

## Artificial Intelligence I

### *Planning algorithms*

**Reading:** AIMA, chapter 11.

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## Problem solving is different to planning

In *search problems* we:

- *Represent states*: and a state representation contains *everything* that's relevant about the environment.
- *Represent actions*: by describing a new state obtained from a current state.
- *Represent goals*: all we know is how to test a state either to see if it's a goal, or using a heuristic.
- *A sequence of actions is a 'plan'*: but we only consider *sequences of consecutive actions*.

Search algorithms are good for solving problems that fit this framework. However for more complex problems they may fail completely...

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## Problem solving is different to planning

Representing a problem such as: '*go out and buy some pies*' is hopeless:

- There are *too many possible actions* at each step.
- A heuristic can only help you rank states. In particular it does not help you *ignore* useless actions.
- We are forced to start at the initial state, but you have to work out *how to get the pies*—that is, go to town and buy them, get online and find a web site that sells pies *etc—before you can start to do it*.

Knowledge representation and reasoning might not help either: although we end up with a sequence of actions—a plan—there is so much flexibility that complexity might well become an issue.

Our aim now is to look at how an agent might *construct a plan* enabling it to achieve a goal.

- We look at how we might update our concept of *knowledge representation and reasoning* to apply more specifically to planning tasks.
- We look in detail at the *partial-order planning algorithm*.

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## Planning algorithms work differently

*Difference 1:*

- Planning algorithms use a *special purpose language*—often based on FOL or a subset— to represent states, goals, and actions.
- States and goals are described by sentences, as might be expected, but...
- ...actions are described by stating their *preconditions* and their *effects*.

So if you know the goal includes (maybe among other things)

Have(pie)

and action Buy(*x*) has an effect Have(*x*) then you know that a plan *including*

Buy(pie)

might be reasonable.

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## Planning algorithms work differently

### *Difference 2:*

- Planners can add actions at *any relevant point at all between the start and the goal*, not just at the end of a sequence starting at the start state.
- This makes sense: I may determine that *Have(carKeys)* is a good state to be in without worrying about what happens before or after finding them.
- By making an important decision like requiring *Have(carKeys)* early on we may reduce branching and backtracking.
- State descriptions are not complete—*Have(carKeys)* describes a *class of states*—and this adds flexibility.

*So:* you have the potential to search both *forwards* and *backwards* within the same problem.

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## Planning algorithms work differently

### *Difference 3:*

It is assumed that most elements of the environment are *independent of most other elements*.

- A goal including several requirements can be attacked with a divide-and-conquer approach.
- Each individual requirement can be fulfilled using a subplan...
- ...and the subplans then combined.

This works provided there is not significant interaction between the subplans.

Remember: the *frame problem*.

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## Running example: gorilla-based mischief

We will use a simple example, based on one from Russell and Norvig.



The intrepid little scamps in the *Cambridge University Roof-Climbing Society* wish to attach an *inflatable gorilla* to the spire of a *Famous College*. To do this they need to leave home and obtain:

- *An inflatable gorilla*: these can be purchased from all good joke shops.
- *Some rope*: available from a hardware store.
- *A first-aid kit*: also available from a hardware store.

They need to return home after they've finished their shopping. How do they go about planning their *jolly escapade*?

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## The STRIPS language

STRIPS: "*Stanford Research Institute Problem Solver*" (1970).

*States*: are *conjunctions of ground literals*. They must not include *function symbols*.

$$\begin{aligned} & \text{At}(\text{home}) \wedge \neg\text{Have}(\text{gorilla}) \\ & \quad \wedge \neg\text{Have}(\text{rope}) \\ & \quad \wedge \neg\text{Have}(\text{kit}) \end{aligned}$$

*Goals*: are *conjunctions of literals* where variables are assumed *existentially quantified*.

$$\text{At}(x) \wedge \text{Sells}(x, \text{gorilla})$$

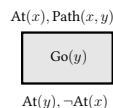
A planner finds a sequence of actions that when performed makes the goal true.

We are no longer employing a full theorem-prover.

