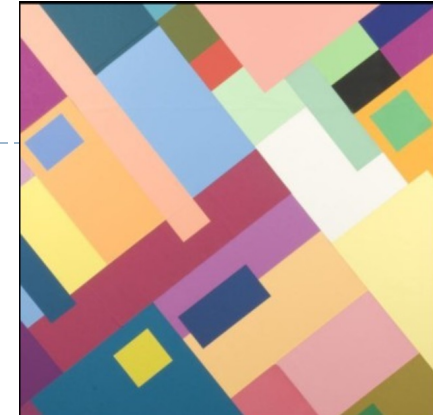
- ▶ Can produce stronger effects with fewer artifacts
- ▶ See „Advanced image processing” lecture



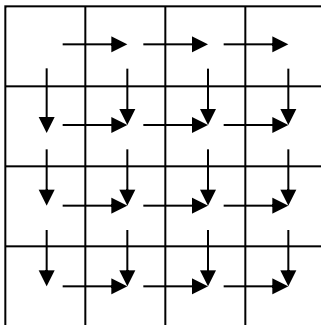
[Farbman et al., SIGGRAPH 2008]

# Retinex

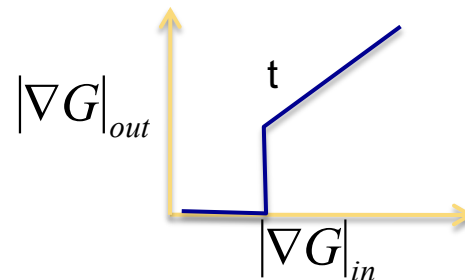
- ▶ Retinex algorithm was initially intended to separate reflectance from illumination [Land 1964]
- ▶ There are many variations of Retinex, but the general principle is to eliminate small gradients from an image. Small gradients are attributed to the illumination



1 step: compute gradients in log domain



2<sup>nd</sup> step: set to 0 gradients less than the threshold



3<sup>rd</sup> step: reconstruct an image from the vector field

$$\nabla^2 I = \text{div } G$$

For example by solving the Poisson equation



# Retinex examples

From: <http://dragon.larc.nasa.gov/retinex/757/>



From: [http://www.ipol.im/pub/algorithm/imps\\_retinex\\_poisson\\_equation/#ref\\_1](http://www.ipol.im/pub/algorithm/imps_retinex_poisson_equation/#ref_1)

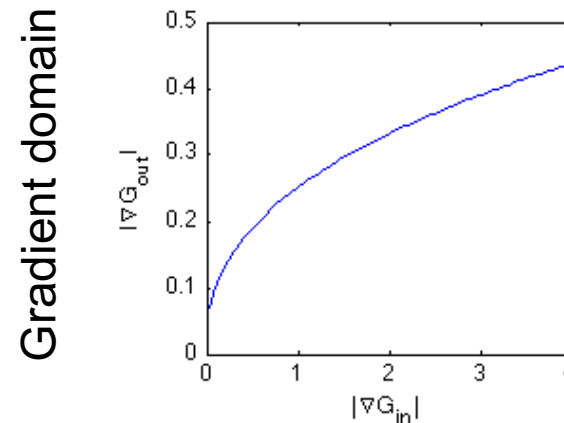
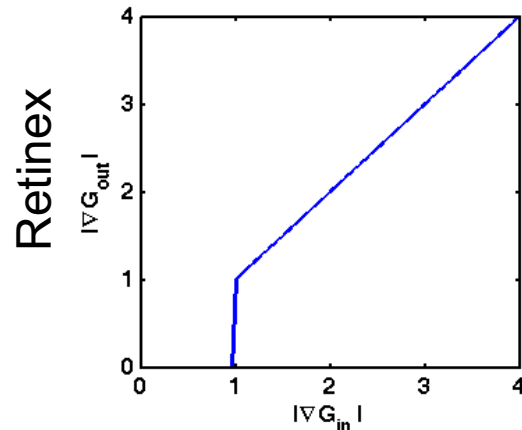


# Gradient domain HDR compression



[Fattal et al., SIGGRAPH 2002]

- ▶ Similarly to Retinex, it operates on log-gradients
- ▶ But the function amplifies small contrast instead of removing it



