## Introduction to Functional Programming Lent 2006 Exercises on functions and lists

- 1. Write a functional to compute the minimum value  $\min_{k=0}^{\ell} f(k)$  of a function f on the integers. Use the functional to express the two dimensional minimum  $\min_{i=0}^{m} \min_{j=0}^{n} g(i, j)$  of an integer valued function g of two integer arguments.
- 2. Write a function of type 'a list list -> bool that checks whether or not its input is a matrix. Give versions with list functionals and without.
- 3. Give implementations for all the operations on sets that you can think of (including membership testing, intersection, union, complement, inverse and direct images, characteristic function, *etc.*) for the following two representations

```
(a) type 'a set = 'a -> bool
(b) type 'a set = 'a list
```

of sets.

4. Consider the following type

```
type ('i,'o,'s) IODAutomata' = 's * 'i -> 'o * 's option
```

of input/output deterministic automata.

Write simple recursive and tail recursive versions of a function

```
val run = fn :
    ('i,'o,'s) IODAutomata' -> 's option -> 'i list -> 'o list
```

such that

```
run A s i
```

runs the automata A from the initial state s with the input sequence i producing the corresponding output sequence.

Repeat the exercise for the following type of automata:

type ('i,'o,'s) IODAutomata = 's \* 'i -> ('o \* 's) option

5. Compare the (evaluation of) the simple recursive, tail recursive, and the following continuation-passing style version

```
fun CPSfact n
= let
    fun auxCPSfact( n , k )
        = if n = 0 then k(1)
            else auxCPSfact( n-1 , fn x => k(n*x) )
    in
        auxCPSfact( n , fn x => x )
    end ;
```

of the factorial function.