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## The STRIPS language

STRIPS represents actions using *operators*. For example



Op(Action: Go( $y$ ), Pre:  $\text{At}(x) \wedge \text{Path}(x, y)$ , Effect:  $\text{At}(y) \wedge \neg\text{At}(x)$ )

All variables are implicitly universally quantified. An operator has:

- An *action description*: what the action does.
- A *precondition*: what must be true before the operator can be used. A *conjunction of positive literals*.
- An *effect*: what is true after the operator has been used. A *conjunction of literals*.

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## The space of plans

We now make a change in perspective—we search in *plan space*:

- Start with an *empty plan*.
- *Operate on it* to obtain new plans. Incomplete plans are called *partial plans*. *Refinement operators* add constraints to a partial plan. All other operators are called *modification operators*.
- Continue until we obtain a plan that solves the problem.

Operations on plans can be:

- *Adding a step*.
- *Instantiating a variable*.
- *Imposing an ordering* that places a step in front of another.
- and so on...

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## Representing a plan: partial order planners

When putting on your shoes and socks:

- It *does not matter* whether you deal with your left or right foot first.
- It *does matter* that you place a sock on *before* a shoe, for any given foot.

It makes sense in constructing a plan *not* to make any *commitment* to which side is done first *if you don't have to*.

*Principle of least commitment*: do not commit to any specific choices until you have to. This can be applied both to ordering and to instantiation of variables.

A *partial order planner* allows plans to specify that some steps must come before others but others have no ordering.

A *linearisation* of such a plan imposes a specific sequence on the actions therein.

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## Representing a plan: partial order planners

A plan consists of:

1. A set  $\{S_1, S_2, \dots, S_n\}$  of *steps*. Each of these is one of the available *operators*.
2. A set of *ordering constraints*. An ordering constraint  $S_i < S_j$  denotes the fact that step  $S_i$  must happen before step  $S_j$ .  $S_i < S_j < S_k$  and so on has the obvious meaning.  $S_i < S_j$  does *not* mean that  $S_i$  must *immediately* precede  $S_j$ .
3. A set of variable bindings  $v = x$  where  $v$  is a variable and  $x$  is either a variable or a constant.
4. A set of *causal links* or *protection intervals*  $S_i \xrightarrow{c} S_j$ . This denotes the fact that the purpose of  $S_i$  is to achieve the precondition  $c$  for  $S_j$ .

A causal link is *always* paired with an equivalent ordering constraint.

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## Representing a plan: partial order planners

The *initial plan* has:

- Two steps, called **Start** and **Finish**.
- A single ordering constraint  $\text{Start} < \text{Finish}$ .
- No *variable bindings*.
- No *causal links*.

In addition to this:

- The step **Start** has no preconditions, and its effect is the start state for the problem.
- The step **Finish** has no effect, and its precondition is the goal.
- Neither **Start** or **Finish** has an associated action.

We now need to consider what constitutes a *solution*...

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## Solutions to planning problems

A solution to a planning problem is any *complete* and *consistent* partially ordered plan.

*Complete*: each precondition of each step is *achieved* by another step in the solution.

A precondition  $c$  for  $S$  is achieved by a step  $S'$  if:

1. The precondition is an effect of the step

$$S' < S \text{ and } c \in \text{Effects}(S')$$

and...

2. ... there is *no other* step that *could* cancel the precondition. That is, no  $S''$  exists where:

- The existing ordering constraints allow  $S''$  to occur *after*  $S'$  but *before*  $S$ .
- $\neg c \in \text{Effects}(S'')$ .

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## Solutions to planning problems

*Consistent*: no contradictions exist in the binding constraints or in the proposed ordering. That is:

1. For binding constraints, we never have  $v = X$  and  $v = Y$  for distinct constants  $X$  and  $Y$ .
2. For the ordering, we never have  $S < S'$  and  $S' < S$ .

