Advanced Graphics and Image Processing

Models of early visual perception
Part 1/6 – perceived brightness of light

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Many graphics/display solutions are motivated by visual perception

Image & video compression

Display spectral emission - metamerism

Camera’s Bayer pattern

Halftoning

Display’s subpixels

Color wheel in DLPs
Luminance (again)

- Luminance – measure of light weighted by the response of the achromatic mechanism. Units: cd/m$^2$

\[
L_V = \int_{350}^{700} kL(\lambda)V(\lambda) d\lambda
\]

\[
k = \frac{1}{683.002}
\]
Steven’s power law for brightness

- Stevens (1906-1973) measured the perceived magnitude of physical stimuli
  - Loudness of sound, tastes, smell, warmth, electric shock and brightness
  - Using the magnitude estimation methods
    - Ask to rate loudness on a scale with a known reference

- All measured stimuli followed the power law:
  \[ \phi(I) = kI^a \]

- For brightness (5 deg target in dark), \( a = 0.3 \)
Steven’s law for brightness

![Graph showing the relationship between perceived brightness and luminance in cd/m².](image)
Steven’s law vs. Gamma correction

Stevens’ law
\[ a = 0.3 \]

Gamma function
Gamma = 2.2
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Models of early visual perception

Part 2/6 – contrast detection

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Detection thresholds

- The smallest detectable difference between
  - the luminance of the object and
  - the luminance of the background
Threshold versus intensity (t.v.i.) function

- The smallest detectable difference in luminance for a given background luminance
t.v.i. measurements – Blackwell 1946
Psychophysics
Threshold experiments

\[ L + \Delta L \]

\[ L \]

Psychometric function

Detection threshold

\[ P = 0.75 \]

Probability

Luminance difference \( \Delta L \)
t.v.i function / c.v.i. function / Sensitivity

- The same data, different representation

**Threshold vs. intensity**

\[ \Delta L = L_{\text{disk}} - L_{\text{background}} \]

**Contrast vs. intensity**

\[ T = \frac{\Delta L}{L} \]

**Sensitivity**

\[ S = \frac{1}{T} = \frac{L}{\Delta L} \]
Sensitivity to luminance

- Weber-law – the just-noticeable difference is proportional to the magnitude of a stimulus

\[ \frac{\Delta L}{L} = k \]

- The smallest detectable luminance difference
- Background (adapting) luminance
- Typical stimuli:

Ernst Heinrich Weber
[From wikipedia]
Consequence of the Weber-law

- Smallest detectable difference in luminance
  \[
  \frac{\Delta L}{L} = k
  \]
  For $k=1\%$

<table>
<thead>
<tr>
<th>L</th>
<th>$\Delta L$</th>
</tr>
</thead>
<tbody>
<tr>
<td>100 cd/m²</td>
<td>1 cd/m²</td>
</tr>
<tr>
<td>1 cd/m²</td>
<td>0.01 cd/m²</td>
</tr>
</tbody>
</table>

- Adding or subtracting luminance will have different visual impact depending on the background luminance
- Unlike LDR luma values, luminance values are not perceptually uniform!
How to make luminance (more) perceptually uniform?

- Using “Fechnerian” integration

\[
\frac{dR}{dl}(L) = \frac{1}{\Delta L(L)}
\]

Derivative of response

Detection threshold

Luminance transducer:

\[
R(L) = \int_{L_{\text{min}}}^{L} \frac{1}{\Delta L(l)} \, dl
\]
Assuming the Weber law

\[ \frac{\Delta L}{L} = k \]

and given the luminance transducer

\[ R(L) = \int \frac{1}{\Delta L(l)} dl \]

the response of the visual system to light is:

\[ R(L) = \int \frac{1}{kL} dL = \frac{1}{k} \ln(L) + k_1 \]
Fechner law

\[ R(L) = a \ln(L) \]

- Response of the visual system to luminance is approximately logarithmic

Gustav Fechner
[From Wikipedia]
But...the Fechner law does not hold for the full luminance range

- Because the Weber law does not hold either
- Threshold vs. intensity function:

![Graph showing the threshold vs. intensity function with a region labeled as the Weber law region]
Weber-law revisited

- If we allow detection threshold to vary with luminance according to the t.v.i. function:

\[ R(L) = \int_0^L \frac{1}{tvi(l)} \, dl \]

