Compiler Construction Lent Term 2020

```
int main( int argc, char *argv[] )
{
   printf("hello world\n");
   return 0;
}
```



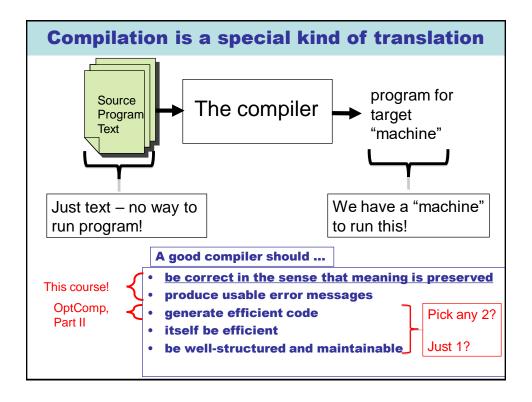
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"hello world" .string .text .globl main .type main, @function main: .LFB0: .cfi_startproc pushq %rbp .cfi_def_cfa_offset 16 .cfi_offset 6, -16 %rsp, %rbp movq .cfi_def_cfa_register 6 \$16, %rsp subq %edi, -4(%rbp) movl %rsi, -16(%rbp) movq \$.LC0, %edi movl call puts movl \$0, %eax leave .cfi_def_cfa 7, 8 ret .cfi_endproc

.LC0:

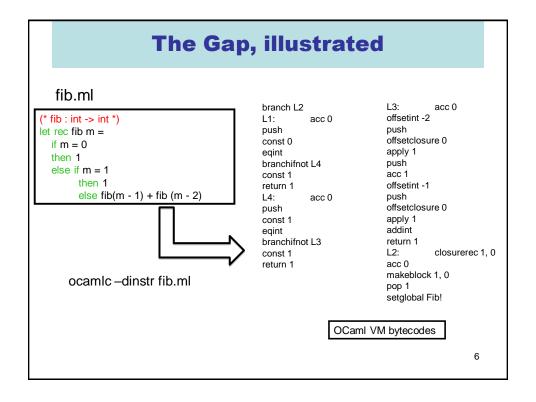
Why Study Compilers?

- Although many of the basic ideas were developed over 60 years ago, compiler construction is still an evolving and active area of research and development.
- Compilers are intimately related to programming language design and evolution.
- Compilers are a Computer Science success story illustrating the hallmarks of our field --higher-level abstractions implemented with lower-level abstractions.
- Every Computer Scientist should have a basic understanding of how compilers work.



Mind The Gap Typical Target Language **High Level Language** • "Machine" independent • "Machine" specific Complex syntax Simple syntax Complex type system Simple types Variables memory, registers, words Nested scope Single flat scope Procedures, functions Objects Help!!! Where do we begin??? Modules 4

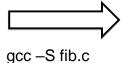
The Gap, illustrated oublic class Fibonacci { public static void public class Fibonacci { public Fibonacci(); main(java.lang.String[]); public static long fib(int m) { Code: Code: if (m == 0) return 1; 0: aload_0 0: aload_0 else if (m == 1) return 1; 1: invokespecial #1 1: iconst_0 else return 4: return 2: aaload fib(m - 1) + fib(m - 2);3: invokestatic #3 public static long fib(int); 6: istore_1 Code: 7: getstatic 0: iload_0 public static void 10: new #5 1: ifne main(String[] args) { 13: dup 4: lconst_1 int m = 5: Ireturn 14: invokespecial #6 Integer.parseInt(args[0]); 6: iload_0 17: iload_1 System.out.println(7: iconst_1 18: invokestatic #2 $fib(m) + "\n");$ 21: invokevirtual #7 8: if_icmpne 11: Iconst 1 24: Idc 26: invokevirtual #9 12: Ireturn 13: iload_0 29: invokevirtual #10 32: invokevirtual #11 14: iconst_1 35: return 15: isub 16: invokestatic #2 19: iload 0 20: iconst_2 javac Fibonacci.java 21: isub JVM bytecodes 22: invokestatic #2 javap -c Fibonacci.class 5 25: ladd 26: Ireturn



The Gap, illustrated

fib.c

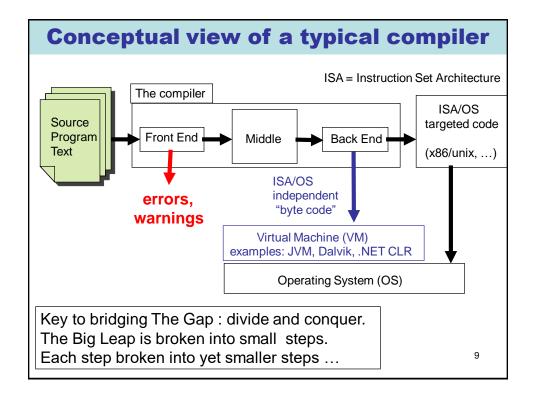
```
#include<stdio.h>
int Fibonacci(int);
int main()
{
    int n;
    scanf("%d",&n);
    printf("%d\n", Fibonacci(n));
    return 0;
}
int Fibonacci(int n)
{
    if ( n == 0 ) return 0;
    else if ( n == 1 ) return 1;
    else return ( Fibonacci(n-1) + Fibonacci(n-2));
}
```

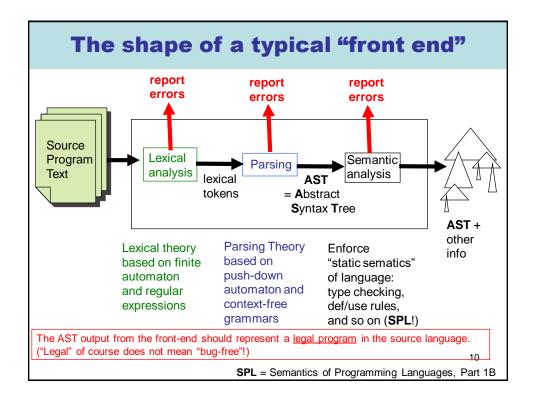


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The Gap, illustrated

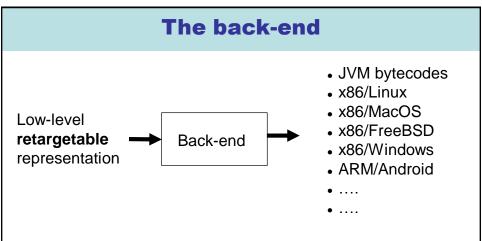
```
_TEXT, _text, regular, pure_instructions
                                                                                                                                                                     .cfi_def_cfa_register %rbp
subq $16, %rsp
movl %edi, -8(%rbp)
cmpl $0, -8(%rbp)
jne LBB1_2
## BB#1:
 .globl
.align
_main:
.cfi_startproc
## BB#0:
                                    _main
4, 0x90
                                                 ##@main
 pushq
Ltmp2:
                                   %rbp
                                                                                                                                                                     movl
jmp
LBB1_2:
Ltmp2:
.cf_def_cfa_offset 16
Ltmp3:
.cfi_offset %rbp, -16
%rsp, %rbp
                                                                                                                                                                    LBB1_2:
cmpl
jne
## BB#3:
movl
jmp
LBB1_4:
                                                                                                                                                                                                       $1, -8(%rbp)
LBB1_4
$1, -4(%rbp)
LBB1_5
                                                                                                                                                                                                      -8(%rbp), %eax
$1, %eax
%eax, %edi
Fibonacci
-8(%rbp), %edi
$2, %edi
%eax, -12(%rbp)
Fibonacci
-12(%rbp), %edi
%eax, %edi
%edi, -4(%rbp)
                                                                                                                                                                     ## 4-byte Spill
                                                                                                                                                                                                                                           ## 4-byte Spill
                                  Fibonacci
L_str1(%rip), %rdi
%eax, %esi
$0, %al
_printf
$0, %esi
%eax, -16(%rbp)
%esi, %eax
$16, %rsp
%rbp
                                                                                                                                                                                                                                           ## 4-byte Reload
                                                                                                                                                                     LBB1_5:
movl
addq
popq
ret
.cfi_endproc
                                                                                                                                                                                                        -4(%rbp), %eax
$16, %rsp
%rbp
                                                                       ## 4-byte Spill
                                                                                                                                                                      .section
L_.str:
.asciz
                                                                                                                                                                                                        __TEXT,__cstring,cstring_literals
## @.str
 .globl
.align
_Fibonacci:
.cfi_startproc
## BB#0:
                                   _Fibonacci
4, 0x90
                                                                                                                                                                                                      ## @.str1
"%d\n"
                                                  ## @Fibonacci
                                                                                                                                                                      L_.str1:
 pushq %
Ltmp7:
.cfi_def_cfa_offset 16
                                   %rbp
                                                                                                                                                                      .subsections_via_symbols
.cfi_0ei_cn__
Ltmp8:
.cfi_offset %rbp, -16
.crsp, %rbp
                                                                                                                                                                                                                                                                                                                   8
                                                                                                                                   x86/Mac OS
```



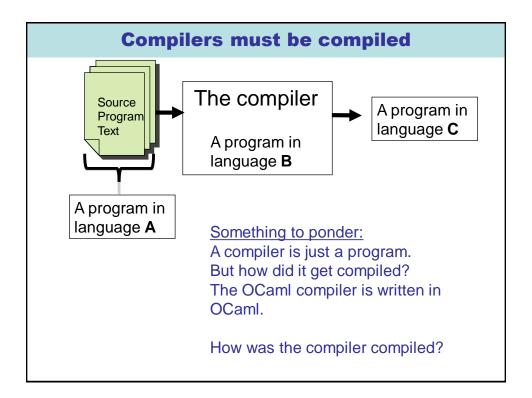


--High-level to low-level retargetable representation --Optimisations

Trade-off: with more optimisations the generated code is (normally) **faster**, but the compiler is **slower**

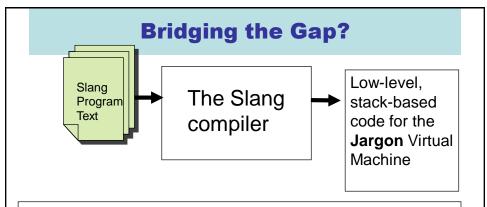


- Requires intimate knowledge of instruction set and details of target machine
- When generating assembler, need to understand details of OS interface
- Target-dependent optimisations happen here!



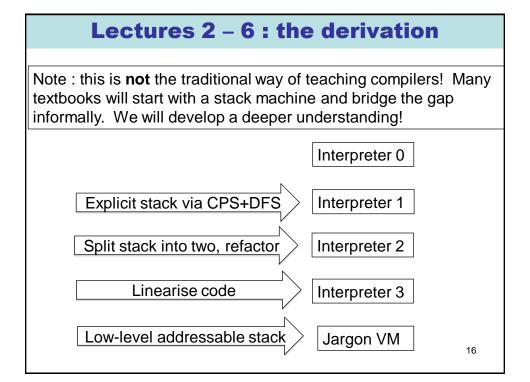
The Slang compiler

- The compiler is available from the course web site.
- · It is written in Ocaml
- Slang = Simple Language. Based on L3 from Semantics of Programming Languages, Part 1B.
- The best way to learn about compilers is to modify one.
- There are several suggested improvements listed on the course web site. I hope that some of you will implement these. If they work, I'll let you commit your changes to the repository. Fame! Fortune!



Question: How do we leap from the mathematical semantics of L3 to a low-level stack machine?

Answer: We will start with a high-level interpreter based on semantics, and then **derive** the stack machine by a sequence of semantics preserving transformations!



The Shape of this Course

- Lectures 2 6 : Derivation of Jargon Stack Machine
- Lectures 7 12 : Assorted topics.
 - From Jargon code to x86
 - The OS interface
 - Implementing exceptions
 - Implementing OOP
 - Runtime systems and garbage collection
 - Compiling a compiler via boot strapping
- Lectures 13 16: The front end.
 - Lexical analysis
 - Parsing

LECTURE 2 Slang front end and interpreter 0

- Slang (= <u>Simple LANGuage</u>)
 - A subset of L3 from Semantics ...
 - ... with very ugly concrete syntax
 - You are invited to experiment with improvements to this concrete syntax.
- Slang: concrete syntax, types
- Abstract Syntax Trees (ASTs)
- The Front End
- Interpreter 0 : The high-level "definitional" interpreter
 - 1. Slang/L3 values represented directly as OCaml values
 - 2. Recursive interpreter implements a denotational semantics
 - 3. The interpreter implicitly uses OCaml's runtime stack and heap

Clunky Slang Syntax (informal)

```
uop := - | ~
                                                            (~ is boolean negation)
bop ::= + | - | * | < | = | && | ||
t ::= bool | int | unit | (t) | t * t | t + t | t -> t | t ref
e ::= () | n | true | false | x | (e) | ? |
                                                            (? requests an integer
     e bop e | uop e |
                                                               input from terminal)
     if e then else e end |
     e e | fun (x : t) -> e end |
     let x : t = e in e end |
     let f(x:t): t = e in e end |
     !e | ref e | e := e | while e do e end |
     begin e; e; ... e end |
     (e, e) | snd e | fst e |
                                                          (notice type annotation
     inl t e | inr t e |
                                                            on inl and inr constructs)
     case e of inl(x:t) -> e | inr(x:t) -> e end
```

From slang/examples

```
let fib( m : int) : int =
                                  let gcd(p:int*int):int=
  if m = 0
                                     let m: int = fst p
  then 1
                                     in let n: int = snd p
  else if m = 1
                                     in if m = n
                                         then m
        then 1
                                         else if m < n
         else fib (m - 1) +
                                              then gcd(m, n - m)
              fib (m -2)
                                              else gcd(m - n, n)
         end
                                              end
   end
                                         end
in
                                        end
  fib(?)
                                      end
end
                                  in gcd(?, ?) end
```

The ? requests an integer input from the terminal

Slang Front End

Input file foo.slang



Parse (we use Ocaml versions of LEX and YACC, covered in Lectures 3 --- 6)

Parsed AST (Past.expr)



Static analysis: check types, and contextsensitive rules, resolve overloaded operators

Parsed AST (Past.expr)



Remove "syntactic sugar", file location information, and most type information

Intermediate AST (Ast.expr)

Parsed AST (past.ml)

```
type var = string
```

type loc = Lexing.position

type type_expr =

l TEint

TEbool

TEunit

| TEref of type_expr

| TEarrow of type_expr * type_expr

| TEproduct of type_expr * type_expr

| TEunion of type_expr * type_expr

type oper = ADD | MUL | SUB | LT |
AND | OR | EQ | EQB | EQI

type unary_oper = NEG | NOT

Locations (loc) are used in generating error messages.

```
type expr =
    | Unit of loc
    | What of loc
    | Var of loc * var
    | Integer of loc * int
     Boolean of loc * bool
     UnaryOp of loc * unary_oper * expr
     Op of loc * expr * oper * expr
    If of loc * expr * expr * expr
    Pair of loc * expr * expr
    | Fst of loc * expr
    | Snd of loc * expr
    | Inl of loc * type_expr * expr
    | Inr of loc * type_expr * expr
     Case of loc * expr * lambda * lambda
     While of loc * expr * expr
     Seq of loc * (expr list)
     Ref of loc * expr
     Deref of loc * expr
    Assign of loc * expr * expr
     Lambda of loc * lambda
    App of loc * expr * expr
     Let of loc * var * type_expr * expr * expr
    | LetFun of loc * var * lambda
                   * type_expr * expr
    | LetRecFun of loc * var * lambda
                    * type expr * expr
```

static.mli, static.ml

```
val infer: (Past.var * Past.type_expr) list
-> (Past.expr * Past.type_expr)
```

val check : Past.expr -> Past.expr (* infer on empty environment *)

- Check type correctness
- Rewrite expressions to resolve EQ to EQI (for integers) or EQB (for bools).
- Only LetFun is returned by parser. Rewrite to LetRecFun when function is actually recursive.