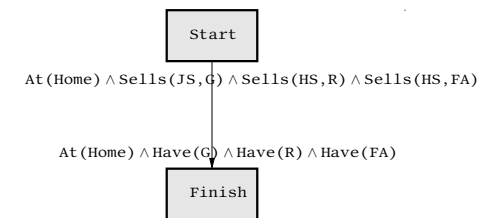
Returning to the roof-climbers' shopping expedition, here is the basic approach:

- Begin with only the **Start** and **Finish** steps in the plan.
- At each stage add a new step.
- Always add a new step such that a *currently non-achieved precondition is achieved*.
- Backtrack when necessary.

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## An example of partial-order planning

Here is the *initial plan*:



Thin arrows denote ordering.

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### An example of partial-order planning

There are *two actions available*:



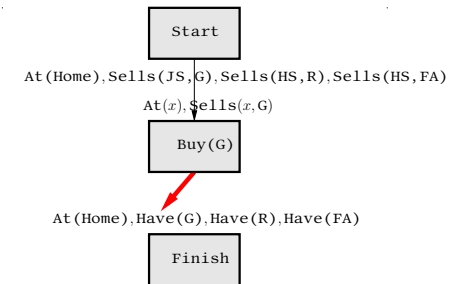
A planner might begin, for example, by adding a **Buy(G)** action in order to achieve the **Have(G)** precondition of **Finish**.

*Note*: the following order of events is by no means the only one available to a planner.

It has been chosen for illustrative purposes.

### An example of partial-order planning

Incorporating the suggested step into the plan:

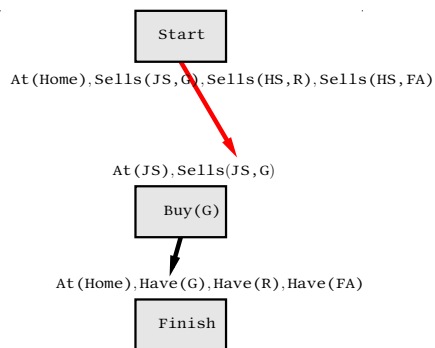


Thick arrows denote causal links. They always have a thin arrow underneath.

Here the new **Buy** step achieves the **Have(G)** precondition of **Finish**.

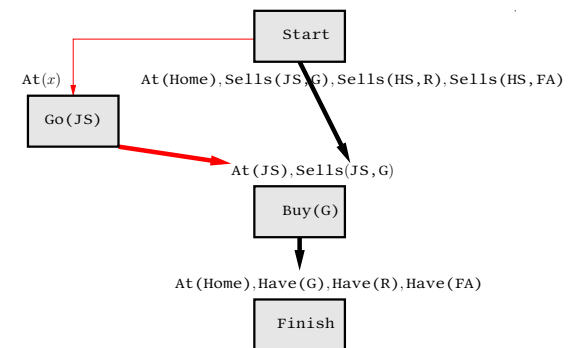
### An example of partial-order planning

The planner can now introduce a second causal link from **Start** to achieve the **Sells(x, G)** precondition of **Buy(G)**.



### An example of partial-order planning

The planner's next obvious move is to introduce a **Go** step to achieve the **At(JS)** precondition of **Buy(G)**.



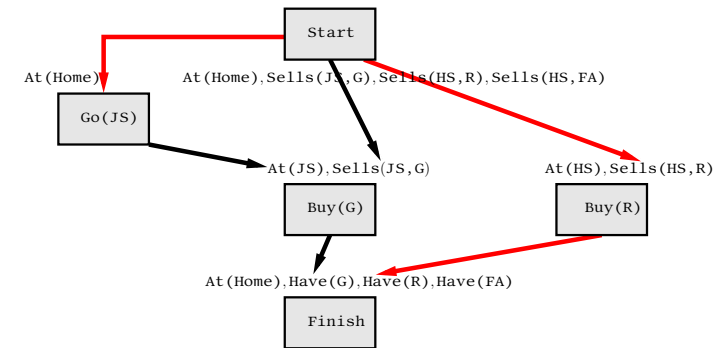
And we continue...

### An example of partial-order planning

Initially the planner can continue quite easily in this manner:

- Add a causal link from **Start** to **Go(JS)** to achieve the **At(x)** precondition.
- Add the step **Buy(R)** with an associated causal link to the **Have(R)** precondition of **Finish**.
- Add a causal link from **Start** to **Buy(R)** to achieve the **Sells(HS,R)** precondition.