- Contrast compression achieved by global contrast reduction
  - Enhance reflectance, then compress everything

# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Colour transfer
- ▶ Base-detail separation
- ▶ Glare



# Glare

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"Alan Wake" © Remedy Entertainment



# Glare Illusion



Photography



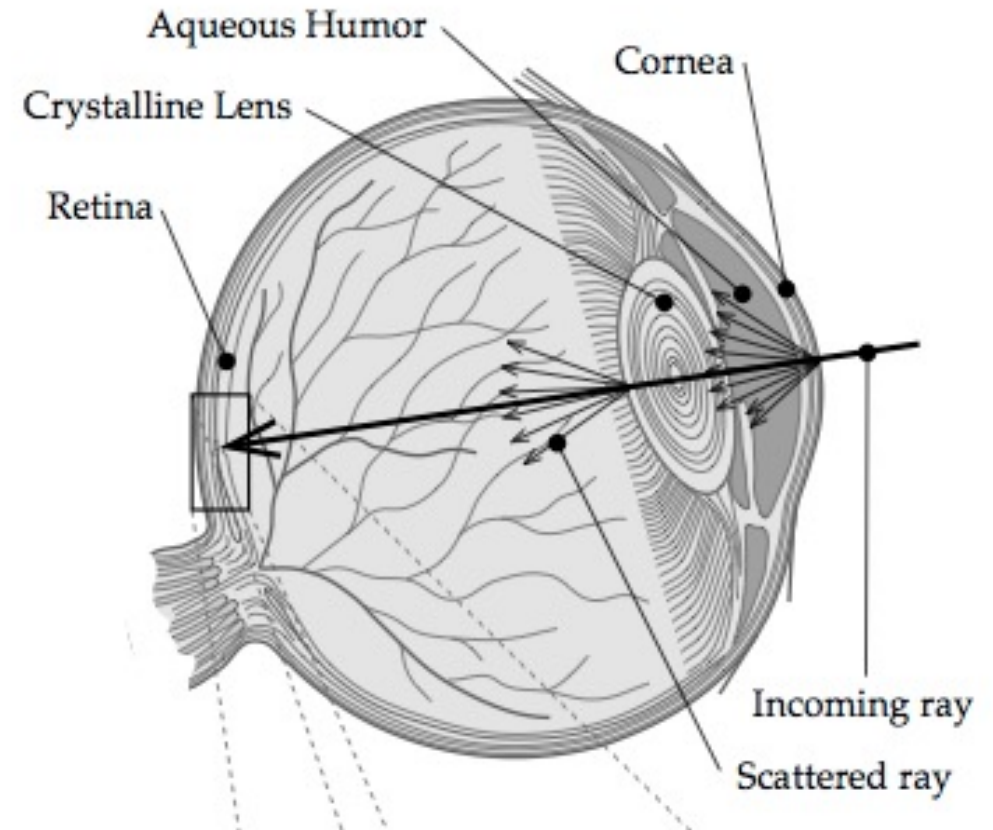
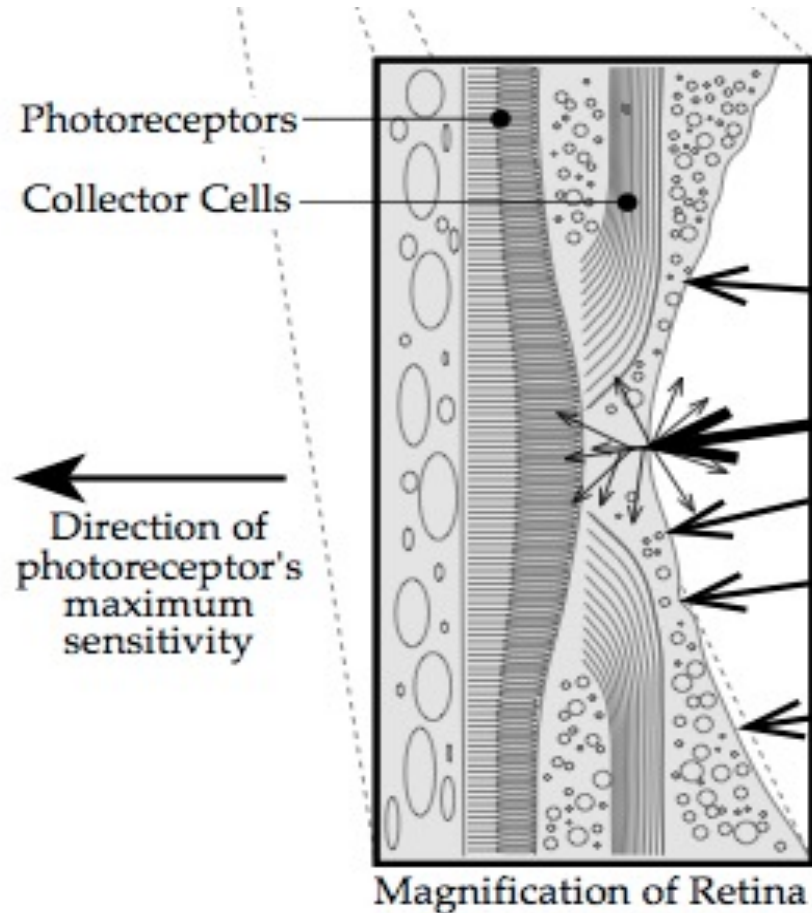
Painting



