



# High dynamic range and tone mapping

**Advanced Graphics**

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# Cornell Box: need for tone-mapping in graphics

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Rendering



Photograph

# Real-world scenes are more challenging

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- ▶ The match could not be achieved if the light source in the top of the box was visible
- ▶ The display could not reproduce the right level of brightness

# Dynamic range



Luminance  
↓  
 $\frac{\max L}{\min L}$   
↑  
(for SNR>3)

# Dynamic range (contrast)

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- ▶ As ratio:

$$C = \frac{L_{\max}}{L_{\min}}$$

- ▶ Usually written as C:1, for example 1000:1.

- ▶ As “orders of magnitude”  
or log10 units:

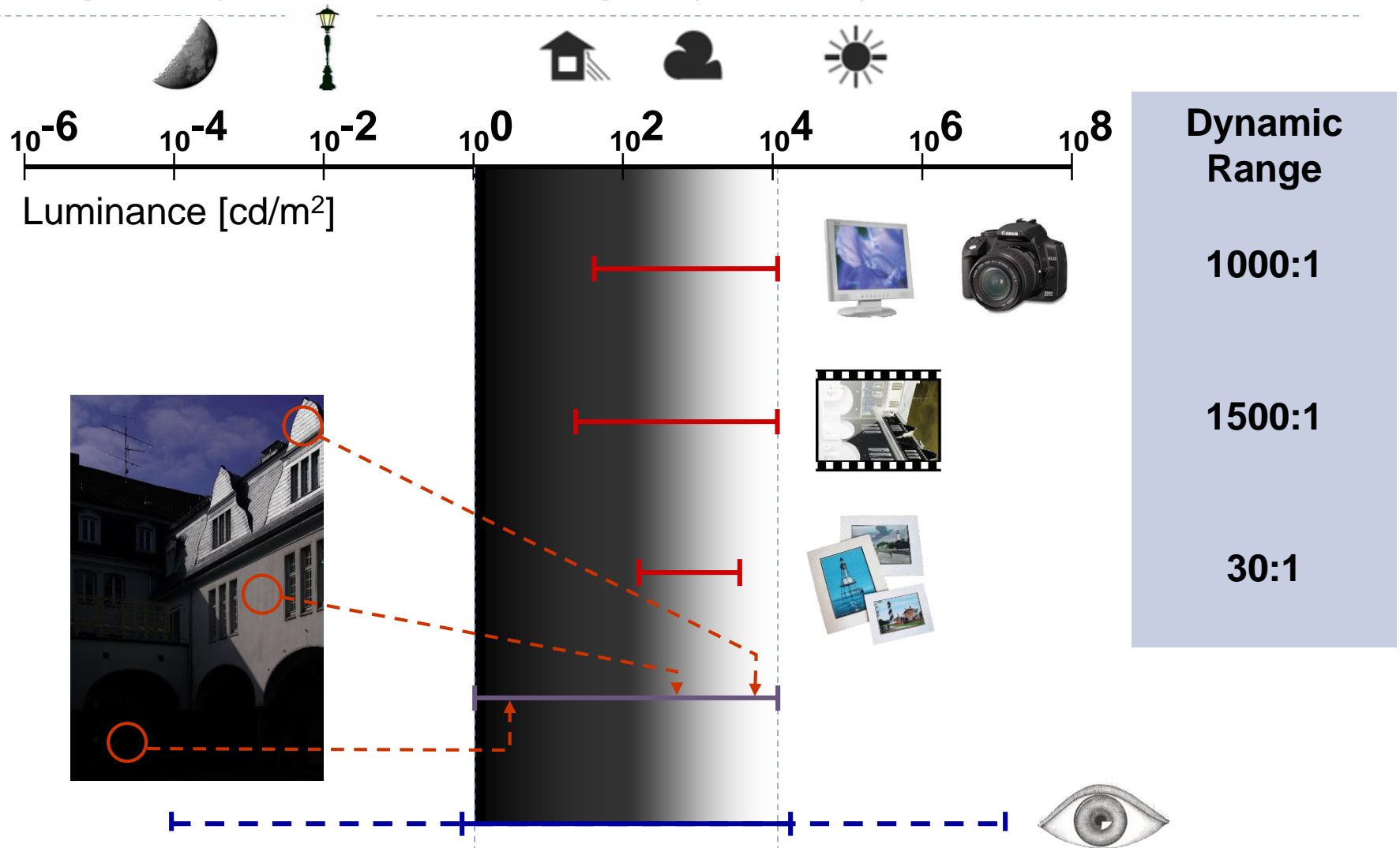
$$C_{10} = \log_{10} \frac{L_{\max}}{L_{\min}}$$

- ▶ As stops:

$$C_2 = \log_2 \frac{L_{\max}}{L_{\min}}$$

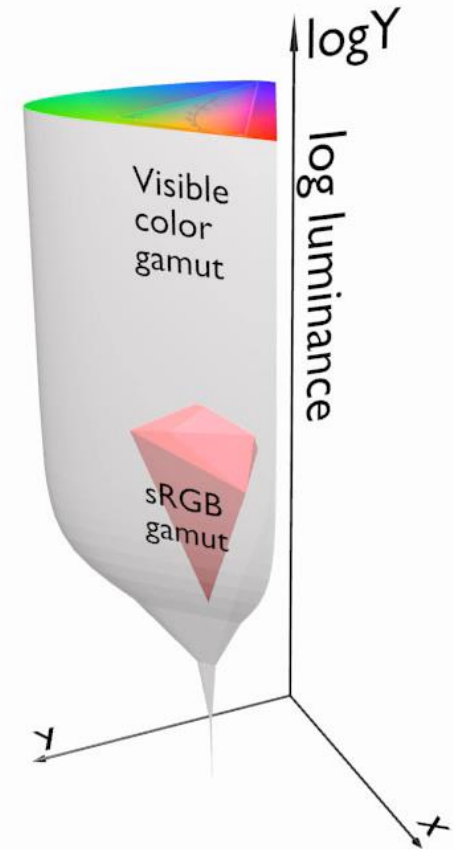
One stop is doubling  
of halving the amount of light

# High dynamic range (HDR)

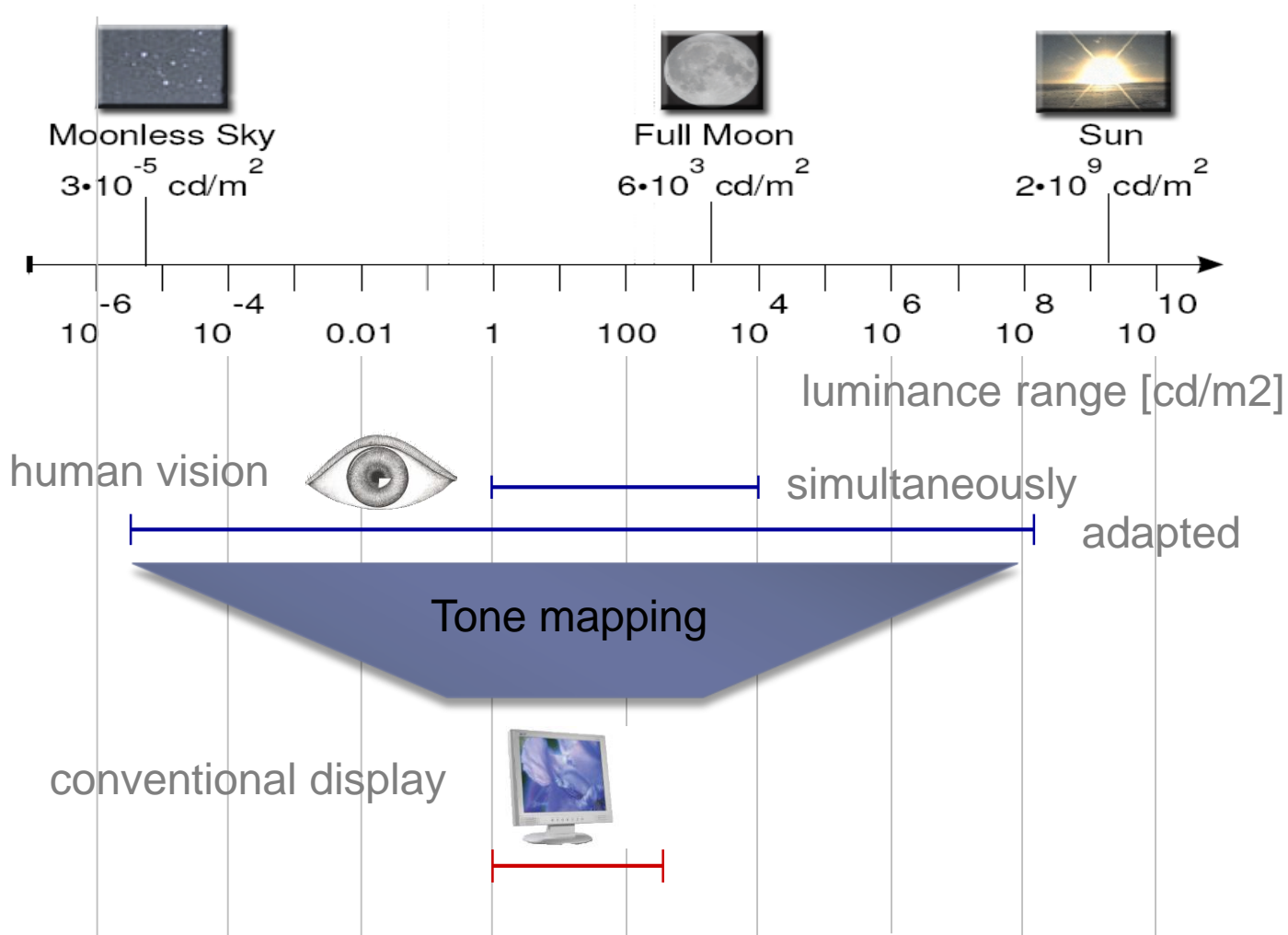


# Visible colour gamut

- ▶ The eye can perceive more colours and brightness levels than
  - ▶ a display can produce
  - ▶ a JPEG file can store
- ▶ The premise of HDR:
  - ▶ Visual perception and not the technology should define accuracy and the range of colours
  - ▶ The current standards not fully follow to this principle



# Tone-mapping problem





# Why do we need tone mapping?

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- ▶ To reduce excessive dynamic range
  - ▶ To customize the look (colour grading)
  - ▶ To simulate human vision
    - ▶ for example night vision
  - ▶ To adapt displayed images to a display and viewing conditions
  - ▶ To make rendered images look more realistic
- 
- ▶ Different tone mapping operators achieve different goals



# Tone-mapping in rendering

- ▶ Any physically-based rendering requires tone-mapping
- ▶ “HDR rendering” in games is pseudo-physically-based rendering
- ▶ Goal: to simulate a camera or the eye
- ▶ Greatly enhances realism

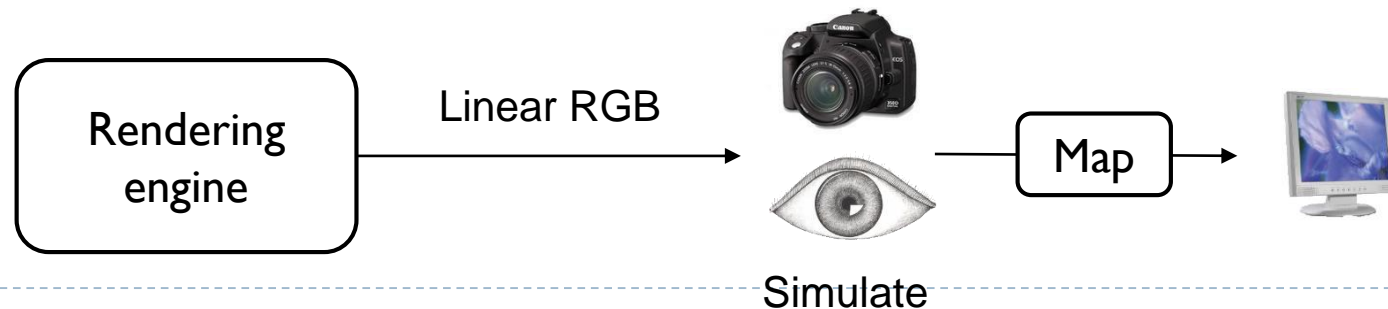
LDR illumination  
No tone-mapping



HDR illumination  
Tone-mapping



Half-Life 2: Lost coast



# Techniques

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- ▶ **Arithmetic of HDR images**
- ▶ Display model
- ▶ Tone-curve
- ▶ Color transfer
- ▶ Base-detail separation
- ▶ Glare
- ▶ Simulation of night vision

# Arithmetic of HDR images

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- ▶ How does the basic arithmetic operations
  - ▶ Addition
  - ▶ Multiplication
  - ▶ Power function
- ▶ affect the appearance of an HDR image?
- ▶ We work in the luminance space (NOT luma)
- ▶ The same operations can be applied to linear RGB
  - ▶ Or to luminance-only and the colour can be transferred

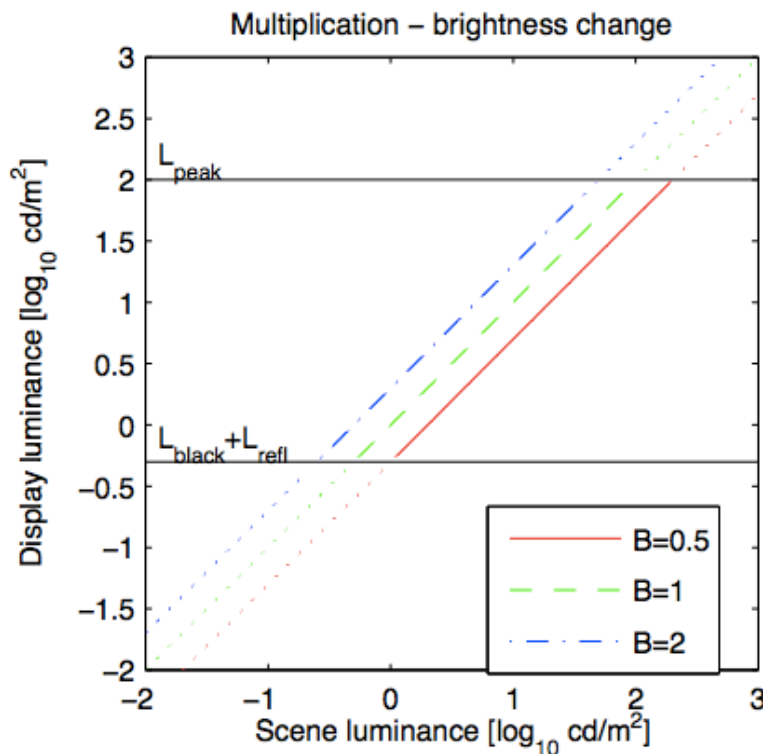
# Multiplication – brightness change

Resulting  
luminance

Input  
luminance

$$T(L_p) = B \cdot L_p$$

Brightness change  
parameter



- Multiplication makes the image brighter or darker
- It does not change the dynamic range!

