

Advanced Graphics & Image Processing

Advanced image processing

Part 1/2 – edge stopping filters

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Edge stopping filters



Original



Edge-aware smoothing



Detail enhancement



Stylization

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Recoloring



Pencil drawing



Depth-of-field

Examples from [Gastal & Oliveira 2011]

Nonlinear filters: Bilateral filter

Goal: Smooth out the image without blurring edges







How to make the bilateral filter fast?

- A number of approximations have been proposed
 - Combination of linear filters [Durand & Dorsey 2002, Yang et al. 2009]
 - Bilateral grid [Chen et al. 2007]
 - Permutohedral lattice [Adams et al. 2010]
 - Domain transform [Gastal & Oliveira 2011]

Joint-bilateral filter (a.k.a guided/cross b.f.)

- The "range" term does not need to operate in the same domain as the filter output
 - Example:



A simplified

Joint bilateral filter: Flash / no-flash



Flash

No-flash

- Preserve colour and illumination from the no-flash image
- Use flash image to remove noise and add details
- [Petshnigg et al. 2004]



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Example of edge preserving filtering

- Domain Transform for Edge-Aware Image and Video Processing
- Video:
 - https://youtu.be/UIIxhIIQrTY?t=4mI0s
 - From: <u>http://inf.ufrgs.br/~eslgastal/DomainTransform/</u>





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Part 1/2 – processing by optimization

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Optimization-based methods



cloning

seamless cloning

Poisson image editing [Perez et al. 2003]

sources/destinations

Gradient Domain compositing

Compositing [Wang et al. 2004]



Gradient domain methods

Operate on pixel gradients instead of pixel values



Forward Transformation

Forward Transformation

 Compute gradients as differences between a pixel and its two neighboors

$$\nabla I_{x,y} = \begin{bmatrix} I_{x+1,y} - I_{x,y} \\ I_{x,y+1} - I_{x,y} \end{bmatrix}$$

Result: 2D gradient map (2 x more values then the number of pixels)

Processing gradient field

 Usually gradient magnitudes are modified while gradient direction (angle) remains the same
 Gradient editing

 $G_{x,y} = \nabla I_{x,y} \cdot \frac{f\left(||\nabla I_{x,y}||\right)}{||\nabla I_{x,y}||}$

function

• Examples of gradient editing functions:



Inverse transform: the difficult part

 There is no strightforward transformation from gradients to luminance



Instead, a minimization problem is solved:

$$\underset{I}{\operatorname{arg\,min}} \sum_{x,y} \left[\left(I_{x+1,y} - I_{x,y} - G_{x,y}^{(x)} \right)^2 + \left(I_{x,y+1} - I_{x,y} - G_{x,y}^{(y)} \right)^2 \right]$$

$$\underbrace{\left[\operatorname{Image\,Pixels} \right]}_{\text{Image Pixels}}$$

Inverse transformation

- Convert modified gradients to pixel values
 - Not trivial!
 - Most gradient fields are inconsistent - do not produce valid images
 - If no accurate solution is available, take the best possible solution
 - Analogy: system of springs



Gradient field reconstruction: derivation

The minimization problem is given by:

$$\arg\min_{I} \sum_{x,y} \left[\left(I_{x+1,y} - I_{x,y} - G_{x,y}^{(x)} \right)^2 + \left(I_{x,y+1} - I_{x,y} - G_{x,y}^{(y)} \right)^2 \right]$$

After equating derivatives over pixel values to 0 we get:

Derivation done in the lecture

$$I_{x-1,y} + I_{x+1,y} + I_{x,y-1} + I_{x,y+1} - 4I_{x,y} = G_{x,y}^{(x)} - G_{x-1,y}^{(x)} + G_{x,y}^{(y)} - G_{x,y-1}^{(y)}$$

In matrix notation:

$$\nabla^{2}I = \operatorname{div}G$$

$$\nabla^{2}I = \operatorname{div}G$$

$$\int \operatorname{I}_{x,y} = I_{x-1,y} + I_{x+1,y} + I_{x,y-1} + I_{x,y+1} - 4I_{x,y}$$

$$\int \operatorname{Image as}_{a \text{ column}} I_{x,y}$$

$$I_{x,y} = I_{x-1,y} + I_{x+1,y} + I_{x,y-1} + I_{x,y+1} - 4I_{x,y}$$

$$\int \operatorname{Image as}_{a \text{ column}} I_{x,y}$$

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$$\int I_{x,y} = I_{x-1,y} + I_{x+1,y} + I_{x,y-1} + I_{x,y+1} - 4I_{x,y}$$

$$\nabla^{2} = \begin{bmatrix} -2 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & -3 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & -2 & 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & -3 & 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & -4 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & -3 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & -2 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & -3 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & -2 \end{bmatrix}$$

Solving sparse linear systems

- Just use "\" operator in Matlab / Octave:
 - ▶ x = A \ b;
- Great "cookbook":
 - TEUKOLSKY, S.A., FLANNERY, B.P., PRESS, W.H., AND VETTERLING, W.T. 1992. Numerical recipes in C. Cambridge University Press, Cambridge.
- Some general methods
 - Cosine-transform fast but cannot work with weights (next slides) and may suffer from floating point precision errors
 - Multi-grid fast, difficult to implement, not very flexible
 - Conjugate gradient / bi-conjugate gradient general, memory efficient, iterative but fast converging
 - Cholesky decomposition effective when working on sparse matrices