Computer Graphics  
HDR rendering in games

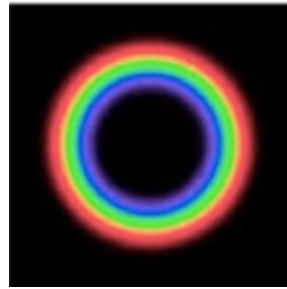


# Scattering of the light in the eye

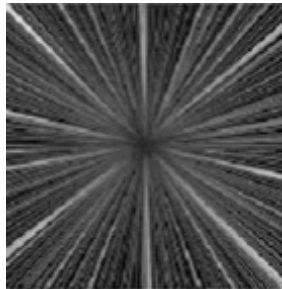


From: Sekuler, R., and Blake, R. Perception, second ed. McGraw- Hill, New York, 1990

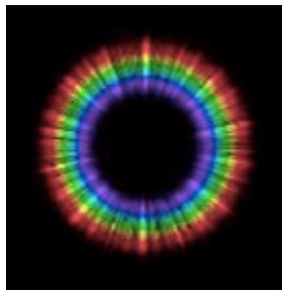
# Ciliary corona and lenticular halo



\*



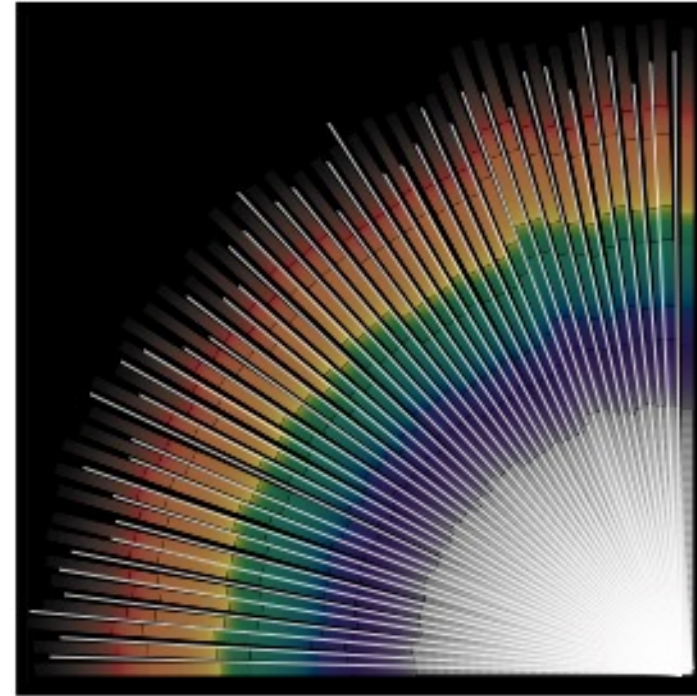
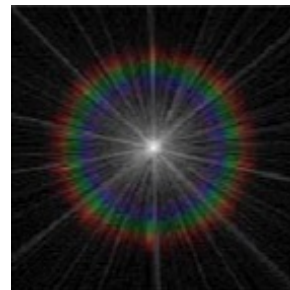
=



