L95: Natural Language Syntax and Parsing
3) Dependency Parsing

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Reminder:

So far we have: (for statistical parsing more generally we need...)

- Used CFGs to define a legal set of structures for a set of strings (a grammar)
- Used the CKY algorithm to find all structures for a given string (a parsing algorithm)
- Used PCFGs to assign probabilities to the structures deriving the strings (a scoring model for parses)
- Used a modified CKY algorithm to find the best structure from all the possibilities (an algorithm for finding best parse)
Reminder:

Recall that:

$$\hat{T}(W) = \arg\max_{trees \text{ that yield } W} P(T|W)$$

- finding $T$s that yield $W$ requires a parsing algorithm over a grammar
- knowing $P(T|W)$ requires a probabilistic model over $T$
- $\arg\max$ requires an algorithm for finding best parse

More generally:

$$\hat{T}(W) = \arg\max_{trees \text{ that yield } W} \text{Score}(T|W)$$

- Generative models use the product of estimated probabilities of parse pieces to find $P(T|W)$ but we could use other scoring functions...
Generative models have some issues

Recall that:

\[ P(T, W) = \prod_{i=1}^{n} P(A_i \rightarrow B_i) \]

- But \( P(T, W) = P(T)P(W|T) \) and that \( P(W|T) = 1 \) so
  \[ P(T, W) = P(T) \] and thus \( P(T) = \prod_{i=1}^{n} P(A_i \rightarrow B_i) \)

- How do we know how to break the parse into pieces?
- Is the independence assumption valid?
- Generative models simultaneously model the tree and the string—**discriminative models** define \( P(T|W) \) directly
- Models are **discriminative** because they compare the correct parse against incorrect parses in training to set parameters... can use machine learning approaches.
- First we’re going to learn about a grammar that we will use to define \( T \) within a discriminative model—**dependency grammars**.
A *dependency tree* is a directed graph representation of a string—each edge represents a grammatical relationship between the symbols.
A dependency grammar derives dependency trees

Formally $G_{dep} = (\Sigma, D, s, \perp, P)$ where:

- $\Sigma$ is the finite set of alphabet symbols
- $D$ is the set of symbols to indicate whether the dependent symbol (the one on the RHS of the rule) will be located on the left or right of the current item within the string $D = \{L, R\}$
- $s$ is the root symbol for the dependency tree (we will use $s \in \Sigma$ but sometimes a special extra symbol is used)
- $\perp$ is a symbol to indicate an allowed endpoint to the graph
- $P$ is a set of rules for generating dependencies:
  $P = \{ (\alpha \rightarrow \beta, d) \mid \alpha \in (\Sigma \cup s), \beta \in (\Sigma \cup \perp), d \in D \}$

In dependency grammars we refer to the term on the LHS of a rule as the head and the RHS as the dependent (as opposed to parents and children in phrase structure grammars).
Dependency trees have several representations

Two diagrammatic representations of a dependency tree for the string \textit{bacdfe} generated using $G_{dep} = (\Sigma, D, s, \perp, P)$ where:

- $\Sigma = \{a...f\}$
- $D = \{L, R\}$
- $s = a$
- $P = \{(a \rightarrow b, L | c, R | d, R)$
  $(d \rightarrow e, R)$
  $(e \rightarrow f, L)$
  $(b \rightarrow \perp, L | \perp, R)$
  $(c \rightarrow \perp, L | \perp, R)$
  $(f \rightarrow \perp, L | \perp, R)\}$

The same rules would have been used to generate the string \textit{badfec}. Useful when there is flexibility in the symbol order of grammatical strings.
Valid trees may be **projective** or **non-projective**

- **Valid derivation** is one that is **rooted** in $s$ and is **weakly connected**.
- Derivation trees may be **projective** or **non-projective**.
- Non-projective trees can be needed for long distance dependencies.

The difference has implications for parsing complexity.
**Labels** can be added to the dependency edges

A label can be added to each generated dependency:

$$\mathcal{P} = \{(\alpha \rightarrow \beta : r, d) \mid \alpha \in (\Sigma \cup s), \, \beta \in (\Sigma \cup \bot), \, d \in \mathcal{D}, \, r \in \mathcal{B}\}$$

where $\mathcal{B}$ is the set of dependency labels.