Lesson: while enforcing "context-sensitive rules" we can resolve ambiguities that cannot be specified in context-free grammars.

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Internal AST (ast.ml)

```
type var = string
```

type oper = ADD | MUL | SUB | LT |
AND | OR | EQB | EQI

type unary_oper = NEG | NOT | READ

No locations, types. No Let, EQ.

Is getting rid of types a bad idea? Perhaps a full answer would be language-dependent...

```
type expr =
    | Unit
    | Var of var
    Integer of int
     Boolean of bool
    | UnaryOp of unary_oper * expr
    Op of expr * oper * expr
    If of expr * expr * expr
    Pair of expr * expr
    | Fst of expr
     Snd of expr
    Inl of expr
     Inr of expr
     Case of expr * lambda * lambda
     While of expr * expr
     Seq of (expr list)
     Ref of expr
     Deref of expr
    Assign of expr * expr
    Lambda of lambda
    App of expr * expr
    | LetFun of var * lambda * expr
    | LetRecFun of var * lambda * expr
and lambda = var * expr
```

past_to_ast.ml

val translate_expr : Past.expr -> Ast.expr

let x : t = e1 in e2 end



(fun (x: t) -> e2 end) e1

This is done to simplify some of our code. Is it a good idea? Perhaps not!

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Approaches to Mathematical Semantics

- Axiomatic: Meaning defined through logical specifications of behaviour.
 - Hoare Logic (Part II)
 - Separation Logic
- Operational: Meaning defined in terms of transition relations on states in an abstract machine.
 - Semantics (Part 1B)
- Denotational: Meaning is defined in terms of mathematical objects such as functions.
 - Denotational Semantics (Part II)

A denotational semantics for L3?

N = set of integers
 B = set of booleans
 A = set of addresses
 Expr = set of L3 expressions

E = set of environments = $I \rightarrow V$ **S** = set of stores = $A \rightarrow V$

V = set of value ≈ A + N + B + { () } + V × V + (V + V) + (V × S) → (V × S)

Set of values **V** solves this "domain equation" (here + means disjoint union).

Solving such equations is where some difficult maths is required ...

M = the meaning function

 $M : (Expr \times E \times S) \rightarrow (V \times S)$

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Interpreter 0 : An OCaml approximation

```
A = set of addresses
```

S = set of stores =
$$\mathbf{A} \rightarrow \mathbf{V}$$

V = set of value

≈ A

+ **N**

+ **B**

+ { () }

+ **V** × **V**

+ (V + V)

 $+ (\mathbf{V} \times \mathbf{S}) \rightarrow (\mathbf{V} \times \mathbf{S})$

E = set of environments = $\mathbf{A} \rightarrow \mathbf{V}$

M = the meaning function

 $M : (Expr \times E \times S) \rightarrow (V \times S)$

```
type address
type store = address -> value
and value =
   | REF of address
   INT of int
   I BOOL of bool
   I UNIT
   | PAIR of value * value
   | INL of value
   INR of value
   | FUN of ((value * store)
                     -> (value * store))
type env = Ast.var -> value
val interpret:
  Ast.expr * env * store
                      -> (value * store)
```

Most of the code is obvious!

```
let rec interpret (e, env, store) =
   match e with
  | If(e1, e2, e3) ->
    let (v, store') = interpret(e1, env, store) in
         (match v with
         | BOOL true -> interpret(e2, env, store')
         BOOL false -> interpret(e3, env, store')
         v -> complain "runtime error. Expecting a boolean!")
  | Pair(e1, e2) ->
    let (v1, store1) = interpret(e1, env, store) in
    let (v2, store2) = interpret(e2, env, store1) in (PAIR(v1, v2), store2)
  | Fst e ->
     (match interpret(e, env, store) with
     (PAIR (v1, _), store') -> (v1, store')
     | (v, _) -> complain "runtime error. Expecting a pair!")
  I Snd e ->
     (match interpret(e, env, store) with
     (PAIR (_, v2), store') -> (v2, store')
     | (v, _) -> complain "runtime error. Expecting a pair!")
   | Inl e -> let (v, store') = interpret(e, env, store) in (INL v, store')
  | Inr e -> let (v, store') = interpret(e, env, store) in (INR v, store')
                                                                                        29
```

Tricky bits: Slang functions mapped to OCaml functions!

```
let rec interpret (e, env, store) =
  match e with
   Lambda(x, e) -> (FUN (fun (v, s) -> interpret(e, update(env, (x, v)), s)), store)
  | App(e1, e2) -> (* I chose to evaluate argument first! *)
    let (v2, store1) = interpret(e2, env, store) in
    let (v1, store2) = interpret(e1, env, store1) in
       (match v1 with
       | FUN f -> f (v2, store2)
       | v -> complain "runtime error. Expecting a function!")
  | LetFun(f, (x, body), e) ->
    let new_env =
        update(env, (f, FUN (fun (v, s) -> interpret(body, update(env, (x, v)), s))))
    in interpret(e, new_env, store)
  | LetRecFun(f, (x, body), e) ->
    let rec new_env g = (* a recursive environment!!! *)
       if g = f then FUN (fun (v, s) \rightarrow interpret(body, update(new_env, (x, v)), s))
              else env q
    in interpret(e, new_env, store)
```

update: env * (var * value) -> env

Interpreter 0 is using OCaml's runtime stack. How can we move toward the Jargon VM?

```
let fun f (x) = x + 1

fun g(y) = f(y+2)+2

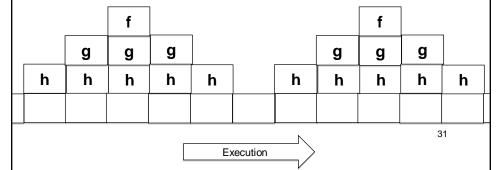
fun h(w) = g(w+1)+3

in

h(h(17))

end
```

The run-time data structure is the <u>call stack</u> containing an <u>activation record</u> for each function invocation.



Recall tail recursion: fold_left vs fold_right

From ocaml-4.01.0/stdlib/list.ml:

```
(* fold_left: ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a
   fold_left f a [b1; ...; bn]] = f (... (f (f a b1) b2) ...) bn
let rec fold left f a l =
                                                                         This is tail
match I with
      -> a
                                                                         recursive
| b :: rest -> fold_left f (f a b) rest
(* fold_right: ('a -> 'b -> 'b) -> 'a list -> 'b -> 'b
   fold_right f [a1; ...; an] b = f a1 (f a2 (... (f an b) ...))
                                                                          This is NOT
let rec fold_right f I b =
 match I with
                                                                          tail
          -> b
                                                                          recursive
 a::rest -> f a (fold_right f rest b)
```

Convert tail-recursion to iteration

```
(* gcd : int * int -> int *)
let rec gcd(m, n) =
   if m = n
   then m
   else if m < n
      then gcd(m, n - m)
      else gcd(m - n, n)</pre>
```

Here we have illustrated tail-recursion elimination as a source-to-source transformation. However, the OCaml compiler will do something similar to a lower-level intermediate representation. Upshot: we will consider all tail-recursive OCaml functions as representing iterative programs.

```
(* gcd_iter : int * int -> int *)
let gcd iter (m, n) =
  let rm = ref m
  in let rn = ref n
  in let result = ref 0
  in let not done = ref true
  in let =
      while !not_done
       do
           if !rm = !rn
           then (not done := false;
                   result := !rm)
           else if !rm < !rn
                  then rn := !rn - !rm
                  else rm := !rm - !rn
        done
  in !result
```

Question: can we transform any recursive function (such as interpreter 0) into a tail recursive function?

The answer is YES!

- We add an extra argument, called a continuation, that represents "the rest of the computation"
- This is called the Continuation Passing Style (CPS) transformation.
- We will then "defunctionalize" (DFC) these continuations and represent them with a stack.
- Finally, we obtain a tail recursive function that carries its own stack as an extra argument!

We will apply this kind of transformation to the code of interpreter 0 as the first steps towards deriving interpreter 1.

LECTURES 3 & 4 Derivation of Interpreters 1 & 2

- Continuation Passing Style (CPS): transform any recursive function to a tail-recursive function
- "Defunctionalisation" (DFC): replace higher-order functions with a data structure
- Putting it all together:
 - Derive the Fibonacci Machine
 - Derive the Expression Machine, and "compiler"!
- This provides a roadmap for the interp_0 → interp_1 → interp_2 derivations.

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(CPS) transformation of fib

```
(* fib: int -> int *)
let rec fib m =
    if m = 0
    then 1
    else if m = 1
        then 1
        else fib(m - 1) + fib (m - 2)

(* fib_cps: int * (int -> int) -> int *)
let rec fib_cps (m, cnt) =
    if m = 0
    then cnt 1
    else if m = 1
        then cnt 1
    else fib_cps(m - 1, fun a -> fib_cps(m - 2, fun b -> cnt (a + b)))
```

A closer look

```
The rest of the computation after computing "fib(m)". That is, cnt is a function expecting the result of "fib(m)" as its argument.
```

```
let rec fib_cps (m, cnt) =

if m = 0
then cnt 1
else if m = 1
then cnt 1
else fib_cps(m-1, fun a -> fib_cps(m-2, fun b -> cnt (a + b)))
```

This makes explicit the order of evaluation that is implicit in the original "fib(m-1) + fib(m-2)":

- -- first compute fib(m-1)
- -- then compute fib(m-1)
- -- then add results together
- -- then return

The computation waiting for the result of "fib(m-2)"

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Expressed with "let" rather than "fun"

```
(* fib_cps_v2: (int -> int) * int -> int *)
let rec fib_cps_v2 (m, cnt) =
  if m = 0
  then cnt 1
  else if m = 1
    then cnt 1
  else let cnt2 a b = cnt (a + b)
    in let cnt1 a = fib_cps_v2(m - 2, cnt2 a)
    in fib_cps_v2(m - 1, cnt1)
```

Some prefer writing CPS forms without explicit funs

Use the identity continuation ...

```
(* fib_cps : int * (int -> int) -> int *)
let rec fib_cps (m, cnt) =
    if m = 0
    then cnt 1
    else if m = 1
        then cnt 1
        else fib_cps(m-1, fun a -> fib_cps(m-2, fun b -> cnt (a + b)))

let id (x : int) = x

let fib_1 x = fib_cps(x, id)

List.map fib_1 [0; 1; 2; 3; 4; 5; 6; 7; 8; 9; 10];;
        = [1; 1; 2; 3; 5; 8; 13; 21; 34; 55; 89]
```

Correctness?

For all c: int -> int, for all m, $0 \le m$, we have, $c(fib m) = fib_cps(m, c)$.

Proof: assume c: int -> int. By Induction on m. Base case: m = 0:

 $fib_cps(0, c) = c(1) = c(fib(0).$

NB: This proof pretends that we can treat OCaml functions as ideal mathematical functions, which of course we cannot. OCaml functions might raise exceptions like "stack overflow" or "you burned my toast", and so on. But this is a convenient fiction as long as we remember to be careful.

Induction step: Assume for all n < m, $c(fib n) = fib_cps(n, c)$. (That is, we need course-of-values induction!)

```
fib_cps(m + 1, c)
= if m + 1 = 1
then c 1
else fib_cps((m+1) -1, fun a -> fib_cps((m+1) -2, fun b -> c (a + b)))
= if m + 1 = 1
then c 1
else fib_cps(m, fun a -> fib_cps(m-1, fun b -> c (a + b)))
= (by induction)
if m + 1 = 1
then c 1
else (fun a -> fib_cps(m -1, fun b -> c (a + b))) (fib m)
```

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Correctness?

```
= if m + 1 = 1
 then c 1
 else fib cps(m-1, fun b \rightarrow c ((fib m) + b))
= (by induction)
 if m + 1 = 1
 then c 1
 else (fun b -> c ((fib m) + b)) (fib (m-1))
= if m + 1 = 1
 then c 1
 else c ((fib m) + (fib (m-1)))
= c (if m + 1 = 1)
    then 1
    else ((fib m) + (fib (m-1))))
= c(if m + 1) = 1
    then 1
    else fib((m + 1) - 1) + fib((m + 1) - 2))
= c (fib(m + 1))
```

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QED.

Can with express fib_cps without a functional argument?

```
(* fib_cps_v2: (int -> int) * int -> int *)
let rec fib_cps_v2 (m, cnt) =
  if m = 0
  then cnt 1
  else if m = 1
      then cnt 1
      else let cnt2 a b = cnt (a + b)
            in let cnt1 a = fib_cps_v2(m - 2, cnt2 a)
            in fib_cps_v2(m - 1, cnt1)
```

Idea of "defunctionalisation" (DFC): replace id, cnt1 and cnt2 with instances of a new data type:

```
type cnt = ID | CNT1 of int * cnt | CNT2 of int * cnt
```

Now we need an "apply" function of type cnt * int -> int

"Defunctionalised" version of fib_cps

```
(* datatype to represent continuations *)
type cnt = ID | CNT1 of int * cnt | CNT2 of int * cnt
(* apply_cnt : cnt * int -> int *)
let rec apply_cnt = function
 | (ID, a)
 | (CNT1 (m, cnt), a) -> fib_cps_dfc(m - 2, CNT2 (a, cnt))
 (CNT2 (a, cnt), b) -> apply_cnt (cnt, a + b)
(* fib_cps_dfc: (cnt * int) -> int *)
and fib_cps_dfc (m, cnt) =
  if m = 0
  then apply_cnt(cnt, 1)
  else if m = 1
        then apply_cnt(cnt, 1)
        else fib_cps_dfc(m -1, CNT1(m, cnt))
(* fib 2: int -> int *)
                                                                           43
let fib_2 m = fib_cps_dfc(m, ID)
```

Correctness?

```
Let < c > be of type cnt representing a continuation c : int -> int constructed by fib_cps.
```

Proof left as an exercise!

