

Introduction to Julia

Markus Kuhn

Department of Computer Science and Technology University of Cambridge

https://www.cl.cam.ac.uk/teaching/2223/TeX+MATLAB/

julia-slides-2up.pdf 2022-10-11 01:14 debea0e

Technical computing languages

- aimed at rapid prototyping for exploration of numerical algorithms and data sets
- high-level language (garbage collecting, var-len structures)
- comprehensive support for linear algebra, statistics, and plotting
- basic data type: 2- or 3-dimensional floating-point matrix
- most operators and functions work on entire matrices ⇒ rarely necessary to write out loops
- use internally highly optimized numerics libraries (BLAS, LAPACK, FFTW)
- support interactive use via read-evaluate-print loop (REPL)
- interpreted or just-in-time compiled, notebook support
- comprehensive toolboxes/modules for easy access to standard algorithms from many fields: statistics, machine learning, image processing, signal processing, neural networks, wavelets, communications systems, etc.
- very easy I/O for many data/multimedia file formats
- widely used as a visualization and teaching tool

Older contenders

▶ MATLAB – "matrix laboratory" student tool (University of New Mexico, 1970s), commercial product since 1984, very widely used since 1990s in engineering simulations and teaching, initially not a general-purpose language (e.g., object classes only from 2008, dictionaries only added in 2022), integrated IDE, since 2000 based on Java JVM code generation



Campus licence:

https://uk.mathworks.com/academia/tah-portal/the-university-of-cambridge-666637.html

- Similar to (earlier versions of) MATLAB, subset compatible: GNU Octave, SciLab, FreeMat
- ▶ R focus on statistics and plotting https://www.r-project.org/



- numpy MATLAB-like numerical arrays, fast linear algebra
- matplotlib MATLAB-like plotting functions https://matplotlib.org/
- SciPy scientific computing, Pandas data analysis, etc.
- others: LuaJIT (SciLua), Perl Data Language (PDL), OCaml (Owl)

R and especially Python become very popular $\approx\!2000\text{--}2010$, but are much slower than compiled statically typed C/C++/Fortran, as their dynamic types were intended for interpreted execution. In HPC applications, they remain mainly configuration/glue languages for C/C++/Fortran libraries.





Julia

Modern, fast, full-featured, compiled, interactive language, initially created 2009–2012 at Massachusetts Institute of Technology by J. Bezanson, A. Edelman, S. Karpinski, V.B. Shah.

- MATLAB-inspired syntax (especially much nicer and compacter array syntax than NumPy)
- julia

- not intended to be MATLAB compatible
- combines dynamic and static type systems via multiple dispatch
- just-in-time compiled by LLVM backend
- ▶ with some care, Julia code can execute nearly as fast as C/C++
- aims to solve the two-language problem (e.g., Python having to call C++ code for performance)
- ► can also call C, C++, Python, R, Fortran functions
- ► LISP-like metaprogramming, rich flexible parametric type system
- built-in package manager for easy access to package ecosystem, version-controlled virtual package environments ("projects")
- multiple dispatch helps with reusing types across packages
- ▶ Backwards-compatible since version 1.0 (2018)

Julia shortcomings

- start-up delay when loading/calling large packages, as they need to be JIT compiled first ("time to first plot" problem)
 Julia precompiles to on-disc cache the results of type inference, but not yet the object code.
- not aimed at compilation of stand-alone binaries
 Possible with PackageCompiler.jl, but requires extra effort and can lead to large (> 100 MB) binaries.
- not aimed at hard real-time applications: heap memory allocation and automatic mark-and-sweep garbage collection can introduce non-deterministic delays
 - Manual control of memory allocation is possible, but not typical Julia style, and often not supported by ecosystem packages.
- package ecosystem and package documentation sometimes still less mature or complete than that of Python, R, MATLAB But it is very easy to get involved via Pkg.develop and GitHub pull requests.
- diversity of package ecosystem can be confusing initially (e.g. several competing major plotting libraries), usually more than one way of doing everything (esp. compared to MATLAB) Hence this quick introductory tour!

