### Concepts in Programming Languages

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CST Paper 7: 2019–2020 (Easter Term)

www.cl.cam.ac.uk/teaching/1920/ConceptsPL/

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#### Main books

- ► J. C. Mitchell. *Concepts in programming languages*. Cambridge University Press, 2003.
- ► T. W. Pratt and M. V. Zelkowitz. *Programming Languages:*Design and implementation (3RD EDITION).

  Prentice Hall, 1999.
- ★ M. L. Scott. Programming language pragmatics (4TH EDITION). Elsevier, 2016.
- R. Harper. Practical Foundations for Programming Languages.
   Cambridge University Press, 2013.

#### **Practicalities**

Course web page:

www.cl.cam.ac.uk/teaching/1920/ConceptsPL/with *lecture slides*, *exercise sheet* and *reading material*. These slides play two roles – both "lecture notes" and "presentation material"; not every slide will be lectured in detail.

- ► There are various code examples (particularly for JavaScript and Java applets) on the 'materials' tab of the course web page.
- One exam question.
- ► The syllabus and course has changed somewhat from that of 2015/16. I would be grateful for comments on any remaining 'rough edges', and for views on material which is either over- or under-represented.

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#### Context:

so many programming languages

Peter J. Landin: "The Next 700 Programming Languages", CACM (published in 1966!).

Some programming-language 'family trees' (too big for slide):

http://www.levenez.com/lang/
http://rigaux.org/language-study/diagram.html

Wikipedia's historical summary page: https://en. wikipedia.org/wiki/History\_of\_programming\_languages

Plan of this course: pick out interesting programming-language concepts and major evolutionary trends.

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<sup>&</sup>lt;sup>1</sup>Acknowledgement: various slides are based on Marcelo Fiore's 2013/14 course.

# **Topics**

Introduction and motivation.

Part A: Meet the ancestors

II. The first *procedural* language: FORTRAN (1954–58).

III. The first *declarative* language: LISP (1958–62).

IV. Block-structured languages: Algol (1958–68), Pascal (1970).

V. *Object-oriented* languages: Simula (1964–67), Smalltalk (1972).

Part B: Types and related ideas

VI. *Types* in programming languages: ML, Java.

VII. Scripting Languages: JavaScript.

VIII. Data abstraction and modularity: SML Modules.

Part C: Distributed concurrency, Java lambdas, Scala, Monads

IX. Languages for *concurrency and parallelism*.

X. Functional-style programming meets object-orientation.

XI. Miscellaneous concepts: Monads, GADTs.

# ~ Topic I ~

Introduction and motivation

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#### Goals

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- Critical thinking about programming languages.
  - What is a programming language!?
  - ▶ Who defines it?
  - ► How can it be changed?
- Study programming languages.
  - ▶ Be familiar with basic language *concepts*.
  - ► Appreciate trade-offs in language *design*.
- ► Trace *history*, appreciate *evolution* and diversity of *ideas*.
- ▶ Be prepared for new programming *methods*, *paradigms*.

# Why study programming languages?

- ► To improve the ability to develop effective algorithms.
- ► To improve the use of familiar languages.
- ► To increase the vocabulary of useful programming constructs.
- ► To allow a better choice of programming language.
- ► To make it easier to learn a new language.
- ► To make it easier to design a new language.
- ▶ To simulate useful features in languages that lack them.
- ► To make better use of language technology wherever it appears.

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### What makes a good language?

- Clarity, simplicity, and unity.
- Orthogonality.
- Naturalness for the application.
- Support of abstraction.
- Ease of program verification.
- Programming environments.
- Portability of programs.
- Cost of use.
  - Cost of execution.
  - Cost of program translation.
  - ► Cost of program creation, testing, and use.
  - Cost of program maintenance.

- ? Why are there so many languages?
- Evolution.
- Special purposes.
- No one language is good at expressing all programming styles.
- Personal preference.
- ? What makes languages evolve?
  - ► Changes in hardware or implementation platform
  - Changes in attitudes to safety and risk
  - New ideas from academic or industry

### What makes a language successful?

- ► Expressive power.
- Ease of use for the novice.
- ► Ease of implementation.
- Standardisation.
- Many useful libraries.
- Excellent compilers (including open-source)
- ► Economics, patronage, and inertia.

Note the recent trend of big companies to create/control their own languages: C# (Microsoft), Hack (Facebook), Go (Google), Objective-C/Swift (Apple), Rust (Mozilla) and perhaps even Python (Dropbox hired Guido van Rossum).

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# Motivating purpose and language design

A specific purpose or motivating application provides *focus* for language design—what features to include and (harder!) what to leave out. E.g.

- Lisp: symbolic computation, automated reasoning
- ▶ FP: functional programming, algebraic laws
- ▶ BCPL: compiler writing
- ► Simula: simulation
- C: systems programming [Unix]
- ML: theorem proving
- Smalltalk: Dynabook [1970-era tablet computer]
- ► Clu, SML Modules: modular programming
- ► C++: object orientation
- ► Java, JavaScript: Internet applications

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### Program execution model

Good language design presents abstract machine.

- Fortran: Flat register machine; memory arranged as linear array
- Lisp: cons cells, read-eval-print loop
- ► Algol family: stack of activation records; heap storage
- ▶ BCPL, C: underlying machine + abstractions
- Simula: Object references
- ▶ FP, ML: functions are basic control structure
- Smalltalk: objects and methods, communicating by messages
- Java: Java virtual machine

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#### Language standardisation

Consider: int i; i = (1 && 2) + 3;

- ? Is it valid C code? If so, what's the value of i?
- ? How do we answer such questions!?
  - ! Read the reference manual (ISO C Standard).
  - ! Try it and see!

Other languages may have *informal* standards (defined by a particular implementation but what do we do if the implementation is improved?) or *proprietary* standards.

### Classification of programming languages

See en.wikipedia.org/wiki/Programming\_paradigm for more detail:

Imperative

procedural C, Ada, **Pascal**, **Algol**, **Fortran**, ... object-oriented scripting C, Ada, **Pascal**, **Algol**, **Fortran**, ... **Scala**, C#,Java, **Smalltalk**, **SIMULA**, ... Perl, Python, PHP, JavaScript, ...

Declarative

functional Haskell, SML, Lisp, Scheme, ...

logic Prolog dataflow Id, Val

constraint-based spreadsheets

template-based XSLT

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### Language-standards issues

Timeliness. When do we standardise a language?

Conformance. What does it mean for a program to adhere to a standard and for a compiler to compile a standard?

Ambiguity and freedom to optimise – Machine dependence – Undefined behaviour.

A language standard is a treaty setting out the rights and obligations of the programmer and the implementer.

Obsolescence. When does a standard age and how does it get modified?

Deprecated features.

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### Language standards: unintended mis-specification

- ► Function types in Algol 60, see later.
- In language PL/1 the type DEC (p, q) meant a decimal number of p digits (at most 15) with q digits after the decimal point, so 9, 8, 3 all had type DEC (1, 0). Division was defined to so that 8/3 was DEC (15, 14) with value 2.666 666 666 666.
  But addition was defined so that adding these two was also of type DEC (15, 14), which meant that 9 + 8/3 gave 11.666 666 666 666 666, which didn't fit. This gave either overflow or the wrong answer of 1.666 666 666 666.
- ► A more recent example is C++11's "out of thin air" behaviour, whereby the ISO specification allows the value 42 to appear as the result of a program only involving assignments of 0 and 1.

Argh! Be careful how you specify a language.

#### **Ultra-brief history**

1951–55: Experimental use of expression compilers.
1956–60: Fortran, COBOL, Lisp, Algol 60.
1961–65: APL notation, Algol 60 (revised), SNOBOL, CPL.
1966–70: APL, SNOBOL 4, Fortran 66, BASIC, SIMULA,
Algol 68, Algol-W, BCPL.
1971–75: Pascal, PL/1 (Standard), C, Scheme, Prolog.
1976–80: Smalltalk, Ada, Fortran 77, ML.
1981–85: Smalltalk-80, Prolog, Ada 83.
1986–90: C++, SML, Haskell.
1991–95: Ada 95, TCL, Perl.
1996–2000: Java, JavaScript
2000–05: C#, Python, Ruby, Scala.

1990- : Open/MP, MPI, Posix threads, Erlang, X10,

#### For more information:

en.wikipedia.org/wiki/History\_of\_programming\_ languages

MapReduce, Java 8 features.

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#### Meet the ancestors

Santayana 1906: "Those who cannot remember the past are condemned to repeat it."



FORTRAN: A simple procedural language

#### **Further reading:**

The History of FORTRAN I, II, and III by J. Backus. In History of Programming Languages by R. L. Wexelblat. Academic Press, 1981.

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### FORTRAN = FORmula TRANslator (1957)

- Developed (1950s) by an IBM team led by John Backus: "As far as we were aware, we simply made up the language as we went along. We did not regard *language design* as a difficult problem, merely a simple prelude to the real problem: designing a compiler which could produce efficient programs."
- ► The first high-level programming language to become widely used. At the time the utility of any high-level language was open to question(!), and complaints focused on efficiency of generated code. This heavily influenced the design, orienting it towards execution efficiency.
- Standards: 1966, 1977 (FORTRAN 77), 1990 (Fortran 90, spelling change), ..., 2018 (Fortran 2018).
- ► Remains main language for scientific computing.
- Easier for a compiler to optimise than C.

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### Overview: Data types and storage allocation

▶ Numerics: Integer, real, complex, double-precision real.

▶ Boolean.

called logical

Arrays.

of fixed declared length

Character strings.

of fixed declared length

- Files.
- ► Fortran 90 added 'derived data types' (like C structs).

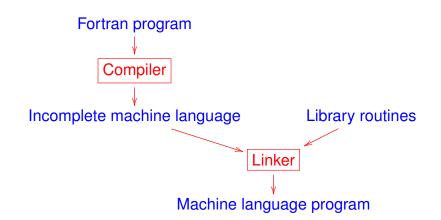
#### Allocation:

- Originally all storage was allocated statically before program execution, even local variables (as early Fortran lacked recursion—machines often lacked the index registers needed for a cheap stack—and we didn't realise how useful stacks and recursion would be!).
- Modern Fortran has recursion and heap-allocated storage.

#### Overview: Compilation

Fortran program = main program + subprograms

- Each is compiled separately from all others.
   (Originally no support for cross-module checking, still really true for C and C++.)
- ► Translated programs are *linked* into final executable form.



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#### Overview

#### Control structures

► FORTRAN 66

Relied heavily on statement labels and GOTO statements, but did have DO (for) loops.

► FORTRAN 77

Added some modern control structures (*e.g.*, if-then-else blocks), but WHILE loops and recursion had to wait for Fortran 90.

► Fortran 2008

Support for concurrency and objects

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# Example (Fortran 77)

```
PROGRAM MAIN
        PARAMETER (MaXsIz=99)
        REAL A (mAxSiZ)
  10
        READ (5,100,END=999) K
 100
        FORMAT (I5)
          IF (K.LE.O .OR. K.GT.MAXSIZ) STOP
          READ \star, (A(I), I=1, K)
          PRINT \star, (A(I), I=1, K)
          PRINT *, 'SUM=', SUM(A, K)
          GO TO 10
        PRINT *, 'All Done'
 999
        STOP
        END
C SUMMATION SUBPROGRAM
      FUNCTION SUM(V,N)
        REAL V(N)
        SUM = 0.0
        DO 20 I = 1.N
          SUM = SUM + V(I)
          CONTINUE
        RETURN
        END
```

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- Data formats for I/O.
- ▶ Historically functions are compiled separately from the main program with no consistency checks. Failure may arise (either at link time or execution time) when subprograms are linked with main program.
  - Fortran 90 provides a module system.
- ► Function parameters are uniformly transmitted by reference (like C++ '&' types). But Fortran 90 provided INTENT(IN) and INTENT(OUT) type qualifiers and Fortran 2003 added pass-by-value for C interoperability.
- ► Traditionally all allocation is done statically. But Fortran 90 provides dynamic allocation and recursion.
- ► A value is returned in a Fortran function by assigning a value to the name of a function.

#### Example

#### Commentary

- Originally columns and lines were relevant, and blanks and upper/lower case are ignored except in strings. Fortran 90 added free-form and forbade blanks in identifiers (use the .f90 file extension on Linux).
- Variable names are from 1 to 6 characters long (31 since Fortran 90), letters, digits, underscores only.
- ▶ Variables need not be declared: implicit naming convention determines their type, hence the old joke "GOD is REAL (unless declared INTEGER)"; good programming style uses IMPLICIT NONE to disable this.
- ► Programmer-defined constants (PARAMETER)
- Arrays: subscript ranges can be declared as (Iwb: upb) with (size) meaning (1 : size).

### Program consistency checks

- ► Static type checking is used in Fortran, but the checking is traditionally incomplete.
- Many language features, including arguments in subprogram calls and the use of COMMON blocks, were not statically checked (in part because subprograms are compiled independently).
- Constructs that could not be statically checked were often left unchecked at run time (e.g. array bounds). (An early preference for speed over ease-of-bug-finding still visible in languages like C.)
- ► Fortran 90 added a MODULE system with INTERFACES which enables checking across separately compiled subprograms.

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### Parameter-passing modes

- ▶ Recall the terms *formal parameter* and *actual parameter*.
- ► Fortran provides *call-by-reference* as historic default, similar to *reference parameters* in C++ (the formal parameter becomes an *alias* to the actual parameter).
- ► The language specifies that if a value is assigned to a formal parameter, then the actual parameter must be a variable. This is a traditional source of bugs as it needs cross-module compilation checking:

```
SUBROUTINE SUB(X,Y,Z)

X = Y

PRINT *,Z

END

CALL SUB(-1.0, 1.0, -1.0)
```

▶ Modern Fortran adds *call-by-value* as in C/C++.

We will say more about parameter-passing modes for other languages.



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LISP: functions, recursion, and lists

#### Fortran lives!

- Fortran is one of the first languages, and the only early language still in mainstream use (LISP dialects also survive, e.g. Scheme).
- ▶ Lots of CS people will tell you about all the diseases of Fortran based on hearsay about Fortran 66, or Fortran 77.
- Modern Fortran still admits (most) old code for backwards compatibility, but also has most of the things you expect in a modern language (objects, modules, dynamic allocation, parallel constructs). There's even a proposal for "units of measure" to augment types. (Language evolution is preferable to extinction!)
- Don't be put off by the syntax—or what ill-informed people say.