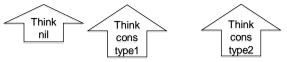
```
Then
apply_cnt(< c >, m) = c(m)
and
```

 $fib_cps(n, c) = fib_cps_dfc(n, < c >).$

Eureka! Continuations are just lists (used like a stack)

type int_list = NIL | CONS of int * int_list

type cnt = ID | CNT1 of int * cnt | CNT2 of int * cnt



Replace the above continuations with lists! (I've selected more suggestive names for the constructors.)

```
type tag = SUB2 of int | PLUS of int
type tag_list_cnt = tag list
```

4

The continuation lists are used like a stack!

```
type tag = SUB2 of int | PLUS of int
type tag_list_cnt = tag list
(* apply_tag_list_cnt : tag_list_cnt * int -> int *)
let rec apply_tag_list_cnt = function
 | ([], a)
                          -> a
 | ((SUB2 m) :: cnt, a) -> fib_cps_dfc_tags(m - 2, (PLUS a):: cnt)
 | ((PLUS a) :: cnt, b) -> apply_tag_list_cnt (cnt, a + b)
(* fib_cps_dfc_tags : (tag_list_cnt * int) -> int *)
and fib_cps_dfc_tags (m, cnt) =
  if m = 0
  then apply_tag_list_cnt(cnt, 1)
  else if m = 1
       then apply_tag_list_cnt(cnt, 1)
       else fib_cps_dfc_tags(m - 1, (SUB2 m) :: cnt)
(* fib_3: int -> int *)
                                                                              46
let fib_3 m = fib_cps_dfc_tags(m, [])
```

Combine Mutually tail-recursive functions into a single function

```
type state type =
 SUB1 (* for right-hand-sides starting with fib_ *)
 APPL (* for right-hand-sides starting with apply_ *)
type state = (state_type * int * tag_list_cnt) -> int
(* eval : state -> int
                            A two-state transition function*)
let rec eval = function
                         cnt) -> eval (APPL, 1,
 (SUB1, 0,
                                                                 cnt)
 (SUB1, 1,
                         cnt) -> eval (APPL, 1,
                                                                 cnt)
 | (SUB1, m,
                         cnt) -> eval (SUB1, (m-1), (SUB2 m) :: cnt)
 | (APPL, a, (SUB2 m) :: cnt) -> eval (SUB1, (m-2), (PLUS a) :: cnt)
 | (APPL, b, (PLUS a) :: cnt) -> eval (APPL, (a+b),
 | (APPL, a,
                           []) -> a
(* fib_4 : int -> int *)
let fib_4 m = eval (SUB1, m, [])
                                                                        47
```

Eliminate tail recursion to obtain The Fibonacci Machine!

```
(* step : state -> state *)
let step = function
                          cnt) -> (APPL, 1,
 (SUB1, 0,
                                                             cnt)
 | (SUB1, 1,
                          cnt) -> (APPL, 1,
                                                             cnt)
                          cnt) -> (SUB1, (m-1), (SUB2 m) :: cnt)
 (SUB1, m,
 | (APPL, a, (SUB2 m) :: cnt) -> (SUB1, (m-2), (PLUS a) :: cnt)
 | (APPL, b, (PLUS a) :: cnt) -> (APPL, (a+b),
                                                             cnt)
 | _ -> failwith "step : runtime error!"
                                          In this version we have
(* clearly TAIL RECURSIVE! *)
                                          simply made the
let rec driver state = function
                                          tail-recursive
  | (APPL, a, []) -> a
                                          structure very explicit.
                -> driver (step state)
  state
(* fib 5 : int -> int *)
let fib_5 m = driver (SUB1, m, [])
                                                              48
```

Here is a trace of fib 5 6.

```
1 SUB1 || 6 || []
                                                                       26 APPL || 1 || [SUB2 6, PLUS 5, SUB2 3, PLUS 1]
2 SUB1 || 5 || [SUB2 6]
3 SUB1 || 4 || [SUB2 6, SUB2 5]
                                                                       27 APPL || 2 || [SUB2 6, PLUS 5, SUB2 3]
                                                                       28 SUB1 || 1 || [SUB2 6, PLUS 5, PLUS 2]
4 SUB1 || 3 || [SUB2 6, SUB2 5, SUB2 4]
                                                                       29 APPL || 1 || [SUB2 6, PLUS 5, PLUS 2]
5 SUB1 || 2 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3]
                                                                       30 APPL || 3 || [SUB2 6, PLUS 5]
6 SUB1 || 1 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3, SUB2 2]
7 APPL || 1 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3, SUB2 2]
                                                                       31 APPL || 8 || [SUB2 6]
                                                                       32 SUB1 || 4 || [PLUS 8]
8 SUB1 || 0 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3, PLUS 1]
                                                                       33 SUB1 || 3 || [PLUS 8, SUB2 4]
9 APPL || 1 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3, PLUS 1]
                                                                       34 SUB1 || 2 || [PLUS 8, SUB2 4, SUB2 3]
10 APPL || 2 || [SUB2 6, SUB2 5, SUB2 4, SUB2 3]
                                                                       35 SUB1 || 1 || [PLUS 8, SUB2 4, SUB2 3, SUB2 2]
11 SUB1 || 1 || [SUB2 6, SUB2 5, SUB2 4, PLUS 2]
                                                                       36 APPL || 1 || [PLUS 8, SUB2 4, SUB2 3, SUB2 2]
12 APPL || 1 || [SUB2 6, SUB2 5, SUB2 4, PLUS 2]
                                                                       37 SUB1 || 0 || [PLUS 8, SUB2 4, SUB2 3, PLUS 1]
13 APPL || 3 || [SUB2 6, SUB2 5, SUB2 4]
                                                                       38 APPL || 1 || [PLUS 8, SUB2 4, SUB2 3, PLUS 1]
                                                                       39 APPL || 2 || [PLUS 8, SUB2 4, SUB2 3]
14 SUB1 || 2 || [SUB2 6, SUB2 5, PLUS 3]
15 SUB1 || 1 || [SUB2 6, SUB2 5, PLUS 3, SUB2 2]
                                                                       40 SUB1 || 1 || [PLUS 8, SUB2 4, PLUS 2]
16 APPL || 1 || [SUB2 6, SUB2 5, PLUS 3, SUB2 2]
                                                                       41 APPL || 1 || [PLUS 8, SUB2 4, PLUS 2]
17 SUB1 || 0 || [SUB2 6, SUB2 5, PLUS 3, PLUS 1]
                                                                       42 APPL || 3 || [PLUS 8, SUB2 4]
                                                                       43 SUB1 || 2 || [PLUS 8, PLUS 3]
18 APPL || 1 || [SUB2 6, SUB2 5, PLUS 3, PLUS 1]
19 APPL || 2 || [SUB2 6, SUB2 5, PLUS 3]
                                                                       44 SUB1 || 1 || [PLUS 8, PLUS 3, SUB2 2]
                                                                       45 APPL || 1 || [PLUS 8, PLUS 3, SUB2 2]
20 APPL | 5 | | | SUB2 6, SUB2 5
                                                                       46 SUB1 || 0 || [PLUS 8, PLUS 3, PLUS 1]
47 APPL || 1 || [PLUS 8, PLUS 3, PLUS 1]
21 SUB1 || 3 || [SUB2 6, PLUS 5]
22 SUB1 || 2 || [SUB2 6, PLUS 5, SUB2 3]
23 SUB1 || 1 || [SUB2 6, PLUS 5, SUB2 3, SUB2 2]
                                                                       48 APPL || 2 || [PLUS 8, PLUS 3]
24 APPL || 1 || [SUB2 6, PLUS 5, SUB2 3, SUB2 2]
                                                                       49 APPL || 5 || [PLUS 8]
25 SUB1 || 0 || [SUB2 6, PLUS 5, SUB2 3, PLUS 1]
                                                                       50 APPL ||13|| []
```

The OCaml file in basic_transformations/fibonacci_machine.ml contains some code for pretty printing such traces....

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Pause to reflect

- What have we accomplished?
- We have taken a recursive function and turned it into an iterative function that does not require "stack space" for its evaluation (in OCaml)
- However, this function now carries its own evaluation stack as an extra argument!
- We have derived this iterative function in a stepby-step manner where each tiny step is easily proved correct.
- Wow!

That was fun! Let's do it again!

```
type expr =
| INT of int
| PLUS of expr * expr
| SUBT of expr * expr
| MULT of expr * expr
```

This time we will derive a stack-machine AND a "compiler" that translates expressions into a list of instructions for the machine.

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Here we go again: CPS

```
type cnt_2 = int -> int
type state 2 = expr * cnt 2
(* eval_aux_2 : state_2 -> int *)
let rec eval_aux_2 (e, cnt) =
 match e with
 INT a
             -> cnt a
 | PLUS(e1, e2) ->
    eval_aux_2(e1, fun v1 -> eval_aux_2(e2, fun v2 -> cnt(v1 + v2)))
 | SUBT(e1, e2) ->
    eval_aux_2(e1, fun v1 -> eval_aux_2(e2, fun v2 -> cnt(v1 - v2)))
 | MULT(e1, e2) ->
    eval_aux_2(e1, fun v1 -> eval_aux_2(e2, fun v2 -> cnt(v1 * v2)))
(* id_cnt : cnt_2 *)
let id_cnt(x:int) = x
(* eval_2 : expr -> int *)
let eval 2 e = eval aux 2(e, id_cnt)
```

Defunctionalise!

```
type cnt_3 =
 IID
 OUTER_PLUS of expr * cnt_3
 OUTER_SUBT of expr * cnt_3
 OUTER_MULT of expr * cnt_3
 | INNER_PLUS of int * cnt_3
 INNER SUBT of int * cnt 3
 | INNER_MULT of int * cnt_3
type state_3 = expr * cnt_3
(* apply_3 : cnt_3 * int -> int *)
let rec apply_3 = function
 | (ID,
                                 -> V
 | (OUTER_PLUS(e2, cnt), v1) -> eval_aux_3(e2, INNER_PLUS(v1, cnt))
 | (OUTER_SUBT(e2, cnt), v1) -> eval_aux_3(e2, INNER_SUBT(v1, cnt))
 | (OUTER_MULT(e2, cnt), v1) -> eval_aux_3(e2, INNER_MULT(v1, cnt))
 | (INNER_PLUS(v1, cnt), v2) -> apply_3(cnt, v1 + v2)
 | (INNER_SUBT(v1, cnt), v2) -> apply_3(cnt, v1 - v2)
 | (INNER_MULT(v1, cnt), v2) -> apply_3(cnt, v1 * v2)
                                                                        53
```

Defunctionalise!

Eureka! Again we have a stack!

```
type tag =
 O_PLUS of expr
 | I_PLUS of int
 O_SUBT of expr
 | I_SUBT of int
 O_MULT of expr
 | I_MULT of int
type cnt_4 = tag list
type state_4 = expr * cnt_4
(* apply_4 : cnt_4 * int -> int *)
let rec apply_4 = function
 | ([],
              v)
                             -> V
 | ((O_PLUS e2) :: cnt, v1) -> eval_aux_4(e2, (I_PLUS v1) :: cnt)
  | ((O_SUBT e2) :: cnt, v1) -> eval_aux_4(e2, (I_SUBT v1) :: cnt)
 | ((O_MULT e2) :: cnt, v1) -> eval_aux_4(e2, (I_MULT v1) :: cnt)
  |((I_PLUS v1) :: cnt, v2) -> apply_4(cnt, v1 + v2)|
 | ((I_SUBT v1) :: cnt, v2) -> apply_4(cnt, v1 - v2)
                                                                           55
  | ((I_MULT v1) :: cnt, v2) -> apply_4(cnt, v1 * v2)
```

Eureka! Again we have a stack!

Eureka! Can combine apply_4 and eval aux 4

```
type acc =
    |A_INT of int
    |A_EXP of expr

type cnt_5 = cnt_4

type state_5 = cnt_5 * acc

val : step : state_5 -> state_5

val driver : state_5 -> int
```

val eval_5 : expr -> int

Type of an "accumulator" that contains either an int or an expression.

The driver will be clearly tail-recursive ...

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Rewrite to use driver, accumulator

```
let step 5 = function
                   A EXP (INT a)) \rightarrow (cnt, A INT a)
 (cnt,
 (cnt, A EXP (PLUS(e1, e2))) -> (O PLUS(e2) :: cnt, A EXP e1)
  (cnt, A EXP (SUBT(e1, e2))) -> (O SUBT(e2) :: cnt, A EXP e1)
         A_EXP (MULT(e1, e2))) -> (O_MULT(e2) :: cnt, A_EXP e1)
  | ((O PLUS e2) :: cnt, A INT v1) -> ((I PLUS v1) :: cnt, A EXP e2)
  | ((O_SUBT e2) :: cnt, A_INT v1) -> ((I_SUBT v1) :: cnt, A_EXP e2)
  | ((O MULT e2) :: cnt, A INT v1) -> ((I MULT v1) :: cnt, A EXP e2)
  | ((I_PLUS v1) :: cnt, A_INT v2) -> (cnt, A_INT (v1 + v2))
 | ((I_SUBT v1) :: cnt, A_INT v2) -> (cnt, A_INT (v1 - v2))
  | ((I_MULT v1) :: cnt, A_INT v2) -> (cnt, A_INT (v1 * v2))
                            A INT v) -> ([], A INT v)
 | ([],
let rec driver 5 = function
  |([], A | INT v) -> v
                -> driver_5 (step_5 state)
  state
                                                                       58
let eval_5 e = driver_5([], A_EXP e)
```

Eureka! There are really two independent stacks here --- one for "expressions" and one for values

```
| E of expr
| DO_PLUS
| DO_SUBT
| DO_MULT

type directive_stack = directive list

type value_stack = int list

type state_6 = directive_stack * value_stack

val step_6 : state_6 -> state_6

val driver_6 : state_6 -> int

val exp_6 : expr -> int
```

type directive =

The state is now two stacks!

Split into two stacks

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An eval_6 trace

e = PLUS(MULT(INT 89, INT 2), SUBT(INT 10, INT 4))

```
state 1 DS = [E(PLUS(MULT(INT(89), INT(2)), SUBT(INT(10), INT(4))))]
                VS = []
        state 2 DS = [DO_PLUS; E(SUBT(INT(10), INT(4))); E(MULT(INT(89), INT(2)))]
                VS = []
        state 3 DS = [DO_PLUS; E(SUBT(INT(10), INT(4))); DO_MULT; E(INT(2)); E(INT(89))]
                VS = []
        state 4 DS = [DO_PLUS; E(SUBT(INT(10), INT(4))); DO_MULT; E(INT(2))]
                VS = [89]
compute
        state 5 DS = [DO_PLUS; E(SUBT(INT(10), INT(4))); DO_MULT]
                VS = [89; 2]
        state 6 DS = [DO_PLUS; E(SUBT(INT(10), INT(4)))]
                VS = [178]
        state 7 DS = [DO_PLUS; DO_SUBT; E(INT(4)); E(INT(10))]
inspect
                VS = [178]
        state 8 DS = [DO_PLUS; DO_SUBT; E(INT(4))]
                VS = [178; 10]
        state 9 DS = [DO_PLUS; DO_SUBT]
compute
                                                                       Top of each
                VS = [178; 10; 4]
        state 10DS = [DO_PLUS]
                                                                       stack is on
                VS = [178; 6]
                                                                       the right
        state 11DS = []
                VS = [184]
```

Key insight

This evaluator is interleaving two distinct computations:

- (1) decomposition of the input expression into sub-expressions
- (2) the computation of +, -, and *.

Idea: why not do the decomposition BEFORE the computation?

Key insight: An interpreter can (usually) be <u>refactored</u> into a translation (compilation!) followed by a lower-level interpreter.

Interpret_higher (e) = interpret_lower(compile(e))

Note: this can occur at many levels of abstraction: think of machine code being interpreted in micro-code ...

Refactor --- compile!

```
(* low-level instructions *)
type instr =
 | Ipush of int
 | Iplus
                                        Never put off till run-time what
 Isubt
 I Imult
                                        you can do at compile-time.
                                                    -- David Gries
type code = instr list
type state_7 = code * value_stack
(* compile : expr -> code *)
let rec compile = function
 I INT a
                   -> [lpush a]
 | PLUS(e1, e2) -> (compile e1) @ (compile e2) @ [lplus]
 | SUBT(e1, e2) -> (compile e1) @ (compile e2) @ [Isubt]
 | MULT(e1, e2) -> (compile e1) @ (compile e2) @ [Imult]
                                                                       63
```

Evaluate compiled code.

```
(* step_7 : state_7 -> state_7 *)

let step_7 = function

| (lpush v :: is, vs) -> (is, v :: vs)
| (lplus :: is, v2::v1::vs) -> (is, (v1 + v2) :: vs)
| (lsubt :: is, v2::v1::vs) -> (is, (v1 - v2) :: vs)
| (lmult :: is, v2::v1::vs) -> (is, (v1 * v2) :: vs)
| _ -> failwith "eval : runtime error!"

let rec driver_7 = function
| ([], [v]) -> v
| _ -> driver_7 (step_7 state)

let eval_7 e = driver_7 (compile e, []) |
```

```
An eval 7 trace
inspect
         compile (PLUS(MULT(INT 89, INT 2), SUBT(INT 10, INT 4)))
           = [push 89; push 2; mult; push 10; push 4; subt; plus]
          state 1 IS = [add; sub; push 4; push 10; mul; push 2; push 89]
                 VS = []
          state 2 IS = [add; sub; push 4; push 10; mul; push 2]
                 VS = [89]
          state 3 IS = [add; sub; push 4; push 10; mul]
                 VS = [89; 2]
compute
          state 4 IS = [add; sub; push 4; push 10]
                 VS = [178]
         state 5 IS = [add; sub; push 4]
                 VS = [178; 10]
         state 6 IS = [add; sub]
                 VS = [178; 10; 4]
          state 7 IS = [add]
                                                            Top of each
                 VS = [178; 6]
                                                            stack is on
          state 8 IS = []
                                                            the right
                 VS = [184]
```

interpret is implicitly using Ocaml's runtime stack

```
let rec interpret (e, env, store) =
match e with
| Integer n -> (INT n, store)
| Op(e1, op, e2) ->
let (v1, store1) = interpret(e1, env, store) in
let (v2, store2) = interpret(e2, env, store1) in
(do_oper(op, v1, v2), store2)
:
:
```

- Every invocation of interpret is building an activation record on Ocaml's runtime stack.
- We will now define interpreter 2 which makes this stack explicit

Interp_0.ml \rightarrow interp_1.ml \rightarrow interp_2.ml

The derivation from eval to compile+eval_7 can be used as a guide to a derivation from Interpreter 0 to interpreter 2.