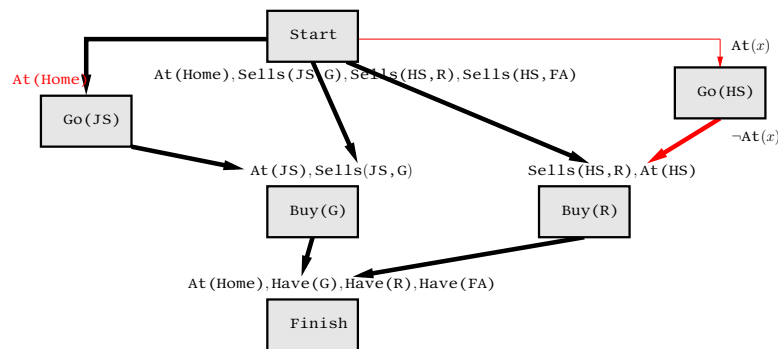
But then things get more interesting...



At this point it starts to get tricky...

The **At(HS)** precondition in **Buy(R)** is not achieved.

### An example of partial-order planning

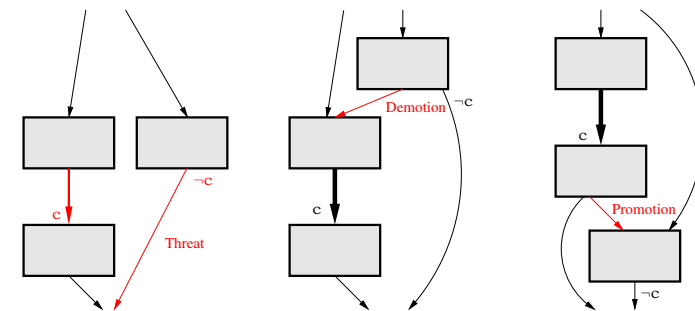


The **At(HS)** precondition is easy to achieve.

*But if we introduce a causal link from **Start** to **Go(HS)** then we risk invalidating the precondition for **Go(JS)**.*

### An example of partial-order planning

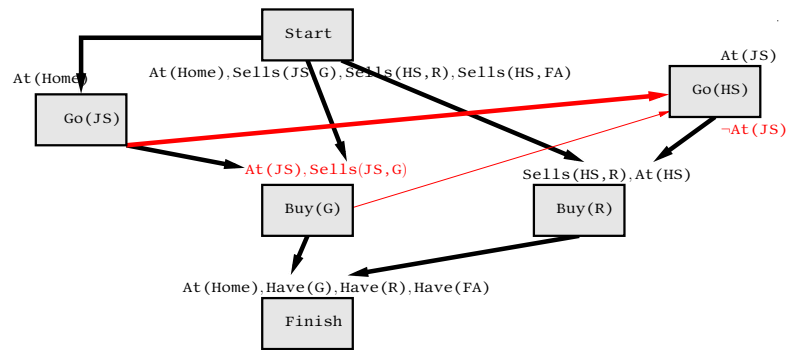
A step that might invalidate (sometimes the word *lobber* is employed) a previously achieved precondition is called a *threat*.



A planner can try to fix a threat by introducing an ordering constraint.

### An example of partial-order planning

The planner could backtrack and try to achieve the  $At(x)$  precondition using the existing  $Go(JS)$  step.



This involves a threat, but one that can be fixed using promotion.

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### The algorithm

Simplifying slightly to the case where there are *no variables*.

Say we have a partially completed plan and a set of the preconditions that have yet to be achieved.

- Select a precondition  $p$  that has not yet been achieved and is associated with an action  $B$ .
- At each stage *the partially complete plan is expanded into a new collection of plans*.
- To expand a plan, we can try to achieve  $p$  *either* by using an action that's already in the plan or by adding a new action to the plan. In either case, call the action  $A$ .

We then try to construct consistent plans where  $A$  achieves  $p$ .