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# LISP = LISt Processing (circa 1960)

- Developed in the late 1950s and early 1960s by a team led by John McCarthy at MIT. McCarthy described LISP as a "a scheme for representing the partial recursive functions of a certain class of symbolic expressions".
- Motivating problems: Symbolic computation (symbolic differentiation), logic (Advice taker), experimental programming.
- Software embedding LISP: Emacs (text editor),
   GTK (Linux graphical toolkit), Sawfish (window manager),
   GnuCash (accounting software).
- Current dialects: Common Lisp, Scheme, Clojure. Common Lisp is 'most traditional', Clojure is implemented on JVM.

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# Programming-language phrases

[This classification arose in the Algol 60 design.]

- Expressions. A syntactic entity that may be evaluated to determine its value.
- Statement. A command that alters the state of the machine in some explicit way.
- ► *Declaration*. A syntactic entity that introduces a new identifier, often specifying one or more attributes.

► LISP is an *expression-based* language. LISP introduced the idea of *conditional expressions*.

▶ Lists – dynamic storage allocation, *hd* (CAR) and *tl* (CDR).

Some contributions of LISP

- Recursive functions.
- Garbage collection.
- Programs as data.
- ► Self-definitional interpreter (LISP interpreter explained as a LISP program).

The core of LISP is pure functional, but *impure* (side-effecting) constructs (such as SETQ, RPLACA, RPLACD) were there from the start.

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#### Overview

- Values in LISP are either atoms, e.g. x, FOO, NIL, or cons cells which contain two values.
  (Numbers are also atoms, but only literal atoms above can be used as variables below.)
- ► A LISP program is just a special case of a LISP value known as an *S-expression*. An S-expression is either an *atom* or a NIL-terminated list of S-expressions (syntactically written in parentheses and separated by spaces), e.g. (FOO ((1 2) (3)) NIL (4 X 5)).
- ► So right from the start programs are just data, so we can construct a value and then execute it as a program.
- ► LISP is a *dynamically typed* programming language, so heterogeneous lists like the above are fine.

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Programs represented as S-expressions are evaluated to give values, treating atoms as variables to be looked up in an environment, and lists as a function (the first element of the list) to be called along with its arguments (the rest of the list).

#### **Example:**

```
(APPEND (QUOTE (FOO 1 Y)) (CONS 3 (CONS 'Z NIL))) evaluates to (FOO 1 Y 3 Z).
```

Note: the functions cons and APPEND behaves as in ML, and the function QUOTE returns its argument unevaluated. Numbers and the atoms NIL and T (also used as booleans) evaluate to themselves.

To ease typing LISP programs, (QUOTE e) can be abbreviated 'e, see 'Z above.
 This is done as part of the READ function which reads values (which of course can also be programs).

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#### ? How does one recognise a LISP program?

```
( defvar x 1 )
                               val x = 1;
(defun g(z) (+ x z))
                               fun g(z) = x + z ;
( defun f(y)
                               fun f(y)
                                 = g(y) +
   (+(qy)
       ( let
                                   let
                                    val x = y
           ((xy))
             gx)
                                    q(x)
         ) ) )
                                   end ;
(f (+ x 1))
                               f(x+1);
```

! It is full of brackets ("Lots of Irritating Silly Parentheses")!

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### Core LISP primitives (2)

#### Example:

Life is simpler with arithmetic and higher-order functions:

```
+, -, < etc. E.g. (+ X 1)

LAMBDA: e.g. (LAMBDA (X Y) (+ X Y))

APPLY: e.g. (APPLY F '(1 2))</pre>
```

Note LAMBDA is also a special form.

### Core LISP primitives

The following primitives give enough (Turing) power to construct any LISP function.

- ► CONS, CAR, CDR: cons, hd, tl.
- ► CONSP, ATOM: boolean tests for being a cons cell or atom.
- ▶ EQ, boolean equality test for equal atoms (but beware using it on large numbers which may be boxed, cf. Java boxing).
- ▶ QUOTE: return argument unevaluated.
- ► COND, conditional expression: e.g.

  (COND ((CONSP X) (CDR X)) (T NIL)).

Note that most LISP functions evaluate their arguments before they are called, but ('special forms') QUOTE and COND do not.

Along with a top-level form for recursion (LISPs vary):

```
► DEFUN, e.g. (DEFUN F (X Y Z) ⟨body⟩)
```

These give Turing power.

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#### Static and dynamic scope (or binding)

There are two main rules for finding the declaration of an identifier:

- Static scope. A identifier refers to the declaration of that name that is declared in the closest enclosing scope of the program text.
- ► Dynamic scope. A global identifier refers to the declaration associated with the most recent environment.

Historically, LISP was a dynamically scoped language; [Sethi pp.162] writes: when the initial implementation of Lisp was found to use dynamic scope, its designer, McCarthy[1981], "regarded this difficulty as just a bug".

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### Static and dynamic scope (example)

```
(defun main () (f 1))

(defun f (x) (g 2 (lambda () x)))

(defun g (x myfn) (apply myfn ()))
```

The question is whether the interpreter looks up the free variable  $\times$  of the lambda in its static scope (getting 1), or in the (dynamic) scope at the time of the call (getting 2).

Newer dialects of LISP (such as Common Lisp and Scheme) use static scoping for this situation.

However, top-level defvar in Common Lisp can be used to mark a variable as using dynamic binding.

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#### Programs as data

- One feature that sets LISP apart from many other languages is that it is possible for a program to build a data structure that represents an expression and then evaluates the expression as if it were written as part of the program. This is done with the function EVAL. But the environment used is that of the caller of EVAL so problems can arise if the expression being evaluated contains free variables (see 'call by text' below).
- McCarthy showed how a self-definitional (or meta-circular) interpreter for LISP could be written in LISP. See

for Paul Graham's article re-telling McCarthy's construction.

#### Abstract machines

The terminology *abstract machine* is generally used to refer to an idealised computing device that can execute a specific programming language directly. Systems people use *virtual machine* (as in JVM) for a similar concept.

- ► The original Fortran abstract machine can be seen as having only *static* (global, absolute address) *storage* (without a stack as there was no recursion), allocated before execution.
- ► The abstract machine corresponding to McCarthy's LISP implementation had a heap and garbage collection.<sup>2</sup> However, static locations were used to store variables (variables used by a recursive function were saved on entry and restored on exit, leading to dynamic scope).
- ▶ We had to wait for Algol 60 for *stacks* as we know them.

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#### Parameter passing in LISP

- ► Function parameters are transmitted either all *by value* or all *by text* (unevaluated expressions); only built-in functions (such as QUOTE, LAMBDA, COND) should really use pass-by-text. Why: because we need a special variant of EVAL to evaluate the arguments to COND in the calling environment, and similarly need to capture the free variable of a LAMBDA in the environment of the caller.
- ► The *actual parameters* in a function call are always expressions, represented as list structures.
- ► Note that pass by text (using either a special form, or explicit programmer use of QUOTE, and with EVAL to get the value of an argument) *resembles* call by name<sup>3</sup> (using LAMBDA to pass an unevaluated expression, and with APPLY to get the value of an argument), but is only equivalent if the EVAL can evaluate the argument in the environment of the function call!

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<sup>&</sup>lt;sup>2</sup>He worried whether this term would pass the publication style guides of the day.

<sup>&</sup>lt;sup>3</sup>See Algol 60 later in the course

### Dangers of eval

In LISP, I can write: (eval '(+ x 1))

If you've been to 1B Semantics then your first question should be "where do I lookup the value of x?" This is a real issue – should the following give 11 or 12?

```
(defvar x 1)
(defvar e '(add x 10))
(defun f (x) (eval e))
(f 2)
```

Unless you're very careful any use of eval involving user input produces a security hole. Consider: (eval (read)) and inputs like (fire-all-missiles) or (+ 1 top-security-code).

This applies to *any* language with a one-argument eval. When using Python (where eval takes a string), use the (sadly optional) additional environment-specifying parameters.



Block-structured procedural languages
Algol, Pascal and Ada

# Calling by value, by name, by text — dangers of eval **Example:** Consider the following function definitions

Now suppose the caller has variables x, y and z all bound to 7 and consider:

Note: on Common Lisp implementations this exact behaviour only manifests if we say (defvar y 7) before defining myTextIf; but all uses of eval are risky.

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### Parameter passing

Note: 'call-by-XXX' and 'pass-by-XXX' are synonymous.

- ▶ In *call by value*, the actual parameter is evaluated. The value of the actual parameter is then stored in a new location allocated for the formal parameter.
- ▶ In *call by reference*, the formal parameter is an alias to the actual parameter (normally achieved by a 'hidden' pointer).
- ► In *call by value/result* (IN/OUT parameters in Ada) the formal is allocated a location and initialised as in call-by-value, but its final value is copied back to the actual parameter on procedure exit.
- ► Algol 60 introduced *call by name*, see later.

Exercise: write code which gives different results under call-by reference and call-by-value/result.

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**Example Pascal program:** The keyword var indicates call by reference.

```
program main;
begin
  function f(var x, y: integer): integer;
  begin
        x := 2;
        y := 1;
        if x = 1 then f := 3 else f:= 4
        end;

var z: integer;
  z := 0;
  writeln( f(z,z) )
end
```

The difference between call-by-value and call-by-reference is important to the programmer in several ways:

- ► Side effects. Assignments inside the function body may have different effects under pass-by-value and pass-by-reference.
- ▶ Aliasing. Aliasing may occur when two parameters are passed by reference or one parameter passed by reference has the same location as a global variable of the procedure.
- ► Efficiency. Beware of passing arrays or large structures by value.

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#### **Examples:**

► A parameter in Pascal is normally passed by value. It is passed by reference, however, if the keyword var appears before the declaration of the formal parameter.

```
procedure proc(x: Integer; var y: Real);
```

- ► The only parameter-passing method in C is call-by-value; however, the effect of call-by-reference can be achieved using pointers. In C++ true call-by-reference is available using *reference parameters*.
- Ada supports three kinds of parameters:
  - 1. in parameters, corresponding to value parameters;
  - 2. out parameters, corresponding to just the copy-out phase of call-by-value/result; and
  - 3. in out parameters, corresponding to either reference parameters or value/result parameters, at the discretion of the implementation.

# Parameter passing

Pass/Call-by-name

The Algol 60 report describes call-by-name.

- ➤ Such actual parameters are (re-)evaluated every time the formal parameter is used—this evaluation takes place in the scope of the caller (cf. the Lisp discussion).
- ► This is like beta-reduction in lambda calculus, but can be very hard to understand in the presence of side-effects.
- ► Lazy functional languages (e.g. Haskell) use this idea, but the absence of side-effects enables re-evaluation to be avoided in favour of caching.

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### Parameters: positional vs. named

In most languages actual parameters are matched to formals *by position* but some languages additionally allow matching by name and also allow optional parameters, e.g. Ada and to some extent C++.

```
procedure Proc(Fst: Integer:=0; Snd: Character);
Proc(24,'h');
Proc(Snd => 'h', Fst => 24);
Proc(Snd => 'o');
```

ML can simulate named parameters by passing a record instead of a tuple.

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### Algol innovations

- ▶ Use of BNF syntax description.
- Block structure.
- Scope rules for local variables.
- Dynamic lifetimes for variables.
- ▶ Nested if-then-else expressions and statements.
- Recursive subroutines.
- Call-by-value and call-by-name arguments.
- Explicit type declarations for variables.
- Static typing.
- Arrays with dynamic bounds.

# Algol

#### HAD A MAJOR EFFECT ON LANGUAGE DESIGN

- ► The Algol-like programming languages evolved in parallel with the LISP family of languages, beginning with Algol 58 and Algol 60 in the late 1950s.
- ► The main characteristics of the Algol family are:
  - ▶ the familiar semicolon-separated sequence of statements,
  - block structure.
  - functions and procedures, and
  - static typing.

ALGOL IS DEAD BUT ITS DESCENDANTS LIVE ON!

▶ Ada, C, C++, Java etc.

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### Algol 60

#### **Features**

- Simple statement-oriented syntax.
- Block structure.
  - blocks contain declarations and exectable statements delimited by begin and end markers.
  - May be nested, declaration visibility: scoping follows lambda calculus (Algol had no objects so no richer O-O visibility from inheritance as well as nesting).
- ▶ Recursive functions and stack storage allocation.
- ► Fewer ad-hoc restrictions than previous languages (e.g., general expressions inside array indices, procedures that could be called with procedure parameters).
- ► A primitive *static type system*, later improved in Algol 68 and Pascal.

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### Algol 60

#### Some trouble-spots

- ► The Algol 60 type discipline had some shortcomings. For instance:
  - ► The type of a procedure parameter to a procedure does not include the types of parameters.

```
procedure myapply(p, x)
  procedure p; integer x;
  begin p(x);
  end;
```

- ► An array parameter to a procedure is given type array, without array bounds.
- Algol 60 was designed around two parameter-passing mechanisms, *call-by-name* and *call-by-value*.
   Call-by-name interacts badly with side effects; call-by-value is expensive for arrays.

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#### Pascal (1970)

- Pascal is a quasi-strong, statically typed programming language.
  - An important contribution of the Pascal *type system* is the rich set of data-structuring concepts: *e.g.* enumerations, subranges, records, variant records, sets, sequential files.
- ► The Pascal *type system* is more expressive than the Algol 60 one (repairing some of its loopholes), and simpler and more limited than the Algol 68 one (eliminating some of the compilation difficulties).
- Pascal was the first language to propose index checking. The index type (typically a sub-range of integer) of an array is part of its type.
- ▶ Pascal lives on (somewhat) as the Delphi language.

### Algol 68

- ► Algol 68 contributed a *regular, systematic type system*.

  The types (referred to as *modes* in Algol 68) are either *primitive* (int, real, complex, bool, char, string, bits, bytes, semaphore, format, file) or *compound* (array, struct, union, procedure, set, pointer).
  - Type constructors could be combined without restriction a more systematic type system than previous languages.
- ► Algol 68 used a *stack* for local variables and *heap* storage. Heap data are explicitly allocated, and are reclaimed by *garbage collection*.
- ► Algol 68 parameter passing is by value, with pass-by-reference accomplished by pointer types. (This is essentially the same design as that adopted in C.)
- Too complicated (both linguistically and to compile) for its time.

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#### Pascal variant records

*Variant records* have a part common to all records of that type, and a variable part, specific to some subset of the records.

```
type kind = (unary, binary);
type
                         | datatype
                               UBtree = mkUB of
 UBtree = record
   value: integer ;
                                    int * UBaux
   case k: kind of
                         | and UBaux =
     unary: ^UBtree ;
                               unary of UBtree option
     binary: record
                         | | binary of
       left: ^UBtree ;
                                 UBtree option *
       right: ^UBtree
                                 UBtree option;
     end
end ;
```

We use UBaux because ML datatype can only express variants at its top level. Note the use of option to encode NULL.