- 1. Apply CPS to the code of Interpreter 0
- 2. Defunctionalise
- Arrive at interpreter 1, which has a single continuation stack containing expressions, values and environments (analogous to eval_6)
- Spit this stack into two stacks : one for instructions and the other for values and environments
- 5. Refactor into compiler + lower-level interpreter
- 6. Arrive at interpreter 2. (analogous to eval_7)

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Interpreter 0 → Interpreter 2

Interpreter 2: A high-level stack-oriented machine

- 1. Makes the Ocaml runtime stack explicit
- 2. Complex values pushed onto stacks
- 3. One stack for values and environments
- 4. One stack for instructions
- 5. Heap used only for references
- 6. Instructions have tree-like structure

(we will not look at the details of interpreter 1 ...)

Inpterp_2 data types

type address = int

I INT of int

REF of address

BOOL of bool

INL of value

INR of value

| PAIR of value * value

type value =

I UNIT

```
CLOSURE of bool * closur
and closure = code * env
```

Interp_2

and instruction = | PUSH of value | LOOKUP of var | UNARY of unary_oper | OPER of oper ASSIGN SWAP I POP I BIND of var I FST SND | DEREF APPLY MK_PAIR MK_INL MK_INR MK_REF MK_CLOSURE of code MK_REC of var * code | TEST of code * code CASE of code * code | WHILE of code * code

Interp_2.ml: The Abstract Machine

and code = instruction list

and binding = var * value

and env = binding list

type env_or_value = EV of env | V of value

type env_value_stack = env_or_value list

type state = code * env_value_stack

val step: state -> state

val driver: state -> value

val compile: expr -> code

val interpret : expr -> value

The state is actually comprised of a heap --- a global array of values --- a pair of the form

(code, evn_value_stack)

Interpreter 2: The Abstract Machine

```
type state = code * env_value_stack
val step : state -> state
```

The state transition function.

The driver. Correctness

```
(* val driver : state -> value *)

let rec driver state =
  match state with
  | ([], [V v]) -> v
  | _ -> driver (step state)
```

val compile : expr -> code

The idea: if e passes the frond-end and Interp_0.interpret e = v then driver (compile e, []) = v' where v' (somehow) represents v.

In other words, evaluating compile e should leave the value of e on top of the stack

Implement inter_0 in interp_2

```
let rec interpret (e, env, store) =
                                                                   interp_0.ml
  match e with
| Pair(e1, e2) ->
    let (v1, store1) = interpret(e1, env, store) in
    let (v2, store2) = interpret(e2, env, store1) in (PAIR(v1, v2), store2)
  | Fst e ->
     (match interpret(e, env, store) with
     (PAIR (v1, ), store') -> (v1, store')
     | (v, _) -> complain "runtime error. Expecting a pair!")
  let step = function
  | (MK_PAIR :: ds, (V v2) :: (V v1) :: evs) -> (ds, V(PAIR(v1, v2)) :: evs)
                      V(PAIR (v, _)) :: evs) -> (ds, (V v) :: evs)
  | (FST :: ds,
  let rec compile = function
  | Pair(e1, e2) -> (compile e1) @ (compile e2) @ [MK_PAIR]
                 -> (compile e) @ [FST]
                                                                   interp_2.ml 73
```

Implement inter_0 in interp_2

```
let rec interpret (e, env, store) =
                                                                   interp_0.ml
  match e with
  | If(e1, e2, e3) ->
    let (v, store') = interpret(e1, env, store) in
        (match v with
        BOOL true -> interpret(e2, env, store')
        BOOL false -> interpret(e3, env, store')
        | v -> complain "runtime error. Expecting a boolean!")
let step = function
| ((TEST(c1, c2)) :: ds, V(BOOL true) :: evs) -> (c1 @ ds, evs)
| ((TEST(c1, c2)) :: ds, V(BOOL false) :: evs) -> (c2 @ ds, evs)
let rec compile = function
| If(e1, e2, e3) -> (compile e1) @ [TEST(compile e2, compile e3)]
                                                                  interp_2.ml
                                                                                 74
```

```
Tricky bits again!
let rec interpret (e, env, store) =
                                                                          interp_0.ml
  match e with
  Lambda(x, e) -> (FUN (fun (v, s) -> interpret(e, update(env, (x, v)), s)), store)
  | App(e1, e2) -> (* I chose to evaluate argument first! *)
   let (v2, store1) = interpret(e2, env, store) in
   let (v1, store2) = interpret(e1, env, store1) in
       (match v1 with
       | FUN f -> f (v2, store2)
      | v -> complain "runtime error. Expecting a function!")
let step = function
                                                                          interp_2.ml
| (POP :: ds,
                                s :: evs) -> (ds, evs)
| (SWAP :: ds,
                         s1 :: s2 :: evs) -> (ds, s2 :: s1 :: evs)
| ((BIND x) :: ds,
                            (V v) :: evs) -> (ds, EV([(x, v)]) :: evs)
| ((MK_CLOSURE c) :: ds,
                                    evs) -> (ds, V(mk_fun(c, evs_to_env evs)) :: evs)
| (APPLY :: ds, V(CLOSURE (_, (c, env))) :: (V v) :: evs)
                                        -> (c @ ds, (V v) :: (EV env) :: evs)
let rec compile = function
| Lambda(x, e) -> [MK_CLOSURE((BIND x) :: (compile e) @ [SWAP; POP])]
| App(e1, e2)
               -> (compile e2) @ (compile e1) @ [APPLY; SWAP; POP]
                                                                                  75
```

Example : Compiled code for rev_pair.slang

```
let rev_pair (p : int * int) : int * int = (snd p, fst p)
in
   rev_pair (21, 17)
end
 MK_CLOSURE([BIND p; LOOKUP p; SND; LOOKUP p; FST; MK_PAIR; SWAP; POP]);
 BIND rev_pair;
 PUSH 21;
 PUSH 17;
 MK PAIR:
 LOOKUP rev_pair;
 APPLY;
                            DEMO TIME!!!
 SWAP;
 POP:
 SWAP:
 POP
```

LECTURE 5 Derive Interpreter 3

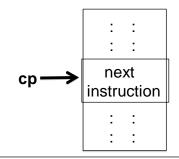
- 1. "Flatten" code into linear array
- 2. Add "code pointer" (cp) to machine state
- 3. New instructions: LABEL, GOTO, RETURN
- 4. "Compile away" conditionals and while loops

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Linearise code

Interpreter 2 copies code on the code stack.

We want to introduce one global array of instructions indexed by a code pointer (**cp**). At runtime the **cp** points at the next instruction to be executed.



This will require two new instructions:

LABEL L: Associate label L with this location in the code array

GOTO L : Set the cp to the code address associated with L

Compile conditionals, loops

If(e1, e2, e3)

code for e1

TEST k

code for e2

GOTO_m

k: code for e3

m:

While(e1, e2)

m: code for e1

TEST k

code for e2

GOTO m

k:

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If ? = 0 Then 17 else 21 end

interp_2

__

interp_3

PUSH UNIT; UNARY READ;

PUSH 0; OPER EQI;

TEST([PUSH 17],

[PUSH 21]

)

.....

PUSH UNIT; UNARY READ;

PUSH 0;

OPER EQI;

TEST L0; PUSH 17;

GOTO L1;

LABEL L0; PUSH 21;

LABEL L1; HALT

Symbolic code locations

interp_3 (loaded)

0: PUSH UNIT; 1: UNARY READ;

2: PUSH 0;

3: OPER EQI;

4: TEST L0 = 7;

5: PUSH 17;

6: GOTO L1 = 9;

7: LABEL L0; 8: PUSH 21;

9: LABEL L1;

10: HALT

Numeric code locations

Implement inter_2 in interp_3

Code locations are represented as

```
("L", None) : not yet loaded (assigned numeric address)
```

("L", Some i) : label "L" has been assigned numeric address i

```
Tricky bits again!
let step = function
                                                                 interp 2.ml
| (POP :: ds,
                            s :: evs) -> (ds, evs)
| (SWAP :: ds,
                      s1 :: s2 :: evs) -> (ds, s2 :: s1 :: evs)
((MK_CLOSURE c) :: ds,
                               evs) -> (ds, V(mk_fun(c, evs_to_env evs)) :: evs)
| (APPLY :: ds, V(CLOSURE (_, (c, env))) :: (V v) :: evs)
                                    -> (c @ ds, (V v) :: (EV env) :: evs)
let step (cp, evs) =
                                                                 interp 3.ml
match (get_instruction cp, evs) with
I (POP,
                               s :: evs) -> (cp + 1, evs)
I (SWAP,
                        s1 :: s2 :: evs) -> (cp + 1, s2 :: s1 :: evs)
(BIND x,
                        (V v) :: evs) \rightarrow (cp + 1, EV([(x, v)]) :: evs)
| (MK_CLOSURE loc,
                                 evs) -> (cp + 1,
                                            V(CLOSURE(loc, evs_to_env evs)) ::
| (RETURN, (V v) :: _ :: (RA i) :: evs) -> (i, (V v) :: evs)
(APPLY, V(CLOSURE ((_, Some i), env)) :: (V v) :: evs)
Note that in interp_2 the body of a closure is consumed from
the code stack. But in interp_3 we need to save the return
```

address on the stack (here i is the location of the closure's code).

```
Tricky bits again!
                                                                      interp_2.ml
let rec compile = function
| Lambda(x, e) -> [MK_CLOSURE((BIND x) :: (compile e) @ [SWAP; POP])]
| App(e1, e2)
               -> (compile e2) @ (compile e1) @ [APPLY; SWAP; POP]
let rec comp = function
                                                                      Interp_3.ml
| App(e1, e2) ->
 let (defs1, c1) = comp e1 in
 let (defs2, c2) = comp e2 in
     (defs1 @ defs2, c2 @ c1 @ [APPLY])
| Lambda(x, e) ->
 let (defs, c) = comp e in
 let f = new_label () in
 let def = [LABEL f; BIND x] @ c @ [SWAP; POP; RETURN] in
    (def @ defs, [MK_CLOSURE((f, None))])
                                                                     Interp_3.ml
let compile e =
   let (defs, c) = comp e in
                 (* body of program *)
    @ [HALT] (* stop the interpreter *)
                 (* function definitions *)
    @ defs
                                                                              83
```

Interpreter 3 (very similar to interpreter 2)

Some observations

- · A very clean machine!
- But it still has a very inefficient treatment of environments.
- Also, pushing complex values on the stack is not what most virtual machines do. In fact, we are still using OCaml's runtime memory management to manipulate complex values.

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Example: Compiled code for rev_pair.slang

```
let rev_pair (p : int * int) : int * int = (snd p, fst p)
in
rev_pair (21, 17)
end
```

```
MK_CLOSURE(
[BIND p; LOOKUP p; SND;
LOOKUP p; FST; MK_PAIR;
SWAP; POP]);
BIND rev_pair;
PUSH 21;
PUSH 17;
MK_PAIR;
LOOKUP rev_pair;
APPLY;
SWAP;
POP;
SWAP;
POP
```

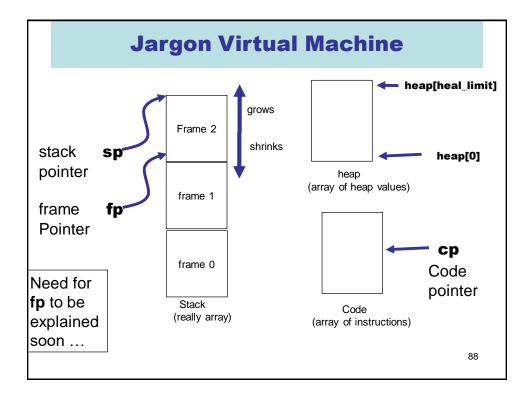
```
MK_CLOSURE(rev_pair)
BIND rev_pair
PUSH 21
PUSH 17
MK_PAIR
LOOKUP rev_pair
APPLY
SWAP
POP
HALT
Interp_3
```

LABEL rev_pair BIND p LOOKUP p SND LOOKUP p FST MK_PAIR SWAP POP RETURN

DEMO TIME!!!

LECTURES 6 Deriving The Jargon VM (interpreter 4)

- 1. First change: Introduce an addressable stack.
- 2. Replace variable lookup by a (relative) location on the stack or heap determined at **compile time**.
- 3. Relative to what? A **frame pointer** (**fp**) pointing into the stack is needed to keep track of the current **activation record**.
- **4. Second change**: Optimise the representation of closures so that they contain <u>only</u> the values associated with the <u>free</u> variables of the closure and a pointer to code.
- **5. Third change**: Restrict values on stack to be simple (ints, bools, heap addresses, etc). Complex data is moved to the heap, leaving pointers into the heap on the stack.
- 6. How might things look different in a language without firstclass functions? In a language with multiple arguments to function calls?



The stack in interpreter 3

A stack in interpreter 3

(1, (2, 17)) Inl(inr(99)) : : :

"All problems in computer science can be solved by another level of indirection, except of course for the problem of too many indirections."

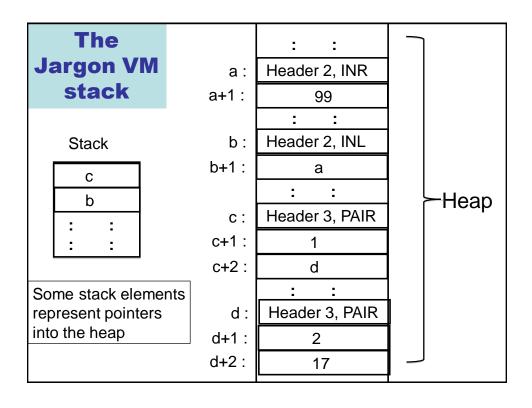
--- David Wheeler

Stack elements in interpreter 3 are not of <u>fixed size</u>.

Virtual machines (JVM, etc) typically restrict stack elements to be of a fixed size

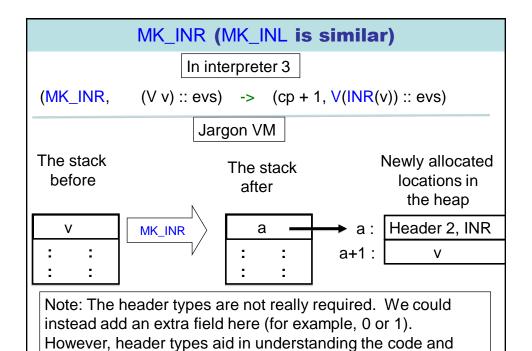
We need to shift data from the high-level stack of interpreter 3 to a lower-level stack with fixed size elements.

Solution: put the data in the heap. Place pointers to the heap on the stack.