+



=



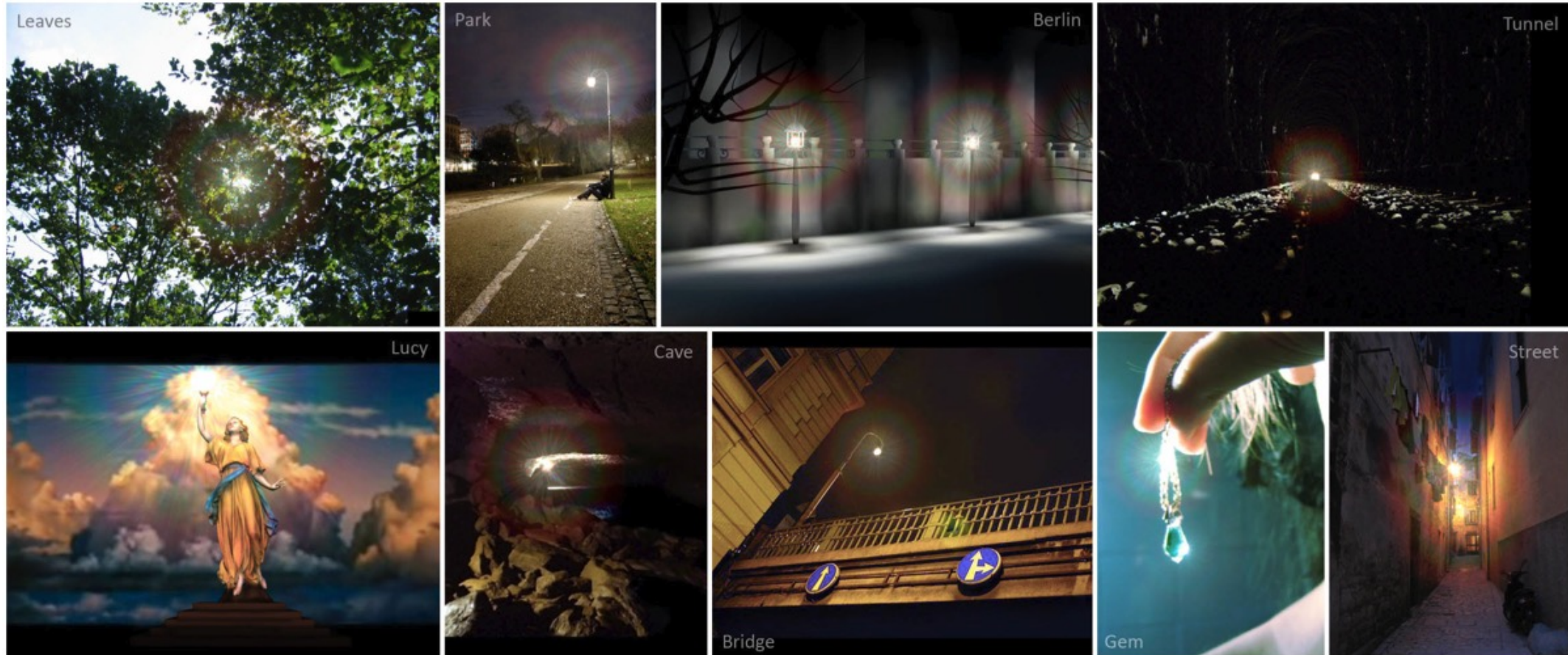
3.8°  
3.5°  
3.2°  
2.9°  
2.6°  
2.3°  
2.0°  
Lenticular  
Halo  
Ciliary  
Corona

From: Spencer, G. et al.  
1995. Proc. of  
SIGGRAPH. (1995)