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Pascal variant records introduced *weaknesses* into its type system.

- Compilers do not usually check that the value in the tag field is consistent with the state of the record.
- ► Tag fields are optional. If omitted, no checking is possible at run time to determine which variant is present when a selection is made of a field in a variant.

C still provides this model with struct and union. Modern languages provide safe constructs instead (think how a compiler can check for appropriate use):

- ► ML provides datatype and case to express similar ideas. In essence the constructor names provide the discriminator k but this is limited to being the first component of the record.
- Object-oriented languages provide subclassing to capture variants of a class.

See also the 'expression problem' discussion (slide 202).

#### Objects in ML!?

# ∼ Topic V ~

# Object-oriented languages: concepts and origins SIMULA and Smalltalk

#### Further reading for the interested:

► Alan Kay's "The Early History Of Smalltalk"

http://worrydream.com/EarlyHistoryOfSmalltalk/

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#### Objects in ML!?

#### NB:

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- ► ! The *stack discipline of Algol*<sup>4</sup> for activation records fails!
- ▶ ? Is ML an object-oriented language?
  - ! Of course not!
  - ? Why?

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<sup>&</sup>lt;sup>4</sup>The stack discipline is that variables can be allocated on entry to a procedure, and deallocated on exit; this conflicts with returning functions (closures) as values as we know from ML. Algol 60 allowed functions to be passed *to* a procedure but not returned *from* it (nor assigned to variables).

### Basic concepts in object-oriented languages

Four main language concepts for object-oriented languages:

- 1. Dynamic lookup.
- 2. Abstraction.
- 3. Subtyping.
- 4. Inheritance.

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# Subtyping

- Subtyping is a relation on types that allows values of one type to be used in place of values of another. Specifically, if an object a has all the functionality of another object b, then we may use a in any context expecting b.
- ► The basic principle associated with subtyping is substitutivity: If A is a subtype of B, then any expression of type A may be used without type error in any context that requires an expression of type B.

### Dynamic lookup

- ► Dynamic lookup<sup>5</sup> means that when a method of an object is called, the method body to be executed is selected dynamically, at run time, according to the implementation of the object that receives the message (as in Java or C++ virtual methods).
- ▶ For the idea of *multiple dispatch* (not on the course), rather than the Java-style (or single) dispatch, see

http://en.wikipedia.org/wiki/Multiple\_dispatch

#### **Abstraction**

► *Abstraction* means that implementation details are hidden inside a program unit with a specific interface. For objects, the interface usually consists of a set of methods that manipulate hidden data.

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#### Inheritance

- ▶ *Inheritance* is the ability to reuse the definition of one kind of object to define another kind of object.
- ▶ The importance of inheritance is that it saves the effort of duplicating (or reading duplicated) code and that, when one class is implemented by inheriting from another, changes to one affect the other. This has a significant impact on code maintenance and modification.

NB: although Java treats subtyping and inheritance as synonyms, it is quite possible to have languages which have one but not the other.

- ► A language might reasonably see int as a subtype of double but there isn't any easy idea of inheritance here.
- ► One can simulate inheritance (avoiding code duplication)

with C-style #include, but this doesn't add subtyping to C.

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<sup>&</sup>lt;sup>5</sup>Also called 'dynamic dispatch' and occasionally 'dynamic binding' (but avoid the latter term as 'dynamic scoping' is quite a different concept).

### Behavioural Subtyping - 'good subclassing'

Consider two classes for storing collections of integers:

Questions: Is MySet a subclass of MyBag? A subtype?

Java says 'yes'. But should it?

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# History of object-oriented languages SIMULA and Smalltalk

- Objects were invented in the design of SIMULA and refined in the evolution of Smalltalk.
- ► SIMULA: The first object-oriented language.
  - Extremely influential as the first language with classes, objects, dynamic lookup, subtyping, and inheritance. Based on Algol 60.
  - Originally designed for the purpose of simulation by Dahl and Nygaard at the Norwegian Computing Center, Oslo,
- ► Smalltalk: A dynamically typed object-oriented language.

  Many object-oriented ideas originated or were popularised by the Smalltalk group, which built on Alan Kay's then-futuristic idea of the Dynabook (Wikipedia shows Kay's 1972 sketch of a modern tablet computer).

# Behavioural Subtyping – 'good subclassing' (2)

It shouldn't really be a subype, because it violates *behavioural subtyping* – members of a subtype should have the same behaviour as the members of the supertype. Consider:

For every MyBag this returns 1. However if I pass it a MySet already containing 42, then it returns 0.

So MySet shouldn't be subtype of MyBag as its values behave differently, e.g. results of foo. So properties of MyBag which I've proved to hold may no longer hold! We say that MySet is not a behavioural subtype of MyBag. (It is legally a subclass in Java, but arguably reflects 'bad programmer design'.)

[Liskov and Wing's paper "A Behavioral Notion of Subtyping" (1994) gives more details.]

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► A generic event-based simulation program (pseudo-code):

```
Q := make_queue(initial_event);
repeat
  select event e from Q
  simulate event e
  place all events generated by e on Q
until Q is empty
```

#### naturally requires:

- ► Ways in which to structure the implementation of related kinds of events. 

  → inheritance

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### SIMULA: Object-oriented features

- Objects: A SIMULA object is an activation record produced by call to a class.
- Classes: A SIMULA class is a procedure that returns a pointer to its activation record. The body of a class may initialise the objects it creates.
- Dynamic lookup: Operations on an object are selected from the activation record of that object.
- ► *Abstraction*: Hiding was not provided in SIMULA 67; it was added later and inspired the C++ and Java designs.
- ► *Subtyping*: Objects are typed according to the classes that create them. Subtyping is determined by class hierarchy.
- ► Inheritance: A SIMULA class could be defined, by class prefixing, to extend an already-defined class including the ability to override parts of the class in a subclass.

### SIMULA: Sample code

```
CLASS POINT(X,Y); REAL X, Y;

COMMENT***CARTESIAN REPRESENTATION

BEGIN

BOOLEAN PROCEDURE EQUALS(P); REF(POINT) P;

IF P =/= NONE THEN

EQUALS := ABS(X-P.X) + ABS(Y-P.Y) < 0.00001;

REAL PROCEDURE DISTANCE(P); REF(POINT) P;

IF P == NONE THEN ERROR ELSE

DISTANCE := SQRT((X-P.X)**2 + (Y-P.Y)**2);

END***POINT***
```

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```
CLASS LINE (A, B, C); REAL A, B, C;
  COMMENT * * * Ax + By + C = 0 REPRESENTATION
BEGIN
  BOOLEAN PROCEDURE PARALLELTO(L); REF(LINE) L;
    IF L = /= NONE THEN
      PARALLELTO := ABS ( A \star L.B - B \star L.A ) < 0.00001;
  REF (POINT) PROCEDURE MEETS (L); REF (LINE) L;
    BEGIN REAL T;
      IF L =/= NONE and \simPARALLELTO(L) THEN
        BEGIN
          MEETS :- NEW POINT(...,...);
        END;
    END; ***MEETS***
  COMMENT*** INITIALISATION CODE (CONSTRUCTOR)
  REAL D;
  D := SQRT (A**2 + B**2)
  IF D = 0.0 THEN ERROR ELSE
    BEGIN
      A := A/D; B := B/D; C := C/D;
    END;
END***LINE***
```

#### [Squint and it's almost Java!]

#### SIMULA: Subclasses and inheritance

SIMULA syntax: POINT CLASS COLOUREDPOINT.

To create a COLOUREDPOINT object, first create a POINT object (activation record) and then add the fields of COLOUREDPOINT.

#### Example:

```
POINT CLASS COLOUREDPOINT(C); COLOUR C; << note arg
BEGIN
   BOOLEAN PROCEDURE EQUALS(Q); REF(COLOUREDPOINT) Q;
    ...;
END***COLOUREDPOINT***

REF(POINT) P; REF(COLOUREDPOINT) CP;
P :- NEW POINT(1.0,2.5);
CP :- NEW COLOUREDPOINT(2.5,1.0,RED); << note args</pre>
```

NB: SIMULA 67 did not hide fields. Thus anyone can change the colour of the point referenced by CP:

```
CP.C := BLUE;
```

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### SIMULA: Object types and subtypes

- ▶ All instances of a class are given the same *type*. The name of this type is the same as the name of the class.
- ► The class names (types of objects) are arranged in a subtype hierarchy corresponding exactly to the subclass hierarchy.
- ► The Algol-60-based type system included explicit REF types to objects.

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#### **Smalltalk**

- Extended and refined the object metaphor.
  - ▶ Used some ideas from SIMULA; but it was a completely new language, with new terminology and an original syntax.
  - ► Abstraction via private *instance variables* (data associated with an object) and public *methods* (code for performing operations).
  - ▶ Everything is an object; even a class. All operations are messages to objects. Dynamically typed.
  - Objects and classes were shown useful organising concepts for building an entire programming environment and system. Like Lisp, easy to build a self-definitional interpreter.
- Very influential, one can regard it as an object-oriented analogue of LISP: "Smalltalk is to Simula (or Java) as Lisp is to Algol".

#### **Subtyping Examples** – essentially like Java:

```
1. CLASS A; A CLASS B;
  REF(A) a; REF(B) b;
  a :- b; COMMENT***legal since B is
                 ***a subclass of A
  b :- a; COMMENT***also legal, but checked at
                 ***run time to make sure that
                 ***a points to a B object, so
                 ***as to avoid a type error
2. inspect a
    when B do b :- a
    otherwise ...
```

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#### Smalltalk Example

Most implementations of Smalltalk are based around an IDE environment ("click here to add a method to a class"). The example below uses GNU Smalltalk which is terminal-based with st> as the prompt.

```
st> Integer extend [
      mvfact [
       self=0 ifTrue: [^1] ifFalse: [^((self-1) myfact) * self]
st> 5 myfact
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```

- ► Send an extend message to (class) Integer containing myfact and its definition.
- ► The body of myfact sends the two-named-parameter message ([^1], [^((self-1) myfact) \* self]) to the boolean resulting from self=0, which has a method to evaluate one or the other.
- ▶ '^' means return and (self-1) myfact sends the message myfact to the Integer given by self-1.

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# Reflection, live coding and IDEs

Above, I focused on Smalltalk's API, e.g. the ability to dynamically add methods to a class.

Note that objects and classes are often shared (via *reflection*) between the interpreter and the executing program, so swapping the 'add' and 'multiply' methods in the Integer class may have rather wider effects than you expect!

While the API is of interest to implementers, often a user interface will be menu-driven using an IDE:

- click on a class, click on a method, adjust its body, etc.
- the reflective structure above gives us a way to control the interpreter and IDE behaviour by adjusting existing classes.
- this is also known as 'live coding', and gives quite a different feel to a system than (say) the concrete syntax for Smalltalk.

Remark: *Sonic Pi* is a live-coding scripting language for musical performance.

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# Types and related ideas

Safety, static and dynamic types, forms of polymorphism, modules

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### Types in programming

- ► A *type* is a collection of computational entities that share some common property.
- ► Three main uses of types in programming languages:
  - 1. naming and organising concepts,
  - 2. making sure that bit sequences in computer memory are interpreted consistently,
  - 3. providing information to the compiler about data manipulated by the program.
- Using types to organise a program makes it easier for someone to read, understand, and maintain the program. Types can serve an important purpose in documenting the design and intent of the program.
- ► Type information in programs can be used for many kinds of optimisations.



Types in programming languages

#### **Additional Reference:**

► Sections 4.9 and 8.6 of *Programming languages:* Concepts & constructs by R. Sethi (2ND EDITION).

Addison-Wesley, 1996.

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# Type systems

- ► A *type system* for a language is a set of rules for associating a type with phrases in the language.
- ➤ Terms strong and weak refer to the effectiveness with which a type system prevents errors. A type system is *strong* if it accepts only *safe* phrases. In other words, phrases that are accepted by a strong type system are guaranteed to evaluate without type error. A type system is *weak* if it is not strong.
- Perhaps the biggest language development since the days of Fortran, Algol, Simula and LISP has been how type systems have evolved to become more expressive (and perhaps harder to understand)—e.g. Java generics and variance later in this lecture.

Type safety

A programming language is *type safe* if no program is allowed to violate its type distinctions.

Safety	Example language	Explanation
Not safe	C, C++	Type casts,
		pointer arithmetic
Almost safe	Pascal	Explicit deallocation;
		dangling pointers
Safe	LISP, SML, Smalltalk, Java	Type checking

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### Type checking

A *type error* occurs when a computational entity is used in a manner that is inconsistent with the concept it represents. *Type checking* is used to prevent some or all type errors, ensuring that the operations in a program are applied properly. Some questions to be asked about type checking in a language:

- ▶ Is the type system *strong* or *weak*?
- ▶ Is the checking done *statically* or *dynamically*?
- ► How *expressive* is the type system; that is, amongst safe programs, how many does it accept?

### Static and dynamic type checking

Run-time (dynamic) type checking:

- ► Compiler generates code, typically adding a 'tag' field to data representations, so types can be checked at run time.
- Examples: LISP, Smalltalk. (We will look at dynamically typed languages more later.)

Compile-time (static) type checking:

- ► Compiler checks the program text for potential type errors and rejects code which does not conform (perhaps including code which would execute without error).
- ► Examples: SML, Java.
- ▶ Pros: faster code, finds errors earlier (safety-critical?).
- ► Cons: may restrict programming style.

**NB:** It is arguable that object-oriented languages use a mixture of compile-time and run-time type checking, see the next slide.

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#### Java Downcasts

Consider the following Java program:

- Variable a has Java type A whose valid values are all those of class A along with those of all classes subtyping class A (here just class B).
- ► Subtyping determines when a variable of one type can be used as another (here used by assignment):

Mixed static and dynamic type checking!

See also the later discussion of subtype polymorphism.

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#### **Examples:**

► Type equality in C/C++. In C, type equality is structural for typedef names, but nominal for structs and unions; note that in

```
struct { int a; } x; struct { int a; } y;
```

there are two different (anonymously named) structs so x and y have unequal types (and may not be assigned to one another).