Installing Julia

or

Download the current stable release (e.g. v1.8.2) from:

https://julialang.org/downloads/

Windows: Run the 64-bit installer (e.g., julia-1.8.2-win64.exe), then add "C:\Program Files\Julia-1.8\bin" to your PATH environment variable.

Alternatively: using the Microsoft Store or "winget install julia -s msstore" will install Julia via the new Juliaup update manager. Also: install Windows Terminal and call Julia inside that, for much better terminal-emulation behaviour than in cmd.exe.

```
Homebrew: (on macOS or Linux)
$ brew install --cask julia
```

macOS: Install the 64-bit .dmg package, then add to your PATH the path "/Applications/Julia-1.8.app/Contents/Resources/julia/bin".

Linux: Download the julia-1.8.2-linux-x86_64.tar.gz tarball and unpack somewhere convenient, e.g. at /opt/julia-1.8.2 with e.g.

```
$ sudo bash
# cd /opt && tar xvzf /path/to/julia-1.8.2-linux-x86_64.tar.gz
Then add "/opt/julia-1.8.2/bin" to your PATH environment variable.
```

Documentation

The Julia documentation at

```
https://docs.julialang.org/
```

consists of the core langange manual, plus the reference manuals for

- ► "Base" the built-in standard functions and types
- "Standard Library" packages preinstalled with Julia

These reference manuals are autogenerated from "docstrings" embedded in the source code. You can also read these docstrings from the REPL help mode with "? function".

Most of "Base" and "Standard Library" are written in Julia, with some C. The @less macro followed by a function call displays the called method in the Julia source code, e.g.

```
julia> @less exit()
exit() = exit(0)
```

shows that exit() just calls exit(0), while providing an integer exit code calls the internal C function jl_exit:

```
julia> @less exit(0)
exit(n) = ccall(:jl_exit, Cvoid, (Int32,), n)
```

Basic REPL use

Invoking julia without a script.jl filename prints a banner and starts the REPL. Enter Julia expressions and it will display the result:

```
$ julia
```

Press one of the keys ?] ; to switch the julia> REPL prompt into one of these alternate REPL modes: help mode, package manager, shell mode:

```
help?> exit
(@v1.8) pkg> status
shell> date
```

Press backspace to leave each mode and return to the julia> prompt. Type Ctrl-D or exit() to leave julia.

Installing packages

Julia's Standard Library does not contain e.g. plotting, audio or digital-signal-processing functions, but add-on packages that provide these (and their dependencies) can be installed easily from the REPL. Hit the] key to enter pkg mode, then type e.g.

```
(@v1.8) pkg> add Plots WAV DSP
(@v1.8) pkg> status
Status `/home/mgk25/.julia/environments/v1.8/Project.toml`
  [717857b8] DSP v0.7.7
  [91a5bcdd] Plots v1.35.3
  [8149f6b0] WAV v1.2.0
```

Julia's Pkg manager downloads https://github.com/JuliaRegistries/General and searches in it for the latest versions of the registered packages you asked to add. [You can also ask for specific versions (add Plots@1.35.3) or add unregistered packages by providing a git URL.]

To modify a downloaded package, use e.g. "dev WAV" to prepare and use a local git clone of that package in ~/.julia/dev/WAV/. Later use "free WAV" to return to a registered version.

```
Quick docs: type? or prefix a pkg-mode command with?
Full Pkg.jl documentation: https://pkgdocs.julialang.org/
Packages and their metadata are all installed into ~/.julia/ by default. Set the environment variable JULIA_DEPOT_PATH if you want them elsewhere.
```

Julia matrices

```
Assign a 3 \times 3 matrix of integers:
```

```
julia> a = [8 1 6; 3 5 7; 4 9 2]
3×3 Matrix{Int64}:
    8  1  6
    3  5  7
    4  9  2
```

Semicolons equal line feeds:

Access a single element:

```
julia> a[2,3]
7
```

Vector and matrix indices start at 1. The first index selects the row, the second the column, like in linear algebra notation.

```
julia> a[3,2];
julia> ans
9
```

The REPL normally prints the value returned by each expression entered (assignment returns the value assigned). Following an expression with a semicolon suppresses this.