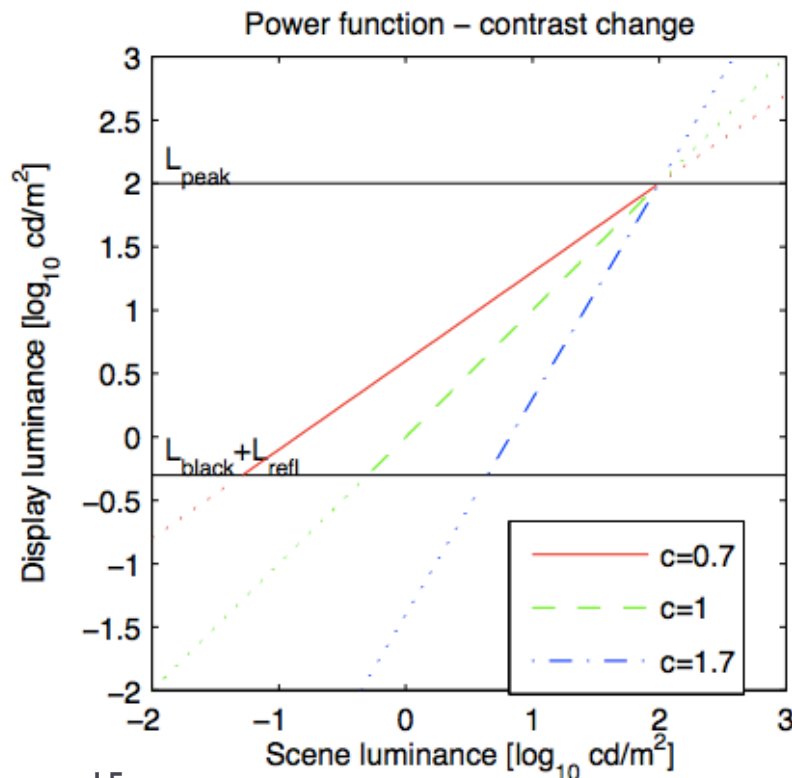
# Power function – contrast change

Contrast change  
(gamma)

Luminance of  
white

$$T(L_p) = \left( \frac{L_p}{L_{white}} \right)^c$$

- ▶ Power function stretches or shrinks image dynamic range
- ▶ It is usually performed relative to reference white
- ▶ Apparent brightness changes is the side effect of pushing tones towards or away from the white point

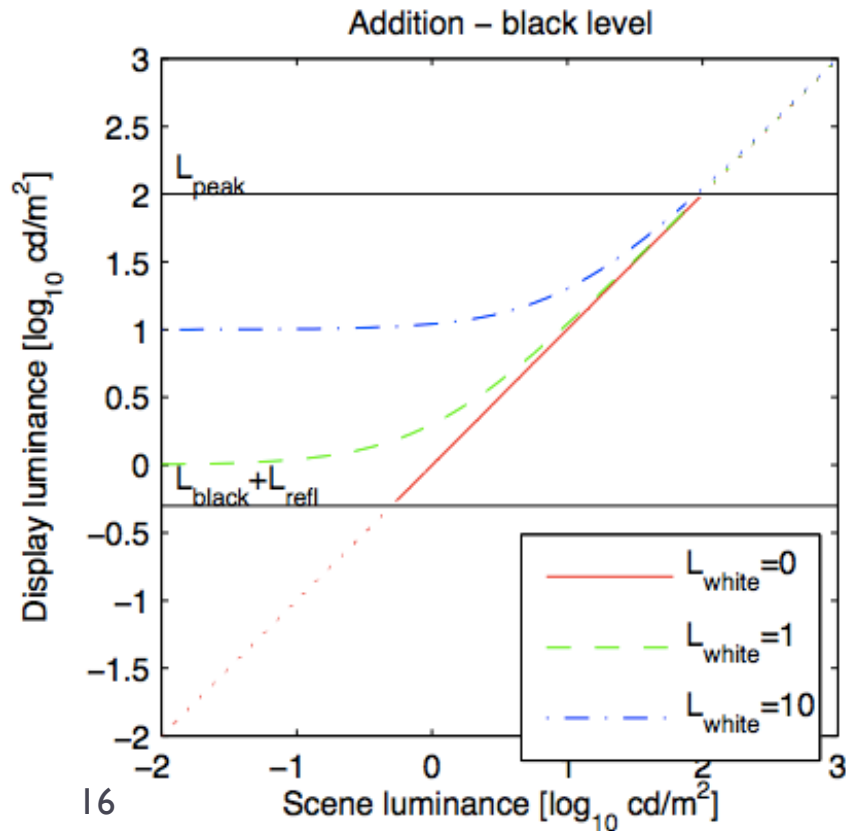


# Addition – black level

Black level (flare,  
fog)

$$T(L_p) = L_p + F$$

- ▶ Addition elevates black level, adds fog to an image
- ▶ It does NOT make the overall image brighter
- ▶ It reduces dynamic range



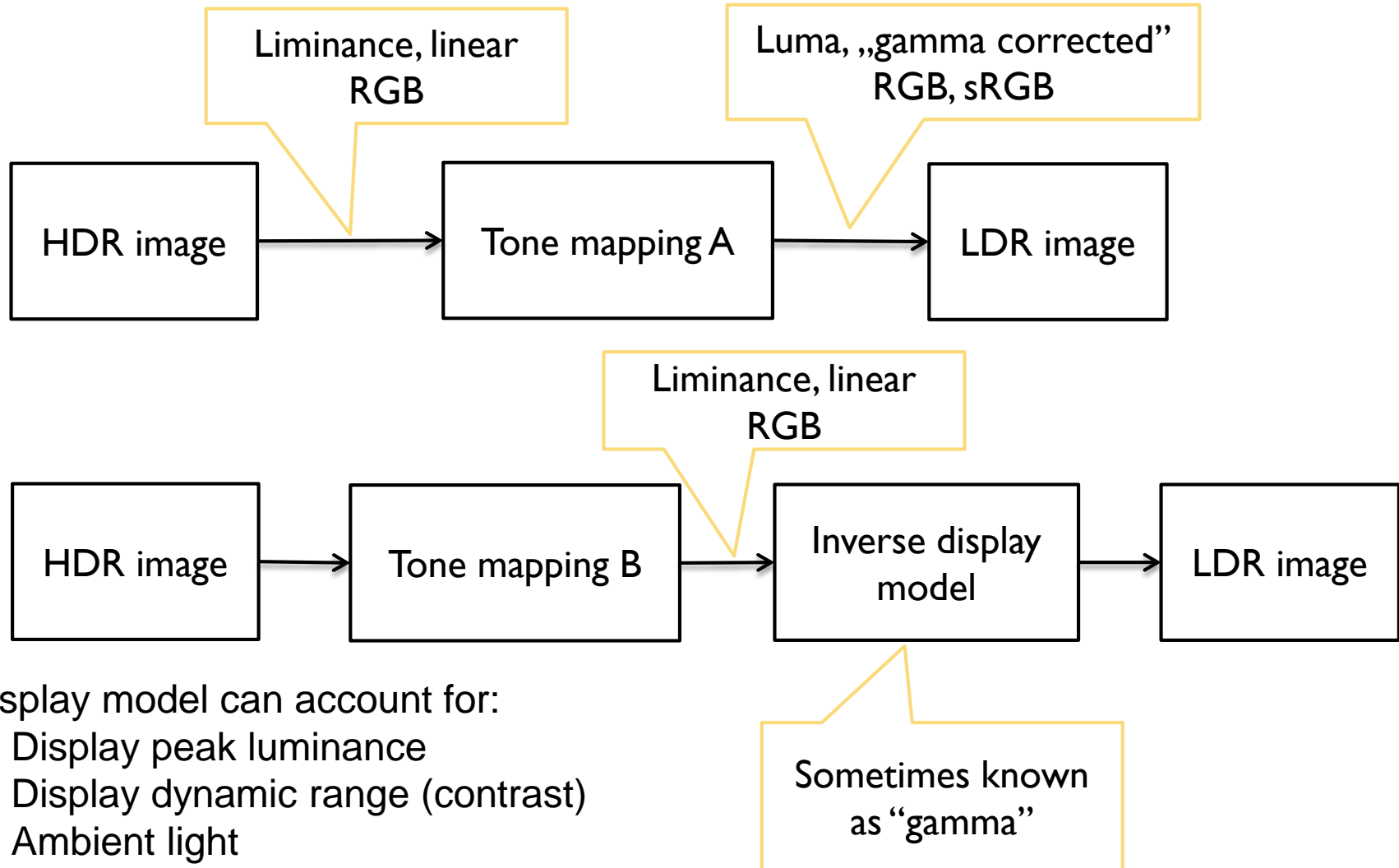
# Techniques

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- ▶ Arithmetic of HDR images
- ▶ **Display model**
- ▶ Tone-curve
- ▶ Color transfer
- ▶ Base-detail separation
- ▶ Glare
- ▶ Simulation of night vision



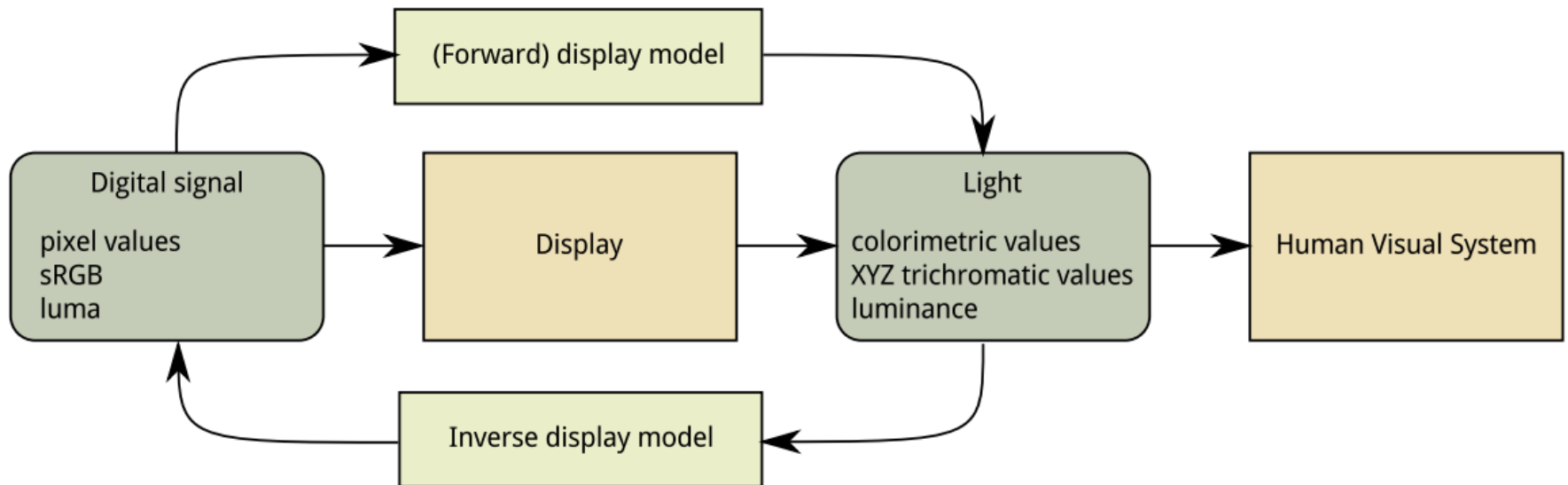
# Two ways to do tone-mapping



# Display model

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- ▶ Tone-mapping needs to account for the physical model of a display
  - ▶ How a display transforms pixel values into emitted light



# (Forward) Display model

## ► GOG: Gain-Gamma-Offset

Luminance

Peak  
luminance

Gamma

Display  
black level

Screen  
reflections

$$L = (L_{peak} - L_{black}) V^\gamma + L_{black} + L_{refl}$$

Gain

Pixel value  
0-1

Offset

Reflectance  
factor (0.01)

$$L_{refl} = \frac{k}{\pi} E_{amb}$$

Ambient illumination  
(in lux)

# Inverse display model

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Symbols are the same as for the forward display model

$$V = \left( \frac{L - L_{black} - L_{refl}}{L_{peak} - L_{black}} \right)^{(1/\gamma)}$$

Note: This display model does not address any colour issues. The same equation is applied to red, green and blue color channels. The assumption is that the display primaries are the same as for the sRGB color space.

# Ambient illumination compensation

Non-adaptive TMO



Display adaptive TMO





# Ambient illumination compensation

Non-adaptive TMO



Display adaptive TMO



10<sup>23</sup>

300

10 000

lux

# Example: Ambient light compensation

- ▶ We are looking at the screen in bright light

$$L_{peak} = 100 [cd \cdot m^{-2}] \quad k = 0.005$$

$$L_{black} = 0.1 [cd \cdot m^{-2}]$$

$$E_{amb} = 2000 [lux] \quad L_{refl} = \frac{0.005}{\pi} 2000 = 3.183 [cd \cdot m^{-2}]$$

Modern screens have reflectivity of around 0.5%

- ▶ We assume that the dynamic of the input is 2.6 ( $\approx 400:1$ )

$$r_{in} = 2.6 \quad r_{out} = \log_{10} \frac{L_{peak}}{L_{black} + L_{refl}} = 1.77$$

- ▶ First, we need to compress contrast to fit the available dynamic range, then compensate for ambient light

$$L_{out} = \left( \frac{L_{in}}{L_{peak}} \right)^{\frac{r_{out}}{r_{in}}} - L_{refl}$$

The resulting value is in luminance, must be mapped to display luma / gamma corrected values

Simplest, but not the best tone mapping

# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ **Tone-curve**
- ▶ Color transfer
- ▶ Base-detail separation
- ▶ Glare
- ▶ Simulation of night vision