- ► Type equality in ML. ML works very similarly to C/C++, structural equality except for datatype names which are only equivalent to themselves.
- ► Type equality in Pascal/Modula-2. Type equality was left ambiguous in Pascal. Its successor, Modula-2, avoided ambiguity by defining two types to be compatible if
  - 1. they are the same name, or
  - 2. they are s and t, and s = t is a type declaration, or
  - 3. one is a subrange of the other, or
  - 4. both are subranges of the same basic type.

## Type equality

When type checking we often need to know when two types are *equal*. Two variants of this are *structural equality* and *nominal equality*.

Let *t* be a type expression (e.g. int \* bool in ML) and make two type definitions

```
type n1 = t; type n2 = t;
```

- ► Type names n1 and n2 are structurally equal.
- ► Type names n1 and n2 are not nominally equal.

  Under nominal equality a name is only equal to itself.

We extend these definitions to *type expressions* using structural equivalence for all type constructors not involving names.

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### Type declarations

We can classify type definitions type n = t similarly:

Transparent. An alternative name is given to a type that can also be expressed without this name.

Opaque. A new type is introduced into the program that is not equal to any other type.

In implementation terms, type equality is just tree equality, except when we get to a type name in one or both types, when we either (transparently) look inside the corresponding definition giving a structural system, or choose insist that both nodes should be identical types names giving a nominal system.

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### Type compatibility and subtyping

- Type equality is symmetric, but we might also be interested in the possibly non-symmetric notion of type compatibility (e.g. can this argument be passed to this function, or be assigned to this variable).
- This is useful for subtyping, e.g. given Java A a; B b; a = b; which is valid only if B is a subtype of (or equal to) A.

Similarly we might want type definitions to have one-way transparency. Consider

```
type age = int; type weight = int;
var x : age, y : weight, z : int;
```

We might want to allow implicit casts of age to int but not int to age, and certainly not  $x := y_i$ .

► Ad-hoc polymorphism or overloading. Two or more implementations with different types are referred to by the same name. E.g. Java, also addition is overloaded in SML (which is why fn x => x+x does not type-check). (Remark 1: Haskell's type classes enable rich overloading specifications. These allow functions be to implicitly applied to a range of types specified by a Haskell type constraint.)

(Remark 2: the C++ rules on how to select the 'right' variant of an overloaded function are arcane.)

Although we've discussed these for function application, it's important to note that Java generics and ML parameterised datatypes (e.g. Map<Key, Val> and 'a list) use the same idea for type constructors.

#### Polymorphism

*Polymorphism* [Greek: "having multiple forms"] refers to constructs that can take on different types as needed. There are three main forms in contemporary programming languages:

- Parametric (or generic) polymorphism. A function may be applied to any arguments whose types match a type expression involving type variables. Subcases: ML has implicit polymorphism, other languages have explicit polymorphism where the user must specify the instantiation (e.g. C++ templates, and the type system of "System F").
- ➤ Subtype polymorphism. A function expecting a given class may be applied to a subclass instead. E.g. Java, passing a String to a function expecting an Object. (Note we will return to bounded subtype polymorphism later.)

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### Type inference

- ► *Type inference* is the process of determining the types of phrases based on the constructs that appear in them.
- An important language innovation.
- ► A cool algorithm.

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Gives some idea of how other static analysis algorithms work.

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# Type inference in ML - idea

Idea: give every expression a new type variable and then emit constraints  $\alpha \approx \beta$  whenever two types have to be equal. These constraints can then be solved with Prolog-style unification.

For more detail see Part II course: "Types".

#### Typing rule (variable):

$$\frac{}{\Gamma \vdash x : \tau}$$
 if  $x : \tau$  in  $\Gamma$ 

#### Inference rule:

$$\frac{}{\Gamma \vdash \mathbf{x} : \gamma} \quad \boxed{\gamma \approx \alpha} \text{ if } \mathbf{x} : \alpha \text{ in } \Gamma$$

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#### **Example:**

$$\frac{\sqrt{f:\alpha_{1},x:\alpha_{3}\vdash f:\alpha_{7}} \quad \frac{\sqrt{}}{f:\alpha_{1},x:\alpha_{3}\vdash f:\alpha_{7}} \quad \frac{\sqrt{}}{f:\alpha_{1},x:\alpha_{3}\vdash x:\alpha_{8}}}{f:\alpha_{1},x:\alpha_{3}\vdash f(x):\alpha_{6}}$$

$$f:\alpha_{1},x:\alpha_{3}\vdash f(f(x)):\alpha_{4}$$

$$f:\alpha_{1}\vdash \text{fn }x=>f(f(x)):\alpha_{2}$$

$$\vdash \text{fn }f=>\text{fn }x=>f(f(x)):\alpha_{0}$$

$$\alpha_0 \approx \alpha_1 \rightarrow \alpha_2$$
,  $\alpha_2 \approx \alpha_3 \rightarrow \alpha_4$ ,  $\alpha_5 \approx \alpha_6 \rightarrow \alpha_4$ ,  $\alpha_5 \approx \alpha_1$   
 $\alpha_7 \approx \alpha_8 \rightarrow \alpha_6$ ,  $\alpha_7 \approx \alpha_1$ ,  $\alpha_8 \approx \alpha_3$ 

**Solution:**  $\alpha_0 = (\alpha_3 \rightarrow \alpha_3) \rightarrow \alpha_3 \rightarrow \alpha_3$ 

#### Typing rule (application):

$$\frac{\Gamma \vdash f : \sigma \rightarrow \tau \qquad \Gamma \vdash e : \sigma}{\Gamma \vdash f(e) : \tau}$$

#### Inference rule:

$$\frac{\Gamma \vdash f : \alpha \qquad \Gamma \vdash e : \beta}{\Gamma \vdash f(e) : \gamma} \quad \boxed{\alpha \approx \beta \implies \gamma}$$

#### Typing rule (lamda):

$$\frac{\Gamma, X : \sigma \vdash \boldsymbol{e} : \tau}{\Gamma \vdash (\text{fn } X => \boldsymbol{e}) : \sigma \rightarrow \tau}$$

#### Inference rule:

$$\frac{\Gamma, \mathbf{X} : \alpha \vdash \mathbf{e} : \beta}{\Gamma \vdash (\text{fn } \mathbf{X} = > \mathbf{e}) : \gamma} \quad \boxed{\gamma \approx \alpha \implies \beta}$$

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#### let-polymorphism

- ► The 'obvious' way to type-check let val x = e in e' end is to treat it as (fn x => e') (e).
- ▶ But Milner invented a more generous way to type let-expressions (involving type schemes—types qualified with ∀ which are renamed with new type variables at every use).
- ► For instance

let val  $f = fn x \Rightarrow x in f(f)$  end type checks, whilst  $(fn f \Rightarrow f(f)) (fn x \Rightarrow x)$ 

does not.

► Exercise: invent ML expressions *e* and *e'* above so that both forms type-check but have different types.

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### Surprises/issues in ML typing

The mutable type 'a ref essentially has three operators

```
ref : 'a -> 'a ref
(!) : 'a ref -> 'a
(:=) : 'a ref * 'a -> unit
```

Seems harmless. But think about:

```
val x = ref []; (* x : ('a list) ref *)
x := 3 :: (!x);
x := true :: (!x);
print x;
```

We expect it to type-check, but it doesn't and trying to execute the code shows us it shouldn't type-check!

- ► ML type checking needs tweaks around the corners when dealing with non-pure functional code. See also the exception example on the next slide.
- ► This is related to the issues of *variance* in languages mixing subtyping with generics (e.g. Java).

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But what about the following nonsense:

```
exception Poly of 'a ; (*** ILLEGAL!!! ***)
(raise Poly true) handle Poly x => x+1;
```

When a *polymorphic exception* is declared, SML ensures that it is used with only one type (and not instantiated at multiple types). A similar rule (the 'value restriction') is applied to the declaration

```
val x = ref [];
```

thus forbidding the code on Slide 101.

► This is related to the issue of *variance* in languages like Java to which we now turn.

### Polymorphic exceptions

**Example:** Depth-first search for finitely-branching trees.

```
datatype
  'a FBtree = node of 'a * 'a FBtree list;
fun dfs P (t: 'a FBtree)
  = let
      exception Ok of 'a;
    fun auxdfs( node(n,F) )
      = if P n then raise Ok n
        else foldl (fn(t,_) => auxdfs t) NONE F;
  in
      auxdfs t handle Ok n => SOME n
  end;
```

#### Type-checks to give:

```
val dfs = fn : ('a -> bool) -> 'a FBtree -> 'a option
```

This use of a polymorphic exception is OK.

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### Interaction of subtyping and generics—variance

In Java, we have that String is a subtype of Object.

- ▶ But should String[] be a subtype of Object[]?
- ► And should ArrayList<String> be a subtype of ArrayList<Object>?
- What about Function<Object, String> being a subtype of Function<String, Object>?

#### Given generic G we say it is

- ► covariant if G<String> is a subtype of G<Object>.
- ► contravariant if G<Object> is a subtype of G<String>.
- ▶ *invariant* or *non-variant* if neither hold.
- variance is a per-argument property for generics taking multiple arguments .

But what are the rules?

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#### Java arrays are covariant

The Java language decrees so. Hence the following code type-checks.

However, it surely can't run! Indeed it raises exception ArrayStoreException at the final line. Why?

- ► The last line would be unsound, so all *writes* into a Java array need to check that the item stored is a subtype of the array they are stored into. The type checker can't help.
- ▶ Note that there is no problem with *reads*.
- ▶ this is like the ML polymorphic ref and exception issue.

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#### Java variance specifications

In Java we can have safe covariant generics using syntax like:

But what about reading and writing to o?

```
s.set(2,"Hello");
System.out.println((String)o.get(2)+"World"); //fine
o.set(4,"seems OK"); //faulted at compile-time
```

The trade is that the covariant ArrayList o cannot have its elements written to, in exchange for covariance.

- ▶ Java has use-site variance specifications: we can declare variance at every use of a generic.
- By contrast Scala has declaration-site variance which many find simpler (see later).

### Java generics are invariant (by default)

The Java language decrees so. Hence the following code now fails to type-check.

So generics are safer than arrays. But covariance and contravariance can be useful.

What if I have an immutable array, so that writes to it are banned by the type checker, then surely it's OK for it to be covariant?

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### Java variance specifications (2)

Yes, there is a contravariant specification too (which allows writes but not reads):

```
ArrayList<? super String> ss;
```

So ss can be assigned values of type ArrayList<String> and ArrayList<Object> only.

For more information (beyond the current course) see:

```
en.wikipedia.org/wiki/Covariance_and_
contravariance_(computer_science)
```

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<sup>&</sup>lt;sup>5</sup>Legal note: it doesn't matter here, but to exactly match the previous array-using code I should populate the ArrayList with 10 NULLs. Real code would of course populate both arrays and ArrayLists with non-NULL values.



Scripting Languages and Dynamic Typing

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#### Scripting languages (2)

- A script is just a program written for a scripting language, indeed the usage seems to be 'respectability driven': we write a Python program (respectable language) but a shell script or a Perl script.
- The definition is a bit usage-dependent: ML is a 'proper' stand-alone language, but was originally was the scripting language for creating proof trees in the Edinburgh LCF system (history: ML was the meta-language for manipulating proofs about the object language PPλ).
- ► Similarly, we've seen Lisp as a stand-alone language, but it's also a scripting language for the *Emacs* editor.
- ▶ But it's hard to see Java or C as a scripting language. (But note the recent "Java Shell" – Java not to be 'outdone'??) Let's turn to why.

### Scripting languages

"A scripting language is a programming language that supports scripts; programs written for a special run-time environment that automate the execution of tasks that could alternatively be executed one-by-one by a human operator. Scripting languages are often interpreted (rather than compiled). Primitives are usually the elementary tasks or API calls, and the language allows them to be combined into more complex programs." [Wikipedia]

From this definition it's clear that many (but not all) scripting languages will have a rather ad-hoc set of features – and therefore tend to cause computer scientists to have strong views about their design (indeed it's arguable that we don't really teach any scripting languages on the Tripos).

### Scripting languages (3)

- ▶ scripting language means essentially "language with a REPL (read-evaluate-print loop)" as interface, or "language which can run interactively" (otherwise it's not so good for abbreviating a series of manual tasks, such API calls, into a single manual task).
- ▶ interactive convenience means that scripting languages generally are dynamically typed or use type inference, and execution is either interpretation or JIT compilation.

Incidentally, CSS and HTML are generally called *mark-up languages* to reflect their weaker (non-Turing powerful) expressivity.

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# Dynamically typed languages

#### We previously said:

▶ Using types to organise a program makes it easier for someone to read, understand, and maintain the program. Types can serve an important purpose in documenting the design and intent of the program.

So why would anyone want to lose these advantages?

And why is JavaScript one of the most-popular programming languages on surveys like RedMonk?

Perhaps there is a modern-politics metaphor here, about elites using Java and ordinary programmers using JavaScript to be free of the shackles of types?

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# RedMonk language rankings 2016

Rank	RedMonk (2016)	Rank	Rank RedMonk (2016)	
1	JavaScript	11	Shell	
2	Java	12	R	
3	PHP	13	Perl	
4	Python	14	Scala	
5=	C#	15	Go	
5=	C++	16	Haskell	
5=	Ruby	17	Swift	
8	CSS	18	MATLAB	
9	С	19	Visual Basic	
10	Objective-C	20=	Clojure	
		20=	Groovy	

Note 1. CSS (Cascading Style Sheets) not really a language.

Note 2. Swift is Apple's language to improve on Objective C.

Note 3. Don't trust such surveys too much.

#### Questions on what we teach vs. real life

- why the recent rise in popularity of dynamically typed languages when they are slower and can contain type errors?
- ▶ why C/C++ still used when its type system is unsafe?
- why language support for concurrency is so 'patchwork' given x86 multi-core processors have existed since 2005?

Chatley, Donaldson and Mycroft ("The next 7000 programming languages") explore these questions in more detail:

https://doi.org/10.1007/978-3-319-91908-9\_15

We start by looking at a recent survey (by RedMonk, considering GitHub projects and StackOverflow questions) on programming language popularity.

### What are all these languages?

- ▶ Java, C, C++, C#, Objective-C, Scala, Go, Swift, Haskell These are small variants on what we already teach in Tripos; all are statically typed languages.
- JavaScript, PHP, Python, Ruby, R, Perl, MATLAB, Clojure, Groovy These are all dynamically typed languages (but notably Groovy is mixed as it tries to contains Java as a proper subset).
- Most of the dynamically typed languages have a principal use for scripting.
- ► Some static languages (Scala, Haskell, ML) are also used for scripting (helpful to have type inference and lightweight top-level phrase syntax).