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### The algorithm

This works as follows:

- For *each possible way of achieving  $p$* :
  - Add  $Start < A$ ,  $A < Finish$ ,  $A < B$  and the causal link  $A \xrightarrow{p} B$  to the plan.
  - If the resulting plan is consistent we're done, otherwise *generate all possible ways of removing inconsistencies* by promotion or demotion and *keep any resulting consistent plans*.

At this stage:

- If you have *no further preconditions that haven't been achieved* then *any plan obtained is valid*.

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### The algorithm

But how do we try to *enforce consistency*?

When you attempt to achieve  $p$  using  $A$ :

- Find all the existing causal links  $A' \xrightarrow{p'} B'$  that are *lobbered* by  $A$ .
- For each of those you can try adding  $A < A'$  or  $B' < A$  to the plan.
- Find all existing actions  $C$  in the plan that clobber the *new* causal link  $A \xrightarrow{p} B$ .
- For each of those you can try adding  $C < A$  or  $B < C$  to the plan.
- Generate *every possible combination* in this way and retain any consistent plans that result.

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## Possible threats

What about dealing with *variables*?

If at any stage an effect  $\neg At(x)$  appears, is it a threat to  $At(JS)$ ?

Such an occurrence is called a *possible threat* and we can deal with it by introducing *inequality constraints*: in this case  $x \neq JS$ .

- Each partially complete plan now has a set  $I$  of inequality constraints associated with it.
- An inequality constraint has the form  $v \neq X$  where  $v$  is a variable and  $X$  is a variable or a constant.
- Whenever we try to make a substitution we check  $I$  to make sure we won't introduce a conflict.

If we *would* introduce a conflict then we discard the partially completed plan as inconsistent.

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## Planning II

Unsurprisingly, this process can become complex.

How might we improve matters?

One way would be to introduce *heuristics*. We now consider:

- The way in which *basic heuristics* might be defined for use in planning problems.
- The construction of *planning graphs* and their use in obtaining more sensible heuristics.
- Planning graphs as the basis of the *GraphPlan* algorithm.

Another is to translate into the language of a *general-purpose* algorithm exploiting its own heuristics. We now consider:

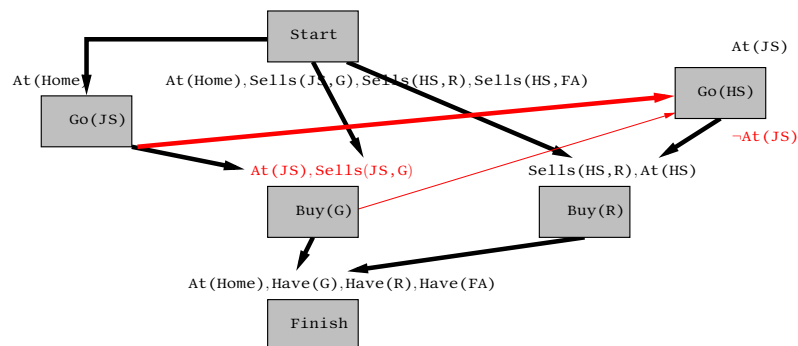
- Planning using *propositional logic*.
- Planning using *constraint satisfaction*.

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## An example of partial-order planning

We left our example problem here:

The planner could backtrack and try to achieve the  $At(x)$  precondition using the existing  $Go(JS)$  step.



This involves a threat, but one that can be fixed using promotion.

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## Using heuristics in planning

We found in looking at search problems that *heuristics* were a helpful thing to have.

Note that now there is no simple representation of a *state*, and consequently it is harder to measure the *distance to a goal*.

Defining heuristics for planning is therefore more difficult than it was for search problems. Simple possibilities:

$$h = \text{number of unsatisfied preconditions}$$

or

$$h = \text{number of unsatisfied preconditions} \\ - \text{number satisfied by the start state}$$

These can lead to underestimates or overestimates:

- Underestimates if *actions can affect one another in undesirable ways*.
- Overestimates if *actions achieve many preconditions*.

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## Using heuristics in planning

We can go a little further by learning from *Constraint Satisfaction Problems* and adopting the *most constrained variable* heuristic:

- Prefer the precondition *satisfiable in the smallest number of ways*.