# Tone-curve

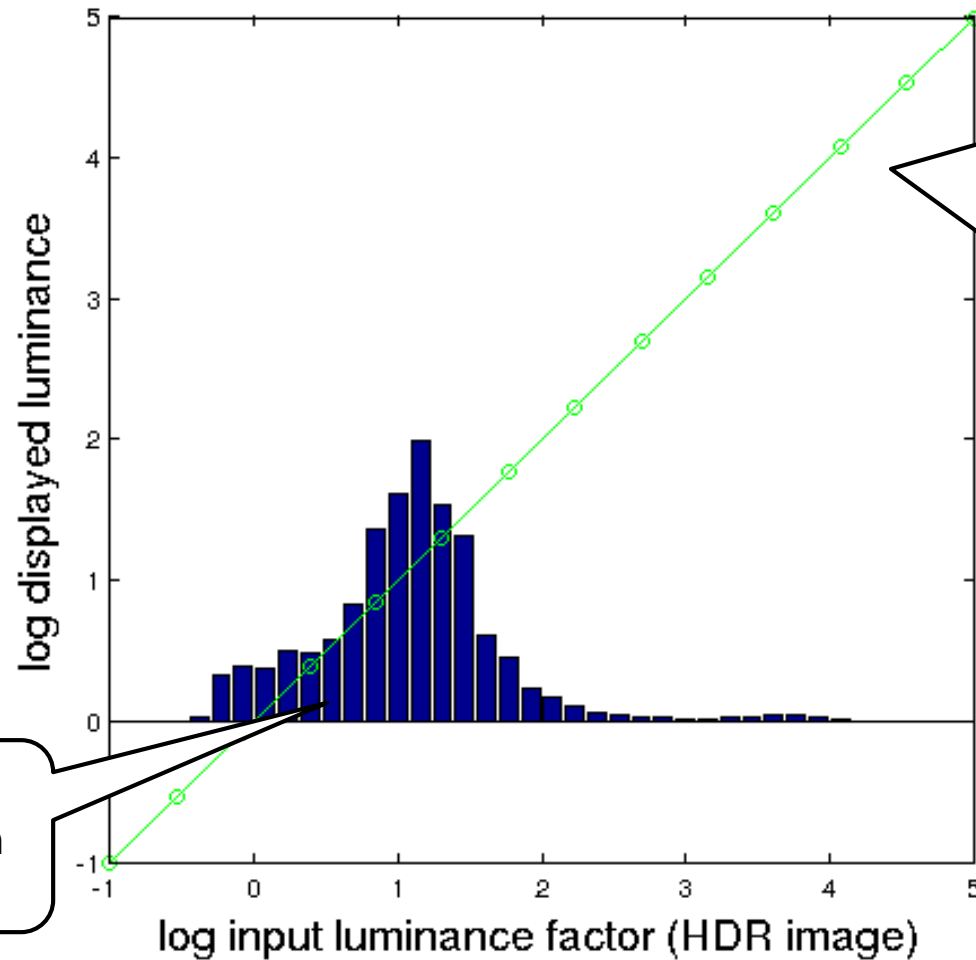
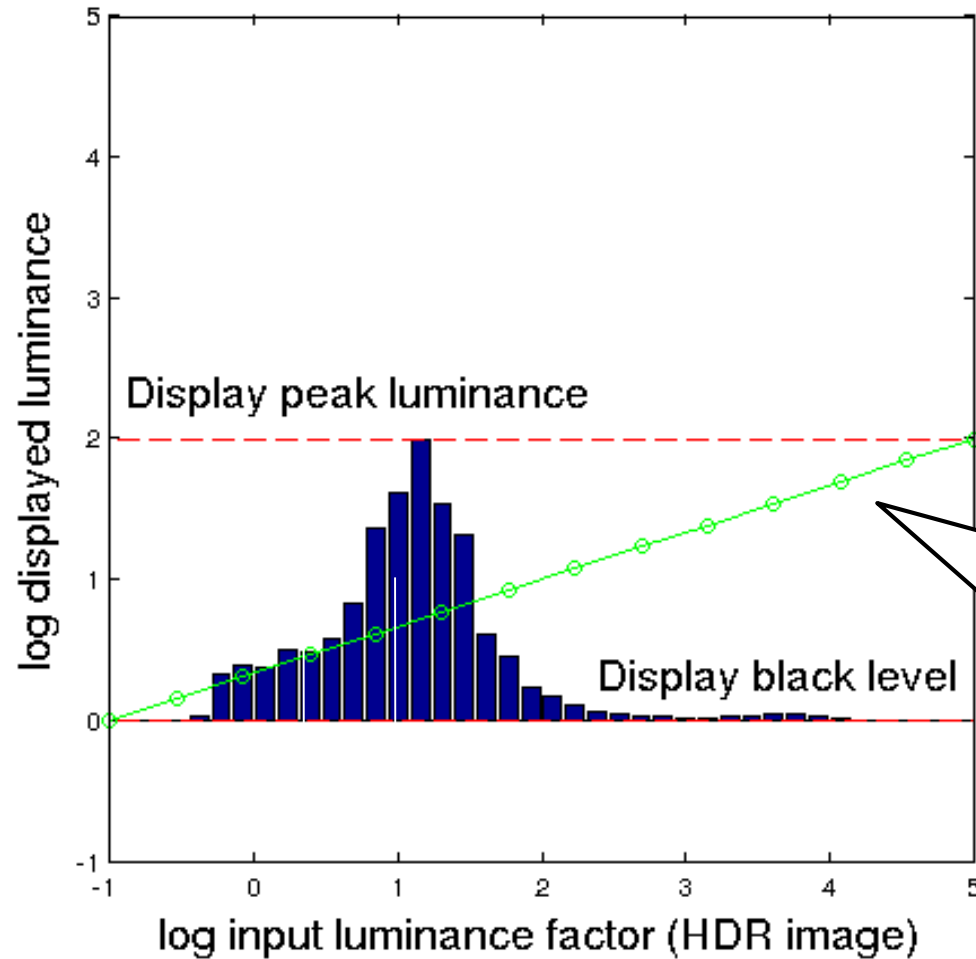


Image histogram

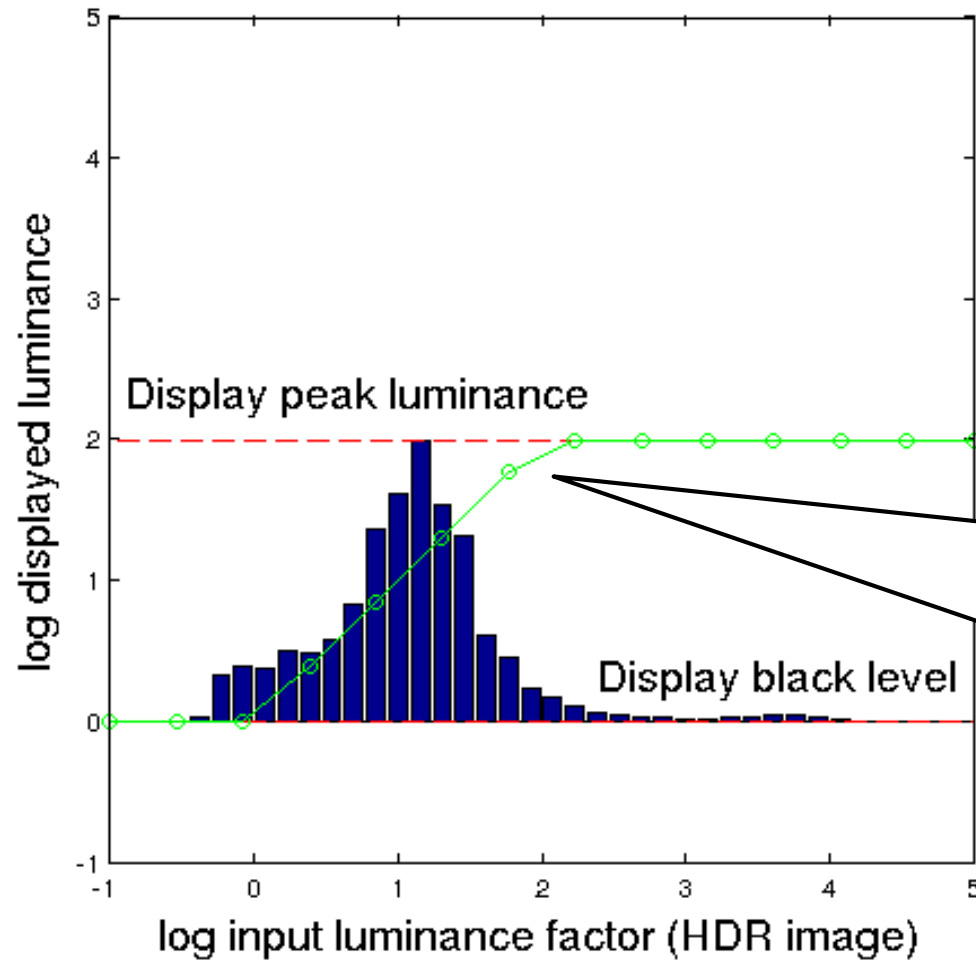
Best tone-mapping is the one which does not do anything, i.e. slope of the tone-mapping curves is equal to 1.

# Tone-curve



But in practice contrast (slope) must be limited due to display limitations.

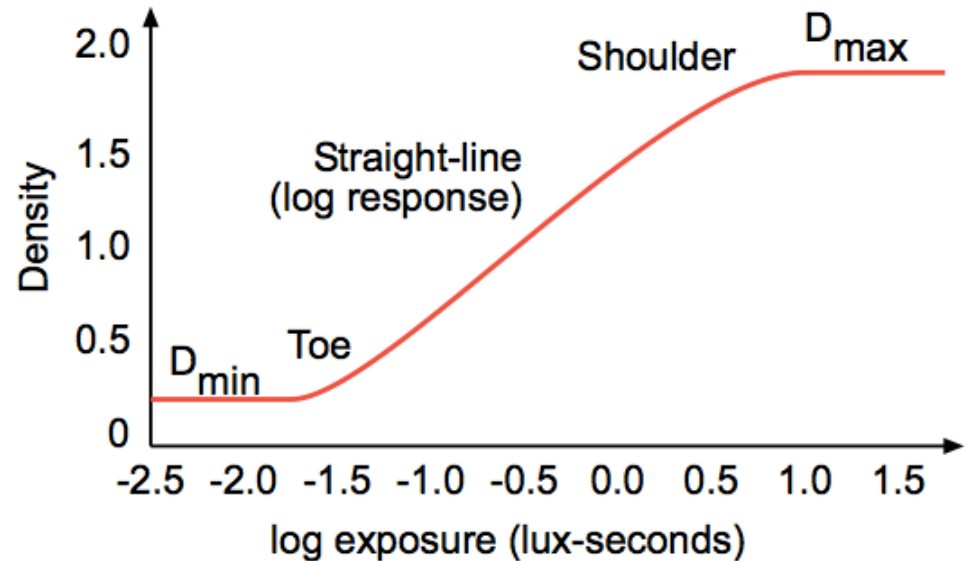
# Tone-curve



Global tone-mapping is a compromise between clipping and contrast compression.

# Sigmoidal tone-curves

- ▶ Very common in digital cameras
  - ▶ Mimic the response of analog film
  - ▶ Analog film has been engineered over many years to produce good tone-reproduction
- ▶ Fast to compute



# Sigmoidal tone mapping

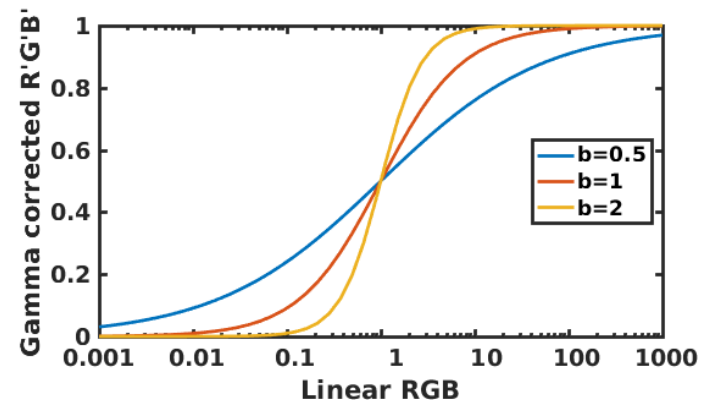
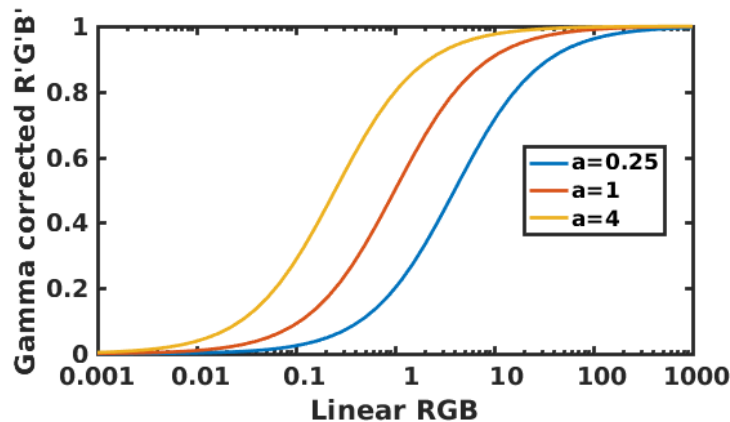
- ▶ Simple formula for a sigmoidal tone-curve:

$$R'(x, y) = \frac{R(x, y)^b}{\left(\frac{L_m}{a}\right)^b + R(x, y)^b}$$

where  $L_m$  is the geometric mean (or mean of logarithms):

$$L_m = \exp\left(\frac{1}{N} \sum_{(x,y)} \ln(L(x, y))\right)$$

and  $L(x, y)$  is the luminance of the pixel  $(x, y)$ .



# Sigmoidal tone mapping example

$a=0.25$



$a=1$



$a=4$



$b=0.5$

$b=1$

$b=2$



# Histogram equalization

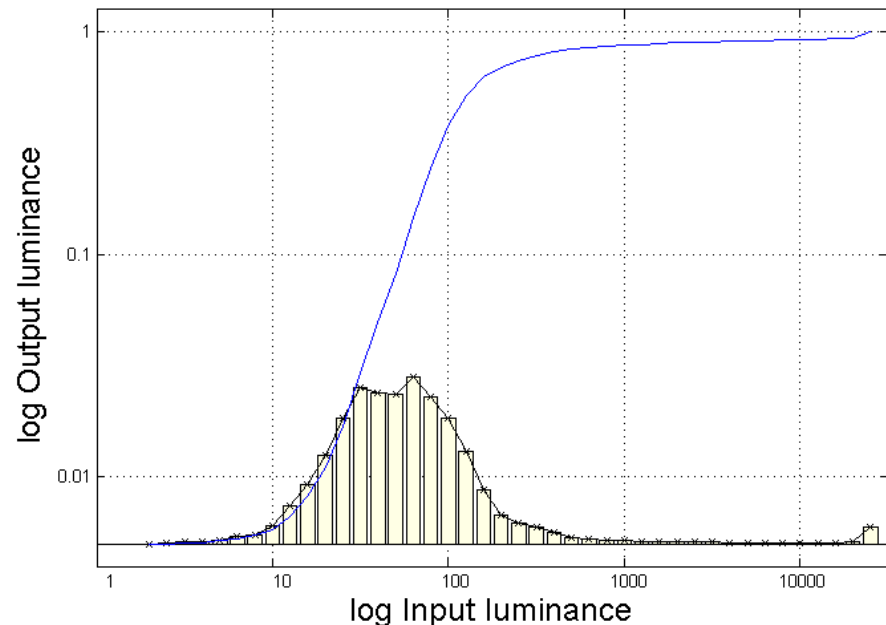
- ▶ 1. Compute cumulative image histogram

$$c(I) = \frac{1}{N} \sum_{i=0}^I h(i) = c(I-1) + \frac{1}{N} h(I)$$

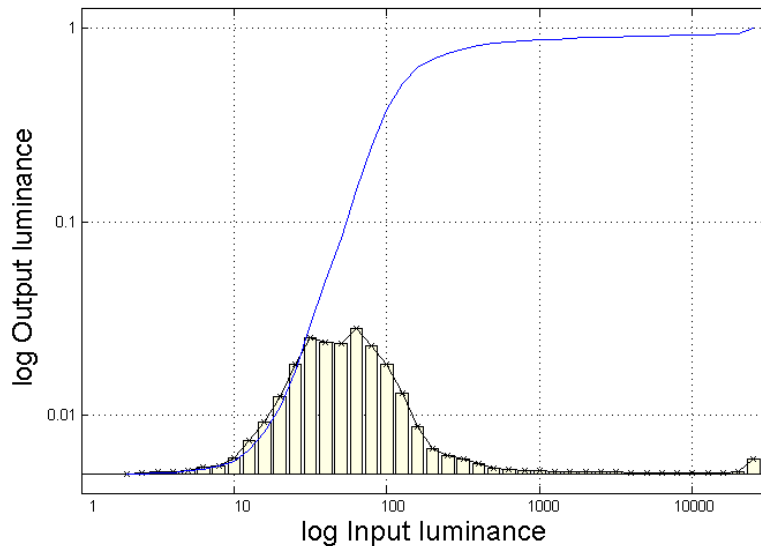
- ▶ For HDR, operate in the log domain
- ▶ 2. Use the cumulative histogram as a tone-mapping function

$$Y_{out} = c(Y_{in})$$

- ▶ For HDR, map the log-I0 values to the  $[-dr_{out}; 0]$  range
  - ▶ where  $dr_{out}$  is the target dynamic range (of a display)



# Histogram equalization



- ▶ Steepest slope for strongly represented bins
  - ▶ If many pixels have the same value - enhance contrast
  - ▶ Reduce contrast, if few pixels
- ▶ Histogram Equalization distributes contrast distortions relative to the “importance” of a brightness level



# Histogram adjustment with a linear ceiling

- ▶ [Larson et al. 1997, IEEE TVCG]