Let's look at some of them.

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### **JavaScript**

- Originally called Mocha, shares little heritage with Java (apart from curly braces), but renamed 'for advertising reasons'.
- ▶ Designed and implemented by Brendan Eich in 10 days (see fuller history on the web).
- ▶ Dynamically typed, prototype-based object system (there was a design requirement not to use Java-like classes).
- ► Has both object-oriented and functional language features (including higher-order functions)
- Implemented within browsers (Java applets did this first, but security and commercial reasons make these almost impossible to use nowadays).
- callback-style approach to scheduling within browsers.

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#### The JavaScript language

Three language inspirations [quoting Douglas Crockford]:

- Java (for its syntax)
- Scheme (a Lisp dialect for its lexical closures)
- ► Self (a Smalltalk dialect with prototypes instead of classes)

What's 'wrong' with classes? Java has:

- Classes to define the basic qualities and behaviours of objects.
- ▶ Object instances as particular manifestations of a class.

So has Smalltalk.

### Browsers: Java Applets and JavaScript

There are two ways to execute code in a browser:

- ► [Java Applets] compile a Java application to JVM code and store it on a web site. A web page references it via the <applet> tag; the JVM code is run in a browser sandbox. In principle the best solution, but historically beset with security holes, and unloved by Microsoft and Apple for commercial reasons. Effectively dead in 2019.
- ► [JavaScript] the browser contains a JavaScript interpreter. JavaScript programs are embedded in source form in a web page with the <script> tag, and interpreted as the page is rendered (now sometimes JIT compiled). Interaction between browser and program facilitated with the DOM model. Questionable confidentiality guarantees.

https://en.wikipedia.org/wiki/Java\_applet https://en.wikipedia.org/wiki/JavaScript

#### Problems with classes

- When designing a system with the waterfall design method, then classes and objects are natural.
- In more flexible design styles (spiral and agile), then we might want to change the classes during program evolution.
- ▶ In Smalltalk this can be achieved by changing the structure of a class, or the class an object belongs to, by assignment.
- But it's not quite so simple, in that users inheriting a class may be surprised by the behaviour change of the superclass (the *fragile base class* problem)
- ▶ One partial solution is to use *prototypes* . . .

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### Prototypes instead of classes

- In JavaScript (and Self), there are no classes.
- When a constructor function is defined, it acquires a prototype property (the JS for 'field' and 'method') initially an empty object.
- When a constructor is called, created objects inherit from the prototype (i.e. field and method lookup look first in the object and then in the prototype).
- ► You can add properties to the prototype object, or indeed replace the it entirely with another object.
- ► This gives a prototype inheritance chain similar to a class inheritance chain.
- ► The Self community argue that this is a more flexible style of programming, but many JavaScript systems start by defining prototypes which play the role of classes, and copying from these plays the role of new.

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### **Duck typing**

If we have classes, we can use Java-style type-testing:

```
if (x instanceof Duck) { ... }
```

This is a form of *nominal* property. But what do we do without classes? One answer is *Duck Typing*:

"In other words, don't check whether it IS-a duck: check whether it QUACKS-like-a duck, WALKS-like-a duck, etc, etc, depending on exactly what subset of duck-like behaviour you need to play your language-games with." [Alex Martelli, comp.lang.python (2000)]

More precisely, we take a *structural* rather than *nominal* view of being a duck: if an object has sufficiently many methods and fields (perhaps walks() and quacks() to be considered a Duck) then it *is* a Duck.

[Beware: JavaScript also has instanceof but this is merely shorthand for a test on an object's prototype.]

### Prototypes example

#### [Taken from the 'prototype' section of

```
https://www.w3schools.com/js/]
function Person(first, last, age, eye) {
    // Constructor: caller needs to use 'new'
    this.firstName = first;
    this.lastName = last;
    this.age = age;
    this.eyeColor = eye;
}
Person.prototype.nationality = "English";
var myFather = new Person("John", "Doe", 50, "blue");
```

After this, then myFather.nationality gives "English".

Note the difference between updating a field in the prototype and replacing the prototype with a new object.

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### The JavaScript DOM model

JavaScript is most often used in browsers, so needs to be tightly connected with web pages. This is done by:

- ► The DOM (Document Object Model), a W3C standard.
- The browser converts the HTML into a tree of objects representing the HTML page structures. This is made available as the JavaScript variable document.
- Executing JavaScript code reads and modifies document which the browser renders on-screen.
- Example button-click2 on 'materials' tab on course web page (view the source as well as clicking).

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# JavaScript interaction within the browser

Uses event-based GUI programming, based on callbacks, just like the Swing library for Java.

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#### Some other scripting Languages

- Python: popular for scripting scientific package API calls.
- ► Ruby: popularised by Heinemeier Hansson's *Rails* framework (server-side web-application programming and easy database integration).
- ► Clojure: Lisp meets the JVM.
- ► Typescript: Microsoft's typed version of JavaScript.
- R: a statistical scripting package.
- Lua: original for scripting for game engines.
- Matlab.

### WebAssembly – turning full circle?

Because JavaScript is the only language universally supported by browsers (we're not counting plug-ins because of lack of ubiquitous support and security risks), we find that various compilers have developed JavaScript-targeting back-ends.

- ► E.g. js\_of\_caml, ghcjs, Scala.js.
- ► Try out OCaml in a browser: http://ocsigen.org/js\_of\_ocaml/2.8.3/files/toplevel/index.html
- But JavaScript is a terrible compiler target language (a Java Applet compiled to JVM would be more effective).
- ► Upcoming answer: WebAssembly. Machine-agnostic, safety-checked assembly language JIT'ted in the browser.
- Isn't this just a variant of applets?

#### Gradual type systems

Dynamically typed languages are great (at least for small programs):

"You can write your whole prototype application in Python while a Java programmer is still writing his/her class hierarchy"

Statically typed languages are better for large programs, due to the documentation and cross-module static checks, provided by types.

► Imagine the discussions at Facebook when management started to confront the issue that they had one million lines of PHP in their system.

So what you might want is:

▶ a language in which small programs can be written without types, but the IDE encourages you to add types faster than software rust overtakes your system – *gradual types*.

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### Gradual type systems (2)

"Gradual typing is a type system in which some variables and expressions may be given types and the correctness of the typing is checked at compile-time (which is static typing) and some expressions may be left untyped and eventual type errors are reported at run-time (which is dynamic typing). Gradual typing allows software developers to choose either type paradigm as appropriate, from within a single language. In many cases gradual typing is added to an existing dynamic language, creating a derived language allowing but not requiring static typing to be used. In some cases a language uses gradual typing from the start." [Wikipedia]

#### Example languages:

- Microsoft's TypeScript
- Facebook's Hack (for PHP)
- Cython and mypy (for Python)
- ► C#'s *dynamic* type.

Sometimes gradual types are called *optional types*.



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# Data abstraction and modularity SML Modules

#### **Additional Reference:**

► Chapter 7 of *ML for the working programmer* (2ND EDITION) by L. C. Paulson. CUP, 1996.

#### May also be useful:

- Purely Functional Data Structures by Chris Okasaki, Cambridge University Press. [Clever functional data structures, implemented in Haskell and SML Modules.]
- Previous versions of this course (available on the teaching pages) had more information on SML Modules.
- ► http://www.standardml.org/

# Object-orientation: static vs dynamic, compiled vs interpreted

- Java and Scala are probably sweet-spots for ahead-of-time compilation for object-oriented languages, due to their static type systems.
- ► The dynamic features of Self and JavaScript (and indeed Smalltalk) mean that these languages need to be interpreted or JIT'ed.
- You might (non-examinably) think about what makes a nice type system possible and what is nice about a type system to enable ahead-of-time compilation.

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#### Need for modules

- ▶ We want control name visibility in large systems.
- ► Name visibility is important because it expresses large-scale architecture (which components can use which other components). Excessive visibility increases the attack surface for malevolent use.
- ► Traditional Java does quite well on class-level visibility (private, protected, public) but less well on package-level visibility (no formal way to control who might use a package-level export, or malevolent uses of reflection).
- ▶ Java 9 has just added a module system.
- We focus on the SML module system (seminal and well-designed).

There are also issues (only briefly mentioned) concerning *versioning*, when modules evolve over time and multiple versions are available, e.g. Linux packages or Windows DLLs.

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### The Core and Modules languages

SML consists of two sub-languages:

- ► The *Core* language is for *programming in the small*, by supporting the definition of types and variables denoting values of those types.
- ► The *Modules* language is for *programming in the large*, by grouping related Core definitions of types and variables into self-contained units, with descriptive interfaces.

The *Core* expresses details of *data structures* and *algorithms*. The *Modules* language expresses *software architecture*. Both languages are largely independent.

### The Modules language

Writing a real program as an unstructured sequence of Core definitions quickly becomes unmanageable.

The SML Modules language lets one split large programs into separate units with descriptive interfaces.

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#### **SML Modules**

#### Signatures and structures

An *abstract data type* is a type equipped with a set of operations, which are the only operations applicable to that type.

Its representation can be changed without affecting the rest of the program.

- Structures let us package up declarations of related types, values, and functions.
- Signatures let us specify what components a structure must contain.
- ▶ Structures are like Core ML records {a = 3, b = [4,5]} but can contain definitions of types (and exceptions) in addition to definitions of values.

Signatures are to structures what types are to values.

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#### **Structures**

In Modules, one can encapsulate a sequence of Core *type* and *value* definitions into a unit called a *structure*.

We enclose the definitions in between the keywords

```
struct ... end.
```

**Example:** A structure representing the natural numbers, as positive integers:

(Slide 139 shows how to name this as IntNat)

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### Concrete signatures

*Signatures* specify the 'types' of structures by listing the specifications of their components.

A signature consists of a *sequence* of component specifications, enclosed in between the keywords sig ... end.

```
sig type nat = int
val zero : nat
val succ : nat -> nat
val 'a iter : 'a -> ('a->'a) -> nat -> 'a
end
```

This signature fully describes the 'type' of IntNat on the previous slide.

(We'll later see signatures which *restrict* the names visible in a structure.)

The specification of type nat is *concrete*: it must be int.

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Naming structures and signatures, and dot notation
The structure keyword binds a structure to an identifier:

```
structure IntNat =
  struct type nat = int
    ...
    fun iter b f i = ...
end
```

The signature keyword similarly names signatures:

```
signature NAT =
    sig type nat
        ...
    val 'a iter : 'a -> ('a->'a) -> nat -> 'a
    end
```

*Dot notation* accesses components of structures (and signatures):

```
fun even (n : IntNat.nat) = IntNat.iter true not n
```

NB: Type IntNat.nat is statically equal to int.

Value IntNat.iter dynamically evaluates to a closure.

### Opaque signatures

On the other hand, the following signature

```
sig type nat
val zero : nat
val succ : nat -> nat
val 'a iter : 'a -> ('a->'a) -> nat -> 'a
end
```

specifies structures that are free to use *any* implementation for type nat (perhaps int, or word, or some recursive datatype).

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This specification of type nat is *opaque*.

**Example:** Polymorphic functional stacks.

```
signature STACK =
 exception E
                             (* <-- opaque *)
 type 'a reptype
 val new: 'a reptype
 val push: 'a -> 'a reptype -> 'a reptype
 val pop: 'a reptype -> 'a reptype
 val top: 'a reptype -> 'a
end ;
structure MyStack: STACK =
struct
 exception E ;
 type 'a reptype = 'a list; (* <-- varied later *)</pre>
 val new = [];
 fun push x s = x::s;
 fun split(h::t) = (h, t) (\star <-- not exported \star)
  | split _ = raise E ;
 fun pop s = #2(split s);
 fun top s = #1(split s);
end ;
```

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```
val e = MyStack.new;
val s0 = MyStack.push 0 e;
val s01 = MyStack.push 1 s0;
val s0' = MyStack.pop s01;
MyStack.top s0';
```

#### Gives:

```
val e = [] : 'a MyStack.reptype
val s0 = [0] : int MyStack.reptype
val s01 = [1,0] : int MyStack.reptype
val s0' = [0] : int MyStack.reptype
val it = 0 : int
```

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#### Properties of signature matching

- ► The components of a structure can be defined in a different order than in the signature; names matter but ordering does not.
- A structure may contain more components, or components of more general types, than are specified in a matching signature.
- Signature matching is structural. A structure can match many signatures and there is no need to pre-declare its matching signatures (unlike "interfaces" in Java and C#).
- ► Although similar to record types, signatures actually play a number of different roles.

### Signature matching

**Q:** When does a structure satisfy a signature?

**A:** The type of a structure *matches* a signature whenever it implements at least the components of the signature.

- ► The structure must *realise* (i.e. define) all of the opaque type components in the signature.
- ► The structure must *enrich* this realised signature, component-wise:
  - \* every concrete type must be implemented equivalently;
  - \* every value must have a more general type scheme;
  - \* every structure must be enriched by a substructure.

Signature matching supports a form of *subtyping* not found in the Core language:

- ► A structure with more type, value, and structure components may be used where fewer components are expected.
- ► A value component may have a more general type scheme than expected.

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#### Using signatures to restrict access

We can use a *signature constraint* to provide a restricted view of a structure. E.g. (restricting IntNat from slide 136)

```
structure SubIntNat =
   IntNat : sig type nat
        val succ : nat->nat
        val iter : nat->(nat->nat)->nat->nat
        end
```

Here the constraint str:sgn prunes the structure str according to the signature sgn. So:

- SubIntNat.zero is faulted ("not a member")
- ► SubIntNat.iter is less polymorphic than IntNat.iter.

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# Transparency of "\_ : \_"

Opaque signature constraints: "\_ :> \_"

- Although the \_:\_ operator can hide names, it does not conceal the definitions of opaque types. It is an transparent signature constraint.
- ► Thus, the fact that SubIntNat.nat = IntNat.nat = int remains *transparent*.
- ► For instance the application SubIntNat.succ(~3) is still well-typed, because ~3 has type int ... but ~3 is negative, so not a valid representation of a natural number!
- ► There is also an opaque signature constraint operator: "\_ :> \_"

Using the ':>' syntax, instead of the ':' syntax used earlier, signature matching can also be used to enforce *data abstraction* by hiding the identity of types:

```
structure AbsNat = IntNat :> sig
    type nat
    val zero: nat
    val succ: nat->nat
    val 'a iter: 'a->('a->'a)->nat->'a
    end
```

The constraint str:>sgn prunes str but also generates a new, *abstract* type for each opaque type in sgn.

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- The actual implementation of AbsNat.nat by int is hidden, so that AbsNat.nat ≠ int.
  AbsNat is just IntNat, but with a hidden type representation.
- ► AbsNat defines an abstract datatype of natural numbers: the only way to construct and use values of the abstract type AbsNat.nat is through the operations, zero, succ, and iter.
  - E.g., the application AbsNat.succ(~3) is ill-typed: ~3 has type int, not AbsNat.nat. This is what we want, since ~3 is not a natural number in our representation. In general, abstractions can also prune and specialise components.
- ▶ Remark: abstractions generalise the expressive power of the Core SML abstype declaration (this works like datatype, but does not export its constructors, and so also hides the representation of a type).

#### Information hiding

#### Opaque signature constraints

```
structure MyOpaqueStack :> STACK = MyStack;

val e = MyOpaqueStack.new;
val s0 = MyOpaqueStack.push 0 e;
val s01 = MyOpaqueStack.push 1 s0;
val s0' = MyOpaqueStack.pop s01;
MyOpaqueStack.top s0';

Gives:

val e = - : 'a MyOpaqueStack.reptype
val s0 = - : int MyOpaqueStack.reptype
val s01 = - : int MyOpaqueStack.reptype
val s0' = - : int MyOpaqueStack.reptype
val s0' = - : int MyOpaqueStack.reptype
val it = 0 : int
```

[Compare slide 141 which exposes reptype as list.]

# Datatype and exception specifications

Signatures can also specify datatypes and exceptions:

```
structure PredNat =
  struct datatype nat = zero | succ of nat
    fun iter b f i = ...
  exception Pred
  fun pred zero = raise Pred
    | pred (succ n) = n
end :> sig datatype nat = zero | succ of nat
    val iter: 'a->('a->'a)->(nat->'a)
        exception Pred
    val pred: nat -> nat (* raises Pred *)
    end
```

This means that clients can still pattern-match on datatype constructors, and handle exceptions.

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#### **SML Modules**

Functors – not examinable in 2019/20

- An SML functor is a structure that takes other structures as parameters.
  - Functors are to structures what functions are to values, in SML they are first-order only (OCaml has higher-order versions).
- ► Functors can be *applied* to structures. The actual argument must *match* the signature of the formal parameter—so it can provide more components, of more general types but these are not available to the body of the functor.
- Functors let us write program units that can be combined in different ways. Functors can also express generic algorithms.

#### Structures and signatures can be nested

```
structure IntNatAdd =
  struct
    structure Nat = IntNat
    fun add n m = Nat.iter m Nat.succ n
  end
  ...
signature Add =
  sig structure Nat: NAT
    val add: Nat.nat -> Nat.nat -> Nat.nat
  end
```

Then IntNatadd: Add holds (slide 139 defines IntNat and NAT).

To avoid nesting, it is also possible to directly include a signature identifier:

```
sig include NAT
val add: nat -> nat -> nat
end
```

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#### **Functors**

The functor AddFun below takes any implementation, N, of naturals and re-exports it with an addition operation.

```
functor AddFun(N:NAT) =
    struct
    structure Nat = N
    fun add n m = Nat.iter n (Nat.succ) m
    end
```

#### AddFun can be applied:

```
structure IntNatAdd = AddFun(IntNat)
structure AbsNatAdd = AddFun(AbsNat)
```

This definition of IntNatAdd evaluates to the same implementation as IntNatAdd seen earlier.

Above, AddFun is applied twice, but to arguments that differ in their implementation of type nat (AbsNat.nat ≠ IntNat.nat).

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#### **Example:** Generic imperative stacks.

```
signature STACK =
siq
 type itemtype
 val push: itemtype -> unit
 val pop: unit -> unit
 val top: unit -> itemtype
end ;
exception E ;
functor Stack( T: sig type atype end ) : STACK =
 struct
 type itemtype = T.atype
 val stack = ref( []: itemtype list )
  fun push x
   = ( stack := x :: !stack )
  fun pop()
   = case !stack of [] => raise E
     | _::s => ( stack := s )
 fun top()
   = case !stack of [] => raise E
     | t::_ => t
end ;
```

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= Stack(struct type atype = int end) ;

structure intStack

intStack.push(0);

val it = () : unit

val it = () : unit

val it = () : unit

structure intStack: STACK

val it = 0 : intStack.itemtype

intStack.top();

intStack.pop(); intStack.push(4);

Gives:

#### Why functors?

#### Functors support:

#### Code reuse.

AddFun may be applied many times to different structures, reusing its body.

#### Code abstraction.

AddFun can be compiled before any argument is implemented.

#### Type abstraction.

AddFun can be applied to different types N.nat.

But there are various complications:

- Should functor application be applicative or generative?
- We need some way of specifying types as being shared.

## Functors: generative or applicative?

The following functor is almost the identity functor, but *re-abstracts* its argument:

```
functor GenFun(N:NAT) = N :> NAT
```

Now, suppose we apply it twice to the same argument:

```
structure X = GenFun(IntNat)
structure Y = GenFun(IntNat)
```

Question: are the types x.nat and y.nat *compatible*?

- ► The applicative interpretation of functor application (used in OCaml) says "yes".
- ▶ The *generative* interpretation (used in SML) says "no". (Abstract types from the body of a functor are replaced by fresh types at each application. This is consistent with inlining the body of a functor at applications.)

This guestion is the tip of a very large iceberg (many papers).

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## Modules in other languages

Java also provides various structuring and hiding features:

- classes
- ▶ interfaces (with default implementations in Java 8)
- packages
- modules (from Java 9)

These offer independently developed, but overlapping, facilities—beyond this current course.

A separate issue is *versioning*. Linux packages (informal modules) come with versions, e.g. <code>libtest.so.1.0.1</code> and meta-information says which versions of a package are compatible for use within another versioned package. The similar Windows problem is 'DLL hell'. There is little linguistic support for this.

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#### Java 9 Modules – non-examinable summary (2)

The module-info.java file names a module and specifies its dependencies (on other modules) (requires keyword) and public API (exports keyword) which exports packages for use by other modules.

There's lots of rich syntax for specifying access control, e.g.

- exports to exporting a package for use only within another module.
- open for allowing reflective access. Modules by default disallow this. (Prior to the addition of modules all Java encapsulation could be circumvented by reflection!)

Remark: designing module systems (especially to fit in existing systems) is *hard*. Project Jigsaw (Java's module system) was originally planned to be part of Java 7 (2011) but didn't appear until Java 9 (2017). There are whole books on the Java Module System.

## Java 9 Modules – non-examinable summary

- ▶ Java classes are good at encapsulation (private, protected, public). Java packages and . jar files are not they are just naming/grouping conventions!
- ▶ Java 9 *modules* provide proper encapsulation. According to Oracle a module is "a uniquely named, reusable group of related packages . . . and a module descriptor"
- ► A module descriptor must be in file module-info.java and be of the form

```
module modulename
{
    // optional sequence of declarations
}
```

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# Linguistic ideas beyond Java and ML

Distributed concurrency, Scala, Monads

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# ~ Topic IX ~

## Languages for Concurrency and Parallelism

#### Sources of parallel computing

#### Five main sources:

- 1. Theoretical models: PRAM, BSP (complexity theory), CSP, CCS,  $\pi$ -calculus (semantic theory), Actors (programming model).
- 2. Multi-core CPUs (possibly heterogeneous—mobile phones).
- 3. Graphics cards (just unusual SIMD multi-core CPUs).
- 4. Supercomputers (mainly for scientific computing).
- 5. Cluster Computing, Cloud Computing.

**NB:** Items 2–5 conceptually only differ in processor-memory communication.

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## Language groups

- 1. Theoretical models (PRAM,  $\pi$ -calculus, Actors, etc.).
- 2. C/C++ and roll-your-own using pthreads.
- 3. Pure functional programming ('free' distribution).
- [Multi-core CPUs] Open/MP, Java (esp. Java 8), Open/MP, Cilk, X10.
- 5. [Graphics cards] CUDA (Nvidia), OpenCL (open standard).
- 6. [Supercomputers] MPI.
- 7. [Cloud Computing] MapReduce, Hadoop, Skywriting.
- 8. [On Chip] Verilog, Bluespec.

**NB:** Language features may fit multiple architectures.

# Painful facts of parallel life

- 1. Single-core clock speeds have stagnated at around 3GHz for the last ten years. Moore's law continues to give more transistors (hence multi-core, many-core, giga-core).
- Inter-processor communication is far far far more expensive than computation (executing an instruction).
- Can't the compiler just take my old C/Java/Fortran (or ML/Haskell) program and, you know, parallelise it? Just another compiler optimisation? NO! (Compiler researchers' pipe-dream/elephants' graveyard.)

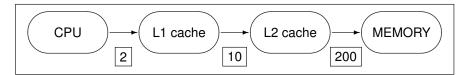
**Takeaway:** optimising performance requires exploiting parallelism, you'll have to program this yourself, and getting it wrong gives slow-downs and bugs due to races.

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# and timings

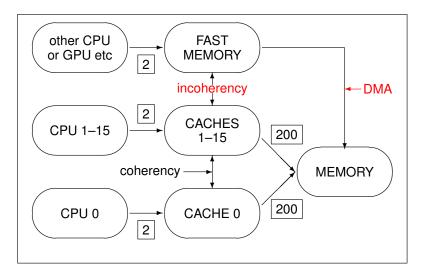
# CPU MEMORY

(This model was pretty accurate in 1985.)



## Multi-core-chip memory models

Today's model (cache simplified to one level):



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#### A Compute Cluster or Cloud-Computing Server

#### Multicore **MEMORY** NIC CPU 999,999 999,999 999,999 Network e.g. Ethernet no connection **MEMORY** NIC Multicore CPU 1 Network e.g. Ethernet no connection **MEMORY** Multicore NIC CPU 0

(The sort of thing which Google uses.)

# Lecture topic: what *programming abstractions*?

- ► We've got a large (and increasing) number of processors available for use within each 'device'
- ► This holds at multiple levels of scale (from on-chip to on-cloud). "Fractal" or "self-similar".
- ► Memory is local to processor units (at each scale)
- ► Communication (message passing) between units is much slower than computation.

Question: what are good programming abstractions for a system containing lots of processors?

Answer: no complete answer, rest of this lecture gives fragmentary answers.

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#### What hardware architecture tells us

- ► Communication latency is far higher than instruction execution time (2–6 orders of magnitude)
- So, realistically a task needs to have need at least 10⁴ instructions for it to be worth moving to another CPU.
- Long-running independent computations fit the hardware best.
- "Shared memory" is an illusion. At the lowest level it is emulated by message passing in the cache-coherency protocol.
- Often best to think of multi-core processors as distributed systems.

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#### SIMD, MIMD

# These words are often used informally as near synonyms.

► Distributed systems have separate processors connected by a network, perhaps on-chip (multi-core)?

Concurrent, Parallel, Distributed

- 'Parallel' suggests multiple CPUs or even SIMD, but "parallel computation" isn't clearly different from "concurrency".
- Concurrent behaviour can happen on a single-core CPU (e.g. Operating System and threads), Theorists often separate 'true concurrency' (meaning parallel behaviour) from 'interleaving concurrency'.

# Communication abstractions for programming

- "Head in sand": What communication I'm just using a multi-core CPU?
- ► "Principled head in sand": the restrictions in my programming language means I can leave this to someone else (or even the compiler).
- ▶ Just use TCP/IP.
- ► Shared memory, message passing, RMI/RPC?
- ► Communication is expensive, expose it to programmer (no lies about 'shared memory').

**Reflection:** does a language implicitly create a programmer mental model of communication?

Most parallel systems nowadays are MIMD.

- ► GPUs (graphical processor units) are a bit of an exception; several cores execute the same instructions, perhaps conditionally based on a previous test which sets per-processor condition codes.
- ▶ Programming Languages for GPUs (OpenCL, CUDA) emphasise the idea of a single program which is executed by many tasks. A program can enquire to find out the numerical value of its task identifier, originally its (x, y) co-ordinate, to behave differently at different places (in addition to having separate per-task pixel data).

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## Theoretical model – process algebra

- ► CCS, CSP, Pi-Calculus (calculus = "simple programming language"). E.g.
- Atomic actions  $\alpha$ ,  $\overline{\alpha}$ , can communicate with each other or the world (non-deterministically if multiple partners offered). Internal communication gives special internal action  $\tau$ .
- ▶ Behaviour  $p := 0 \mid \alpha.p \mid p+p \mid p \mid p \mid X \mid rec X.p$  (Deadlock, prefixing, non-determinism, parallelism, recursive definitions, also (not shown) parameterisation/hiding and value-passing.)
- ▶ Typical questions: "is  $\alpha.0|\beta.0$  the same as  $\alpha.\beta.0 + \beta.\alpha.0$ " and

"what does it mean for two behaviours to be equal"

Part II course: 'Topics in Concurrency'.

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#### Oldest idea: Threads

Java threads – either extend Thread or implement Runnable:

```
class PrimeRun implements Runnable {
    long minPrime;
    PrimeRun(long m) { minPrime = m; }
    public void run() {
        // compute primes larger than minPrime
    }
}
...
p = new PrimeRun(143); // create a thread
new Thread(p).start(); // run it
```

Posix's pthreads are similar.

#### Theoretical model – PRAM model

- ▶ PRAM: parallel random-access machine.
- ▶ N shared memory locations and P processors (both unbounded); each processor can access any location in one cycle.
- ► Execute instructions in lock-step (often SIMD, but MIMD within the model): fetch data, do operation, write result.
- ► Typical question: "given n items can we sort them in O(n) time, or find the maximum in O(1) time"
- ▶ BSP (bulk-synchronous parallel) model refines PRAM by adding costs for communication and synchronisation.

Part II course: 'Advanced Algorithms'.

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#### Threads, and what's wrong with them

- Need explicit synchronisation. Error prone.
- Because they're implemented as library calls, the compiler (and often users) cannot work out where they start and end.
- pthreads as OS-level threads. Need context switch. Heavyweight.
- Various lightweight-thread systems. Often non-preemptive. Blocking operations can block all lightweight operations sharing the same OS thread.
- ▶ Number of threads pretty hard-coded into your program.
- ► Nice IBM article:

```
https://www.ibm.com/developerworks/library/
j-nothreads/
```

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## Language support: Cilk

# Language support: OpenMP

#### Cilk [example from Wikipedia]