This can be computationally demanding but two special cases are helpful:

- Choose preconditions for which *no action will satisfy them*.
- Choose preconditions that *can only be satisfied in one way*.

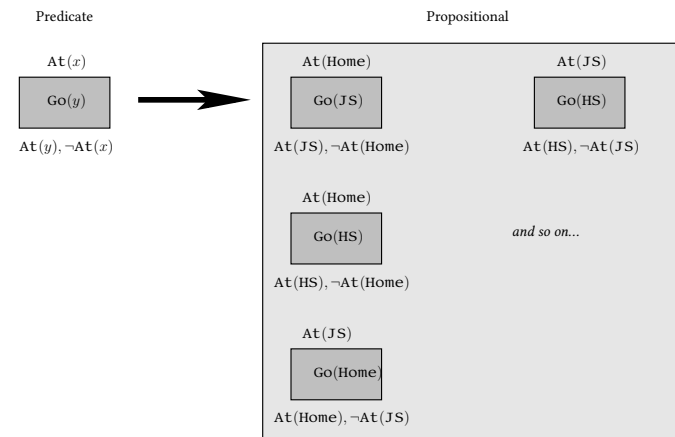
But these still seem somewhat basic.

We can do better using *Planning Graphs*. These are *easy to construct* and can also be used to generate *entire plans*.

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## Planning graphs

Planning Graphs apply when it is possible to work entirely using *propositional* representations of plans. Luckily, STRIPS can always be propositionalized...



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## Planning graphs

A planning graph is constructed in levels:

- Level 0 corresponds to the *start state*.
- At each level we keep *approximate* track of all things that *could* be true at the corresponding time.
- At each level we keep *approximate* track of what actions *could* be applicable at the corresponding time.

The approximation is due to the fact that not all conflicts between actions are tracked. *So*:

- The graph can *underestimate* how long it might take for a particular proposition to appear, and therefore ...
- ... a heuristic can be extracted.

*For example*: the triumphant return of the gorilla-purchasing roof-climbers...

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## Planning graphs: a simple example

Our intrepid student adventurers will of course need to inflate their *gorilla* before attaching it to a *distinguished roof*. It has to be purchased before it can be inflated.

*Start state*: Empty.

We assume that anything not mentioned in a state is false. So the state is actually

$\neg\text{Have}(\text{Gorilla})$  and  $\neg\text{Inflated}(\text{Gorilla})$

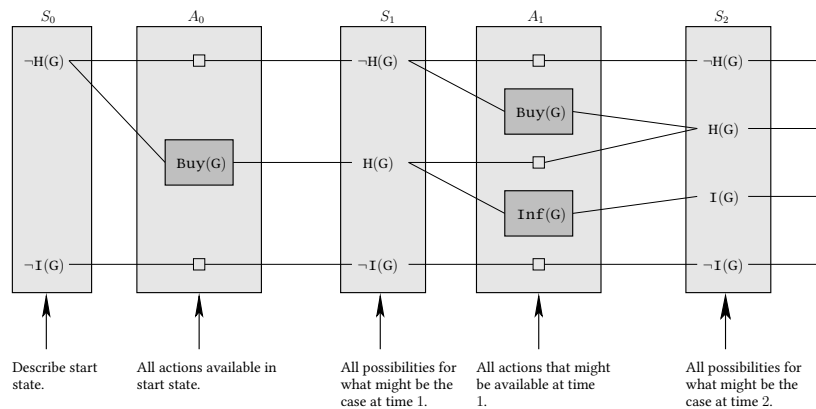
*Actions*:



*Goal*:  $\text{Have}(\text{Gorilla})$  and  $\text{Inflated}(\text{Gorilla})$ .

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## Planning graphs



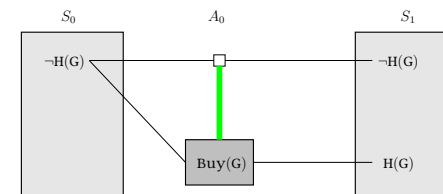
□ = a *persistence action*—what happens if no action is taken.  
 An action level  $A_i$  contains *all* actions that *could* happen given the propositions in  $S_i$ .