Linear mapping



Histogram equalization

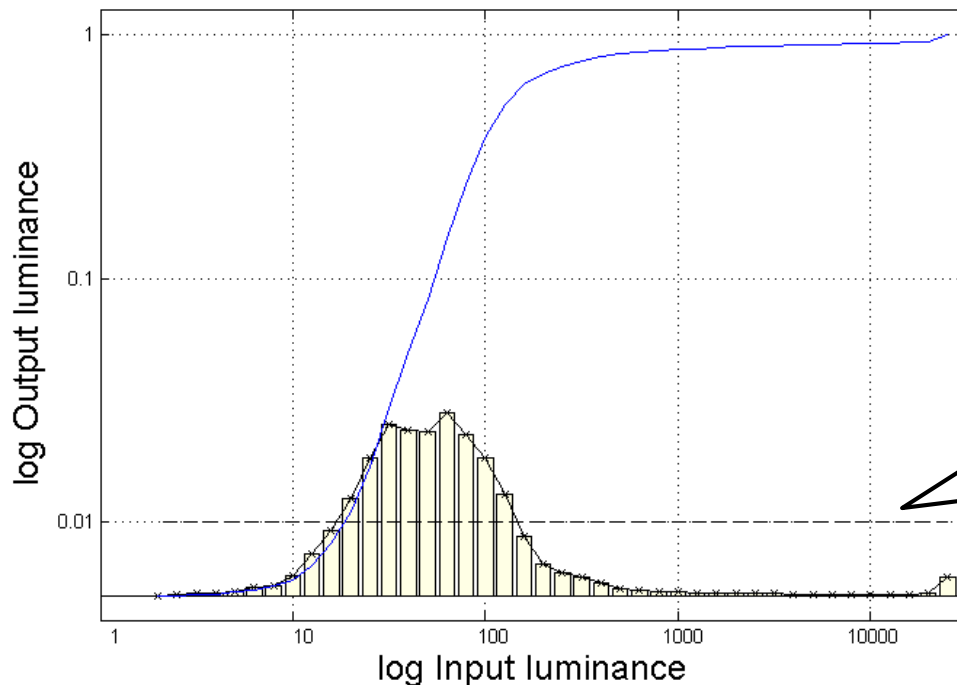


Histogram equalization  
with ceiling



# Histogram adjustment with a linear ceiling

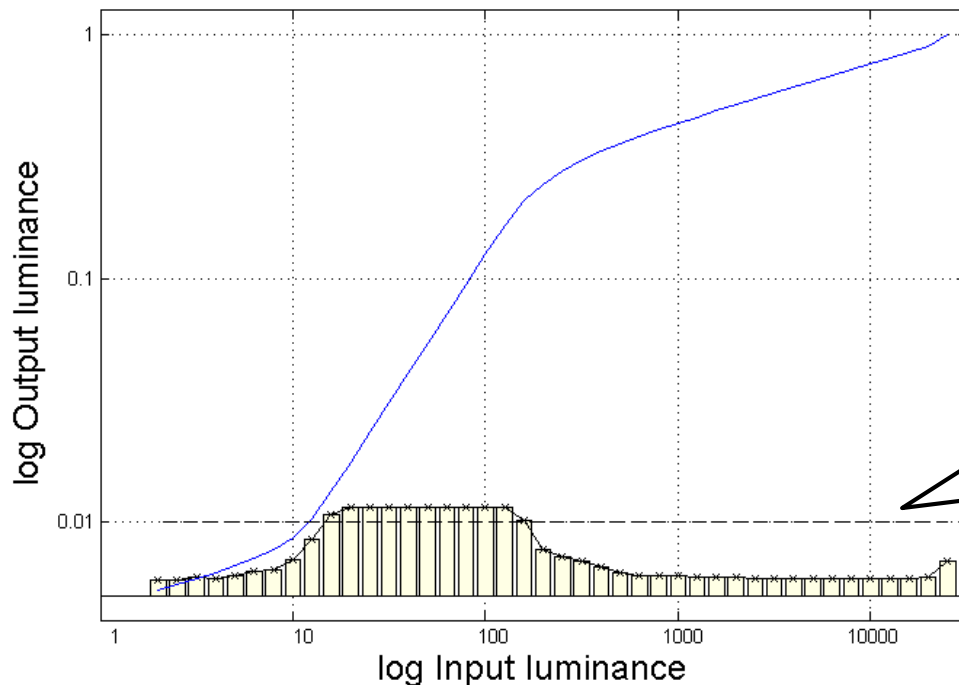
- ▶ Truncate the bins that exceed the ceiling;
- ▶ Distribute the removed counts to all bins;
- ▶ Repeat until converges



Ceiling, based on  
the maximum  
permissible  
contrast

# Histogram adjustment with a linear ceiling

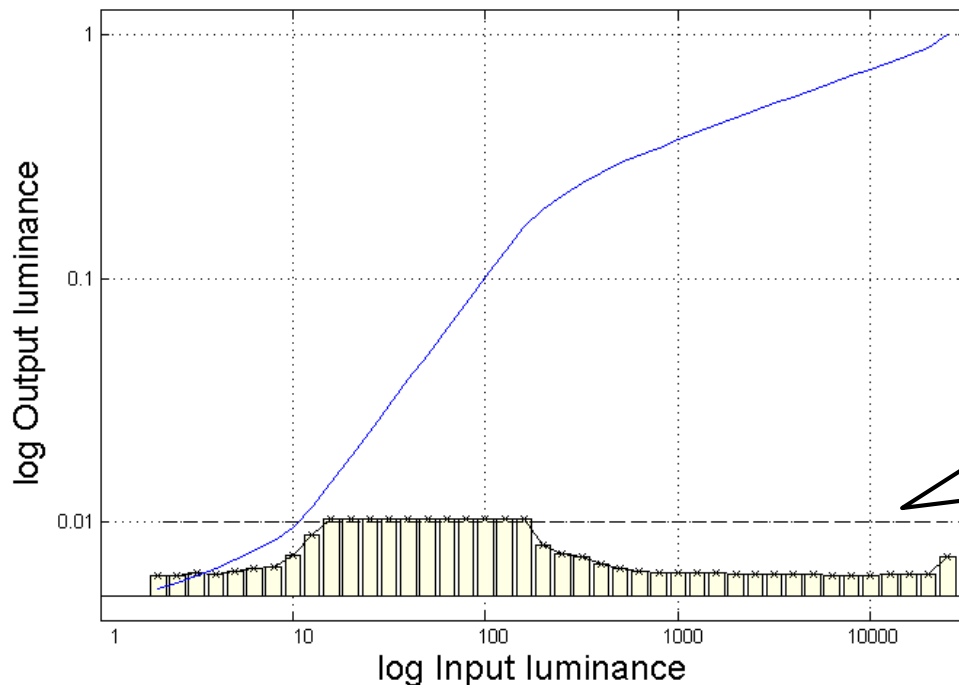
- ▶ Truncate the bins that exceed the ceiling;
- ▶ Distribute the removed counts to all bins;
- ▶ Repeat until converges



Ceiling, based on  
the maximum  
permissible  
contrast

# Histogram adjustment with a linear ceiling

- ▶ Truncate the bins that exceed the ceiling;
- ▶ Distribute the removed counts to all bins;
- ▶ Repeat until converges

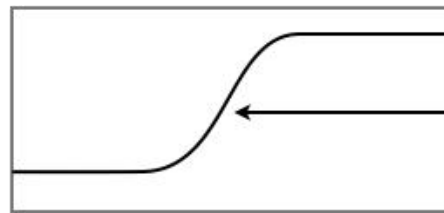


Ceiling, based on  
the maximum  
permissible  
contrast

# Tone-curve as an optimization problem



input scene



tone-mapping



display

Goal: Minimize the visual difference between the input and displayed images

argmin  $E$

Visual  
metric

Display  
model

# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
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- ▶ **Color transfer**
- ▶ Base-detail separation
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# Colour transfer in tone-mapping

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- ▶ Many tone-mapping operators work on luminance
  - ▶ For speed
  - ▶ To avoid colour artefacts
- ▶ Colours must be transferred later from the original image
- ▶ Colour transfer in the linear RGB colour space:

The diagram shows the formula for output color channel (red):  $R_{out} = \left( \frac{R_{in}}{L_{in}} \right)^s \cdot L_{out}$ . Callouts identify the components: 'Output color channel (red)' points to  $R_{out}$ ; 'Saturation parameter' points to  $s$ ; and 'Resulting luminance' points to  $L_{out}$ .

$$\text{Output color channel (red)} \rightarrow R_{out} = \left( \frac{R_{in}}{L_{in}} \right)^s \cdot L_{out}$$

Saturation parameter  $s$

Resulting luminance  $L_{out}$

- ▶ The same formula applies to green (G) and blue (B) linear colour values.

# Colour transfer: out-of-gamut problem

- Colours often fall outside the colour gamut when contrast is compressed



Original image

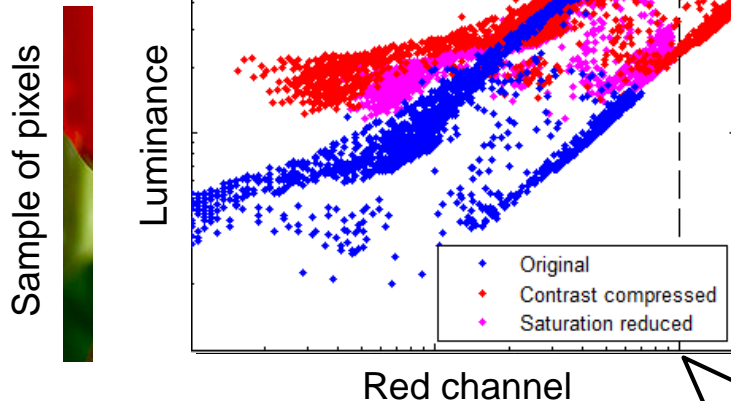


Contrast reduced ( $s=1$ )



Saturation reduced ( $s=0.6$ )

Colours before/after processing



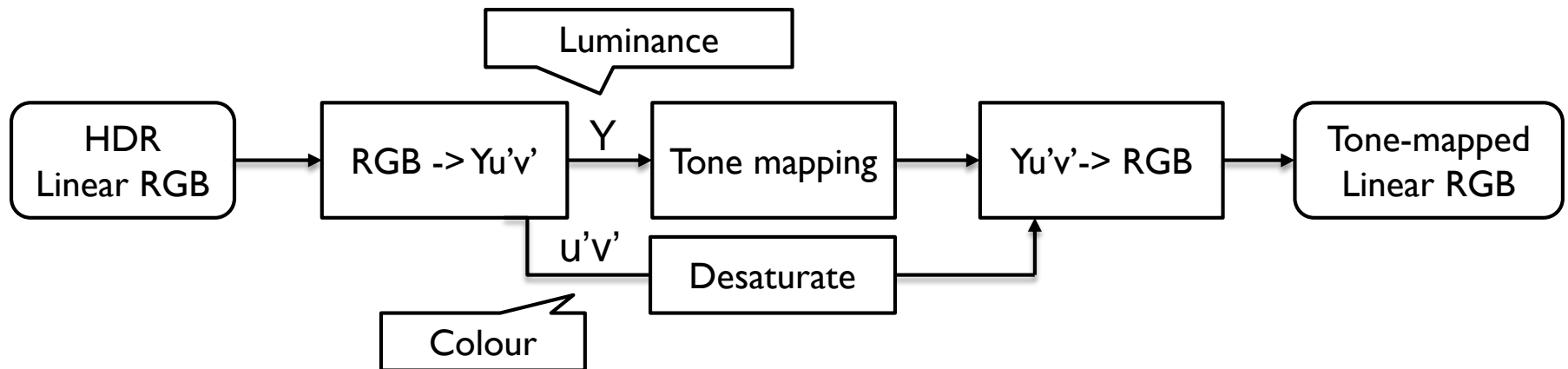
- Reduction in saturation is needed to bring the colors into gamut

Gamut boundary



# Colour transfer: alternative method

- ▶ Colour transfer in linear RGB will alter resulting luminance
- ▶ Colours can be also transferred and saturation adjusted using CIE  $u'v'$  chromatic coordinates



- ▶ To correct saturation:  $u'_{out} = (u'_{in} - u'_w) \cdot s + u'_w$   $u'_w = 0.1978$   
 $v'_{out} = (v'_{in} - v'_w) \cdot s + v'_w$   $v'_w = 0.4683$
- Chroma of the white

# Techniques

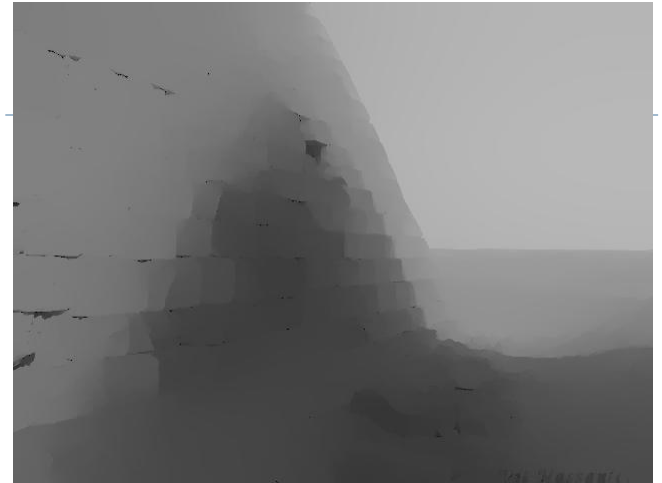
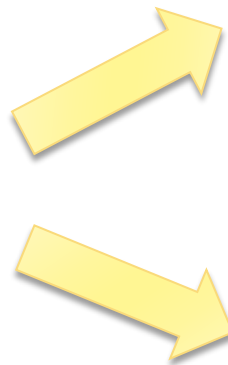
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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Color transfer
- ▶ **Base-detail separation**
- ▶ Glare
- ▶ Simulation of night vision

# Illumination & reflectance separation



Input



Illumination



Reflectance

$$Y = I \times R$$

Image

Illumination

Reflectance

# Illumination and reflectance

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## Reflectance

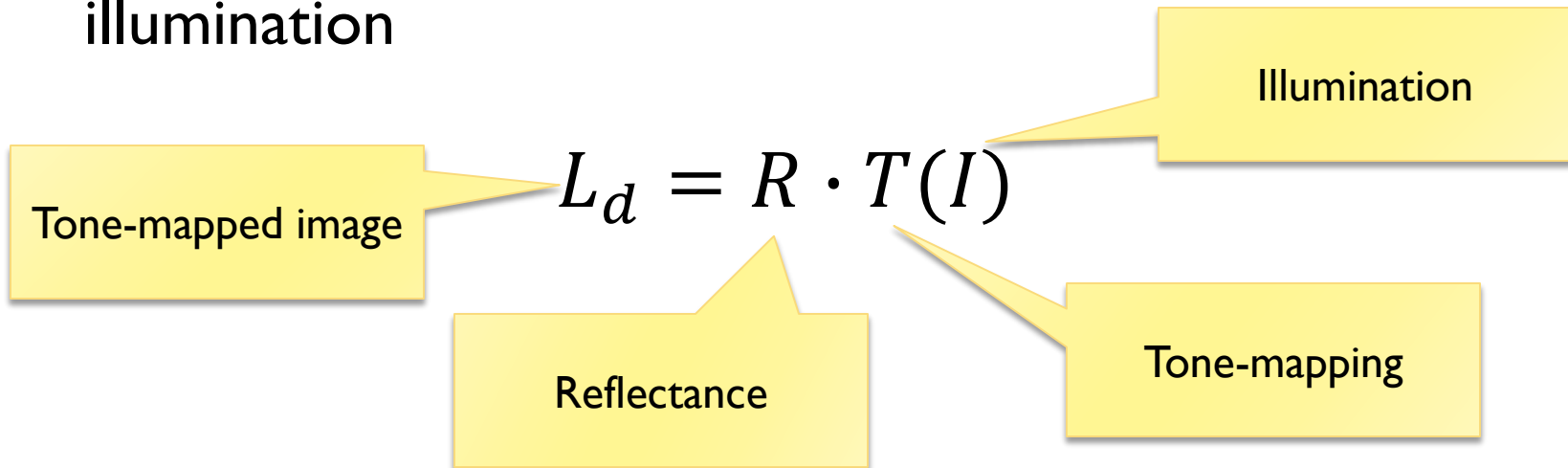
- ▶ White  $\approx 90\%$
- ▶ Black  $\approx 3\%$
- ▶ Dynamic range  $< 100:1$
- ▶ Reflectance critical for object & shape detection