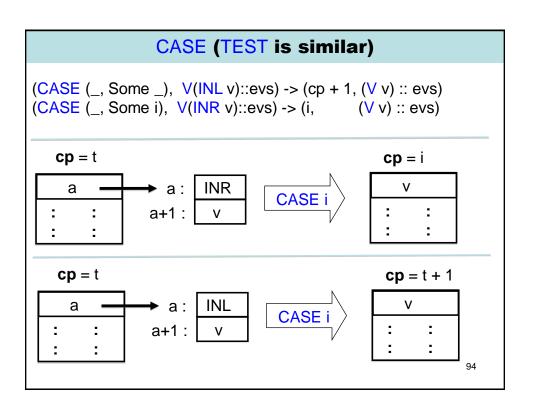


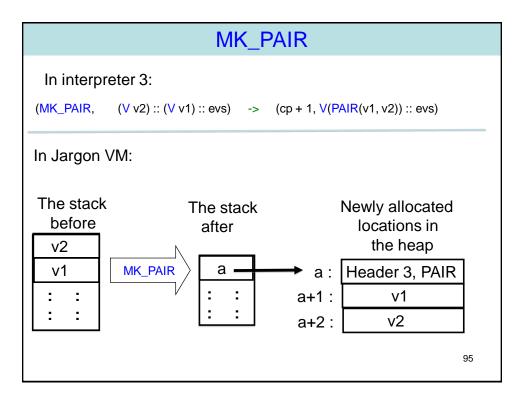
```
Small change to
                                                                     jargon.mli
interp_3.mli
                                  instructions
                                        type instruction =
    type instruction =
                                         | PUSH of stack item
                                                                   (* modified *)
     | PUSH of value
                                         | LOOKUP of value_path
                                                                   (* modified *)
     LOOKUP of Ast.var
                                         | UNARY of Ast.unary_oper
     UNARY of Ast.unary oper
                                         | OPER of Ast.oper
     OPER of Ast.oper
                                         | ASSIGN
     | ASSIGN
                                         I SWAP
     I SWAP
                                         I POP
     I POP
                                         (* | BIND of var
                                                              not needed *)
     | BIND of Ast.var
                                         I FST
     IFST
                                         LSND
     ISND
                                         I DEREF
     DEREF
                                         I APPLY
     | APPLY
                                         I RETURN
     I RETURN
                                         | MK_PAIR
     MK_PAIR
                                         MK_INL
     MK_INL
                                         I MK INR
     MK_INR
                                         IMK REF
     | MK_REF
                                         | MK_CLOSURE of location * int (* modified *)
     MK CLOSURE of location
                                         | TEST of location
     | TEST of location
                                         | CASE of location
     | CASE of location
                                         | GOTO of location
     GOTO of location
                                         | LABEL of label
     | LABEL of label
                                         | HALT
     I HALT
                                                                                  91
```

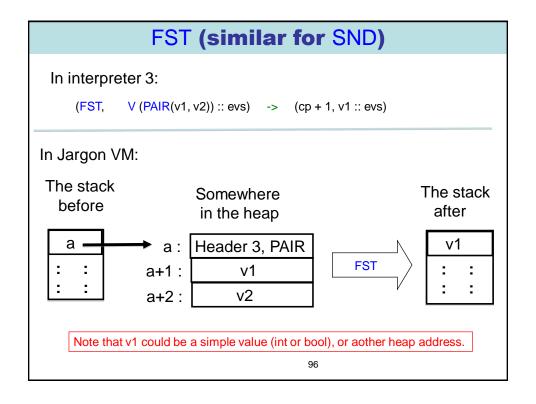
A word about implementation Interpreter 3 type value = | REF of address | INT of int | BOOL of bool | UNIT | PAIR of value * value | INL of value | INR of value | CLOSURE of location * env type env_or_value = | EV of env | V of value | RA of address type env_value_stack = env_or_value list type stack_item = Jargon VM type heap_type = | STACK_INT of int HT_PAIR | STACK_BOOL of bool | HT_INL | STACK_UNIT | HT_INR STACK_HI of heap_index (* Heap Index | HT_CLOSURE STACK_RA of code_index (* Return Address | STACK_FP of stack_index (* (saved) Frame Pointer *) type heap_item = The headers will be essential for | HEAP_INT of int | HEAP_BOOL of bool garbage collection! | HEAP_UNIT | HEAP_HI of heap_index (* Heap Index | HEAP_CI of code_index (* Code pointer for closures | HEAP_HEADER of int * heap_type (* int is number items in heap block *) 92



traces of runtime execution.







These require more care ...

In interpreter 3:

```
let step (cp, evs) =
  match (get_instruction cp, evs) with
| (MK_CLOSURE loc, evs)
  -> (cp + 1, V(CLOSURE(loc, evs_to_env evs)) :: evs)

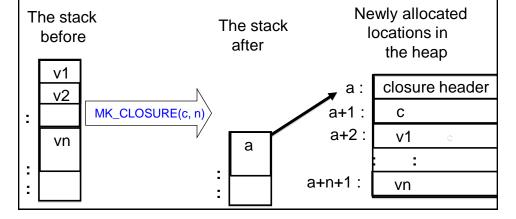
| (APPLY, V(CLOSURE ((_, Some i), env)) :: (V v) :: evs)
  -> (i, (V v) :: (EV env) :: (RA (cp + 1)) :: evs)

| (RETURN, (V v) :: _ :: (RA i) :: evs)
  -> (i, (V v) :: evs)
```

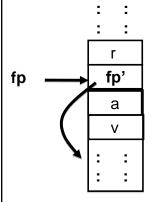
MK_CLOSURE(c, n)

c = code location of start of instructions for closure, n = number of free variables in the body of closure.

Put values associated with <u>free variables</u> on stack, then construct the closure on the heap



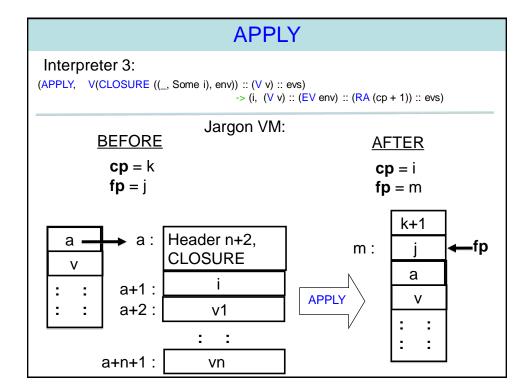
A stack frame

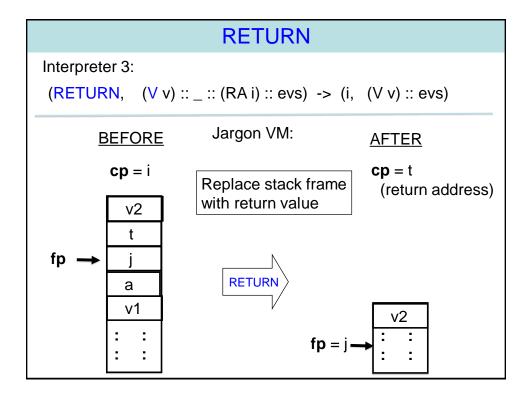


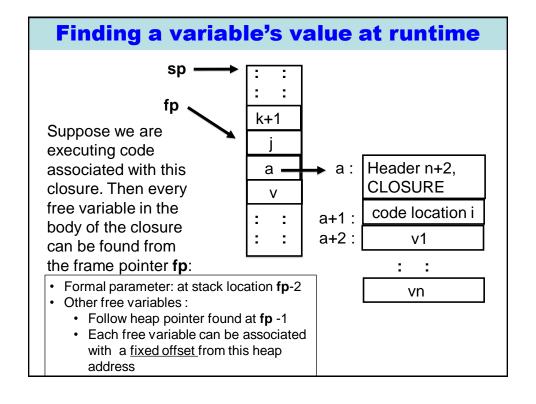
Return address
Saved frame pointer
Pointer to closure
Argument value

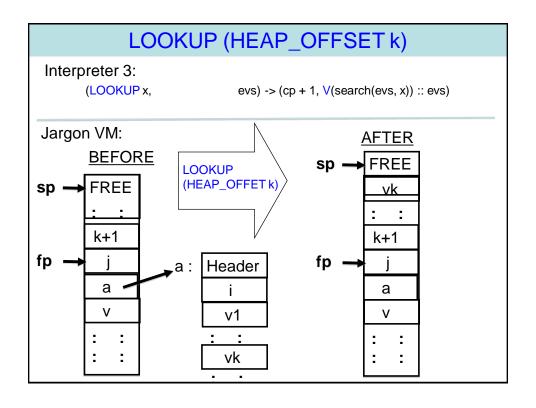
Stack frame. (Boundary May vary in the literature.)

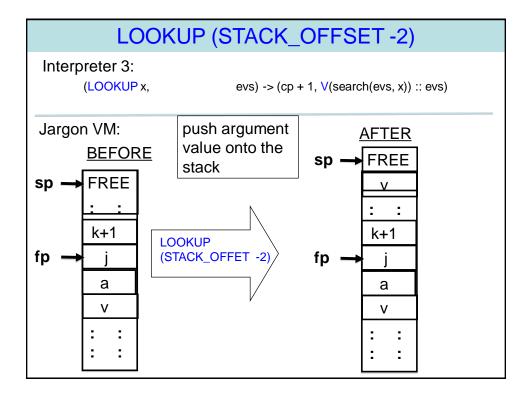
Currently executing code for the closure at heap address "a" after it was applied to argument v.









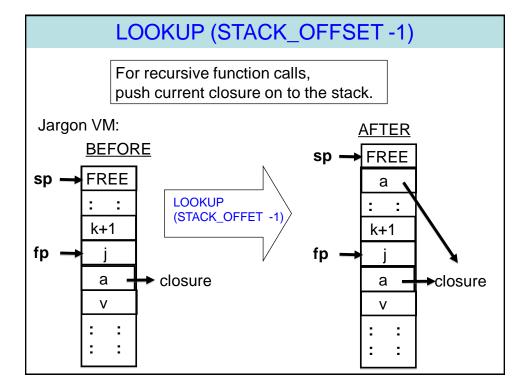


Oh, one problem let rec comp = function interpreter 3 | LetFun(f, (x, e1), e2) -> let (defs1, c1) = comp e1 in let (defs2, c2) = comp e2 in let def = [LABEL f; BIND x] @ c1 @ [SWAP; POP; RETURN] in (def @ defs1 @ defs2, [MK_CLOSURE((f, None)); BIND f] @ c2 @ [SWAP; POP]) Problem: Code c2 can be anything --- how are we going to find the closure for f when we need it? It has to be a fixed offset

from a frame pointer --- we no longer scan the stack for bindings!

```
let rec comp vmap = function
                                                      Solution in Jargon VM
| LetFun(f, (x, e1), e2) -> comp vmap (App(Lambda(f, e2), Lambda(x, e1)))
```

Similar trick for LetRecFun



Example: Compiled code for rev_pair.slang

```
let rev_pair (p : int * int) : int * int = (snd p, fst p)
in
    rev_pair (21, 17)
end
```

After the front-end, compile treats this as follows.

```
App(
Lambda(
"rev_pair",
App(Var "rev_pair", Pair (Integer 21, Integer 17))),
Lambda("p", Pair(Snd (Var "p"), Fst (Var "p"))))
```

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Example: Compiled code for rev_pair.slang

```
App(
  Lambda("rev_pair",
                                                                              "first lambda"
              App(Var "rev_pair", Pair (Integer 21, Integer 17))),
                                                                              'second lambda"
  Lambda("p", Pair(Snd (Var "p"), Fst (Var "p"))))
           MK_CLOSURE(L1, 0)
                                             -- Make closure for second lambda
 MK_CLOSURE(L0, 0)
                                             -- Make closure for first lambda
 APPLY
                                             -- do application
 HALT
                                             -- the end!
           PUSH STACK_INT 21
 L0:
                                             -- code for first lambda, push 21
 PUSH STACK_INT 17
                                             -- push 17
 MK_PAIR
                                             -- make the pair on the heap
 LOOKUP STACK_LOCATION -2
                                             -- push closure for second lambda on stack
 APPLY
                                             -- apply first lambda
 RETURN
                                             -- return from first lambda
          LOOKUP STACK_LOCATION -2
 L1:
                                             -- code for second lambda, push arg on stack
 SND
                                             -- extract second part of pair
 LOOKUP STACK_LOCATION -2
                                             -- push arg on stack again
 FST
                                             -- extract first part of pair
 MK_PAIR
                                             -- construct a new pair
 RETURN
                                             -- return from second lambda
                                                                                    108
```

Example: trace of rev_pair.slang execution

```
Installed Code =
                                       ====== state 1 ======
0: MK\_CLOSURE(L1 = 11, 0)
                                       cp = 0 \rightarrow MK CLOSURE(L1 = 11, 0)
1: MK_CLOSURE(L0 = 4, 0)
                                       fp = 0
2: APPLY
                                       Stack =
3: HALT
                                       1: STACK_RA 0
4: LABEL L0
                                       0: STACK FP 0
5: PUSH STACK_INT 21
6: PUSH STACK INT 17
                                      ======= state 2 =======
7: MK PAIR
                                       cp = 1 \rightarrow MK\_CLOSURE(L0 = 4, 0)
8: LOOKUP STACK_LOCATION-2
                                       fp = 0
9: APPLY
                                       Stack =
10: RETURN
                                       2: STACK HI 0
11: LABEL L1
                                       1: STACK RA 0
12: LOOKUP STACK_LOCATION-2
                                      0: STACK_FP 0
13: SND
14: LOOKUP STACK_LOCATION-2
                                       Heap =
15: FST
                                       0 -> HEAP_HEADER(2, HT_CLOSURE)
16: MK_PAIR
                                       1 -> HEAP CI 11
17: RETURN
```

Example: trace of rev_pair.slang execution

```
======= state 15 =======
                                                ======= state 19 =======
cp = 16 -> MK PAIR
                                                cp = 3 \rightarrow HALT
fp = 8
                                                fp = 0
Stack =
                                                Stack =
11: STACK_INT 21
                                                2: STACK HI 7
10: STACK INT 17
                                                1: STACK_RA 0
9: STACK_RA 10
                                                0: STACK_FP 0
8: STACK_FP 4
7: STACK_HI 0
                                                Heap =
6: STACK HI 4
                                                0 -> HEAP_HEADER(2, HT_CLOSURE)
5: STACK_RA 3
                                                1 -> HEAP_CI 11
4: STACK FP 0
                                                2 -> HEAP_HEADER(2, HT_CLOSURE)
3: STACK_HI 2
                                                3 -> HEAP_CI 4
2: STACK_HI 0
                                                4 -> HEAP_HEADER(3, HT_PAIR)
1: STACK_RA 0
                                               5 -> HEAP_INT 21
0: STACK_FP 0
                                               6 -> HEAP_INT 17
                                                7 -> HEAP_HEADER(3, HT_PAIR)
Heap =
                                                8 -> HEAP_INT 17
0 -> HEAP_HEADER(2, HT_CLOSURE)
                                                9 -> HEAP_INT 21
1 -> HEAP_CI 11
2 -> HEAP_HEADER(2, HT_CLOSURE)
3 -> HEAP CI 4
                                                Jargon VM:
4 -> HEAP_HEADER(3, HT_PAIR)
                                                output> (17, 21)
5 -> HEAP_INT 21
6 -> HEAP_INT 17
```

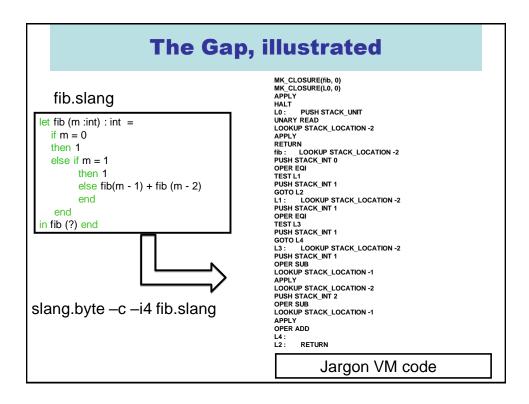
Example: closure_add.slang

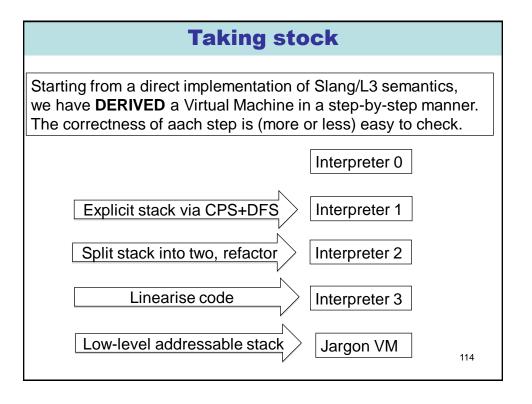
After the front-end, this becomes represented as follows.