The value of the last expression evaluated in the REPL is also assigned to variable ans.

Julia vectors

Vectors are one-dimensional arrays that act in a linear-algebra context like a vertical/column vector:

```
julia> b = [1, 2, 3]
3-element Vector{Int64}:
    1
    2
    3
```

They are different from column vectors, which are stored as two-dimensional $1 \times n$ matrices:

```
julia> b = [10 20 30]
1×3 Matrix{Int64}:
10 20 30
```

11

Julia range objects

```
start:stop generates a range of
numbers:
    julia> collect(-1:3)
    5-element Vector{Int64}:
    -1
        0
        1
        2
        3

    julia> collect(3:0)
    Int64[]
The colon actually generates a range object,
which behaves like a vector when used like one.
The collect function copies that emulated
vector into a real one in memory.
```

```
Specify step size with second colon:
   julia> collect(1:3:12)
4-element Vector{Int64}:
    1
    4
    7
   10

julia> collect(3:-0.5:1)
5-element Vector{Float64}:
   3.0
   2.5
   2.0
   1.5
   1.0
```

Vectors as indices select several rows and columns. When used inside a matrix index, the variable end provides the highest index value:

a[end, end-1] == 9. Using just ":" is equivalent to "1:end" and can be used to select an entire row or column.

Row and column selection

```
Select rows, columns and
submatrices of a:
julia> a[:,:]
3×3 Matrix{Int64}:
   1 6
 3
   5
       7
   9 2
julia> a[1,:]
3-element Vector{Int64}:
 1
julia> a[:,1]
3-element Vector{Int64}:
3
 4
julia > a[2:3,1:2]
2×2 Matrix{Int64}:
 3 5
 4 9
```

```
Matrices can also be accessed as a
1-dimensional vector:
julia > a[1:5]
5-element Vector{Int64}:
 3
 4
 1
 5
julia> a[6:end]
4-element Vector{Int64}:
 6
 7
 2
julia> a[1:4:9]
3-element Vector{Int64}:
 8
 5
 2
Julia matrices use column-major storage
order, like Fortran/MATLAB/R, unlike C.
```

13

Element-wise operators and broadcasting

Prefix any operator with . to apply it element-by-element to matrices and vectors. For element-wise function calls, insert dot before opening parenthesis.

Dotted operators also grow (broadcast) vectors and matrixes along singleton dimensions, until both operands have the same dimensions:

```
julia> [8 1 6; 3 5 7] .+ [10; 20]
2×3 Matrix{Int64}:
    18    11    16
    23    25    27
```

Combining matrices and vectors

Use [] to build new matrices, where ; joins submatrices vertically (dimension 1), space (or ;;) joins them horizontally (dimension 2), ;;; joins them in dimension 3, etc. The , does *not* join matrices or vectors, it separates elements.

```
julia> a = [8 1 6; 3 5 7; 4 9 2]
                                   julia> [[1,2],[3,3]]
                                   2-element Vector{Vector{Int64}}:
3×3 Matrix{Int64}:
 8
    1
       6
                                    [1, 2]
 3
    5 7
                                    [3, 3]
   9 2
                                   You can also mask elements:
                                   julia> a .> 5
julia > d = [a[:,end] \ a[1,:]]
                                   3×3 BitMatrix:
3×2 Matrix{Int64}:
                                    1
                                          1
                                       0
 6
   8
                                    0
                                       0
                                          1
 7
    1
 2
   6
                                   julia > a[a .> 5] .= 0 ; a
julia> e = [zeros(1,3); a[2,:]']
                                   3×3 Matrix{Int64}:
2×3 Matrix{Float64}:
                                    0
 0.0 0.0 0.0
 3.0 5.0 7.0
```

Review: matrix multiplication

Each element of the matrix product is the scalar product of the corresponding in the and the corresponding in the