Pinching artefacts

- A common problem of gradient-based methods is that they may result in "pinching" artefacts (left image)
- Such artefacts can be avoided by introducing weights to the optimization problem



Weighted gradients

The new objective function is:

$$\arg\min_{I} \sum_{x,y} \left[w_{x,y}^{(x)} \left(I_{x+1,y} - I_{x,y} - G_{x,y}^{(x)} \right)^2 + w_{x,y}^{(y)} \left(I_{x,y+1} - I_{x,y} - G_{x,y}^{(y)} \right)^2 \right]$$

 so that higher weights are assigned to low gradient magnitudes (in the original image).

$$w_{x,y}^{(x)} = w_{x,y}^{(y)} = \frac{1}{||\nabla I_{x,y}^{(o)}|| + \epsilon}$$

- The linear system can be derived again
 - but this is a lot of work and is error-prone

Weighted gradients - matrix notation (1)

The objective function:

$$\arg\min_{I} \sum_{x,y} \left[w_{x,y}^{(x)} \left(I_{x+1,y} - I_{x,y} - G_{x,y}^{(x)} \right)^2 + w_{x,y}^{(y)} \left(I_{x,y+1} - I_{x,y} - G_{x,y}^{(y)} \right)^2 \right]$$

In the matrix notation (without weights for now):

$$\underset{I}{\operatorname{arg\,min}} \left\| \begin{bmatrix} \nabla_x \\ \nabla_y \end{bmatrix} I - \begin{bmatrix} G^{(x)} \\ G^{(y)} \end{bmatrix} \right\|^2$$

Gradient operators (for 3x3 pixel image):

Weighted gradients - matrix notation (2)

The objective function again:

$$\underset{I}{\operatorname{arg\,min}} \left\| \begin{bmatrix} \nabla_x \\ \nabla_y \end{bmatrix} I - \begin{bmatrix} G^{(x)} \\ G^{(y)} \end{bmatrix} \right\|^2$$

Such over-determined least-square problem can be solved using pseudo-inverse:

$$\begin{bmatrix} \nabla'_x & \nabla'_y \end{bmatrix} \begin{bmatrix} \nabla_x \\ \nabla_y \end{bmatrix} I = \begin{bmatrix} \nabla'_x & \nabla'_y \end{bmatrix} \begin{bmatrix} G^{(x)} \\ G^{(y)} \end{bmatrix}$$

Or simply:

$$\left(\nabla'_x \nabla_x + \nabla'_y \nabla_y\right) I = \nabla'_x G^{(x)} + \nabla'_y G^{(y)}$$

With weights:

$$\left(\nabla'_x W \nabla_x + \nabla'_y W \nabla_y\right) I = \nabla'_x W G^{(x)} + \nabla'_y W G^{(y)}$$

WLS filter: Edge stopping filter by optimization

Weighted-least-squares optimization



 [Farbman, Z., Fattal, R., Lischinski, D., & Szeliski, R. (2008). Edge-preserving decompositions for multi-scale tone and detail manipulation. ACM SIGGRAPH 2008, 1–10.]

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Poisson image editing



- Reconstruct unknown values f given a source guidance gradient field v and the boundary conditions $f|_{\partial\Omega} = f^*|_{\partial\Omega}$
- [Pérez, P., Michel Gangnet, & Blake, A. (2003). Poisson Image Editing. ACM Transactions on Graphics, 3(22), 313–318. https://doi.org/10.1145/882262.882269]

Color 2 Gray

- Transform color images to gray scale
- Preserve color saliency
 - When gradient in luminance close to 0
 - Replace it with gradient in chrominance
 - Reconstruct an image from gradients
- Gooch, A. A., Olsen, S. C., Tumblin, J., & Gooch, B. (2005). Color2Gray. ACM Transactions on Graphics, 24(3), 634. https://doi.org/10.1145/1073204.1073241



Gradient Domain: applications

- More applications:
 - Lightness perception (Retinex) [Horn 1974]
 - Matting [Sun et al. 2004]
 - Color to gray mapping [Gooch et al. 2005]
 - Video Editing [Perez at al. 2003, Agarwala et al. 2004]
 - Photoshop's Healing Brush [Georgiev 2005]

References

- F. Durand and J. Dorsey, "Fast bilateral filtering for the display of high-dynamic-range images," ACM Trans. Graph., vol. 21, no. 3, pp. 257–266, Jul. 2002.
- E. S. L. Gastal and M. M. Oliveira, "Domain transform for edge-aware image and video processing," *ACM Trans. Graph.*, vol. 30, no. 4, p. 1, Jul. 2011.
- Patrick Pérez, Michel Gangnet, and Andrew Blake. 2003. Poisson image editing. ACM Trans. Graph. 22, 3 (July 2003), 313-318. DOI: <u>http://dx.doi.org/10.1145/882262.882269</u>
- Zeev Farbman, Raanan Fattal, Dani Lischinski, and Richard Szeliski. 2008. Edgepreserving decompositions for multi-scale tone and detail manipulation. ACM Trans. Graph. 27, 3, Article 67 (August 2008), 10 pages. DOI: https://doi.org/10.1145/1360612.1360666