# Examples of simulated glare

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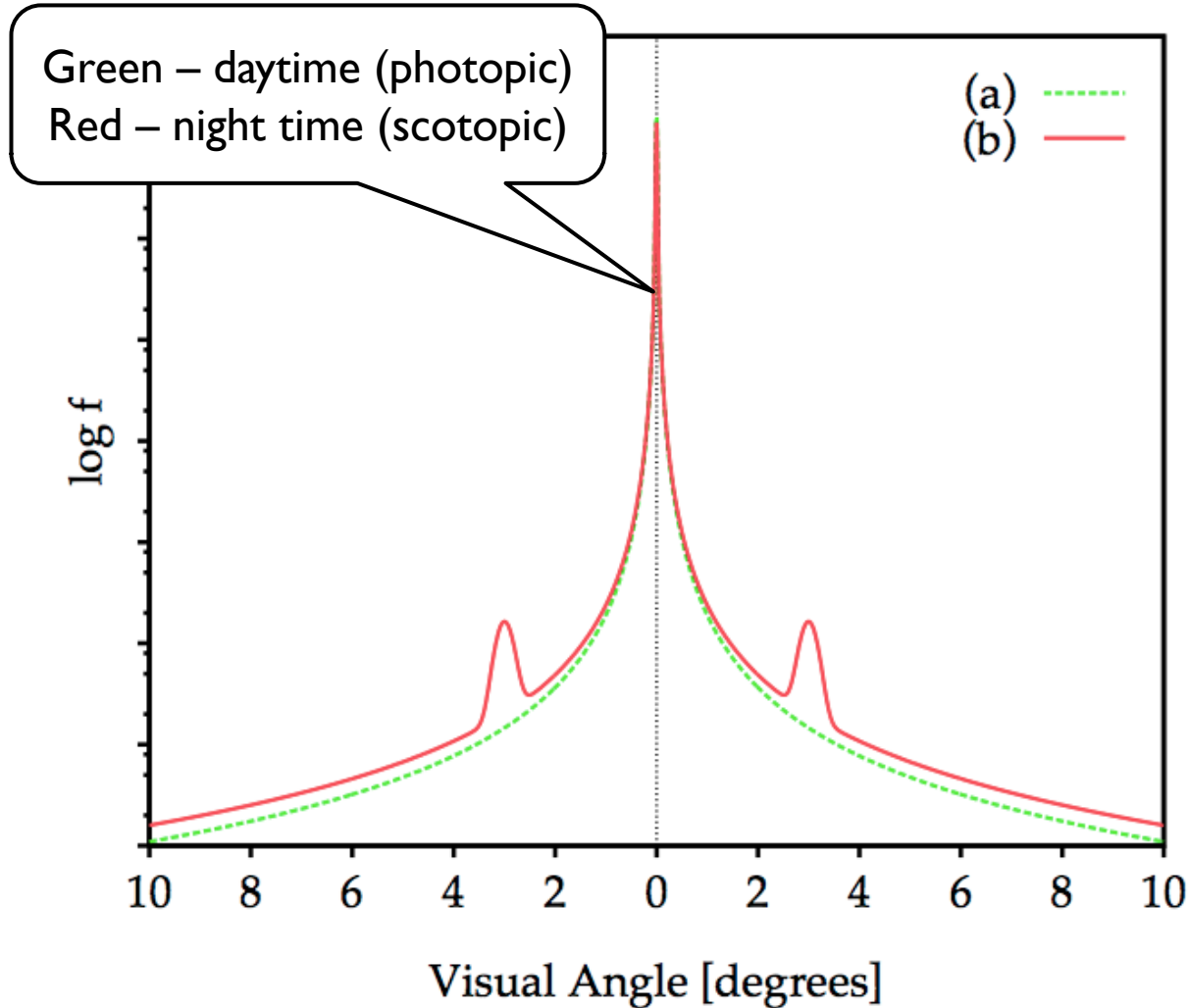
[From Ritschel et al, Eurographics 2009]

# Temporal glare

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# Point Spread Function of the eye



- ▶ What portion of the light is scattered towards a certain visual angle
- ▶ To simulate:
  - ▶ construct a digital filter
  - ▶ convolve the image with that filter

From: Spencer, G. et al. 1995.  
Proc. of SIGGRAPH. (1995)

# Selective application of glare

## A) Glare applied to the entire image

$$I_g = I * G$$

Glare kernel (PSF)