Review: inner and outer product of vectors

Special cases of matrix multiplication

Row vector times column vector:

Column vector times row vector:

17

Matrix multiplication

Operators on scalars and matrices:

```
julia> [1 1; 1 0] * [2 3]'
2×1 Matrix{Int64}:
5
2

julia> [1 2 3] .* [10 10 15]
1×3 Matrix{Int64}:
10 20 45
```

Inner and outer vector product:

```
julia> [2 3 5] * [1 7 11]'
1×1 Matrix{Int64}:
    78

julia> [2 3 5]' * [1 7 11]
3×3 Matrix{Int64}:
    2 14 22
3 21 33
5 35 55
```

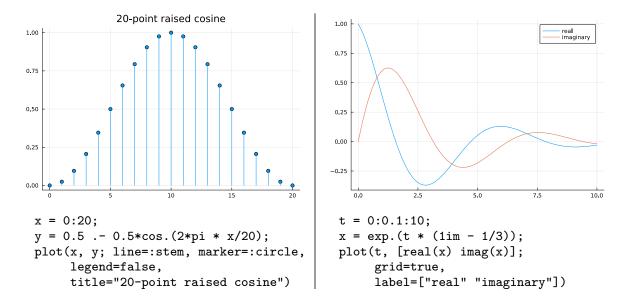
Complex number types: Complex{Int16}, Complex{Float64}, etc.

The imaginary unit vector $\sqrt{-1}$ is available as 1im and and vectors and matrices can also be complex.

Related functions: real, imag, conj, exp, cis, abs, angle

Plotting

using Plots



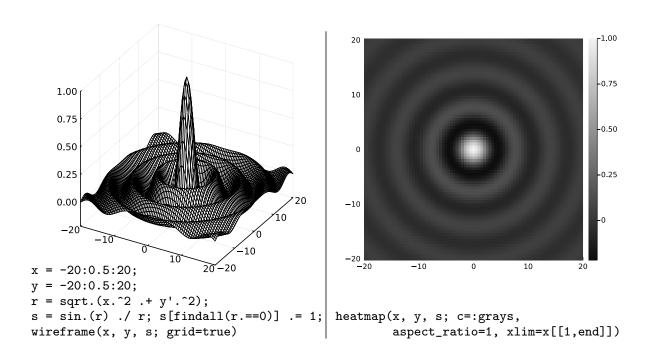
Function plot expects a vectors of x coordinates, and a vector or matrix of y coordinates, one column per curve. Use plot! to add additional curves with independent x coordinates.

Use savefig("plot2.pdf") to save current figure as graphics file.

19

2D plotting

using Plots



Functions

```
To define a new function, for example decibel(x) = 10^{x/20}, write function decibel(x) return 10 .^ (x ./ 20) end or simply decibel(x) = 10 .^ (x ./ 20) and call as julia> decibel(40) 100.0
```

Note that the funtion needs no type declaration for parameters. Each time the function is called with a new type, a new method will be JIT compiled for that type signature.

21

Example: generating an audio illusion

Generate an audio file with 12 sine tones of apparently continuously exponentially increasing frequency, which never leave the frequency range 300–3400 Hz. Do this by letting them wrap around the frequency interval and reduce their volume near the interval boundaries based on a raised-cosine curve applied to the logarithm of the frequency.

First produce a 2 s long waveform in which each tone raises 1/12 of the frequency range, then concatenate that into a 60 s long 16-bit WAV file, mono, with 16 kHz sampling rate. Avoid phase jumps.