## Illumination

- ▶ Sun  $\approx 10^9 \text{ cd/m}^2$
- ▶ Lowest perceivable luminance  $\approx 10^{-6} \text{ cd/m}^2$
- ▶ Dynamic range 10,000:1 or more
- ▶ Visual system partially discounts illumination

# Reflectance & Illumination TMO

- ▶ Hypothesis: *Distortions in reflectance are more apparent than the distortions in illumination*
- ▶ Tone mapping could preserve reflectance but compress illumination



- ▶ for example:

$$L_d = R \cdot (I / L_{white})^c \cdot L_{white}$$

# How to separate the two?

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- ▶ (Incoming) illumination – slowly changing
  - ▶ except very abrupt transitions on shadow boundaries
- ▶ Reflectance – low contrast and high frequency variations



# Gaussian filter

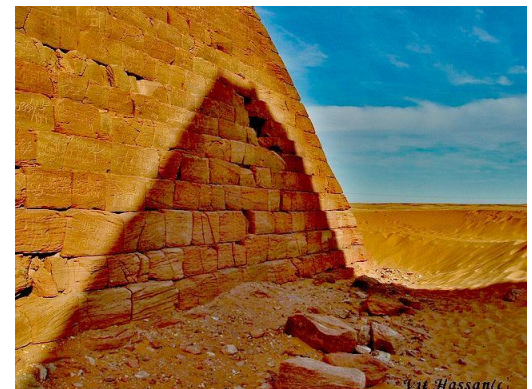
$$f(x) = \frac{1}{2\pi\sigma_s} e^{\frac{-x^2}{2\sigma_s^2}}$$

- ▶ First order approximation



- ▶ Blurs sharp boundaries
- ▶ Causes halos

Tone mapping  
result

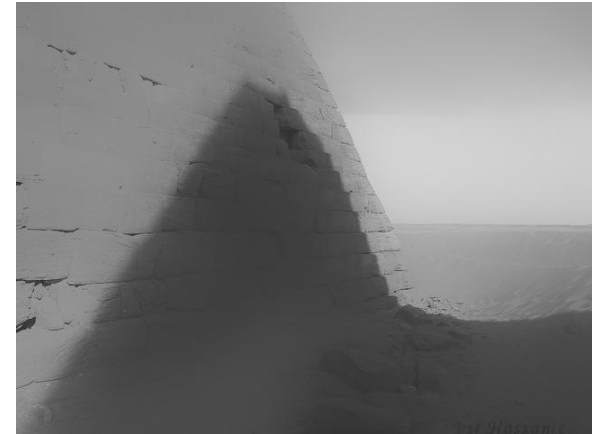




# Bilateral filter

$$I_p \approx \frac{1}{k_s} \sum_{t \in \Omega} f(p-t) g(L_p - L_t) L_p$$

- ▶ Better preserves sharp edges



Tone mapping result

- ▶ Still some blurring on the edges
- ▶ Reflectance is not perfectly separated from illumination near edges

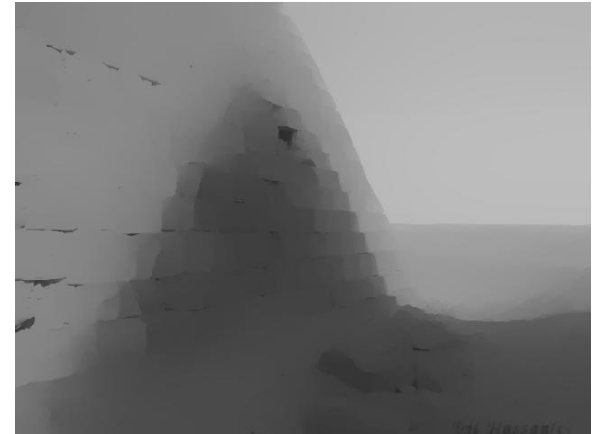




# Weighted-least-squares (WLS) filter

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- ▶ Stronger smoothing and still distinct edges



Tone mapping result

- ▶ Can produce stronger effects with fewer artifacts
- ▶ See image processing lecture

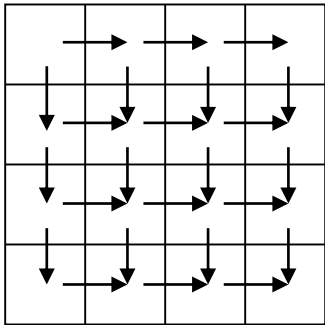


[Farbman et al., SIGGRAPH 2008]

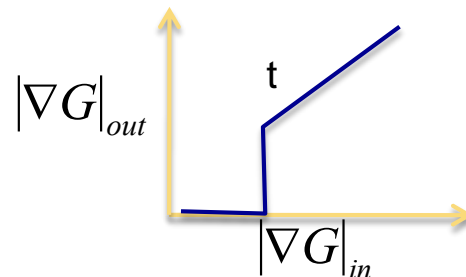
# Retinex

- ▶ Retinex algorithm was initially intended to separate reflectance from illumination [Land 1964]
- ▶ There are many variations of Retinex, but the general principle is to eliminate from an image small gradients, which are attributed to the illumination

1 step: compute gradients in log domain



2<sup>nd</sup> step: set to 0 gradients less than the threshold



3<sup>rd</sup> step: reconstruct an image from the vector field

$$\nabla^2 I = \text{div } G$$

For example by solving the Poisson equation

# Retinex examples

From: <http://dragon.larc.nasa.gov/retinex/757/>



From: [http://www.ipol.im/pub/algo/lmps\\_retinex\\_poisson\\_equation/#ref\\_1](http://www.ipol.im/pub/algo/lmps_retinex_poisson_equation/#ref_1)

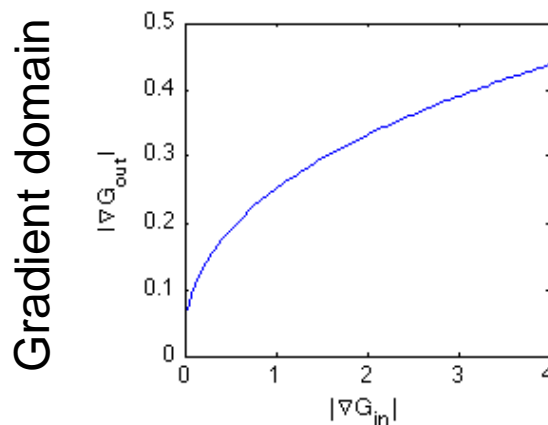
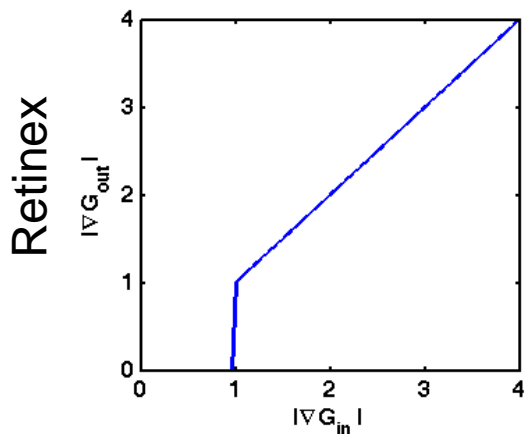


# Gradient domain HDR compression



[Fattal et al.,  
SIGGRAPH 2002]

- ▶ Similarly to Retinex, it operates on log-gradients
- ▶ But the function amplifies small contrast instead of removing it



- Contrast compression achieved by global contrast reduction
  - Enhance reflectance, then compress everything

# Techniques

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- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Color transfer
- ▶ Base-detail separation
- ▶ **Glare**
- ▶ Simulation of night vision



# Glare

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"Alan Wake" © Remedy Entertainment

# Glare Illusion

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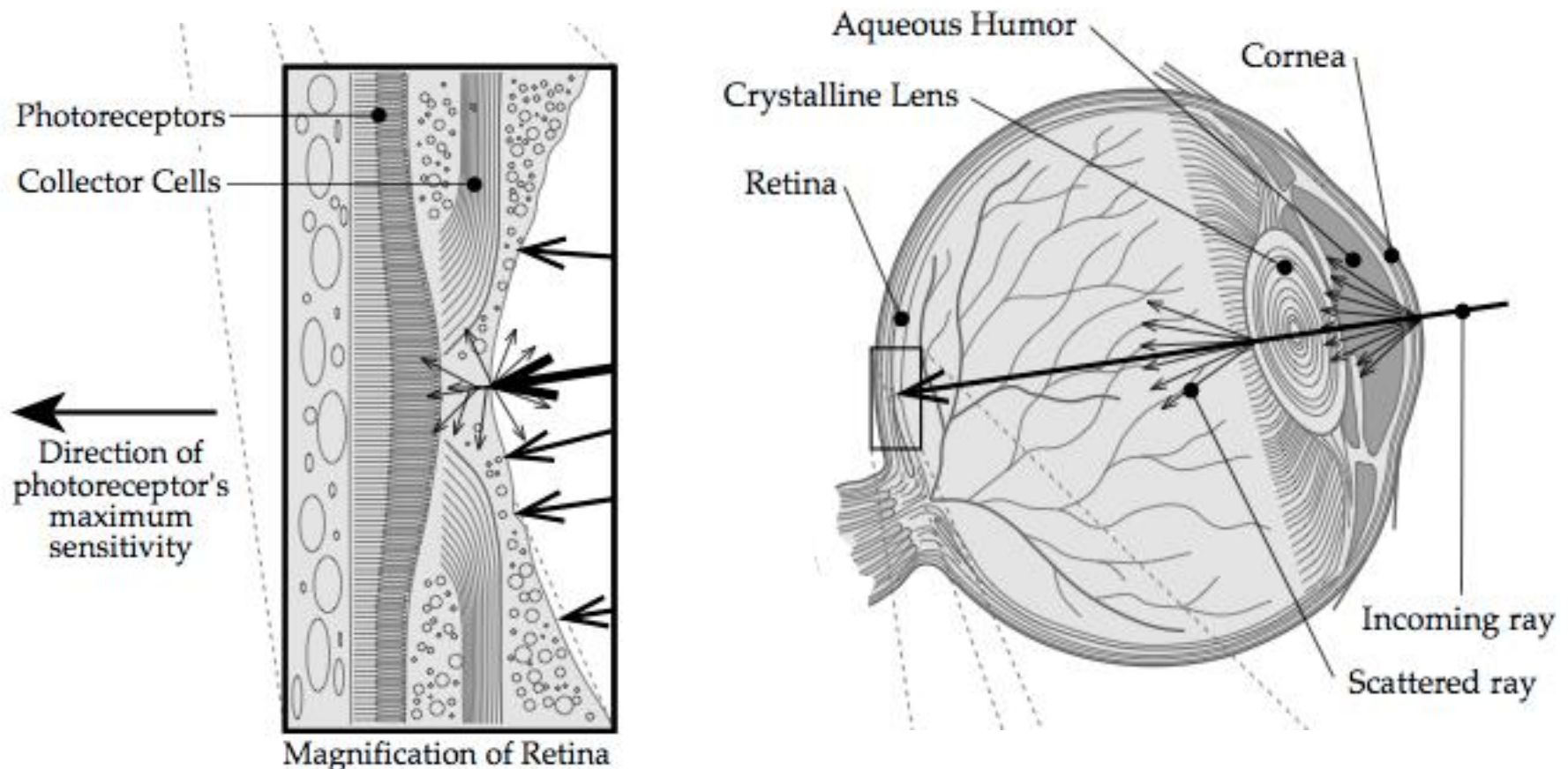
Photography



Painting



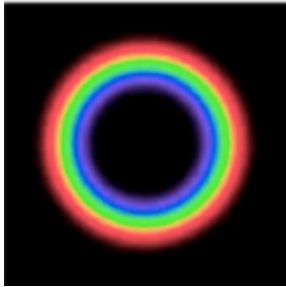
# Scattering of the light in the eye



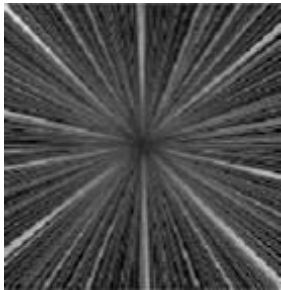
From: Sekuler, R., and Blake, R. Perception, second ed. McGraw- Hill, New York, 1990



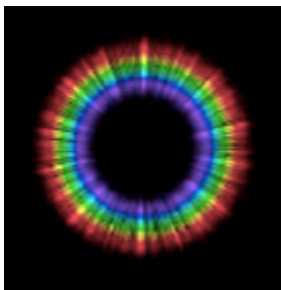
# Ciliary corona and lenticular halo



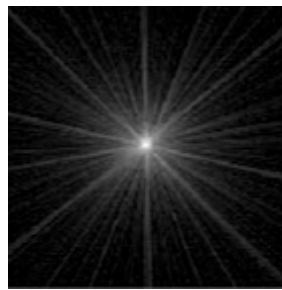
\*



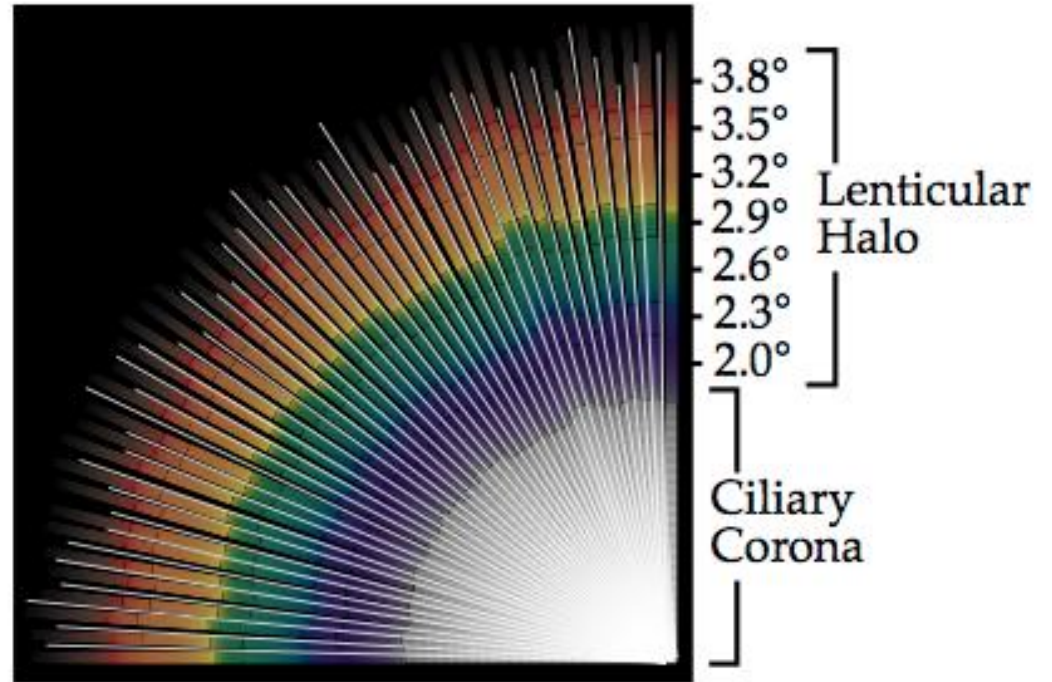
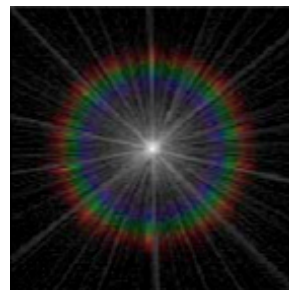
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+