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Can we make sense of this?

```
MK_CLOSURE(L3, 0)
                                      L2:
                                              PUSH STACK INT 3
MK_CLOSURE(L0, 0)
                                      LOOKUP STACK_LOCATION -2
APPLY
                                      APPLY
HALT
                                      PUSH STACK_INT 10
L0:
        PUSH STACK_INT 21
                                      LOOKUP HEAP LOCATION 1
LOOKUP STACK_LOCATION -2
                                      APPLY
APPLY
                                      OPER ADD
LOOKUP STACK_LOCATION -2
                                      RETURN
MK_CLOSURE(L1, 1)
                                              LOOKUP STACK_LOCATION -2
                                      L3:
APPLY
                                      MK CLOSURE(L5, 1)
RETURN
                                      MK_CLOSURE(L4, 0)
L1:
        PUSH STACK INT 17
                                      APPLY
LOOKUP HEAP_LOCATION 1
                                      RETURN
                                              LOOKUP STACK_LOCATION -2
                                      L4:
LOOKUP STACK_LOCATION -2
                                      RETURN
MK_CLOSURE(L2, 1)
                                      L5:
                                              LOOKUP HEAP LOCATION 1
APPLY
                                      LOOKUP STACK_LOCATION -2
RFTURN
                                      OPER ADD
                                      RETURN
                                                                     112
```





Remarks

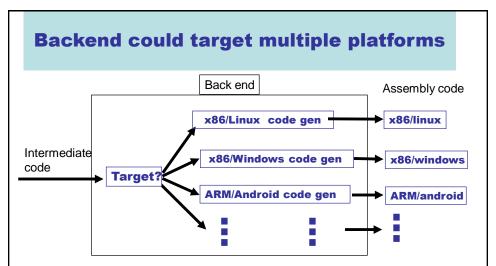
- 1. The semantic GAP between a Slang/L3 program and a low-level translation (say x86/Unix) has been significantly reduced.
- 2. Implementing the Jargon VM at a lower-level of abstraction (in C?, JVM bytecodes? X86/Unix? ...) looks like a <u>relatively</u> easy programming problem.
- However, using a lower-level implementation (say x86, exploiting fast registers) to generate very efficient code is not so easy. See Part II Optimising Compilers.

Verification of compilers is an active area of research. See CompCert, CakeML, and DeepSpec.

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We could implement a Jargon byte code interpreter ...

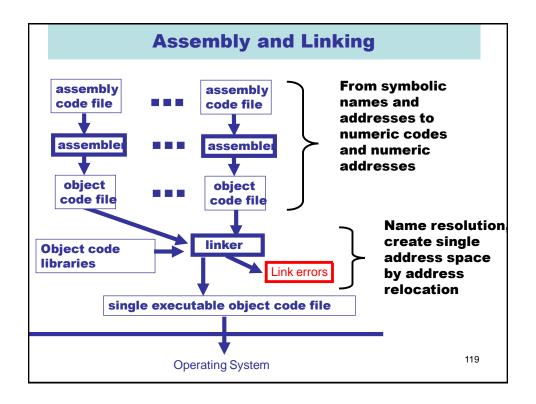
```
void vsm_execute_instruction(vsm_state *state, bytecode instruction)
opcode code = instruction.code;
argument arg1 = instruction.arg1;
switch (code) {
    case PUSH: { state->stack[state->sp++] = arg1; state->pc++; break; }
    case POP: { state->sp--; state->pc++; break; }
    case GOTO: { state->pc = arg1; break; }
    case STACK_LOOKUP: {
state->stack[state->sp++] =
        state->stack[state->fp + arg1];
                                                   Generate compact byte code for
state->pc++; break; }
                                                   each Jargon instruction.
                                                · Compiler writes byte codes to a file.
                                                • Implement an interpreter in C or C++
                                                   for these byte codes.
                                                   Execution is much faster than our
                                                   jargon.ml implementation.
                                                   Or, we could generate assembly
                                                   code from Jargon instructions ....
```



One of the great benefits of Virtual Machines is their portability. However, for more efficient code we may want to compile to assembler. Lost portability can be regained through the extra effort of implementing code generation for every desired target platform.

Lectures 7 --- 12 Assorted Topics

- 1. Separate compilation, linking
- 2. Interface with OS
- 3. Stacks vs registers
- 4. Calling conventions
- 5. Generating assembler code
- 6. Simple optimisations
- 7. The runtime system (automatic memory management, ...)
- 8. Static links (for languages without nested functions/procedures)
- 9. Implementing OOP with inheritance
- 10.Implementing exceptions
- 11. Compiling a compiler, "boot strapping"



The gcc manual (810 pages) https://gcc.gnu.org/onlinedocs/gcc-5.3.0/gcc.pdf

Chapter 9: Binary Compatibility

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9 Binary Compatibility

Binary compatibility encompasses several related concepts:

application binary interface (ABI)

The set of runtime conventions followed by all of the tools that deal with binary representations of a program, including compilers, assemblers, linkers, and language runtime support. Some ABIs are formal with a written specification, possibly designed by multiple interested parties. Others are simply the way things are actually done by a particular set of tools.

Applications Binary Interface (ABI)

We will use x86/Unix as our running example. Specifies many things, including the following.

- C calling conventions used for systems calls or calls to compiled C code.
 - Register usage and stack frame layout
 - How parameters are passed, results returned
 - Caller/callee responsibilities for placement and cleanup
- Byte-level layout and semantics of object files.
 - Executable and Linkable Format (ELF).
 Formerly known as Extensible Linking Format.
- Linking, loading, and name mangling

Note: the conventions are required for portable interaction with compiled C. Your compiled language does not have to follow the same conventions!

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Object files

Must contain at least

- · Program instructions
- · Symbols being exported
- · Symbols being imported
- Constants used in the program (such as strings)

Executable and Linkable Format (ELF) is a common format for both linker input and output.

ELF details (1)

Header information; positions and sizes of sections

- .text segment (code segment): binary data
- .data segment: binary data
- .rela.text code segment relocation table: list of (offset,symbol) pairs giving:
- (i) offset within .text to be relocated; and (iii) by which symbol
- .rela.data data segment relocation table: list of (offset,symbol) pairs giving:
- (i) offset within .data to be relocated; and (iii) by which symbol

. . .

ELF details (2)

. . .

.symtab symbol table:

List of external symbols (as triples) used by the module.

Each is (attribute, offset, symname) with attribute:

- 1. undef: externally defined, offset is ignored;
- 2. defined in code segment (with offset of definition);
- 3. defined in data segment (with offset of definition).

Symbol names are given as offsets within .strtab to keep table entries of the same size.

.strtab string table:

the string form of all external names used in the module

The (Static) Linker

What does a linker do?

- takes some object files as input, notes all undefined symbols.
- recursively searches libraries adding ELF files which define such symbols until all names defined ("library search").
- whinges if any symbol is undefined or multiply defined.

Then what?

- concatenates all code segments (forming the output code segment).
- · concatenates all data segments.
- performs relocations (updates code/data segments at specified offsets.

Dynamic vs. Static linking

Static linking (compile time)

Problem: a simple "hello world" program may give a 10MB executable if it refers to a big graphics or other library.

Dynamic linking (run time)

For shared libraries, the object files contain stubs, not code, and the operating system loads and links the code on demand.

Pros and Cons of dynamic linking:

- (+) Executables are smaller
- (+) Bug fixes to libraries don't require re-linking.
- (-) Non-compatible changes to a library can wreck previously working programs ("dependency hell").

A "runtime system"

A library implementing functionality needed to run compiled code on a given operating system. Normally tailored to the language being compiled.

- Implements interface between OS and language.
- May implement memory management.
- May implement "foreign function" interface (say we want to call compiled C code from Slang code, or vice versa).
- May include efficient implementations of primitive operations defined in the compiled language.
- For some languages, the runtime system may perform runtime type checking, method lookup, security checks, and so on.

• ...

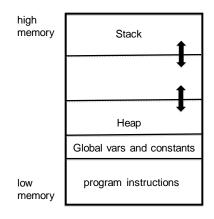
Targeting a VM Generated code Virtual Machine Implementation Includes runtime system Virtual Machine Linker Executable

In either case, implementers of the compiler and the runtime system must agree on many low-level details of memory layout and data representation.

Typical (Low-Level) Memory Layout (UNIX)

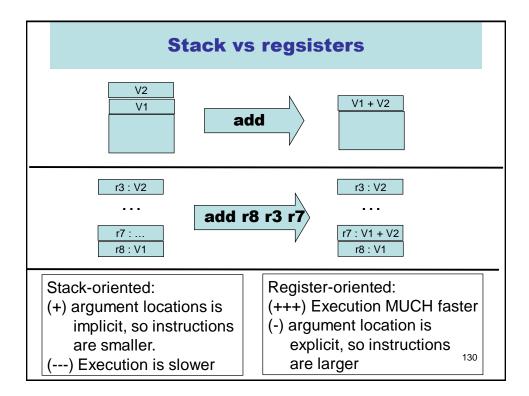
Rough schematic of traditional layout in (virtual) memory.

Dealing with Virtual Machines allows us to ignore some of the low-level details....



The heap is used for dynamically allocating memory. Typically either for very large objects or for those objects that are returned by functions/procedures and must outlive the associated activation record.

In languages like Java and ML, the heap is managed automatically ("garbage collection")



Main dilemma: registers are fast, but are fixed in number. And that number is rather small.

- Manipulating the stack involves RAM access, which can be orders of magnitude slower than register access (the "von Neumann Bottleneck")
- Fast registers are (today) a scarce resource, shared by many code fragments
- How can registers be used most effectively?
 - Requires a careful examination of a program's structure
 - Analysis phase: building data structures (typically directed graphs) that capture definition/use relationships
 - Transformation phase: using this information to rewrite code, attempting to most efficiently utilise registers
 - · Problem is NP-complete
 - One of the central topics of Part II Optimising Compilers.
- Here we focus <u>only</u> on general issues: <u>calling conventions</u> and <u>register spilling</u>

Caller/callee conventions

- Caller and callee code may use overlapping sets of registers
- · An agreement is needed concerning use of registers
 - Are some arguments passed in specific registers?
 - Is the result returned in a specific register?
 - If the caller and callee are both using a set of registers for "scratch space" then caller or callee must save and restore these registers so that the caller's registers are not obliterated by the callee.
- Standard calling conventions identify specific subsets of registers as "caller saved" or "callee saved"
 - Caller saved: if caller cares about the value in a register, then must save it before making any call
 - Callee saved: The caller can be assured that the callee will leave the register intact (perhaps by saving and restoring it)

Another C example. X86, 64 bit, with gcc

```
_caller:
pushq
        %rbp
                    # save frame pointer
        %rsp, %rbp # set new frame pointer
movq
subq
        $16, %rsp # make room on stack
        $7, (%rsp) # put 7th arg on stack
movl
        $1, %edi # put 1st arg on in edi
movl
        $2, %esi # put 2nd arg on in esi
movl
        $3, %edx # put 3rd arg on in edx
movl
movl
        $4, %ecx # put 4th arg on in ecx
movl
        $5, %r8d # put 5th arg on in r8d
        $6, %r9d # put 6th arg on in r9d
movl
calla
        callee
                   #will put resut in eax
addl$5, %eax # add 5
addq
        $16, %rsp # adjust stack
        %rbp
                  # restore frame pointer
popq
ret
            # pop return address, go there
```

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Regsiter spilling

- · What happens when all registers are in use?
- · Could use the stack for scratch space ...
- ... or (1) move some register values to the stack, (2) use the registers for computation, (3) restore the registers to their original value
- This is called <u>register spilling</u>

A Crash Course in x86 assembler

- · A CISC architecture
- · There are 16, 32 and 64 bit versions
- 32 bit version:
 - General purpose registers: EAX EBX ECX EDX
 - · Special purpose registers : ESI EDI EBP EIP ESP
 - · EBP: normally used as the frame pointer
 - · ESP: normally used as the stack pointer
 - · EDI: often used to pass (first) argument
 - · EIP : the code pointer
 - · Segment and flag registers that we will ignore ...
- 64 bit version:
 - Rename 32-bit registers with "R" (RAX, RBX, RCX, ...)
 - More general registers: R8 R9 R10 R11 R12 R13 R14 R15

Register names can indicate "width" of a value. rax: 64 bit version

eax: 32 bit version (or lower 32 bits of rax)ax: 16 bit version (or lower 16 bits of eax)

al: lower 8 bits of ax **ah**: upper 8 bits of ax

See https://en.wikibooks.org/wiki/X86_Assembly

The syntax of x86 assembler comes in several flavours. Here are two examples of "put integer 4 into register eax":

```
movl $4, %eax // GAS (aka AT&T) notation mov eax, 4 // Intel notation
```

I will (mostly) use the GAS syntax, where a suffix is used to indicate width of arguments:

- b (byte) = 8 bits
- w (word) = 16 bits
- I (long) = 32 bits
- q (quad) = 64 bits

For example, we have movb, movw movl, and movq.

Examples (in GAS notation)

```
movl $4, %eax
                     # put 32 bit integer 4 in register eax
movw $4, %eax
                    # put 16 bit integer 4 in lower 16 bits of eax
movb $4, %eax
                     # put 4 bit integer 4 in lowest 4 bits of eax
movl
       %esp, %ebp # put the contents of esp into ebp
movl
       (%esp), %ebp # interpret contents of esp as a memory
                     # address. Copy the value at that address
                     # into register ebp
       %esp, (%ebp) # interpret contents of ebp as a memory
movl
                     # address. Copy the value in esp to
                     # that address.
movl %esp, 4(%ebp)# interpret contents of ebp as a memory
                     # address. Add 4 to that address. Copy
                     # the value in esp to this new address.
```

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A few more examples

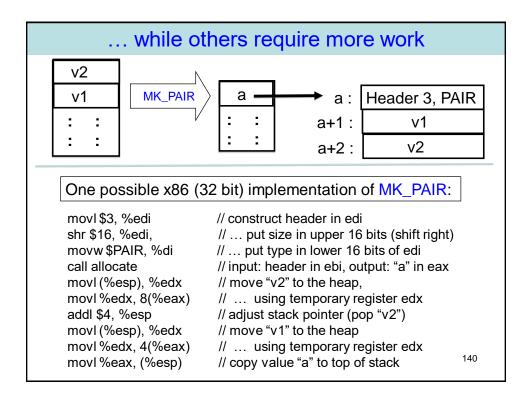
```
call label # push return address on stack and jump to label
ret # pop return address off stack and jump there
# NOTE: managing other bits of the stack frame
# such as stack and frame pointer must be done
# explicitly
subl $4, %esp # subtract 4 from esp. That is, adjust the
# stack pointer to make room for one 32-bit
# (4 byte) value. (stack grows downward!)
```

Assume that we have implemented a procedure in C called allocate that will manage heap memory. We will compile and link this in with code generated by the slang compiler. At the x86 level, allocate will expect a header in **edi** and return a heap pointer in **eax**.

