EQUALITY IN PROOFS

Examples

of and b=c Then a=cof and x=y Then a+x=b+x=b+y

Equality axioms

Just for the record, here are the axioms for *equality*.

Every individual is equal to itself.

$$\forall x. \ x = x$$

► For any pair of equal individuals, if a property holds for one of them then it also holds for the other one.

$$\forall x. \forall y. \ x = y \implies (P(x) \implies P(y))$$

NB From these axioms one may deduce the usual intuitive properties of equality, such as

$$\forall x. \forall y. x = y \implies y = x$$

and

$$\forall x. \forall y. \forall z. \ x = y \implies (y = z \implies x = z)$$
.

However, in practice, you will not be required to formally do so; rather you may just use the properties of equality that you are already familiar with.