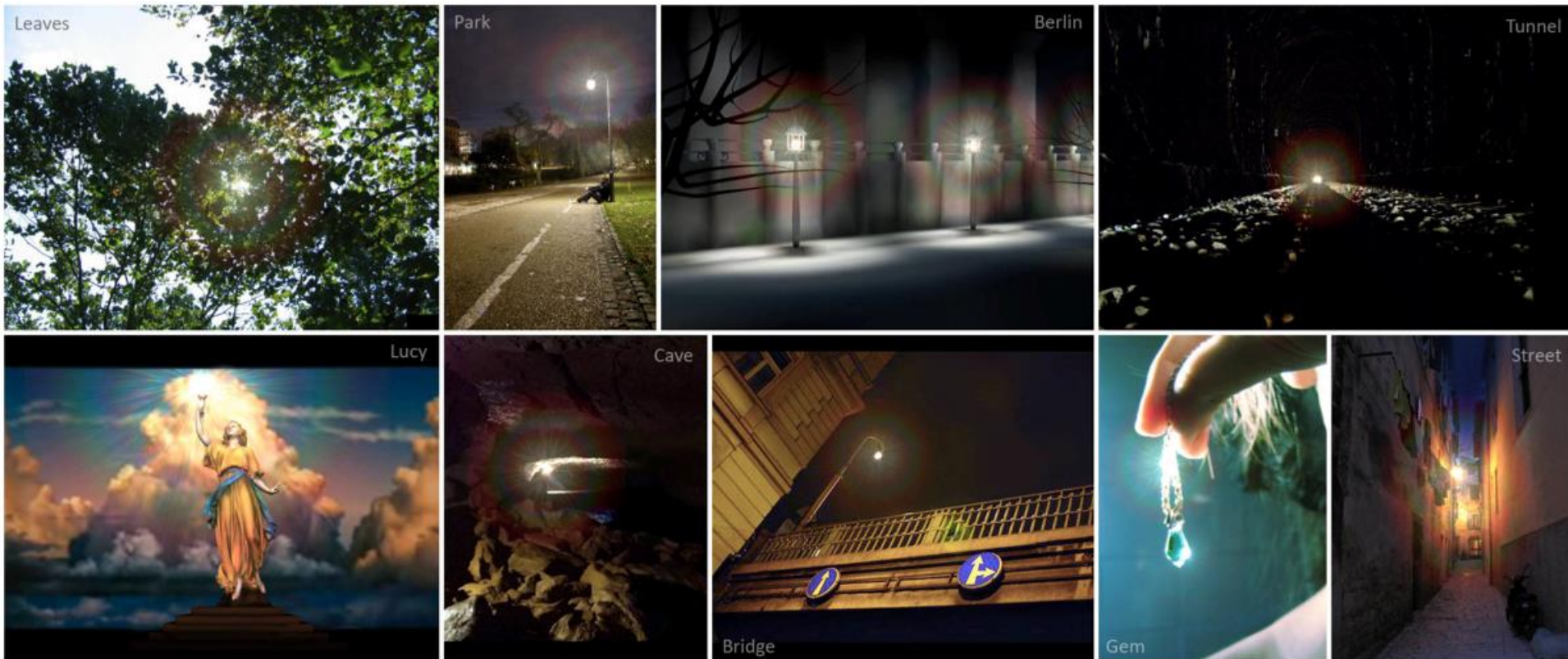
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From: Spencer, G. et al.  
1995. Proc. of  
SIGGRAPH. (1995)

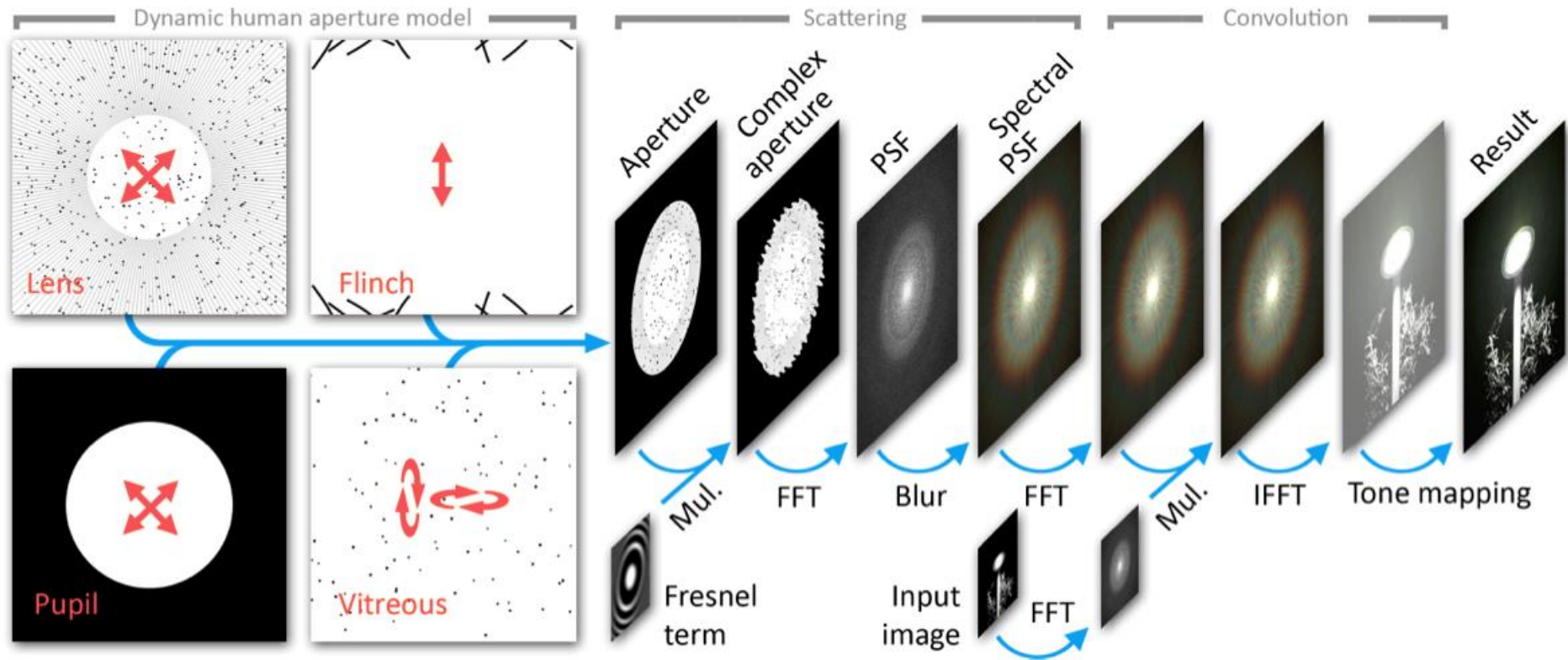
# Examples of simulated glare

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[From Ritschel et al, Eurographics 2009]

# Temporal model of glare (low level)



- ▶ The model assumes that glare is mostly caused by diffraction and scattering
- ▶ Can simulate temporal effects



# Temporal glare

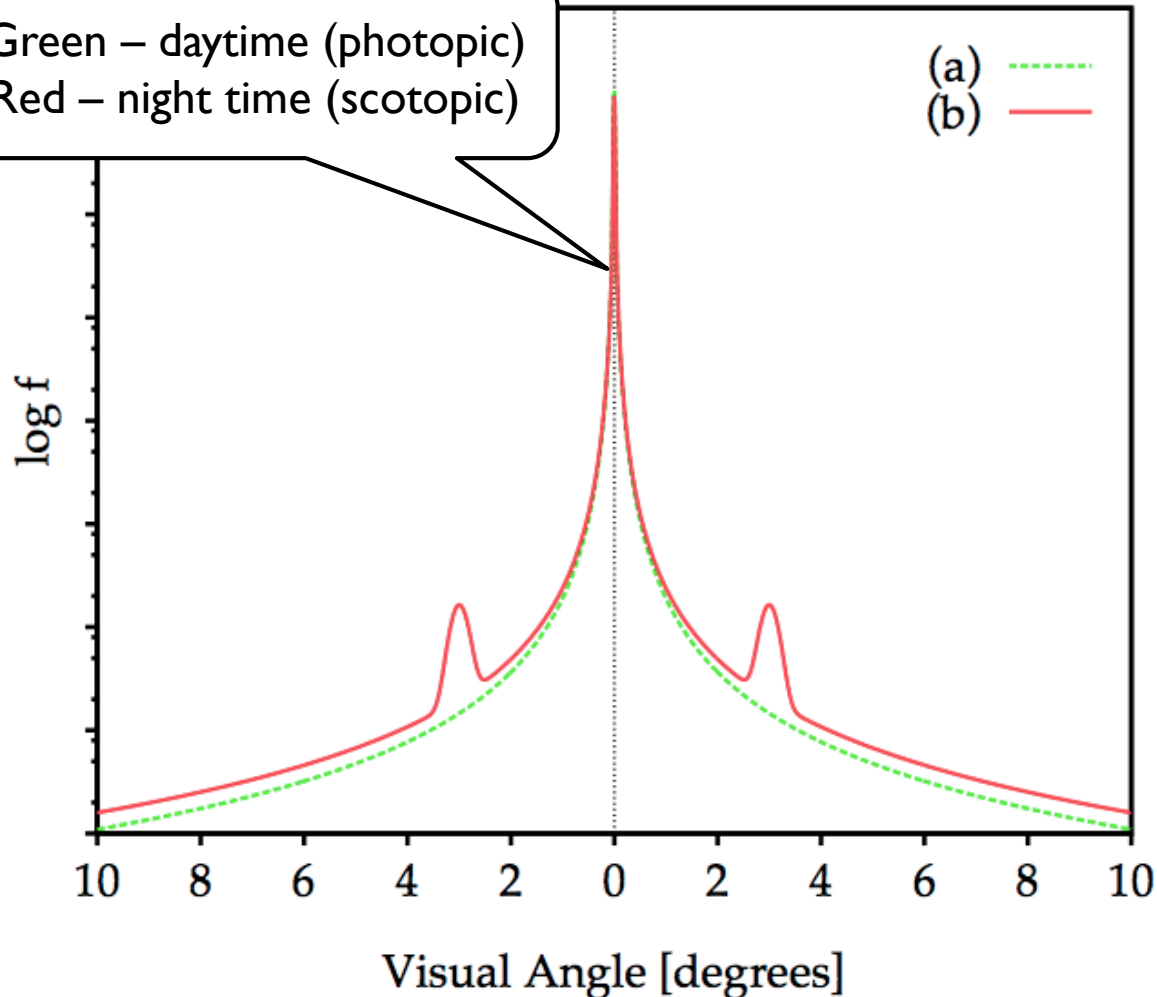
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Dynamic glare



# Point Spread Function of the eye

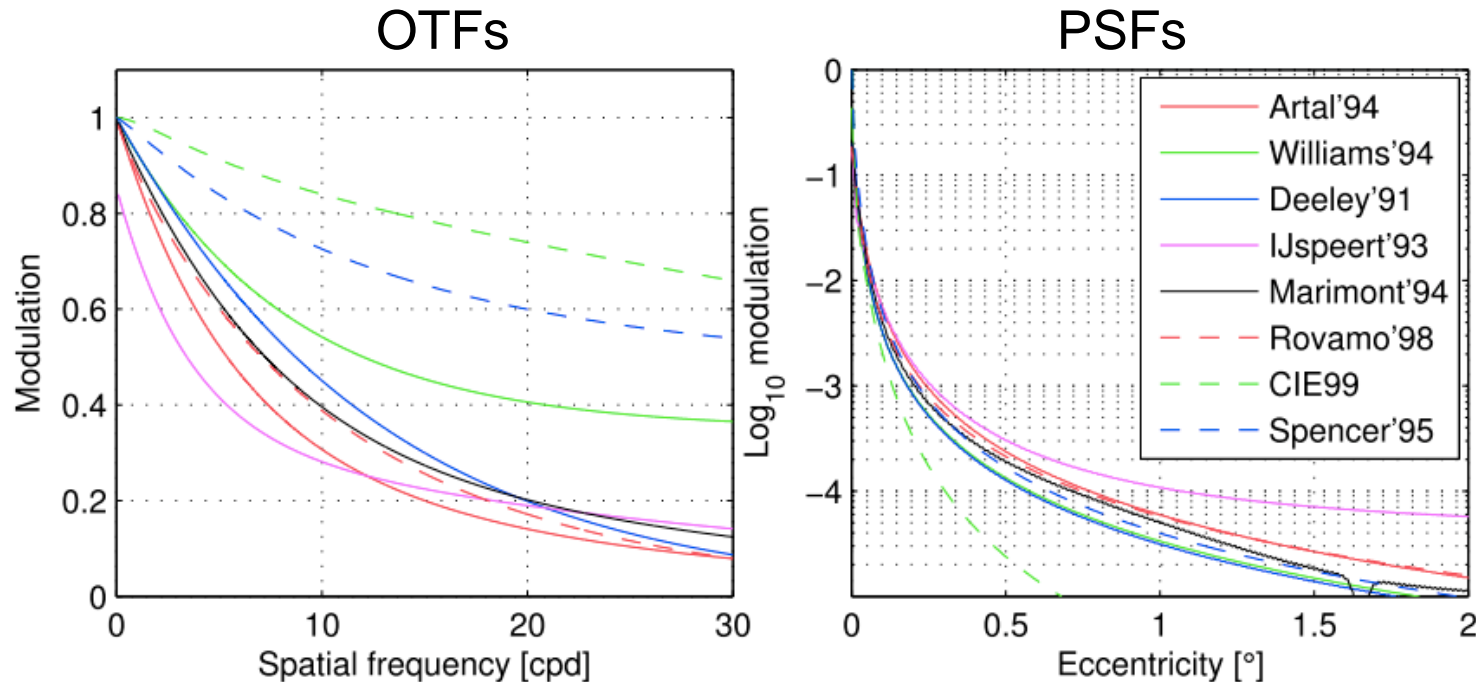
Green – daytime (photopic)  
Red – night time (scotopic)



- ▶ What portion of the light is scattered towards a certain visual angle
- ▶ To simulate:
  - ▶ construct a digital filter
  - ▶ convolve the image with that filter

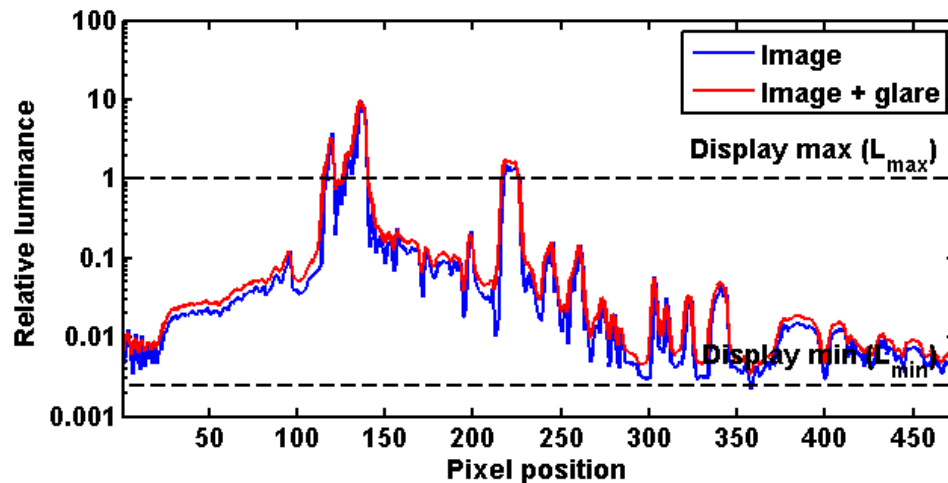
From: Spencer, G. et al. 1995.  
Proc. of SIGGRAPH. (1995)