When used for natural language parsing, dependency grammars will often label each dependency with the *grammatical function* (or the *grammatical relation*) between the words.

![Dependency tree diagram](image)
Dependency grammars can be **weakly equivalent** to CFGs.

**Projective** dependency grammars can be shown to be **weakly equivalent** to context-free grammars.

```
S
 / \  
NP  VP
 /   /
N  VP  PP
 / |  / |
alice V NP P NP
 / |  / |
plays N with N
 / |  / |
croquet A N
 / |
pink flamingos
```
Dependency grammars can be weakly equivalent to CFGs

```
S{plays}
  / \
NP{alice}  VP{plays}
   /   /
  alice  V{plays}  NP{croquet}
   /   /  |
 plays N{croquet}   |
       /  |
       croquet

PP{with}
  /   /
P{with}  NP{flamingos}
    /  |
  with N{flamingos}
    /  |
   pink N{flamingos}
   /  |
   pink flamingos
```
Dependency grammars can be **weakly equivalent** to CFGs

```
S{plays}
  /  
NP{alice}  VP{plays}
   /   
N{alice}  VP{plays}
     /  
V{plays} NP{croquet}
   / 
plays  N{croquet}
   /  
PP{with}
  /  
P{with}
  /  
NP{flamingos}
   /  
A{pink}
  /  
P{with}
  /  
NP{flamingos}
   /  
N{flamingos}
```

alice plays croquet
with flamingos
    pink flamingos
Dependency grammars can be **weakly equivalent** to CFGs.
Dependency grammars can be **weakly equivalent** to CFGs.
Dependency grammars can be \textit{weakly equivalent} to CFGs.

```
S{plays}
  NP{alice}
  PP{with}
    NP{croquet}
    NP{flamingos}
    A{pink}
```
Dependency grammars can be **weakly equivalent** to CFGs.
Dependency grammars can be \textbf{weakly equivalent} to CFGs.

\textbf{Projective} dependency grammars can be shown to be \textbf{weakly equivalent} to context-free grammars.
Recall: shift-reduce parsers and deterministic languages

LR(k) Shift-reduce parsers are most useful for recognising the strings of deterministic languages (languages where no string has more than one analysis) which have been described by an unambiguous grammar.

Quick reminder:

- The parsing algorithm has two actions: SHIFT and REDUCE
- Initially the input string is held in the buffer and the stack is empty.
- Symbols are shifted from the buffer to the stack.
- When the top items of the stack match the RHS of a rule in the grammar then they are reduced, that is, they are replaced with the LHS of that rule.
- $k$ refers to the look-ahead.
### Shift-reduce parsing using a deterministic CFG

Shift-reduce parse for the string *abcd* generated using $G_{cfg} = (\Sigma, \mathcal{N}, s, \mathcal{P})$:

<table>
<thead>
<tr>
<th>STACK</th>
<th>BUFFER</th>
<th>ACTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Sigma = {a, b, c}$</td>
<td>abcd</td>
<td>SHIFT</td>
</tr>
<tr>
<td>$\mathcal{N} = {S, A, B, C, D}$</td>
<td>a</td>
<td>REDUCE</td>
</tr>
<tr>
<td>$s = S$</td>
<td>bcd</td>
<td>SHIFT</td>
</tr>
<tr>
<td>$\mathcal{P} = {S \rightarrow AB, A \rightarrow a, B \rightarrow bC, C \rightarrow cD, D \rightarrow d}$</td>
<td>Ab</td>
<td>SHIFT</td>
</tr>
<tr>
<td></td>
<td>Abc</td>
<td>SHIFT</td>
</tr>
<tr>
<td></td>
<td>Abcd</td>
<td>SHIFT</td>
</tr>
<tr>
<td></td>
<td>AbcD</td>
<td>REDUCE</td>
</tr>
<tr>
<td></td>
<td>AbC</td>
<td>REDUCE</td>
</tr>
<tr>
<td></td>
<td>AB</td>
<td>REDUCE</td>
</tr>
<tr>
<td></td>
<td>S</td>
<td>REDUCE</td>
</tr>
</tbody>
</table>
Dependency parsers use a modified shift-reduce parser