- we can get a more accurate estimate of the “response”:
Fechnerian integration and Stevens’ law

\[ R(L) = \int_{0}^{L} \frac{1}{tvi(l)} \, dl \]
Applications of JND encoding – R(L)

- DICOM grayscale function
  - Function used to encode signal for medical monitors
  - 10-bit JND-scaled (just noticeable difference)
  - Equal visibility of gray levels

- HDMI 2.0a (HDR10)
  - PQ (Perceptual Quantizer) encoding
  - Dolby Vision
  - To encode pixels for high dynamic range images and video
Models of early visual perception

Part 3/6 – spatial contrast sensitivity and contrast constancy

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Resolution and sampling rate

- **Pixels per inch [ppi]**
  - Does not account for vision

- **The visual resolution depends on**
  - screen size
  - screen resolution
  - viewing distance

- **The right measure**
  - Pixels per visual degree [ppd]
  - In frequency space
    - Cycles per visual degree [cpd]
Fourier analysis

- Every N-dimensional function (including images) can be represented as a sum of sinusoidal waves of different frequency and phase.

\[ \sum \]

- Think of “equalizer” in audio software, which manipulates each frequency.
Spatial frequency in images

- Image space units: cycles per sample (or cycles per pixel)

- What are the screen-space frequencies of the red and green sinusoid?

- The visual system units: cycles per degree
  - If the angular resolution of the viewed image is 55 pixels per degree, what is the frequency of the sinusoids in cycles per degree?
Nyquist frequency

- Sampling density restricts the highest spatial frequency signal that can be (uniquely) reconstructed
  - Sampling density – how many pixels per image/visual angle/…

- Any number of sinusoids can be fitted to this set of samples
- It is possible to fit an infinite number of sinusoids if we allow infinitely high frequency
Nyquist frequency

- Sampling density restricts the highest spatial frequency signal that can be (uniquely) reconstructed
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- Any number of sinusoids can be fitted to this set of samples
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Nyquist frequency / aliasing

- Nuquist frequency is the highest frequency that can be represented by a discrete set of uniform samples (pixels)
- Nuquist frequency = 0.5 sampling rate
  - For audio
    - If the sampling rate is 44100 samples per second (audio CD), then the Nyquist frequency is 22050 Hz
  - For images (visual degrees)
    - If the sampling rate is 60 pixels per degree, then the Nyquist frequency is 30 cycles per degree
- When resampling an image to lower resolution, the frequency content above the Nyquist frequency needs to be removed (reduced in practice)
  - Otherwise aliasing is visible
Modeling contrast detection
Campbell & Robson contrast sensitivity chart
Contrast sensitivity function

\[ CSF = S(\rho, \theta, \omega, l, i^2, d, e) \]
CSF as a function of spatial frequency

Sensitivity ($L\Delta L$) vs. Spatial frequency [cpd]

$L_b = 0.001 \text{ cd/m}^2$
CSF as a function of background luminance
CSF as a function of spatial frequency and background luminance
Contrast constancy

Experiment: Adjust the amplitude of one sinusoidal grating until it matches the perceived magnitude of another sinusoidal grating.

Contrast constancy
No CSF above the detection threshold
CSF and the resolution

- CSF plotted as the detection contrast
  \[ \frac{\Delta L}{L_b} = S^{-1} \]
- The contrast below each line is invisible
- Maximum perceivable resolution depends on luminance

Expected contrast in natural images

CSF models:
https://doi.org/10.1117/12.537476
Spatio-chromatic CSF
Spatio-chromatic contrast sensitivity

- CSF as a function of luminance and frequency

Black-White

Red-Green

Violet-Yellow

http://dx.doi.org/10.2352/issn.2169-2629.2020.28.1
CSF and colour ellipses

- Colour discrimination as a function of
  - Background colour and luminance [LMS]
  - Spatial frequency [cpd]
  - Size [deg]
Visibility of blur

- The same amount of blur was introduced into light-dark, red-green and blue-yellow colour opponent channels.
- The blur is only visible in light-dark channel.
- This property is used in image and video compression.
  - Sub-sampling of colour channels (4:2:1)
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Part 4/6 – lateral inhibition and multi-resolution models

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Mach Bands – evidence for band-pass visual processing