# PSF vs. OTF (Optical Transfer Function)



- ▶ An OTF is the Fourier transform of a PSF
- ▶ Convolution with larger kernels is faster in the Fourier domain

# Selective application of glare

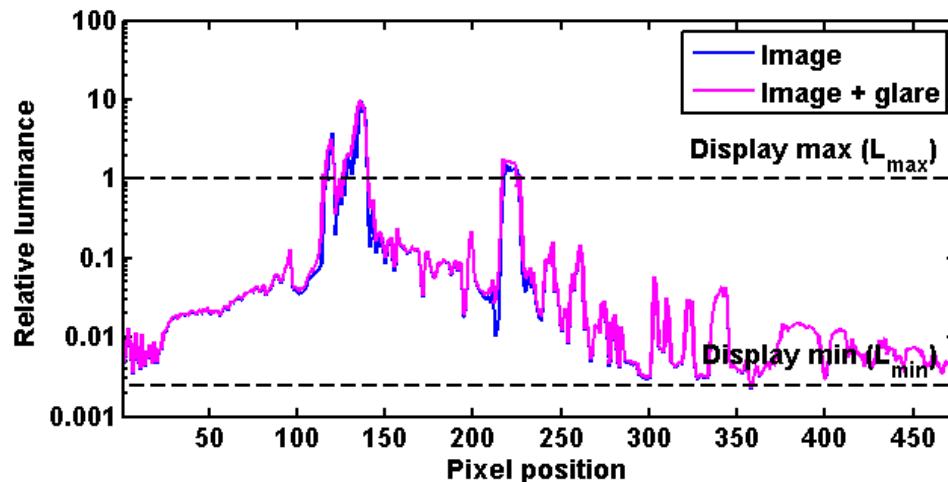


- ▶ A) Glare applied to the entire image

$$I_g = I * G$$

Glare kernel  
(PSF)

- ▶ Reduces image contrast and sharpness



- B) Glare applied only to the clipped pixels

$$I_g = I + I_{clipped} * G - I_{clipped}$$

$$\text{where } I_{clipped} = \begin{cases} I & \text{for } I > 1 \\ 0 & \text{otherwise} \end{cases}$$

Better image quality

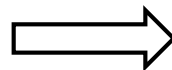
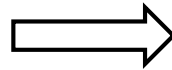
# Selective application of glare

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A) Glare applied to the entire image



Original image



B) Glare applied to clipped pixels only

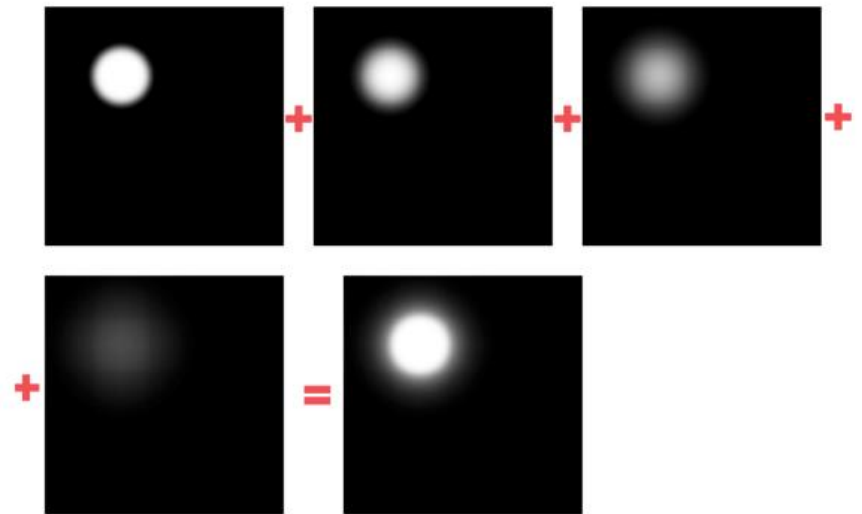




# Glare (or bloom) in games

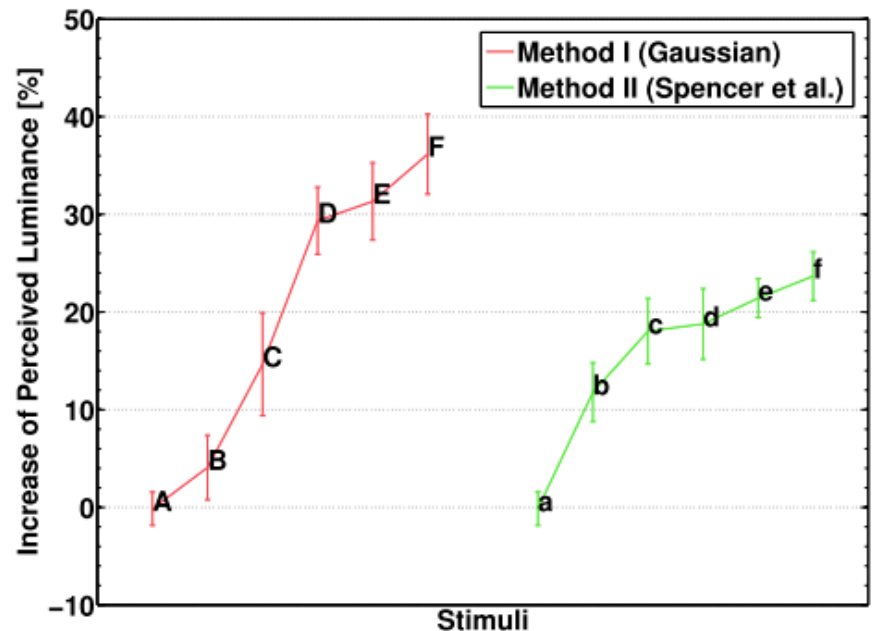
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- ▶ Convolution with large, non-separable filters is too slow
- ▶ The effect is approximated by a combination of Gaussian filters
  - ▶ Each filter with different “sigma”
- ▶ The effect is meant to look good, not be an accurate model of light scattering
- ▶ Some games simulate camera rather than the eye



# Does the exact shape of the PSF matter?

- ▶ The illusion of increased brightness works even if the PSF is very different from the PSF of the eye



red - Gaussian



green - accurate



[Yoshida et al., APGV 2008]

# HDR rendering – motion blur



From LDR pixels

From HDR pixels

# Techniques

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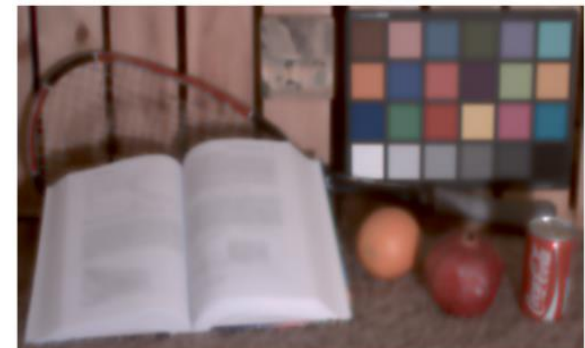
- ▶ Arithmetic of HDR images
- ▶ Display model
- ▶ Tone-curve
- ▶ Color transfer
- ▶ Base-detail separation
- ▶ Glare
- ▶ Simulation of night vision

# What changes at low illumination?

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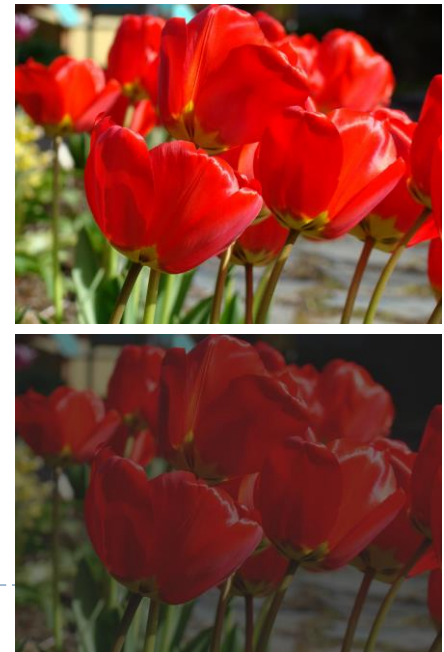
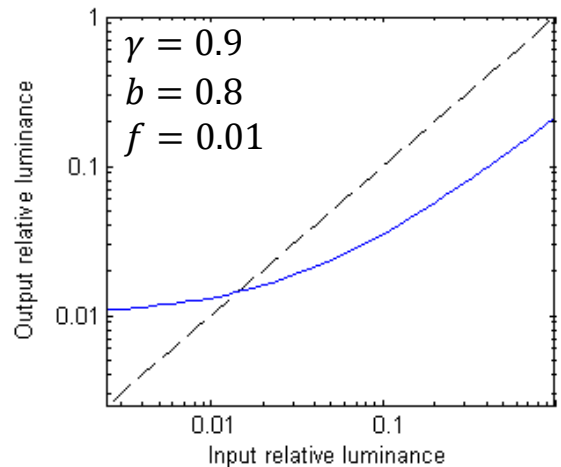
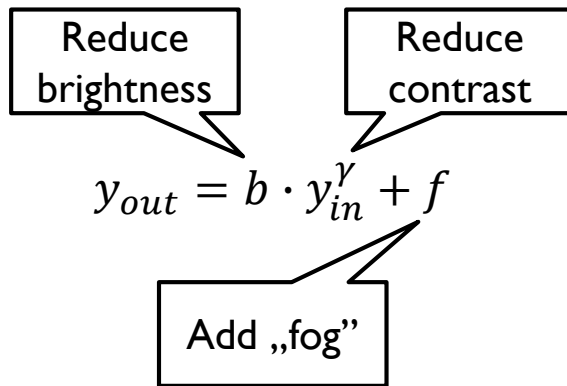
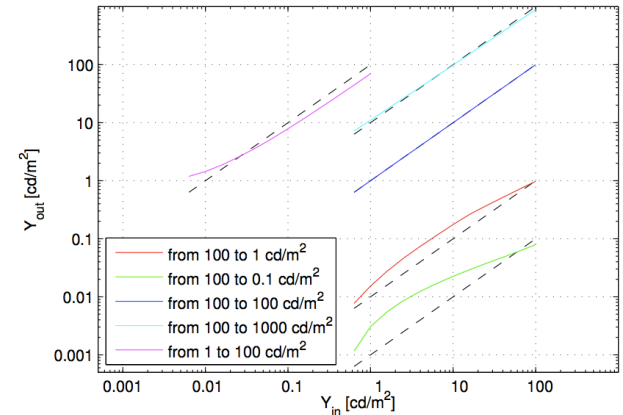
- ▶ **Global contrast**
  - ▶ Relative brightness
- ▶ **Local contrast**
  - ▶ Visibility of small details
- ▶ **Color**
  - ▶ Purkinje shift
  - ▶ Saturation

0.1 -> 100 cd/m<sup>2</sup>



# Brightness reduction – tone-curve

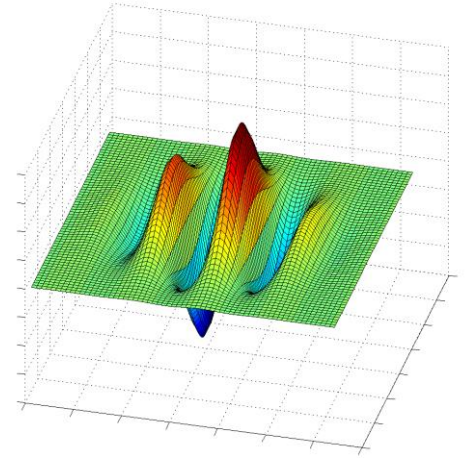
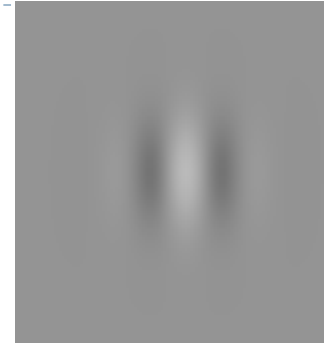
- ▶ Perceptually-based night-vision tone-curve
  - ▶ [Wanat et al. 2014]
  - ▶ Requires rather complex optimization
- ▶ Empirical approach (not perceptual)



# Local contrast

## ▶ Gabor patch

- ▶ basic contrast stimulus
- ▶ the shape matches the response pattern of the receptive fields on the retina