- A common method for dependency parsing of natural language involves a modification of the LR shift-reduce parser
- The shift operator continues to move items of the input string from the buffer to the stack
- The reduce operator is replaced with the operations left-arc and right-arc which reduce the top two stack symbols leaving the head on the stack

Consider $L(G_{dep}) \subseteq \Sigma^*$, during parsing the stack may hold $\gamma ab$ where $\gamma \in \Sigma^*$ and $a, b \in \Sigma$, and $b$ is at the top of the stack:

- **LEFT-ARC** reduces the stack to $\gamma b$ and records use of rule $b \rightarrow a$
- **RIGHT-ARC** reduces the stack to $\gamma a$ and records the use of rule $a \rightarrow b$
Dependency parsers use a **modified** shift-reduce parser.

Example of shift-reduce parse for the string *bacdfe* generated using $G_{dep} = (\Sigma, D, s, \perp, \mathcal{P})$.

<table>
<thead>
<tr>
<th>STACK</th>
<th>BUFFER</th>
<th>ACTION</th>
<th>RECORD</th>
</tr>
</thead>
<tbody>
<tr>
<td>b</td>
<td>bacdfe</td>
<td>SHIFT</td>
<td>a → b</td>
</tr>
<tr>
<td>ba</td>
<td>acdfe</td>
<td>SHIFT</td>
<td>a → c</td>
</tr>
<tr>
<td>a</td>
<td>cdfe</td>
<td>LEFT-ARC</td>
<td>e → f</td>
</tr>
<tr>
<td>ac</td>
<td>dfe</td>
<td>SHIFT</td>
<td>d → e</td>
</tr>
<tr>
<td>a</td>
<td>dfe</td>
<td>SHIFT</td>
<td>a → d</td>
</tr>
<tr>
<td>ad</td>
<td>fe</td>
<td>SHIFT</td>
<td></td>
</tr>
<tr>
<td>adf</td>
<td>e</td>
<td>SHIFT</td>
<td></td>
</tr>
<tr>
<td>adf</td>
<td></td>
<td>LEFT-ARC</td>
<td></td>
</tr>
<tr>
<td>ade</td>
<td></td>
<td>RIGHT-ARC</td>
<td></td>
</tr>
<tr>
<td>ad</td>
<td></td>
<td>RIGHT-ARC</td>
<td></td>
</tr>
<tr>
<td>a</td>
<td></td>
<td>TERMINATE</td>
<td></td>
</tr>
</tbody>
</table>

Note that, for a deterministic parse here, a lookahead is needed.
For natural language there would be considerable effort in manually defining $P$—this would involve determining the dependencies between all possible words in the language.

Creating a deterministic grammar would be impossible (natural language is inherently ambiguous).

Natural language dependency parsing can be achieved deterministically by selecting parsing actions using a machine learning classifier.

The features for the classifier include the items on the stack and in the buffer as well as properties of those items (including word-embeddings for the items).

Training is performed on dependency banks (that is, sentences that have been manually annotated with their correct dependencies).

It is said that the parsing is grammarless—since no grammar is designed ahead of training (although note that e.g. RASP uses a similar transition-based approach with a manually defined PSG).
We can use a **beam** search to record the parse forest.

- The classifier can return a **probability** of an action based on features (or feature templates).
- To avoid the problem of early incorrect resolution of an ambiguous parse, multiple competing parses can be recorded and a **beam search** used to keep track of the best alternative parses.
- Google’s *Parsey McParseface* is an English language dependency parser that uses word-embeddings as features and a neural network to score parse actions. A beam search is used to compare competing parses.
Graph-based dependency parsers score the whole tree

- Transitional-based dependency parsers make local decisions
- Graph-based dependency parsers score the whole tree
- The score for a dependency between word $i$ and $j$, where $\mathcal{F}$ is a feature representation of the dependency and $w$ is a weight vector:
  \[
  \text{score}(i,j) = w \cdot \mathcal{F}(i,j)
  \]
- And the score for the whole tree $T$ over string $S$ is:
  \[
  \text{Score}(T, S) = \sum_{(i,j) \in T} \text{score}(i,j) = \sum_{(i,j) \in T} w \cdot \mathcal{F}(i,j)
  \]
- Can use a modified version of CKY with Viterbi to find the best parse
- More efficient if we treat left and right parsing separately
Dependency parsers can be useful for parsing speech