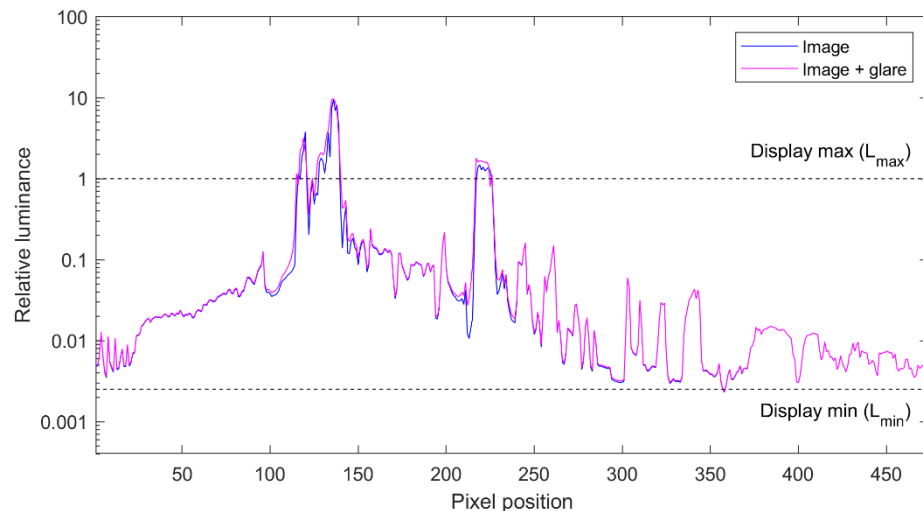
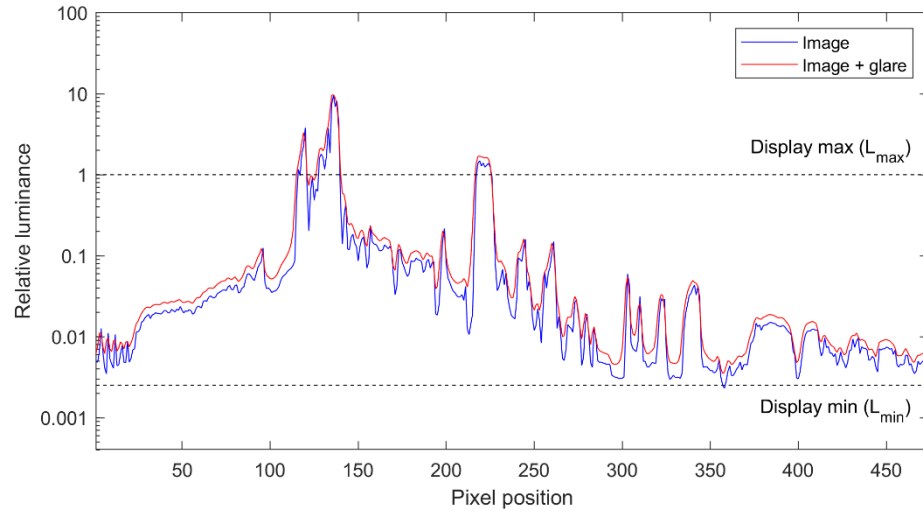
- Reduces image contrast and sharpness

## B) Glare applied only to the clipped pixels

$$I_g = I + I_{clipped} * G - I_{clipped}$$

$$\text{where } I_{clipped} = \begin{cases} I & \text{for } I > 1 \\ 0 & \text{otherwise} \end{cases}$$

Better image quality



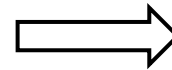
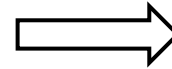