Some Jargon VM instructions are "easy" to translate

Remember: X86 is CISC, so RISC architectures may require more instructions.

```
GOTO loc
            imp loc
POP
            addl $4, %esp
                                    // move stack pointer 1 word = 4 bytes
PUSH v
           subl $4, %esp
                                   // make room on top of stack
            movl $i, (%esp)
                                  // where i is an integer representing v
FST
           movl (%esp), %edx
                                  //store "a" into edx
           movl 4(%edx), %edx
                                 // load v1, 4 bytes, 1 word, after header
                                 // replace "a" with "v1" at top of stack
           movl %edx, (%esp)
SND
           movl (%esp), %edx
                                  //store "a" into edx
           movl 8(%edx), %edx
                                 // vload v2, 8 bytes, 2 words, after header
           movl %edx, (%esp)
                                 // replace "a" with "v2" at top of stack
                           a :
                                 lheader
                                                                v1
              а
 sp
                                                  FST
                         a+1:
                                     ν1
                                     v2
                          a+2:
```



call function computed at runtime?

For things you don't understand, just experiment! OK, you need to pull an address out of a closure and call it. Hmm, how does something similar get compiled from C?

int func (int (*f)(int)) { return (*f)(17); } /* pass a function pointer and apply it /*

```
func:
pushq %rbp
                      # save frame pointer
                                                                X86.
       %rsp, %rbp
                      # set frame pointer to stack pointer
movq
                                                                64 bit
       $16, %rsp
                      # make some room on stack
subq
       $17, %eax
                      # put 17 in argument register eax
movl
                                                                without
movq %rdi, -8(%rbp) # rdi contains the argument f
       %eax, %edi
                      # put 17 in register edi, so f will get it
                                                                 -02
movl
       *-8(%rbp)
                     # WOW, a computed address for call!
callq
       $16, %rsp
addq
                      # restore stack pointer
       %rbp
popq
                      # restore old frame pointer
                       # restore stack
                                                                  141
ret
```

What about arithmetic?

Houston, we have a problem....

- It may not be obvious now, but if we want to have automated memory management we need to be able to distinguish between values (say integers) and pointers at runtime.
- Have you ever noticed that integers in SML or Ocaml are either 31 (or 63) bits rather than the native 32 (or 64) bits?
 - That is because these compilers use a the least significant bit to distinguish integers (bit = 1) from pointers (bit = 0).
 - OK, this works. But it may complicate every arithmetic operation!
 - This is another exercise left for you to ponder

- - -

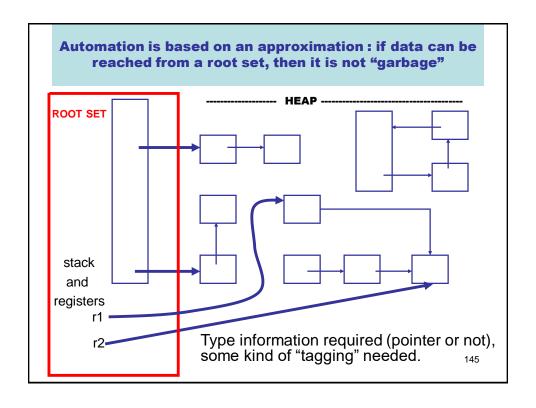
New topic: Memory Management

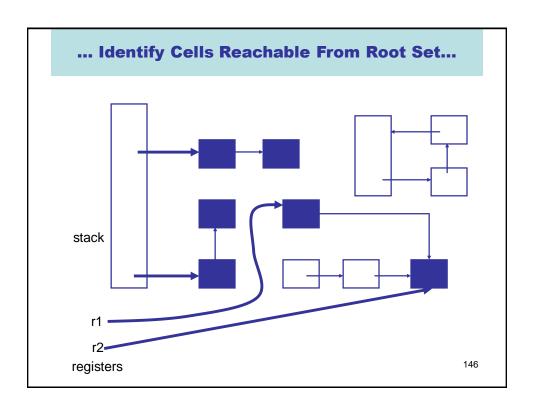
- Many programming languages allow programmers to (implicitly) allocate new storage dynamically, with no need to worry about reclaiming space no longer used.
 - New records, arrays, tuples, objects, closures, etc.
 - Java, SML, OCaml, Python, JavaScript, Python, Ruby, Go, Swift, SmallTalk, ...
- Memory could easily be exhausted without some method of reclaiming and recycling the storage that will no longer be used.
 - Often called "garbage collection"
 - Is really "automated memory management" since it deals with allocation, de-allocation, compaction, and memory-related interactions with the OS.

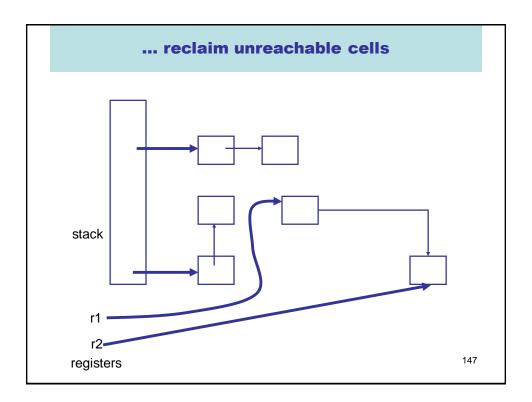
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Explicit (manual) memory management

- User library manages memory; programmer decides when and where to allocate and deallocate
 - void* malloc(long n)
 - void free(void *addr)
 - Library calls OS for more pages when necessary
 - Advantage: Gives programmer a lot of control.
 - Disadvantage: people too clever and make mistakes. Getting it right can be costly. And don't we want to automate-away tedium?
 - Advantage: With these procedures we can implement memory management for "higher level" languages;-)







But How? Two basic techniques, and many variations

- Reference counting: Keep a reference count with each object that represents the number of pointers to it. Is garbage when count is 0.
- **Tracing**: find all objects reachable from root set. Basically transitive close of pointer graph.

For a very interesting (non-examinable) treatment of this subject see

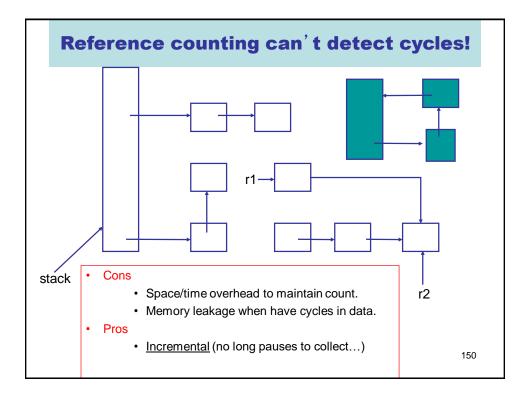
A Unified Theory of Garbage Collection.

David F. Bacon, Perry Cheng, V.T. Rajan. OOPSLA 2004.

In that paper reference counting and tracing are presented as "dual" approaches, and other techniques are hybrids of the two.

Reference Counting, basic idea:

- Keep track of the number of pointers to each object (the reference count).
- When Object is created, set count to 1.
- Every time a new pointer to the object is created, increment the count.
- Every time an existing pointer to an object is destroyed, decrement the count
- When the reference count goes to 0, the object is unreachable garbage



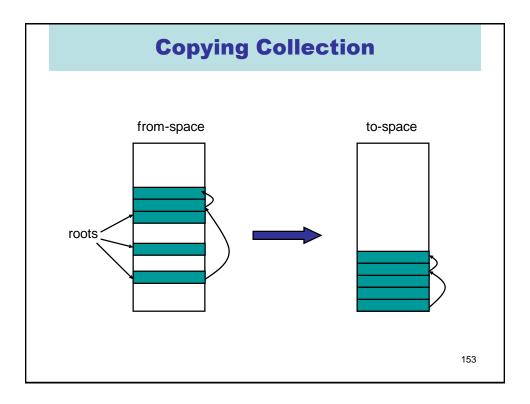
Mark and Sweep

- A two-phase algorithm
 - Mark phase: <u>Depth first</u> traversal of object graph from the roots to <u>mark</u> live data
 - Sweep phase: iterate over entire heap, adding the unmarked data back onto the free list

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Copying Collection

- · Basic idea: use 2 heaps
 - One used by program
 - The other unused until GC time
- GC:
 - Start at the roots & traverse the reachable data
 - Copy reachable data from the active heap (fromspace) to the other heap (to-space)
 - Dead objects are left behind in from space
 - Heaps switch roles



Copying GC

- Pros
 - Simple & collects cycles
 - Run-time proportional to # live objects
 - Automatic compaction eliminates fragmentation
- Cons
 - Twice as much memory used as program requires
 - Usually, we anticipate live data will only be a small fragment of store
 - Allocate until 70% full
 - From-space = 70% heap; to-space = 30%
 - Long GC pauses = bad for interactive, real-time apps

OBSERVATION: for a copying garbage collector

- 80% to 98% new objects die very quickly.
- An object that has survived several collections has a bigger chance to become a long-lived one.
- It's a inefficient that long-lived objects be copied over and over.

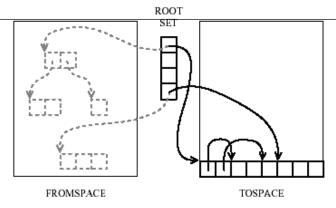


Diagram from Andrew Appel's Modern Compiler Implementation

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IDEA: Generational garbage collection

Segregate objects into multiple areas by age, and collect areas containing older objects less often than the younger ones.

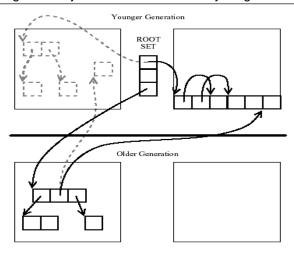


Diagram from Andrew Appel's Modern Compiler Implementation

Other issues...

- When do we promote objects from young generation to old generation
 - Usually after an object survives a collection, it will be promoted
- Need to keep track of older objects pointing to newer ones!
- How big should the generations be?
 - When do we collect the old generation?
 - After several minor collections, we do a major collection
- Sometimes different GC algorithms are used for the new and older generations.
 - Why? Because the have different characteristics
 - Copying collection for the new
 - Less than 10% of the new data is usually live
 - Copying collection cost is proportional to the live data
 - · Mark-sweep for the old

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New topic: Simple optimisations. Inline expansion

fun
$$f(x) = x + 1$$

fun $g(x) = x - 1$
...

fun $h(x) = f(x) + g(x)$

I inline f and g

fun f(x) = x + 1fun g(x) = x - 1... fun h(x) = (x+1) + (x-1)

- (+) Avoid building activation records at runtime
- (+) May allow further optimisations
- (-) May lead to "code bloat" (apply only to functions with "small" bodies?)

Question: if we inline all occurrences of a function, can we delete its definition from the code?
What if it is needed at link time?

Be careful with variable scope

Inline g in h

```
let val x = 1

fun g(y) = x + y

fun h(x) = g(x) + 1

in

h(17)

end
```

NO

```
let val x = 1

fun g(y) = x + y

fun h(x) = x + y + 1

in

h(17)

end
```

YES

What kind of care might be needed will depend on the representation level of the Intermediate code involved.

```
let val x = 1

fun g(y) = x + y

fun h(\mathbf{z}) = x + \mathbf{z} + 1

in

h(17)

end
```

(b) Constant propagation, constant folding

```
let x = 2
let y = x - 1
let z = y * 17
let x = 2
let y = 2 - 1
let z = y * 17
let x = 2
```

let z = y * 17

let x = 2

let y = 1

let z = 1 * 17

let y = 1

let x = 2 let y = 1 let z = 17 Propagate constants and evaluate simple expressions at compile-time

Note: opportunities are often exposed by inline expansion!

David Gries:
"Never put off till
run-time what you can do
at compile-time."

But be careful

How about this?

Replace

x * 0

with

0

OOPS, not if x has type

NAN*0 = NAN,

(c) peephole optimisation

Peephole Optimization

W. M. McKeeman Stanford University, Stanford, California Communications of the ACM, July 1965

Eliminate!

Example 1. Source code:

$$X := Y;$$

$$Z := X + Z$$

Compiled code:

LDA Y load the accumulator from Y

STA X store the accumulator in X

LDA X load the accumulator from X

ADD Z add the contents of Z

STA Z store the accumulator in Z

Results for syntax-directed code generation.

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peephole optimisation



... code sequence ...

Sweep a window over the code sequence looking for instances of simple code patterns that can be rewritten to better code ... (might be combined with constant folding, etc, and employ multiple passes)

Examples

- -- eliminate useless combinations (push 0; pop)
- -- introduce machine-specific instructions
- -- improve control flow. For example: rewrite

"GOTO L1 ... L1: GOTO L2"

to

"GOTO L2 ... L1 : GOTO L2")

```
gcc example.
    -O<m> turns on optimisation to level m
g.c
int h(int n) { return (0 < n) ? n : 101; }
                                               g.s (fragment)
int g(int n) { return 12 * h(n + 17); }
                               _g:
                               .cfi_startproc
    gcc -O2 -S -c g.c
                               pushq %rbp
                                     %rsp, %rbp
                               movq
                                     $17, %edi
                               addl
                               imull
                                     $12, %edi, %ecx
                                     %edi, %edi
                               testl
Wait. What happened to
                                     $1212, %eax
                               movl
the call to h???
                              cmovgl %ecx, %eax
                               popq
                                     %rbp
                               ret
                               .cfi_endproc
     GNU AS (GAS) Syntax
           x86, 64 bit
```

gcc example (-O<m> turns on optimisation)

```
g.c |
int h(int n) { return (0 < n) ? n : 101 ; }
int g(int n) { return 12 * h(n + 17); }
```

The compiler must have done something similar to this:

```
int g(int n) { return 12 * h(n + 17); }

int g(int n) { int t := n+ 17; return 12 * h(t); }

int g(int n) { int t := n+ 17; return 12 *((0 < t) ? t : 101 ); }

int g(int n) { int t := n+ 17; return (0 < t) ? 12 * t : 1212 ; }

...</pre>
```

New topic: static links on the call stack.

- Many textbooks on compilers treat only languages with first-order functions --- that is, functions cannot be passes as an argument or returned as a result. In this case, we can avoid allocating environments on the heap since all values associated with free variables will be somewhere on the stack!
- But how do we find these values? We optimise stack search by following a chain of **static links**. Static links are added to every stack frame and the point to the stack frame of the last invocation of the defining function.
- One other thing: most languages take multiple arguments for a function/procedure call.