The most obvious difference between spoken and written language is the mode of transmission:

- **Prosody** refers to the patterns of stress and intonation in a language.
- **Stress** refers to the relative emphasis or prominence given to a certain part of a word (e.g. CON-tent (the stuff included in something) vs. con-TENT (happy))
- **Intonation** refers to the way speakers’ pitch rises and falls in line with words and phrases, to signal a question, for example.
- Co-speech gestures involve parts of the body which move in coordination with what a speaker is saying, to emphasise, disambiguate or otherwise.

We can use some of these extra features to help the parse-action-classifier when parsing spoken language.
Prosody has been used to resolve parsing ambiguity

- Briscoe suggested using a shift-reduce parser that favours shift over reduce wherever both are possible.
- In the absence of extra-linguistic information the parser delays resolution of the grammatical dependency.
- Extra features enable an override of the shift preference at the point where the ambiguity arises, including:
  - prosodic information (intonational phrase boundary)

The model accounts for frequencies of certain syntactic constructions as attested in corpora.
A fundamental issue that affects syntactic parsing of spoken language is the lack of the sentence unit (i.e. string delimitation)—indicated in writing by a full-stop and capital letter.

Speech units may be identified by pauses, intonation (e.g. rising for a question, falling for a full-stop), change of speaker.

Speech units are not much like written sentences due to speaker overlap, co-constructions, ellipsis, hesitation, repetitions and false starts.

Speech units often contain words and grammatical constructions that would not appear in the written form of the language.
Spoken language **lacks** string delimitation

Excerpt from the Spoken section of the British National Corpus

*set your sights realistically haven’t you and there’s a lot of people unemployed and what are you going to do when you eventually leave college if you get there you’re not gonna step straight into television mm right then let’s see now what we’re doing where’s that recipe book for that chocolate and banana cake chocolate and banana cake which book was it oh right oh some of these chocolate cakes are absolutely mm mm mm mm right what’s the topping what’s that icing sugar cocoa powder and vanilla essence oh luckily I’ve got all those I think yes*
Excerpt from the Spoken section of the British National Corpus

*Set your sights realistically haven’t you? And there’s a lot of people unemployed. And what are you going to do when you eventually leave college? If you get there. You’re not gonna step straight into television. Mm right then, let’s see now what we’re doing… Where’s that recipe book for that chocolate and banana cake? Chocolate and banana cake which book was it? Oh right. Oh, some of these chocolate cakes are absolutely mm mm mm. Right, what’s the topping? what’s that? Icing sugar, cocoa powder and vanilla essence. Oh luckily I’ve got all those I think, yes!*
Dependency parsers can be useful for parsing speech

- Spoken language can look noisy and somewhat *grammarless* but the disfluencies are predictable.
- Honnibal & Johnson’s Redshift parser introduces an *edit* action, to remove disfluent items from spoken language:
  - **EDIT**: on detection of disfluency, remove connected words and their dependencies.
- Parser uses extra classifier features to detect disfluency.
Dependency parsing

Example of dependency parser using an edit action

STACK

his₁
his₁ company₂
company₂
cOMPANY₂ went₃
went₃
went₃ broke₄
went₃
went₃ l − mean₅
company₂
cOMPANY₂ went₆
went₆
went₃ bankrupt₇
went₃

BUFFER

his₁ ... bankrupt₇
company₂ ... bankrupt₇
went₃ ... bankrupt₇
broke₄ ... bankrupt₇
l − mean₅ ... bankrupt₇
went₆ bankrupt₇
went₆ bankrupt₇
bankrupt₇
bankrupt₇

ACTION

SHIFT
SHIFT
LEFT-ARC
SHIFT
LEFT-ARC
SHIFT
RIGHT-ARC
SHIFT
EDIT
SHIFT
LEFT-ARC
SHIFT
RIGHT-ARC
TERMINATE

RECORD

company₂ → his₁
went₃ → company₂
went₃ → broke₄
went₆ → company₂
went₆ → bankrupt₇
root → went₆

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