- “Overshooting“ along edges
  - Extra-bright rims on bright sides
  - Extra-dark rims on dark sides
- Due to “Lateral Inhibition“
Centre-surround (Lateral Inhibition)

- “Pre-processing” step within the retina
- Surrounding brightness level weighted negatively
  - A: high stimulus, maximal bright inhibition
  - B: high stimulus, reduced inhibition & stronger response
  - D: low stimulus, maximal inhibition
  - C: low stimulus, increased inhibition & weaker response

Center-surround receptive fields (groups of photoreceptors)
Centre-surround: Hermann Grid

• Dark dots at crossings

• Explanation
  – Crossings (A)
    • More surround stimulation
      (more bright area)
      ⇒ Less inhibition
      ⇒ Weaker response
  – Streets (B)
    • Less surround stimulation
      ⇒ More inhibition
      ⇒ Greater response

• Simulation
  – Darker at crossings, brighter in streets
  – Appears more steady
  – What if reversed?
some further weirdness
Spatial-frequency selective channels

- The visual information is decomposed in the visual cortex into multiple channels
  - The channels are selective to spatial frequency, temporal frequency and orientation
  - Each channel is affected by different „noise” level
  - The CSF is the net result of information being passed in noise-affected visual channels

From: Wandell, 1995
Multi-scale decomposition

Steerable pyramid decomposition
Multi-resolution visual model

- Convolution kernels are band-pass, orientation selective filters

- The filters have the shape of an oriented Gabor function

From: Wandell, 1995
Predicting visible differences with CSF

- We can use CSF to find the probability of spotting a difference between a pair of images $X_1$ and $X_2$:

$$p(f[X_1] = f[X_2] | X_1, X_2, CSF)$$

Computing contrast:

$$\Delta L = L_b - \frac{\Delta L}{L_b \Delta L_{th}}$$

Psychometric function:

$$P_{detection}$$

(simplified) Visual Difference Predictor

Applications of multi-scale models

- **JPEG2000**
  - Wavelet decomposition

- **JPEG / MPEG**
  - Frequency transforms

- **Image pyramids**
  - Blending & stitching
  - Hybrid images

Hybrid Images by Aude Oliva
http://cvcl.mit.edu/hybrid_gallery
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Models of early visual perception

Part 5/6 – light and dark adaptation

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Light and dark adaptation

- Light adaptation: from dark to bright
- Dark adaptation: from bright to dark (much slower)
Time-course of adaptation

Bright $\rightarrow$ Dark

Dark $\rightarrow$ Bright
Temporal adaptation mechanisms

- **Bleaching & recovery of photopigment**
  - Slow asymmetric (light -> dark, dark -> light)
  - Reaction times (1-1000 sec)
  - Separate time-course for rods and cones

- **Neural adaptation**
  - Fast
  - Approx. symmetric reaction times (10-3000 ms)

- **Pupil**
  - Diameter varies between 3 and 8 mm
  - About 1:7 variation in retinal illumination
Night and daylight vision

Vision mode:

<table>
<thead>
<tr>
<th>Vision mode</th>
<th>SCOTOPIC</th>
<th>MESOPIC</th>
<th>PHOTOPIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>rod activity</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>cone activity</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Luminance $[\log \text{ cd/m}^2]$

Mode properties:

- **Night light**
  - Monochromatic vision
  - Limited visual acuity

- **Office light**
  - Good color perception
  - Good visual acuity

- **Daylight**
  - Rod $V'(\lambda)$
  - Cone $V(\lambda)$

Luminous efficiency
Models of early visual perception

Part 6/6 – high(er) level vision

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Simultaneous contrast
High-Level Contrast Processing
High-Level Contrast Processing
Shape Perception

- Depends on surrounding primitives
  - Directional emphasis
  - Size emphasis

http://www.panoptikum.net/optischetaeuschanungen/index.html
Shape Processing: Geometrical Clues

- Automatic geometrical interpretation
  - 3D perspective
  - Implicit scene depth

http://www.panoptikum.net/optischetaeuschungen/index.html
Impossible Scenes

- Escher et.al.
  - Confuse HVS by presenting contradicting visual clues
  - Local vs. global processing

http://www.panoptikum.net/optischetaeuschungen/index.html
Virtual Movement caused by saccades, motion from dark to bright areas
Law of closure
References

  - Section 2.4
  - Available online: http://www.cl.cam.ac.uk/~rkm38/hdri_book.html