# Selective application of glare



Original image

A) Glare applied to the entire image

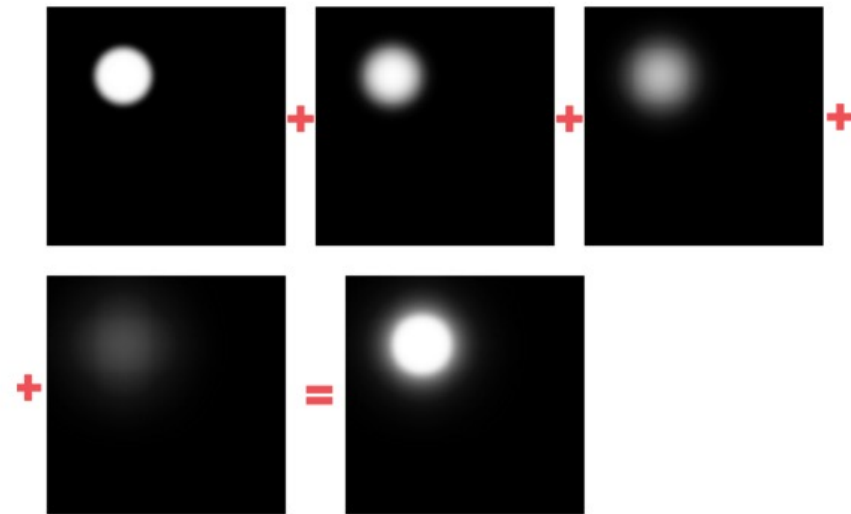


B) Glare applied to clipped pixels only



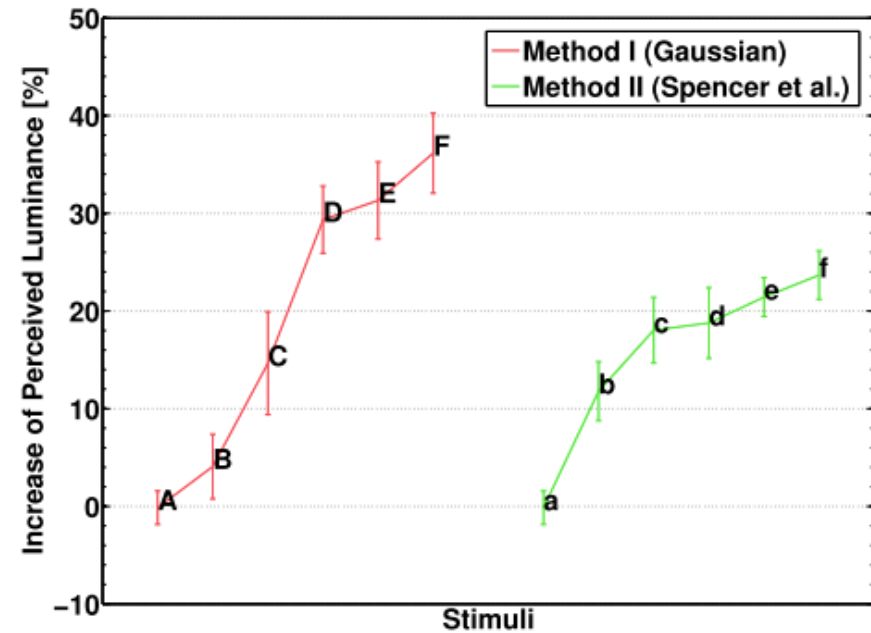
# Glare (or bloom) in games

- ▶ Convolution with large, non-separable filters is too slow
- ▶ The effect is approximated by a combination of Gaussian filters
  - ▶ Each filter with different “sigma”
- ▶ The effect is meant to look good, not be an accurate model of light scattering
- ▶ Some games simulate camera rather than the eye



# Does the exact shape of the PSF matter?

- ▶ The illusion of increased brightness works even if the PSF is very different from the PSF of the eye



red - Gaussian



green - accurate



[Yoshida et al., APGV 2008]

# HDR rendering – motion blur



From LDR pixels

From HDR pixels



# References

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  - ▶ A comparative review of tone-mapping algorithms for high dynamic range video  
*Gabriel Eilertsen, Rafal K. Mantiuk, Jonas Unger*, Eurographics State-of-The-Art Report 2017.
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  - ▶ Spencer, G. et al. 1995. Physically-Based Glare Effects for Digital Images. Proceedings of SIGGRAPH. (1995), 325–334
  - ▶ Ritschel, T. et al. 2009. Temporal Glare: Real-Time Dynamic Simulation of the Scattering in the Human Eye. Computer Graphics Forum. 28, 2 (Apr. 2009), 183–192
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