```
cilk int fib (int n)
{    int x,y;
    if (n < 2) return n;
    x = spawn fib (n-1);
    y = spawn fib (n-2);
    sync;
    return x+y;
}</pre>
```

Compiler/run-time library can manage threads. Neat implementation by "work stealing". Can adapt to hardware. X10 (IBM) adds support for partitioned memory.

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#### Clusters/Cloud Computing

- Memory support for threads, Cilk, OpenMP centres around a shared address space. (Even if secretly multi-core machines behave like distributed machines.)
- What about clusters? Cloud Computing?
- ► More emphasis on message-passing ...

#### OpenMP [example from Wikipedia]

```
int main(int argc, char *argv[]) {
   const int N = 100000;
   int i, a[N];
   #pragma omp parallel for
   for (i = 0; i < N; i++)
       a[i] = 2 * i;
   return 0;
}</pre>
```

The directive "omp parallel for" tells the compiler "it is safe to do the iterations in parallel".

Fortran "FORALL INDEPENDENT".

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# Software support for message passing: MPI

- MPI = Message Passing Interface [nothing to do with OpenMP]
- "de-facto standard for communication among processes that model a parallel program running on a distributed memory system." [no shared memory].
- Standardised API calls for transferring data and synchronising iterations. Message passing is generally synchronous, suitable for repeated sweeps over scientific data.
- Emphasis on message passing (visible and expensive-looking to user) means that MPI programs can work surprisingly well on multi-core, because they encourage within-core locality.

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# Software support for message passing: Erlang

# Cloud Computing (1)

- Shared-nothing language based on the actor model (asynchronous message passing).
- ▶ Dynamically typed, functional-style (no assignment).
- Means tasks can just commit suicide if they feel there's a problem and someone else fixes things, including restarting them
- ► Relatively easy to support hot-swapping of code.

Can mean either "doing one computer's worth of work on a server instead of locally". Google Docs. Or ...

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# Cloud Computing (2)

... massively parallel combinations of computing, e.g. MapReduce invoked by a search engine.

- MapReduce can match a search term against many computers (Map) each holding part of Google index of words, and then combine these result (Reduce).
- ▶ Reduce here means parallel reduce (tree-like, logarithmic cost), not fold/ or fold/ from ML.
- ► Functional style (idempotency) useful for error resilience (errors happen often in big computations). Try to ensure computation units are larger than cost of transmitting arguments and results. (also: Skywriting project in Cambridge)

# **Embarrassingly Parallel**

Program having many separate sub-units of work (typically more than the number of processors) which

- ▶ do not interact (no communication between them, not even via shared memory)
- are large

Example: the map part of MapReduce.

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# **Functional Programming**

In pure functional programming every tuple (perhaps an argument list to an application) can be evaluated in parallel. So functional programming is embarrassingly parallel? Not in general (i.e. not enough for compilers to be able to choose the parallelism for you). Need to find sub-executions with:

- little data to transfer at spawn time (because it needs copying, even if memory claims to be shared);
- ► a large enough unit of work to be done before return Probably only certain stylised code.

#### **Garbage Collection**

While we're talking about functional programming, and as garbage collection has previously been mentioned ...

Just how do we do garbage collection across multiple cores?

- Manage data so that data structures do not move from one processor to another?
- "Stop the world" GC with one big lock doesn't look like it will work.
- Parallel GC: use multiple cores for GC. Concurrent GC: do GC while the mutator (user's program) is running. Hard?
- ► Incremental? Track imported/exported pointers?

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# How have languages adapted to parallel hardware?

- ► Hardware change (multi-core parallelism in 2005) is one of the major changes ever, comparable with adding *index* registers and *interrupts* from the 1960s.
- ▶ It took many years between the early languages we discussed to get to the globals-stack-heap model from the 1970s to today (for sequential processors).
- Programming language support for parallelism today seems rather fragmentary in comparison. Several incomparable solutions. Is 2005 too recent for languages to have got the full answer? Or . . . ?

# Partial language evolution: functional programming ideas

- Concurrency and mutable data structures seem too hard for programmers to correctly use together in large programs.
- ► Pure functional languages can feel too 'hair shirt' for commercial use.
- ► Observation: languages have evolved to use ideas from functional programming such as higher-order functions and reduced exposure of mutable data structures in APIs used concurrently. Let's look at Streams in Java 8.

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#### Java 8: Internal vs. External iteration

Can't trust users to iterate over data. Consider traditional *external iteration*. It's easy to start by writing

```
for (i : collection)
{    // whatever
}
```

and then get lazy. Do we really want to write this?

```
for (k = 0; k<NUMPROCESSORS; k++)
{    spawn for (i : subpart(collection,k))
    {       // whatever
    }
}
sync;
// combine results from sub-parts here</pre>
```

And what about the maintenance load?

#### Java Collections vs Streams

#### Collections

- ► 'Trusty old Java looping'; for-loops, internally using mutable state (Iterators).
- ► Note that Java 8 did not add map and filter to the Collections classes. Why?

#### Streams

- ► Almost ML-style understanding. Items need not be in memory all at the same time (lazy).
- But additional laziness: a stream pipeline, e.g. .filter().max() above, traverses the stream only once.
- .parallel() authorises parallel/arbitrary order of calls to the stream pipeline. Good for parallelism, beware if you use side-effecting functions on stream elements!

It's quite practical to use .stream on a collection and then process it as a stream and then convert back.

#### Internal vs External iteration (2)

- Previous slide was external iteration. It's hard to parallelise (especially in Java where iterators have shared mutable state).
- ► The Java 8 Streams library encourages internal iteration keep the iterator in the library, and use ML-like stream operation to encode the body of the loop

► The library can optimise the iteration based on the number of threads available (and do a better job than users make!).

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Functional-style programming meets object-orientation

#### **References:**

- Scala By Example by M. Odersky. Programming Methods Laboratory, EPFL, 2008.
- ► An overview of the Scala programming language by

M. Odersky *et al.* Technical Report LAMP-REPORT-2006-001, Second Edition, 2006.

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# Big picture

Historically, object-oriented and functional languages were seen as disjoint programming paradigms.

```
en.wikipedia.org/wiki/Programming_paradigm
```

- Recently, mainstream OO languages have acquired functional features (Java, C++, C#).
- ► Why?
- Influences of JavaScript and, more directly, Scala.
- Multi-core parallelism: we just saw how internal iteration can move iteration code into a library, which receives the 'body of the loop' as a lambda expression.
- Other programming paradigms like futures, reactive programming can be added to a language as library features once lambdas are present.

# A procedural language!

```
def qsort( xs: Array[Int] ) {
  def swap(i: Int, j:Int) {
    val t = xs(i); xs(i) = xs(j); xs(j) = t
    def sortaux(l: Int, r: Int) {
    val pivot = xs( (l+r)/2 ); var i = l; var j = r
    while (i <= j) {
        while ( lt( xs(i), pivot ) ) i += 1
        while ( lt( xs(j), pivot ) ) j -= 1
        if ( i<=j ) { swap(i,j); i += 1; j -= 1 } }
        if (l<j) sortaux(l,j)
        if (j<r) sortaux(i,r)
        sortaux(0,xs.length-1)
}</pre>
```

#### Remarks:

- Syntax: reserved word for definitions, colon for types.
- Array selections are written in functional notation. (Achieved by clever use of implicit coercions but gives the appearance that arrays inherit from functions.)
- Block structure.

#### Scala

- Invented at EPFL by a group led by Martin Odersky; first release 2004.
  Implementation shared the JVM: interoperability with Java.
- Minimal expression-oriented language, control-flow operators defined using call-by-name.
- ► Smalltalk-style "everything is an object". Neat unification of OO and functional language features. Function closures are objects.
- Rich polymorphic static type system, including types without NULL. (Tony Hoare described his (1965) invention of the NULL value as his "billion-dollar mistake".)
- ► Lots of other goodies: traits for tamed multiple-inheritance, pattern-matching on objects, actor model for concurrency, singleton objects instead of *static* class members, . . .
- ► Rich source of ideas for other languages (e.g. Java 8).

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# A declarative language!

#### Remarks:

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- ▶ Polymorphism.
- ► Type declarations can often be omitted because the compiler can infer it from the context.
- ► Higher-order functions, lambdas (spelt '=>').
- ► The binary operation  $e \star e'$  is always interpreted a the method call  $e \star (e')$ .

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## Parameter passing; control structures

Scala uses call-by-value by default, but it switches to call-by-name evaluation if the parameter type is preceded by => (a function arrow with no parameters; expressions of this type are simply called whenever they are used).

# Imperative control structures

A functional implementation of while loops (this mirrors the ML definition of while loops, but is expressible within Scala itself):

```
def whileLoop( cond: => Boolean ) ( comm: => Unit )
    { if (cond) { comm ; whileLoop( cond ) ( comm ) } }
```

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#### Implementation by anonymous classes

```
@FunctionalInterface
interface Function<T,R> {
   R apply(T arg);
    public static void main(String[] args) {
        System.out.println(test(new Function<Integer, Integer>() {
            public Integer apply(Integer x) {
                return k + x;
        }));
        System.out.println(test(new Function<Integer, Integer>() {
            public Integer apply(Integer x) {
                return k + x;
        }));
        System.out.println(test(new Function<Integer, Integer>() {
            public Integer apply(Integer x) {
                return s.length() - x;
        }));
```

## How lambdas are implemented: Java

#### Running example:

- ► Lambdas are internally (almost) syntactic sugar for anonymous classes (but much easier for programmers).
- ► Lambdas have (limited) type inference see above example.

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# Implementation by named classes

```
class FunctionI implements Function<Integer, Integer> {
 int myk;
 FunctionI(int k) { myk = k; }
 public Integer apply(Integer x) { return myk + x; }
class FunctionS implements Function<Integer, Integer> {
  String mys;
 FunctionS(String s) { mys = s; }
 public Integer apply(Integer x) { return mys.length() - x; }
public class ClosureDemoClass {
   static int k = 10;
   static int test(Function<Integer, Integer> f) {
      return f.apply(1);
   public static void main(String[] args) {
        System.out.println(test(new FunctionI(k)));
        System.out.println(test(new FunctionI(k)));
        System.out.println(test(new FunctionS("14 char string")));
```

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#### **Function types**

In Scala it's easy: ML  $t1*...*tk \rightarrow t0$  encodes as

```
Functionk[t1,...,tk,t0]
```

for example: function2[Int, Array[Int], Bool].

In Java it's similar, except that Function1 is spelt Function and Function2 is spelt BiFunction.

Worse still in Java, there's the boxed/unboxed issue for generics:you can write Function<Integer, Boolean>, but not Function<Integer, boolean>. So for efficiency the latter has a special 'function' type

```
Predicate<Integer>
```

It's even more ad hoc as you don't .apply a Predicate, you .test it.

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# Case study (I)

```
abstract class Expr {
                      // Scala code - but the Java should be clear
  def isNumber: Boolean
  def isSum: Boolean
  def numValue: Int
  def leftOp: Expr
  def rightOp: Expr
class Number( n: Int ) extends Expr {
  def isNumber: Boolean = true
  def isSum: Boolean = false
  def numValue: Int = n
  def leftOp: Expr = error("Number.leftOp")
  def rightOp: Expr = error("Number.rightOp")
class Sum( e1: Expr; e2: Expr ) extends Expr {
  def isNumber: Boolean = false
  def isSum: Boolean = true
  def numValue: Int = error("Sum.numValue")
  def leftOp: Expr = e1
  def rightOp: Expr = e2
def eval( e: Expr ): Int = {
  if (e.isNumber) e.NumValue
  else if (e.isSum) eval(e.leftOp) + eval(e.rightOp)
  else error ("bad expression")
                                                                 203 / 242
```

# Data structures in functional and object-oriented style

In ML-like languages we use datatype to define (say) trees:

```
datatype Tree = Leaf of t_1
| Branch of Tree * Tree * t_2;
```

In OO languages we define an abstract class for Tree and subclass it as TreeLeaf and TreeBranch.

These define the same data structure at machine-code level – even the discriminator tags (recall the Pascal lecture) are present. ML implements these as numeric case tags, Java as pointers to the run-time-type information (virtual method table).

How does the language paradigm affect programming?

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#### Case study (I): critique

- ▶ It's clumsy; we could use instanceof.
- ▶ It's hard to maintain.
- ▶ It's hard to extend:
  - adding a new form of data (e.g. Prod) requires every existing class and function to be changed.
- It's easy to extend:
  - adding a new operation on the data (e.g. print) requires just adding one function.
  - ML-style pattern matching would shorten the code.

But one advantage is that it highlights the  $n \times m$  complexity of n functions operating on m forms of data.

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# Case study (II)

We could rephrase this more 'object-orientedly' [Scala code, but the Java should be clear]:

```
abstract class Expr {
  def eval: Int
}
class Number( n: Int ) extends Expr {
  def eval: Int = n
}
class Sum( e1: Expr; e2: Expr ) extends Expr {
  def eval: Int = e1.eval + e2.eval
}
```

This implementation is easily extensible with *new forms of data*:

```
class Prod( e1: Expr; e2: Expr ) extends Expr {
  def eval: Int = e1.eval * e2.eval
}
```

But, a new operation (e.g. print) on the existing data *still* requires every existing class to be changed.

# Case study (III): Scala case classes

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```
abstract class Expr
case class Number( n: Int ) extends Expr
case class Sum( e1: Expr, e2: Expr ) extends Expr
case class Prod( e1: Expr, e2: Expr ) extends Expr
```

Case classes implicitly come with a constructor function, with the same name as the class. So can write (e.g.)

```
Sum(Sum(Number(1), Number(2)), Number(3))
```

The match keyword takes as argument a number of cases:

▶ If none of the patterns matches, the pattern matching expression is aborted with a MatchError exception.

#### The expression problem

Constrast this with ML-style datatypes and functions over them:

- a new operation on the existing data (datatypes) is easy; but
- ▶ a new form of data requires every case match on that datatype to be changed.

The language-design problem of allowing a data-type definition where one can add new cases to the datatype and new functions over the datatype (without requiring ubiquitous changes) is known as the 'expression problem':

```
en.wikipedia.org/wiki/Expression_problem
```

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- ► Case classes and case objects implicitly come with implementations of methods toString, equals, and hashCode.
- Case classes implicitly come with nullary accessor methods which retrieve the constructor arguments.
- ► Case classes allow the constructions of *patterns* which refer to the case class constructor (see previous slide).

Scala case classes are essentially ML data types and allow both functional and object-oriented styles of programming to be expressed and (relatively) easily refactored.