Terminology: Caller and Callee

fun f (x, y) = e1
...

fun g(w, v) =
$$w + f(v, v)$$

For this invocation of the function f, we say that g is the <u>caller</u> while f is the callee

Recursive functions can play both roles at the same time ...

```
Pseudo-code

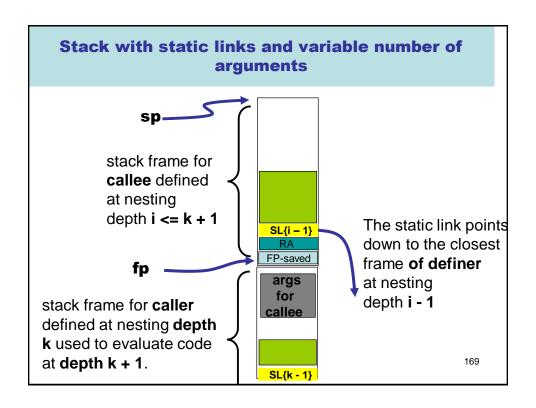
fun b(z) = e

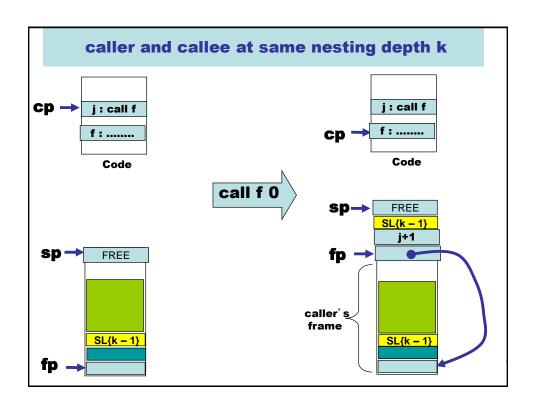
fun g(x1) = fun h(x2) = fun h(x2) = fun f(x3) = e3(x1, x2, x3, b, g h, f) in e2(x1, x2, b, g, h, f) end in e1(x1, b, g, h) end

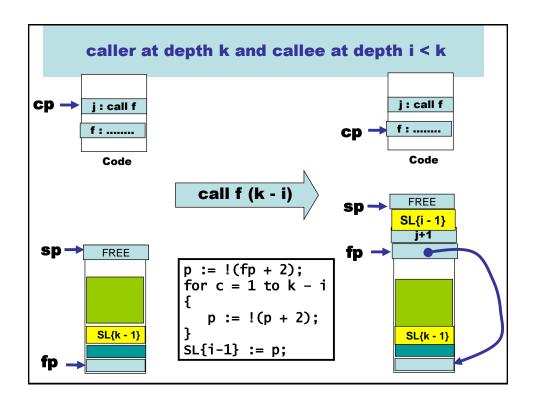
...

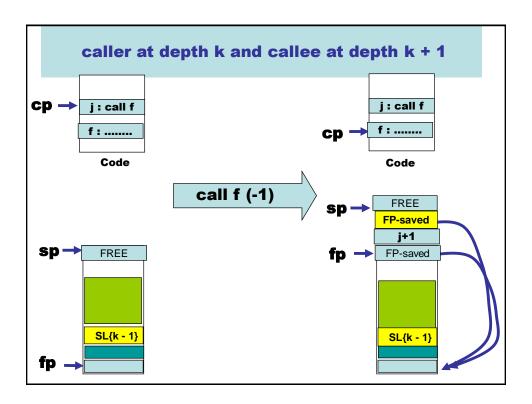
b(g(17))
...
```

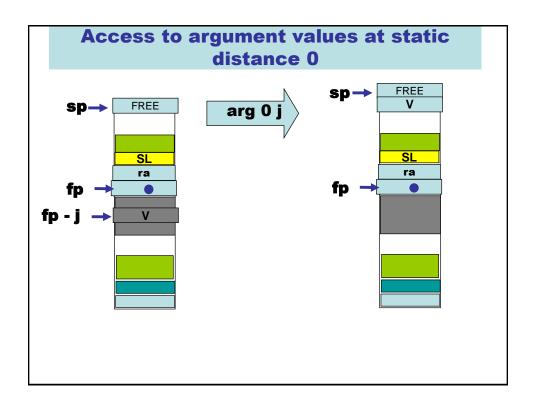
```
Nesting depth
code in big box is at nesting depth k
fun b(z) = e nesting depth k + 1
fun g(x1) =
  fun h(x2) =
    fun f(x3) = e3(x1, x2, x3, b, g h, f)
                                            nesting depth k + 3
       e2(x1, x2, b, g, h, f)
     end
                                        nesting depth k + 2
     e1(x1, b, g, h)
  end
                                    nesting depth k + 1
b(g(17))
 Function g is the definer of h. Functions g and b must
 share a definer defined at depth k-1
```

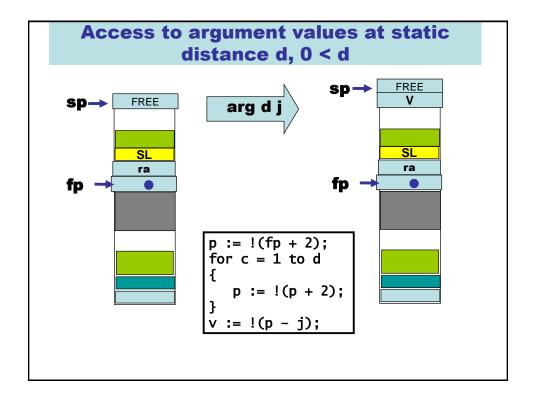












New Topic: OOP Objects (single inheritance)

```
let start := 10
   class Vehicle extends Object {
      var position := start
      method move(int x) = {position := position + x}
   class Car extends Vehicle {
      var passengers := 0
      method await(v : Vehicle) =
         if (v.position < position)</pre>
         then v.move(position - v.position)
         else self.move(10)
   class Truck extends Vehicle {
      method move(int x) = \triangleleft
                                                           method override
         if x \le 55 then position := position +x
   var t := new Truck
   var c := new Car
   var v : Vehicle :=◀
                                                subtyping allows a
   c.passengers := 2;
                                                Truck or Car to be viewed and
   c.move(60);
   v.move(70);
                                                used as a Vehicle
   c.await(t
end
```

Object Implementation?

- how do we access object fields?
 - both inherited fields and fields for the current object?
- how do we access method code?
 - if the current class does not define a particular method, where do we go to get the inherited method code?
 - how do we handle method override?
- How do we implement subtyping ("object polymorphism")?
 - If B is derived from A, then need to be able to treat a pointer to a B-object as if it were an Aobject.

Another 00 Feature

- Protection mechanisms
 - to encapsulate local state within an object,
 Java has "private" "protected" and "public"
 qualifiers
 - private methods/fields can't be called/used outside of the class in which they are defined
 - This is really a scope/visibility issue! Frontend during semantic analysis (type checking and so on), the compiler maintains this information in the symbol table for each class and enforces visibility rules.

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Object representation

```
class A {
   public:
    int a1, a2;
    virtial void m1(int i) {
       a1 = i;
   }
    virtual void m2(int i) {
       a2 = a1 + i;
   }
}
An A object

a1

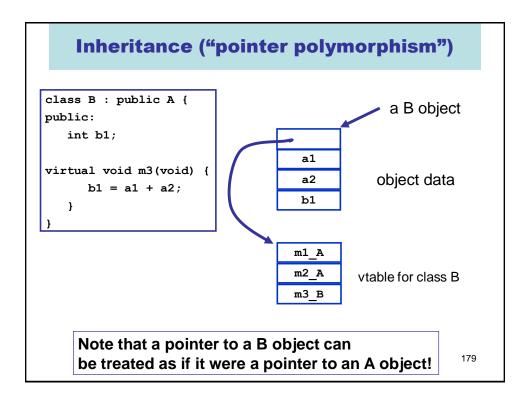
object data

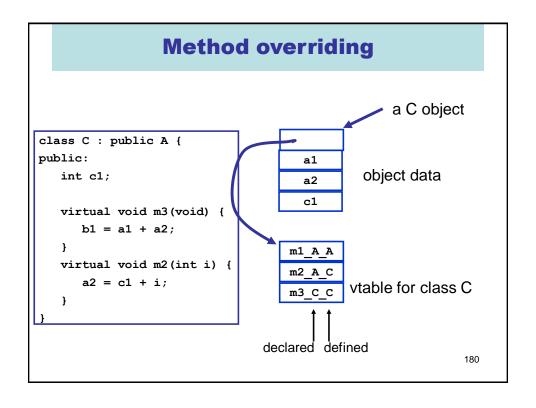
wirtial void m2(int i) {
       a2 = a1 + i;
   }

wtable for class A

m2_A
```

NB: a compiler typically generates methods with an extra argument representing the object (self) and used to access object data.





Static vs. Dynamic

 which method to invoke on overloaded polymorphic types?

```
class C *c = ...;

class A *a = c;

a->m2(3);

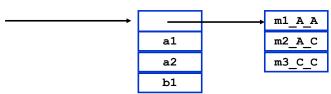
m2_A_A(a, 3); static

m2_A_C(a, 3); dynamic
```

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A pointer to a class C object can be treated as a pointer to a class A object



New Topic: Exceptions (informal description)

e handle f

If expression e evaluates "normally" to value v, then v is the result of the entire expression.

Otherwise, an exceptional value v' is "raised" in the evaluation of e, then result is (f v')

raise e

Evaluate expression e to value v, and then raise v as an exceptional value, which can only be "handled".

Implementation of exceptions may require a lot of language-specific consideration and care. Exceptions can interact in powerful and unexpected ways with other language features. Think of C++ and class destructors, for example.

Viewed from the call stack current frame frame handle for f handle frame frame ٧ Call stack just Push a special "raise v" is "Unwind" call stack. before evaluating frame for the encountered Depending on language, code for handle while evaluating this may involve some a function body "clean up" to free resources. e handle f associated with top-most frame

Possible pseudo-code implementation

e handle f

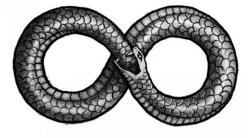
let fun _h27 () =
build special "handle frame"
save address of f in frame;
... code for e ...
return value of e
in _h27 () end

raise e

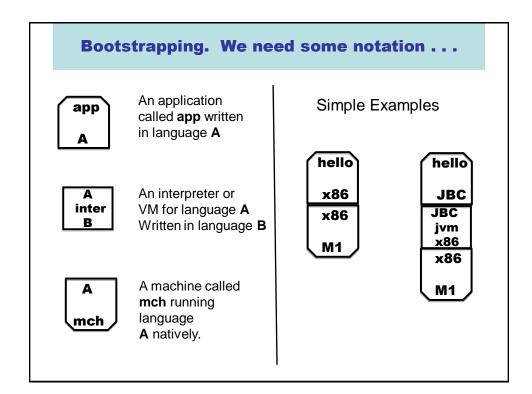
... code for e ...
save v, the value of e;
unwind stack until first
fp found pointing at a handle frame;
Replace handle frame with frame
for call to (extracted) f using
v as argument.

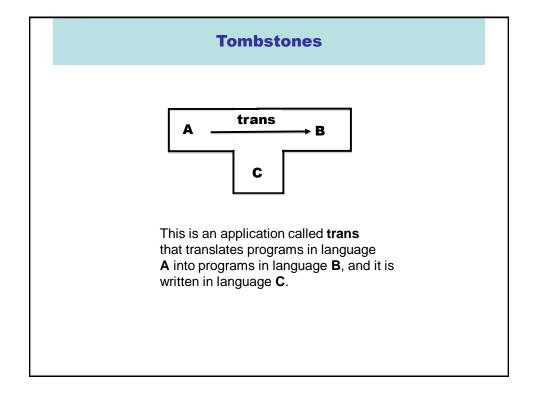
New topic: Bootstrapping a compiler

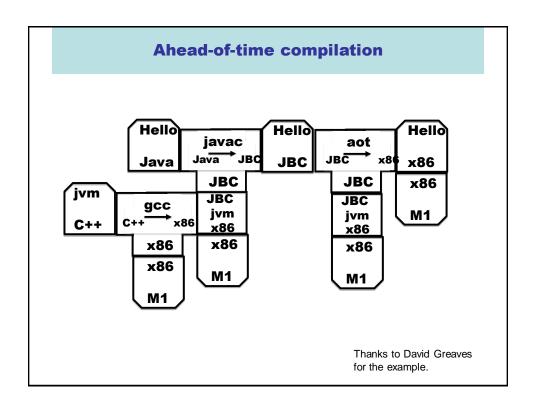
- Compilers compiling themselves!
- · Read Chapter 13 Of
 - Basics of Compiler Design
 - by Torben Mogensen
 http://www.diku.dk/hjemmesider/ansatte/torbenm/Basics/

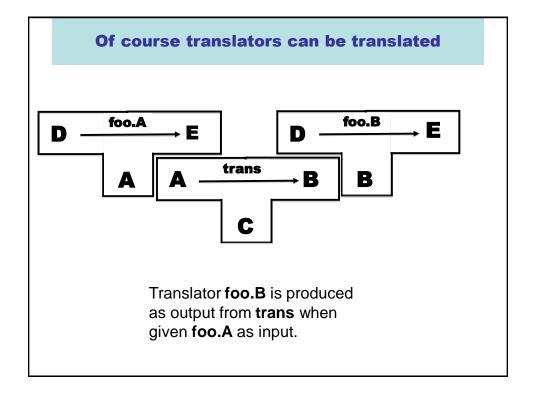


http://mythologian.net/ouroboros-symbol-of-infinity/

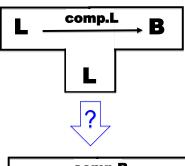




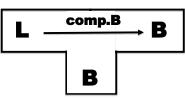




Our seemingly impossible task



We have just invented a really great new language L (in fact we claim that "L is far superior to C++"). To prove how great L is we write a compiler for L in L (of course!). This compiler produces machine code B for a widely used instruction set (say B = x86).



Furthermore, we want to compile our compiler so that it can run on a machine running **B**.

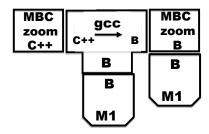
Our compiler is written in L!

How can we compiler our compiler?

There are many many ways we could go about this task. The following slides simply sketch out one plausible route to fame and fortune.

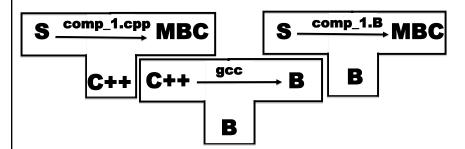
Step 1 Write a small interpreter (VM) for a small language of byte codes

MBC = My Byte Codes



The **zoom** machine!

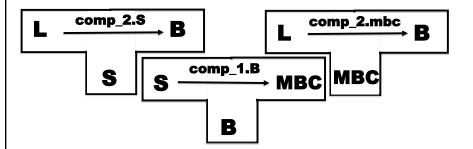
Step 2 Pick a small subset S of L and write a translator from S to MBC



Write **comp_1.cpp** by hand. (It sure would be nice if we could hide the fact that this is written is C++.)

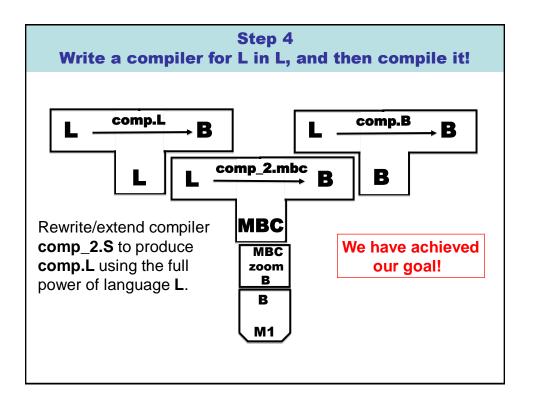
Compiler **comp_1.B** is produced as output from **gcc** when **comp_1.cpp** is given as input.

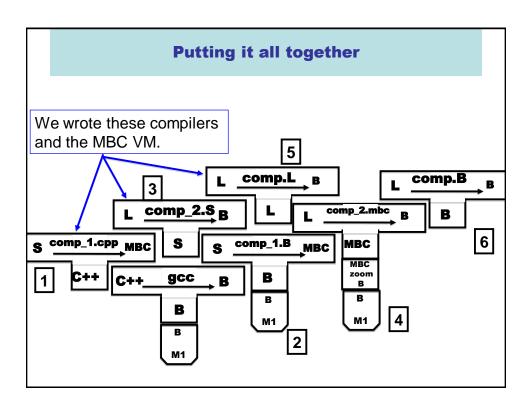
Step 3 Write a compiler for L in S

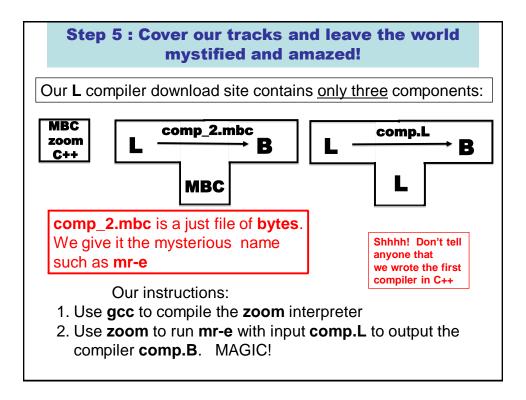


Write a compiler **comp_2.S** for the full language **L**, but written only in the sub-language **S**.

Compile comp_2.S using comp_1.B to produce comp_2.mbc







Another example (Mogensen, Page 285)

Solving a different problem.

You have:

- (1) An ML compiler on ARM. Who knows where it came from.
- (2) An ML compiler written in ML, generating x86 code.

You want:

An ML compiler generating x86 and running on an x86 platform.