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## Mutex links

We also record, using *mutual exclusion (mutex) links* which pairs of actions could not occur together.

*Mutex links 1: Effects are inconsistent.*

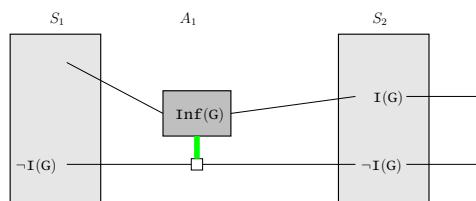


The effect of one action negates the effect of another.

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## Mutex links

*Mutex links 2: The actions interfere.*

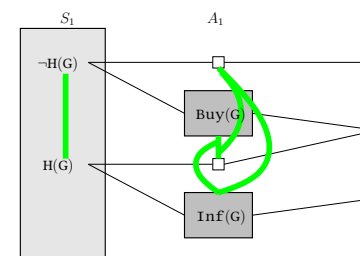


The effect of an action negates the precondition of another.

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## Mutex links

*Mutex links 3: Competing for preconditions.*



The precondition for an action is mutually exclusive with the precondition for another. (See next slide!)

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### Mutex links

A state level  $S_i$  contains *all* propositions that *could* be true, given the possible preceding actions.

We also use mutex links to record pairs that can not be true simultaneously:

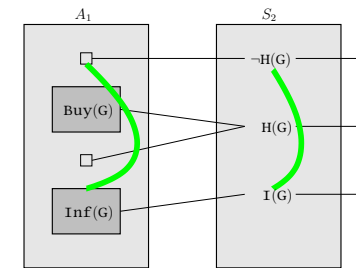
*Possibility 1:* pair consists of a proposition and its negation.



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### Mutex links

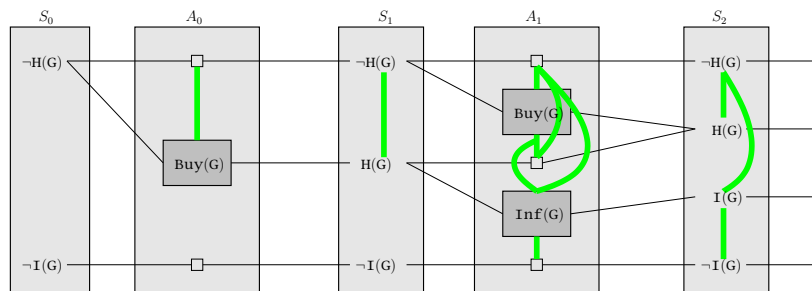
*Possibility 2:* all pairs of actions that could achieve the pair of propositions are mutex.



The construction of a planning graph is continued until two identical levels are obtained.

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### Planning graphs



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### Obtaining heuristics from a planning graph

To estimate the cost of reaching a single proposition:

- Any proposition not appearing in the final level has *infinite cost* and *can never be reached*.
- The *level cost* of a proposition is the level at which it first appears *but* this may be inaccurate as several actions can apply at each level and this cost does not count the *number of actions*. (It is however *admissible*.)
- A *serial planning graph* includes mutex links between all pairs of actions except persistence actions.

*Level cost in serial planning graphs* can be quite a good measurement.

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## Obtaining heuristics from a planning graph

How about estimating the cost to achieve a *collection* of propositions?

- *Max-level*: use the maximum level in the graph of any proposition in the set. Admissible but can be inaccurate.
- *Level-sum*: use the sum of the levels of the propositions. Inadmissible but sometimes quite accurate if goals tend to be decomposable.
- *Set-level*: use the level at which *all* propositions appear with none being mutex. Can be accurate if goals tend *not* to be decomposable.

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## Other points about planning graphs

A planning graph guarantees that:

1. *If* a proposition appears at some level, there *may* be a way of achieving it.
2. *If* a proposition does *not* appear, it can *not* be achieved.

The first point here is a loose guarantee because only *pairs* of items are linked by mutex links.

