## 1997 Paper 1 Question 5

## Foundations of Computer Science

This question has been translated from Standard ML to OCaml
Noughts and Crosses is a game played by two players ( O and X ) on a board with nine positions numbered as follows:

| 1 | 2 | 3 |
| :--- | :--- | :--- |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

The players place their marks ( O and X ) in unoccupied positions on the board until the game is complete. A completed game is when either
(a) there is a straight line of three X s giving a win for X , or
(b) there is a straight line of three Os giving a win for O , or
(c) all nine positions are occupied, in which case the game is drawn.

O is the first player to move.
It is required to construct an OCaml structure representing the tree of all possible games. Each node of the tree should represent a reachable board state, with the root being the empty board, and the leaf nodes corresponding to won, lost or drawn games.

Define the OCaml variant type tree that you would use to represent this game tree.

Define the function mktree : unit -> tree to construct the complete game tree, explaining carefully how it works. There is no need for your implementation to be efficient in either space or time.
[10 marks]
Briefly discuss ways in which your implementation of mktree could be made more efficient.

Define a function winner_is_0 : tree -> int which when applied to the complete tree will yield the number of distinct games in which O wins.