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## Generics and polymorphism in Scala

- Scala has a fairly powerful type inferencer which allows one to omit type parameters to polymorphic functions and constructors.
- Classes in Scala can have type parameters (as in Java generics), but as in Java, mixing generics with subtyping poses the question:

if T is a subtype of a type S, should Array[T] be
a subtype of the type Array[S]?

In Scala, generic types like the following one also have *non-variant* subtyping by default.

```
class Array[A] {
  def apply( index: Int ): A
  def update( index: Int, elem: A )
   ...
}
```

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## Generic types

Type bounds

The following attempt to define a covariant functional stack fails (as it would be unsound just like the Java array example earlier):

One can enforce *covariant* subtyping by prefixing a formal type parameter with a '+'. The prefix '-' indicates *contravariant* subtyping.

This is *declaration-site* variance rather than Java's *use-site* variance declarations.

Scala uses a conservative approximation to verify soundness of variance annotations: a covariant type parameter of a class may only appear in covariant position<sup>7</sup> inside the class. Hence, the following class definition is rejected:

So, how do we define a type like this?

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Scala achieves this by using type bounds (B >: A below) echoing Java's use of extends and super in its use-site variance declarations:

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<sup>&</sup>lt;sup>7</sup>Mathematically this is "left of an even number of function arrow types".

#### **Traits**

Mixins and traits are not on the syllabus in 2019/20.

▶ A trait is a special form of an abstract class that does not have any value (as opposed to type) parameters for its constructor and is meant to be combined with other classes.

```
trait IntSet {
  def incl( x:Int ): IntSet
  def contains( x:Int ): Boolean
}
```

Traits may be used to collect signatures of some functionality provided by different classes.

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Traits can be used in all contexts where other abstract classes appear; however only traits can be used as *mixins* (introduced using the keyword with below):

The class Iter is constructed from a *mixin composition* of the parents StringIterator (called the *superclass*) and RichIterator (called a *mixin*) so as to combine their functionality.

#### Mixin-class composition

Every class or object in Scala can inherit from several traits in addition to a normal class. E.g.

```
trait AbsIterator[T] {
  def hasNext: Boolean
  def next: T
}
trait RichIterator[T] extends AbsIterator[T] {
  def foreach( f: T => Unit ): Unit =
    while (hasNext) f(next)
}
class StringIterator( s: String )
  extends AbsIterator[Char] {
    private var i = 0
    def hasNext = i < s.length
    def next = { val x = s charAt i; i = i+1; x }
}</pre>
```

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The class Iter inherits members from both StringIterator and RichIterator.

**NB:** Mixin-class composition is a form of multiple inheritance, but avoids the 'diamond' problem of C++ and similar languages (where a class containing a field appears at multiple places in the inheritance hierarchy).

```
class A public: int f;
class B: public A ...
class C: public A ...
class D: public B,C ... f ...
// Is this B::f or C::f?
// And do B and C both have an f of type A,
// or share a single one?
```

[End of section on mixins and traits.]

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#### Value types

A *value type* is a type representing an a pure value – such values can be copied, compared and subfields extracted but subfields cannot be mutated. Complex numbers and immutable arrays are examples, but mutable arrays are not. Strings of course should be values, but C and C++ historically have had issues as to whether they are char[] or const char[].

- ► In Java, every value is either of primitive type (spelt with lower case) or is a reference to an object. Assignment '=' copies bit patterns for primitives, but only copies references for object types. Equality '==' differs similarly.
- Worse, every reference-type object has identity, so that new Complex (1.0,2.0) allocates a new distinguishable object.

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# Value types and inefficient representation

Think how we might represent an array of size 100 of complex values in Java.

- ► We'll have an array of 100 pointers (around 800 bytes) and 100 complex values (perhaps 24 bytes each).
- ▶ But at machine level we really just want to store 200 double values (only 1600 bytes).

This costs Java programs in memory use, cache effects and instructions executed.

▶ Java would benefit from C#-like value types.

Value types form part of the 'Valhalla project' originally planned for Java 10:

Incidentally, the Wikipedia entry on value types needs improving (April 2018):

https://en.wikipedia.org/wiki/Value\_type

## Modelling value types in Java

We can model a value type in Java in two ways

- use final to stop modification; or
- ▶ use *deep copy* to snapshot values on operations.

Both of these are fragile during program enhancement.

For example a routine may copy an object to another object, but program enhancement may change a value type into a reference type, resulting in code elsewhere getting a value which is *part copied from, and part aliased with,* a source object.

- An object-copy routine which simply copies the fields of an object is known as shallow copy
- An object-copy routine which recursively copies the fields of an object is known as deep copy

Value types and languages

When talking about value types, we want a type which only admits functional update (copy but changing a field), not mutability and no identity.

Why are value types useful? Increasing use of functional-style APIs (partly due to the need to exploit parallelisms).

Think about defining a class <code>Complex</code> and note that every arithmetic operation is likely to do an allocation. What we want is the equivalent of <code>struct { double re,im; } in C. C#</code> (Microsoft's Java-style language) provides such values:

"Variables [of value type] directly contain values.
Assigning one value-type variable to another copies
the contained value. This differs from the assignment
of reference-type variables, which copies a reference
to the object but not the object itself." [C# reference
manual]

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# Aliasing and mutability

Mixing aliasing and mutability – as Java does – can enable subtle bugs. Adding concurrency enables more subtle bugs (and more-subtle bugs!).

There appear to be two 'easy-to-use' sweet spots to use current languages:

- use mutability freely, but use deep copy so that mutations don't accidentally update some other data structure.
- use aliasing freely, but make data structures immutable.

*Ideally,* future languages will allow these two techniques to be mixed and perhaps also allow aliasing and mutability to be used together locally without impacting whole-program maintainability. But for now, all I can do is to highlight the issues.<sup>8</sup>

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#### Overview

- Monadic I/O
- Generalised Algebraic Data Types (GADTs)
- ► Continuation-passing style (CPS) and call/cc
  Wikipedia:Call-with-current-continuation
- Dependent types (Cog, Agda, Idris)



## Miscellaneous (entertaining) concepts

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# I/O in functional languages

The ML approach: "evaluation is left-right, just let side-effecting I/O happen as in C or Java".

- ▶ Breaks *referential transparency* ('purity'), e.g. that e + e and let x = e in x + x should be equal.
- Not an appropriate solution for lazy languages (order of side effects in arguments in a function call would depend on the detail of the called function).
- ► Haskell is a lazy function language ("laziness keeps us pure").

Everything I say about I/O applies to other side-effecting operations, e.g. mutable variables, exceptions, backtracking . . .

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<sup>&</sup>lt;sup>8</sup>And perhaps mention 'separation logic' for the interested reader.

# Giving different types to pure and impure functions

Suppose we have two types  $A \rightarrow B$  for functions with no side-effects and  $A \rightsquigarrow B$  for impure functions.

- ► Then everything with a side effect would be visible in its type (contagious).
- ► (Later we might have ways of hiding "locally impure" functions within a pure function, but this doesn't apply to I/O.)
- Instead of writing A → B we write A → B M where M is a unary type constructor called a monad.
  Factors the idea of 'call a function' and 'do the resulting computation'.

Syntax: ML type constructors are postfix so we write *t list* or *B M* whereas Haskell writes *M B* and perhaps *List t*.

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#### Composing I/O functions

or Sequencing I/O effects

- ▶ In ML we could just write e; e' to sequence the side effects of e and those in e'. But now all 'effects' like I/O are part of monadic values, and no longer 'side effects'—so this doesn't work
- Instead every monad M (including IO as a special case) has two operators: one to sequence computations and one to create an empty computation.

#### So, how does I/O work?

In ML we might read from and write to stdin/stdout with (writing \simple for emphasis):

```
MLrdint: unit → int MLwrint: int → unit
```

Using monads (either in Haskell or ML) these instead have type

```
rdint: int IO
wrint: int -> unit IO
```

- ► The unary type constructor IO is predefined, just like the binary type constructor '->'.
- ► Shouldn't we have rdint: unit -> int IO?

  We could, but this would be a bit pointless—writing takes an argument and gives a computation, but reading from stdin is just a computation.

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#### Digression - Monad Laws

The idea of monad originates in mathematics, so these operators have axioms relating >>= and return in the *mathematics*; these are seem as laws which all well-behaved *programming* monads satisfy.

```
[left unit]

m >>= return = m
[right unit]

return x >>= f = f x
[associativity]

(m >>= f) >>= q = m >>= \lambda x. (f x >>= q)
```

(The bind operator '>>=' syntactically groups to the left so the brackets in the final line are redundant.)

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# Using the IO monad

In a system using monadic I/O, for example Haskell, the read-eval-print loop not only deals with pure values (integers, lists and the like), but has a special treatment for values in the 10 monad. Given a value of type t 10, it:

- performs the side effects in the monad; then
- prints the resulting value of type t.

So the question is: how do we make a computation which (say) reads an integer, adds one to it, and then prints the result?

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# Using the IO monad – examples (2)

Read pairs of numbers, multiply them, printing the sum of products so far, until the product is zero.

```
fun foo s = rdint >>= fn x =>
            rdint >>= fn y =>
            if (x*y = 0) then return ()
            else wrint(s + x*y) >>= fn () =>
              foo(s + x*y);
foo 0;
```

Note the type of foo is int -> unit IO. Note also the use of return to give a 'do nothing' computation.

## Using the IO monad – examples

Read an integer, adds one to it, and print the result (using ML syntax):

```
rdint >>= (fn x => wrint(x+1));
```

#### Do this twice:

```
let val doit = rdint >>= (fn x => wrint(x+1))
in doit >>= (fn () => doit);
```

Note that doit has type unit IO, so we use >>= to use doit twice.

NB: *computations* are not *called* as they are not functions; they are *combined* using >>= as in the above examples.

#### Practical use

The Mirage OS (most recent Computer Lab spin-out acquired by Docker) is written in OCaml in monadic style. But most monadic-style programs are written in Haskell. GHCi is just like the ML read-eval-print loop, but remember:

- Haskell syntax uses upper case for constants (types, constructors) and lower case for variables.
- ► Haskell swaps ':' and '::' relative to ML
- Type constructors are prefix
- fn x=>e is written x->e

Haskell also provides do-notation to allow programmers to write imperative-looking code which de-sugars to uses of return and >>=.

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#### Other monads

- ▶ Many other unary type constructors have natural monadic structure (at least as important as IO).
- ► For example, using Haskell syntax, List t and Maybe t.

  Another important one is State s t of computations returning a value of type t, but which can mutate a state of type s. (Subtlety: the monad is legally the unary type State s for some given s.)
- Haskell overloads >>= and return to work on all such types (Haskell's type class construct facilitates this).
- ► The common idea is 'threading' some idea of state implicitly through a calculation.

Haskell example using List in GHCi:

```
[1,2,3] >>= \x->if x==2 then return 5 else [x,x] [1,1,5,3,3]
```

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#### How about this:

[This uses OCaml syntax, but Haskell also has GADTs] Allows bool exp values to be checked that Add, Eq etc. are used appropriately. E.g.

```
Val 3: int exp √
Val true: bool exp √
Add(Val 3, Val 4): int exp √
Add(Val 3, Val true) ×
Eq(Val true, Val false): bool exp √
Eq(Val 3, Val 4): bool exp √
Eq(Val 3, Val true) ×
```

Can't do this in SML (special case of *dependent types* later this lecture).

## Generalised Algebraic Data Types (GADTs)

OCaml data type (just like datatype in ML):

Why bother (it's longer and duplicates info)?

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Can even write eval where the *type* of the result depends on the *value* of its type:

```
fun eval(Val(x)) = x
  | eval(Eq(x,y)) = eval(x) = eval(y)
  | eval(Add(x,y)) = eval(x) + eval(y);
eval: 'a exp -> 'a
```

(Some type-checking dust being swept under the carpet here.)

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#### Reified continuations

Make calling continuation appear to be a value in the language (reifying it).

Reminder on continuation-passing style (CPS), perhaps mentioned in Compiler Construction. Can see a function of type  $t_1 \rightarrow t_2$  as a function of type

```
(t_2 
ightarrow 	ext{unit}) 
ightarrow (t_1 
ightarrow 	ext{unit})
```

Or uncurrying

```
(t_2 \rightarrow \text{unit}) \times t_1 \rightarrow \text{unit}
```

(One parameter of type  $t_1$  and the other saying what to do with the result  $t_2$  – like *argument* and *return address!*)

#### Instead of

```
fun f(x) = \dots return e \dots print f(42)
```

```
we write
```

```
fun f'(k, x) = ... return k e' ... f'(print, 42)
```

In CPS all functions return unit and all calls are now tail-calls (so the above isn't just a matter of adjusting a return statement). Sussman and Steele papers from the 1970's ("Lambda the ultimate XXX").

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#### Reified continuations (2)

- ► A function with *two* continuation parameters rather than one can act as normal return vs. exception return. (Or
- ▶ But we don't want to write all our code in CPS style. So: call/cc "call with current continuation". Lots of neat programming tricks in a near-functional language.
- ► Reified? The continuation used at the meta-level (semantics) to explain how a language operates is exposed as an object-level (run-time value).

Prolog success return vs failure return.)

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#### Reified continuations (3)

Core idea (originally in Scheme, a form of Lisp):

```
fun f(k) = let x = k(2) in 3;
```

In ML this function 'always returns 3'. E.g.

```
> f(fn x=>x);
```

But callcc(f) returns 2!

- ► The return address/continuation used in the call to f is reified into a side-effecting function value k which represents the "rest of the computation after the call to f".
- ► Some similarity with f (fn x => raise Foo);

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#### Dependent types

Suppose *f* is a curried function of *n* boolean arguments which returns a boolean. How do we determine if *f* is a tautology (always returns true)?

Works nicely in dynamically typed languages. Fails to type-check in ML. Why?

- ► The *type* of the second argument depends on the *value* of the first.
- ▶ Dependent type systems can capture this (languages like Coq, Agda and Idris).
- ▶ But type checking can require theorem proving.

#### Dependent typing of taut in Idris

```
-- BF n is the type Bool -> ... -> Bool -> Bool
-- \__ /
-- n

BF: Nat -> Type

BF Z = Bool

BF (S n) = Bool -> BF n

taut: (n: Nat) -> BF n -> Bool

taut Z f = f

taut (S n) f = taut n (f False) &&

taut n (f True)
```

▶ Dependent types allow compile-time checking of things which we would expect to cause exceptions, e.g.

```
hd : (n:Nat) -> List (S n) alpha -> alpha
```

- More Idris code on the course website.
- Something to think about: are ML exceptions just dynamically checked types?

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