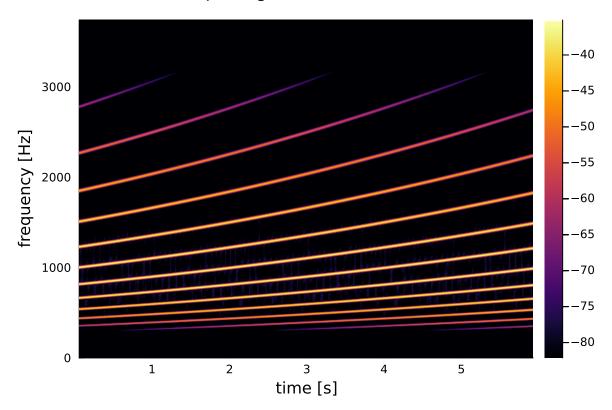
Parameters:

```
fs = 16000; # sampling frequency [Hz]
d = 2; # time after which waveform repeats [s]
n = 12; # number of tones
fmin = 300; # lowest frequency
fmax = 3400; # highest frequency
```

A variant of this audio effect, where each tone is exactly one octave (factor 2 in frequency) from the next, is known as the *Shepard–Risset glissando*.

What changes to the parameters would produce that?

Spectrogram of the first 6 s:



23

Example solution:

```
using DSP, Plots, WAV
```

```
t = 0:1/fs:d-1/fs;  # timestamps for each sample point
# normalized logarithm of frequency of each tone (row)
# for each sample point (column), all rising linearly
# from 0 to 1, then wrap around back to 0
1 = mod.(((0:n-1)/n) .+ (t/(d*n))', 1);
f = fmin * (fmax/fmin) .^ l; # freq. for each tone and sample
p = 2*pi * cumsum(f, dims=2) / fs; # phase for each tone and sample
# make last column a multiple of 2*pi for phase continuity
p = ((2*pi*floor.(p[:,end]/(2*pi))) ./ p[:,end]) .* p;
s = sin.(p);
             # sine value for each tone and sample
# mixing amplitudes from raised-cosine curve over frequency
a = 0.5 .- 0.5 * cos.(2*pi * 1);
w = sum(s .* a, dims=1)/n; # mix tones together, normalize to [-1, +1]
w = repeat(vec(w), 3); # repeat waveform 3x
m = spectrogram(w, 2048, 1800; fs, window=hamming);
ps = 10 * log10.(power(m)); mx = maximum(ps);
heatmap(time(m), freq(m), ps;
        xlabel="time [s]", ylabel="frequency [Hz]",
        ylim=(0, fmax*1.1), clim=(mx-47,mx))
savefig("ladder-jl.pdf")
w = repeat(w, 5);
                        # repeat waveform 5x
#wavplay(w, fs);
wavwrite(w, "ladder.wav", Fs=fs); # make audio file
```

MATLAB, Julia, NumPy: comparative cheat sheet

	MATLAB	Julia	NumPy
vector size (1,n) vector size (n,1) vector size (n)	[1 2 3] [1; 2; 3] n/a	[1 2 3] [1 2 3]' [1, 2, 3]	np.array([1, 2, 3]).reshape(1, 3) np.array([1, 2, 3]).reshape(3, 1) np.array([1, 2, 3])
j to n step k matrix	j:k:n [1 2; 3 4]	j:k:n	np.array([1, 2, 3]) np.arrange(j, n+1, k) np.array([[1, 2], [3, 4]])
0 matrix 1 matrix	zeros(2, 2) ones(2, 2)	zeros(2, 2)	np.zeros((2, 2)) np.ones((2, 2))
identity matrix diagonal matrix	eye(2, 2) diag([1 2 3])	I Diagonal([1, 2, 3])	np.eye(2) np.diag([1, 2, 3])
transpose complex conj. transpose	A.' A'	transpose(A) A'	A.T A.conj()
concat hor.	[[1 2] [1 2]]		B = np.array([1, 2]) np.hstack((B, B))
matrix to vector flip left/right	A(:)	A[:] reverse(A,dims=2)	A.flatten() np.fliplr(A)
broadcast a function	,	$f(x)=x^2; f(x)$	def f(x): return x**2 f(x)
element $A_{2,2}$ rows 1 to 4	A(2, 2) A(1:4, :)		A[1, 1] A[0:4, :]
element-wise multipl. matrix multiplication	A .* B A * B	A .* B A * B	A * B A @ B

• • •

https://cheatsheets.quantecon.org/