Looking at larger collections can strengthen the guarantee, but in practice the gains are outweighed by the increased computation.

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## Graphplan

The *GraphPlan* algorithm goes beyond using the planning graph as a source of heuristics.

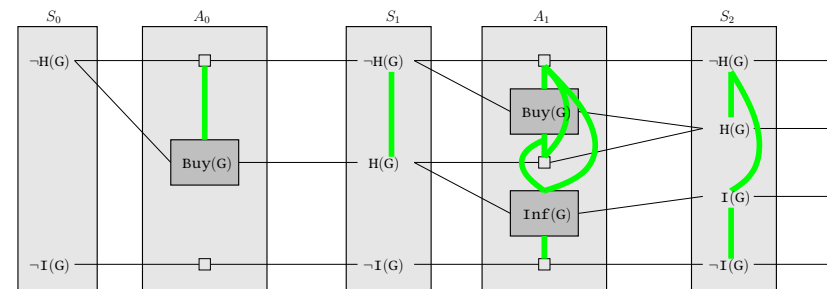
```
1 function GraphPlan()  
2   Start at level 0;  
3   while true do  
4     if All goal propositions appear in the current level AND no pair has a mutex link then  
5       Attempt to extract a plan;  
6       if A solution is obtained then  
7         return SOME solution;  
8     if Graph indicates there is no solution then  
9       return NONE;  
10    Expand the graph to the next level;
```

We *extract a plan* directly from the planning graph. Termination can be proved but will not be covered here.

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## Graphplan in action

Here, at levels  $S_0$  and  $S_1$  we do not have both  $H(G)$  and  $I(G)$  available with no mutex links, and so we expand first to  $S_1$  and then to  $S_2$ .



At  $S_2$  we try to extract a solution (plan).

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### Extracting a plan from the graph

Extraction of a plan can be formalised as a *search problem*.

*States* contain a *level*, and a collection of *unsatisfied goal propositions*.

*Start state*: the current final level of the graph, along with the relevant goal propositions.

*Goal*: a state at level  $S_0$  containing the initial propositions.

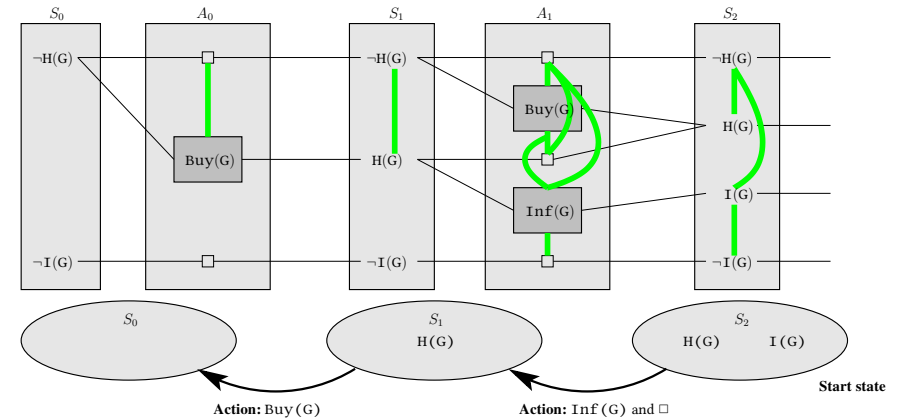
*Actions*: For a state  $S$  with level  $S_i$ , a valid action is to select any set  $X$  of actions in  $A_{i-1}$  such that:

1. no pair has a mutex link;
2. no pair of their preconditions has a mutex link;
3. the effects of the actions in  $X$  achieve the propositions in  $S$ .

The effect of such an action is a state having level  $S_{i-1}$ , and containing the preconditions for the actions in  $X$ .

Each action has a cost of 1.

### Graphplan in action



### Heuristics for plan extraction

We can of course also apply *heuristics* to this part of the process.

For example, when dealing with a *set of propositions*:

- Choose the proposition having *maximum level cost* first.
- For that proposition, attempt to achieve it using the action for which the *maximum/sum level cost of its preconditions is minimum*.