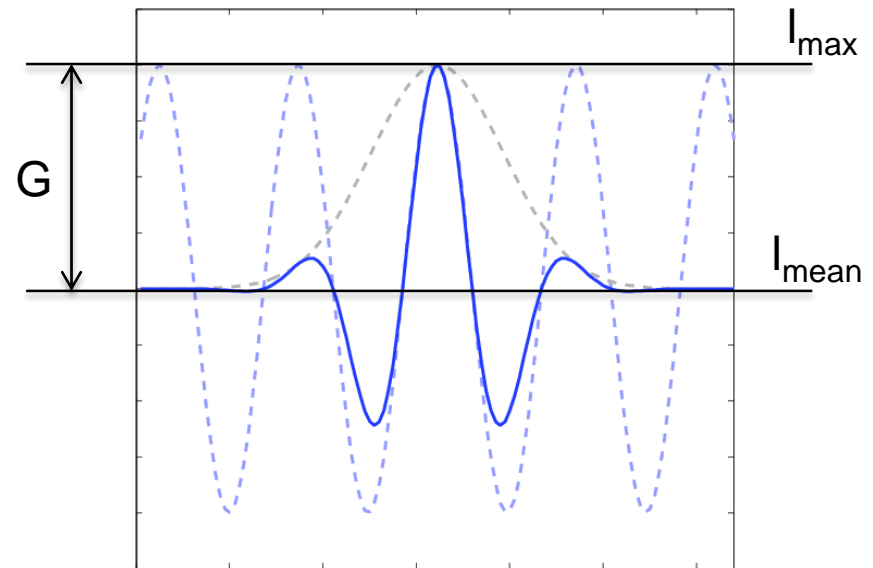


Contrast

$$G = l_{\max} - l_{\text{mean}}$$

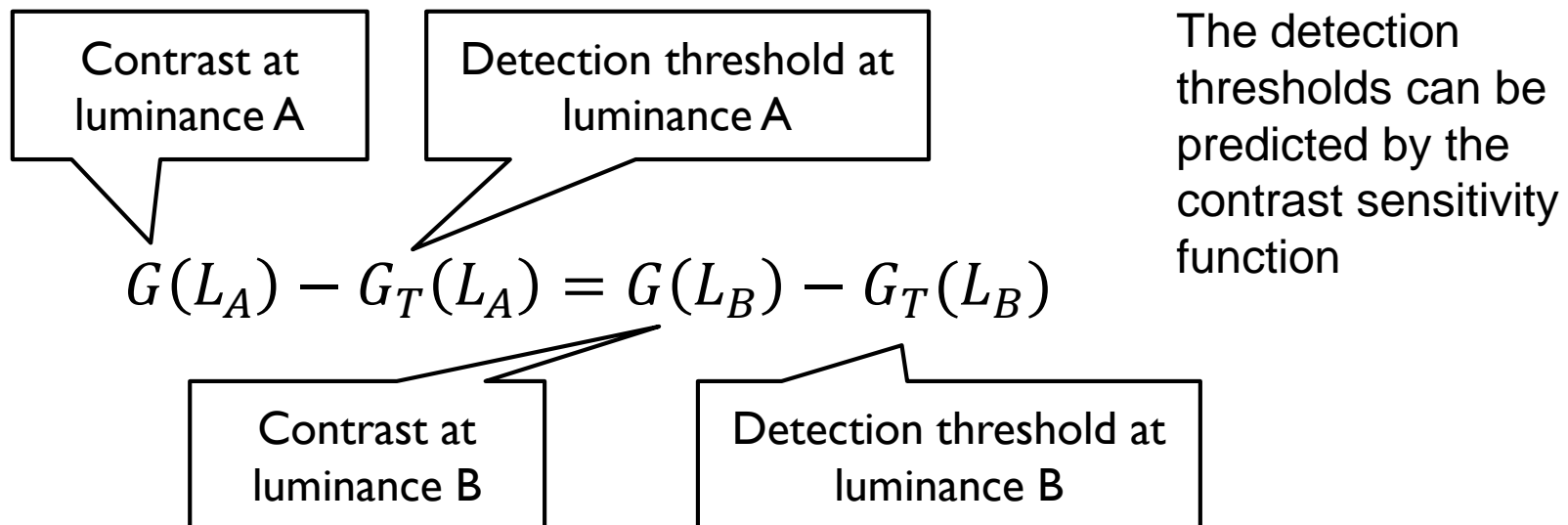
Max log  
luminance

Mean log  
luminance



# Supra-threshold contrast matching

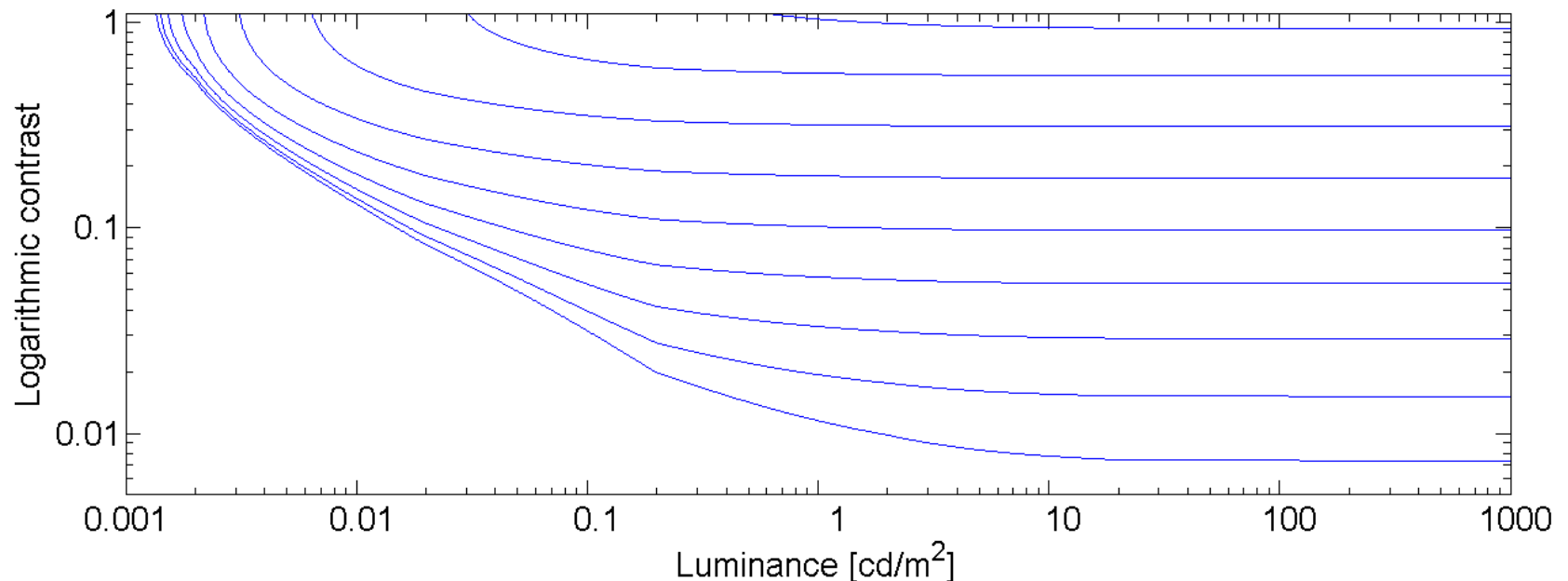
- ▶ Kulikowski's model of matching contrast [Kulikowski 1976]
  - ▶ Contrast is perceived the same at different luminance levels when the physical contrast reduced by the corresponding detection threshold is equal at those luminance levels



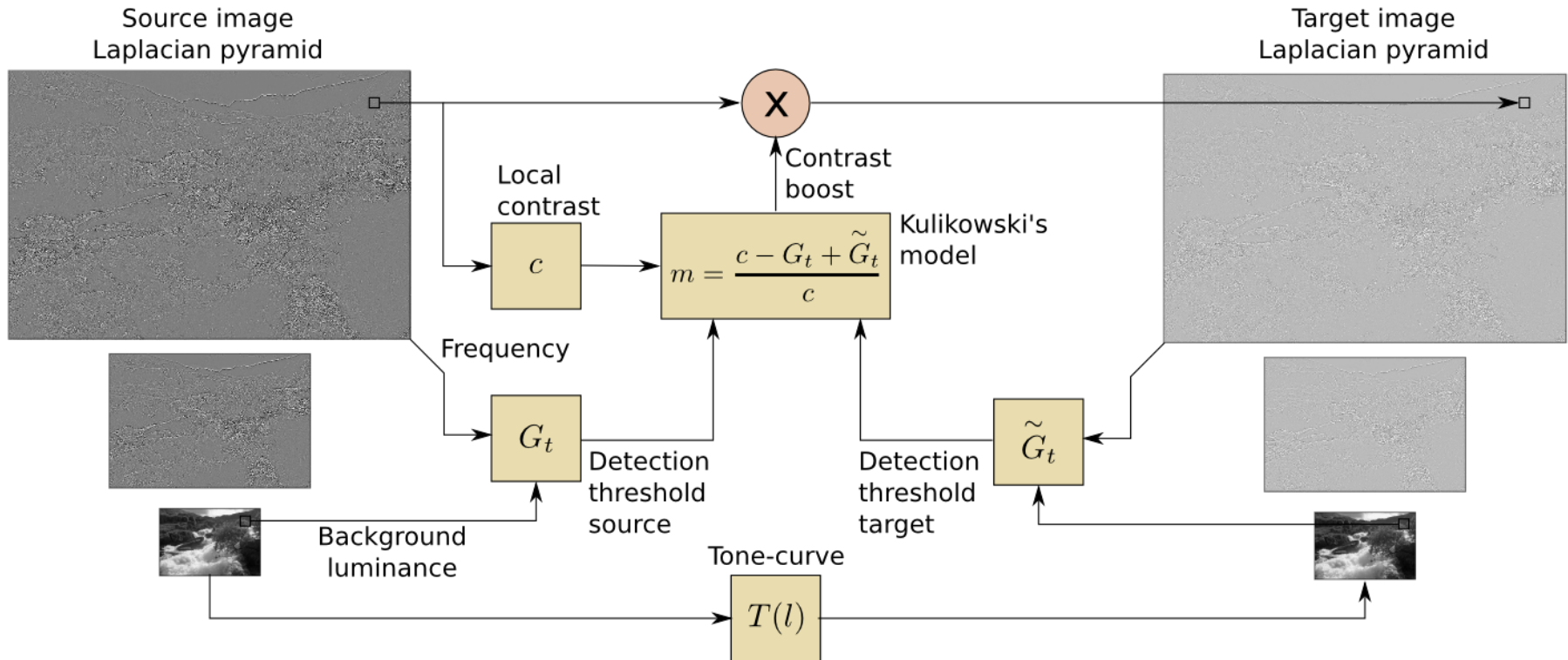


# Supra-threshold contrast matching

- ▶ The lines connect contrast of the same perceived magnitude

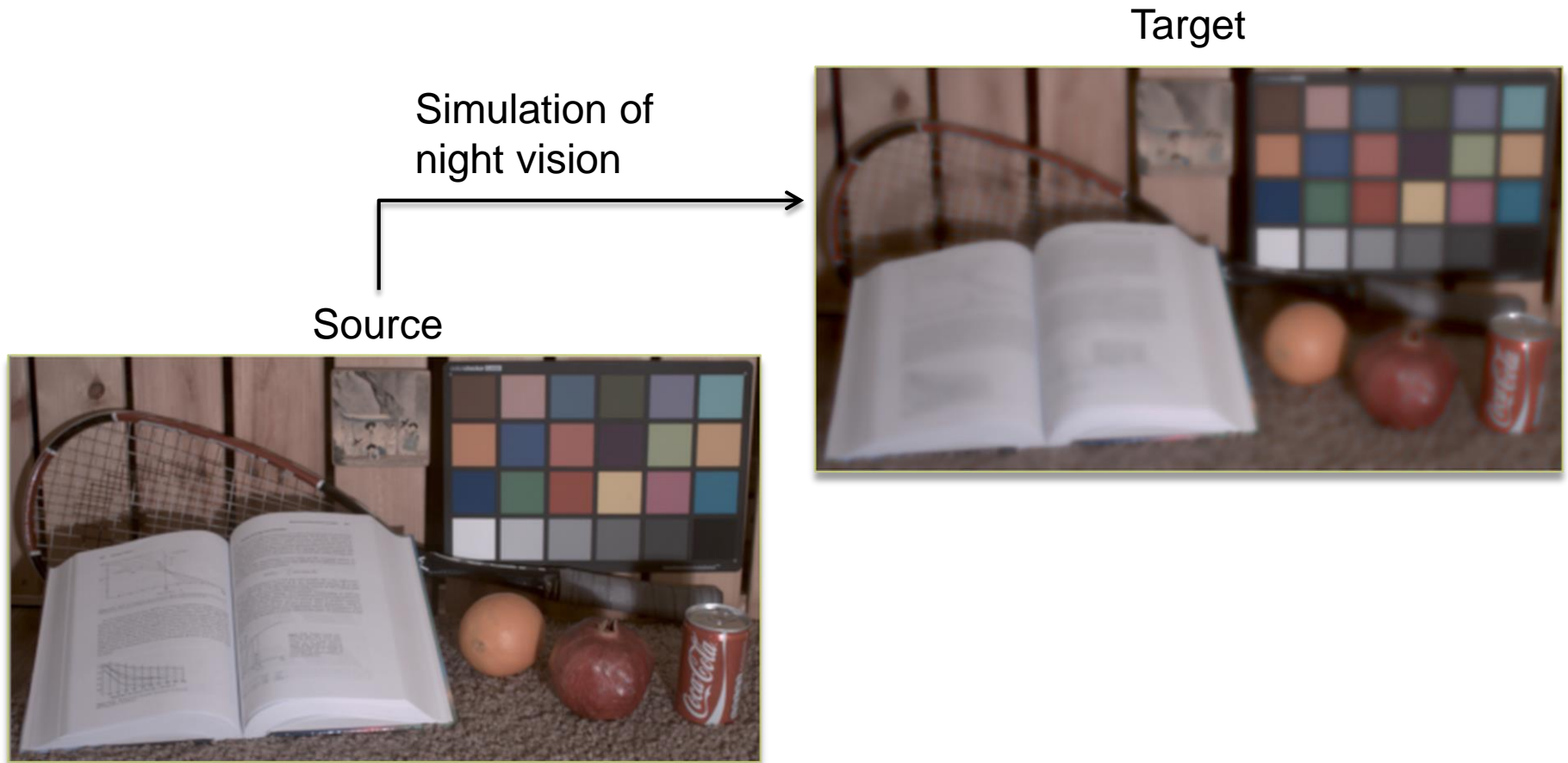


# Local contrast processing



# Example processing

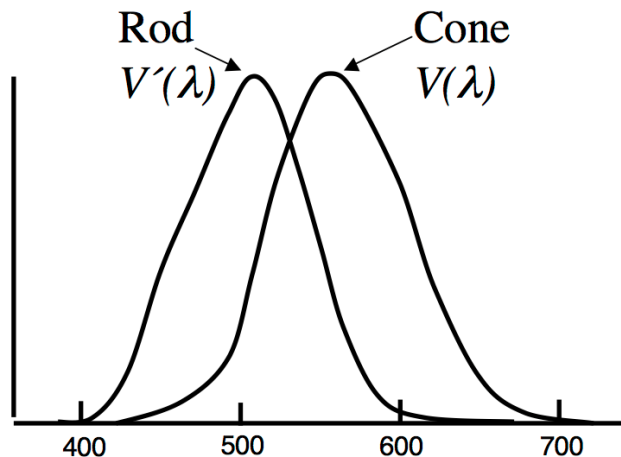
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# Purkinje shift (effect)

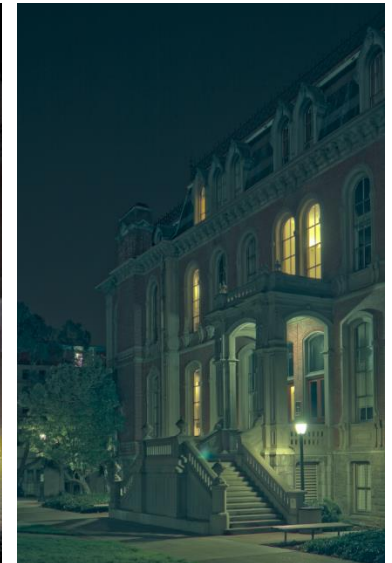
- ▶ A shift in spectral sensitivity associated with the transition of cone to rod vision
  - ▶ Blue appears brighter and red appears darker in twilight
  - ▶ And the reverse is observed in daylight
- ▶ The shift to bluish hues is sometimes attributed to the Purkinje effect
  - ▶ In practice the blue-shift is very subtle
  - ▶ Much more pronounced in movies



Perceptual

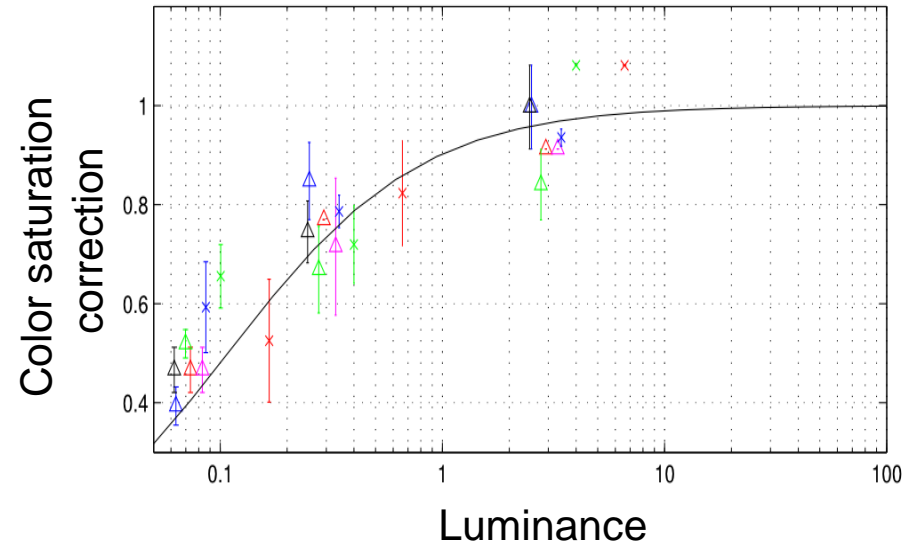


Blue filter



# Loss of colour saturation with luminance

- Cones become less sensitive at low light
- Colours become less saturated
- Empirical formula [Wanat 2014]



# References

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  - ▶ E. Reinhard, W. Heidrich, P. Debevec, S. Pattanaik, G. Ward, and K. Myszkowski, High Dynamic Range Imaging: Acquisition, Display, and Image-Based Lighting, 2nd edition. Morgan Kaufmann, 2010.
- ▶ Overview of HDR imaging & tone-mapping
  - ▶ [http://www.cl.cam.ac.uk/~rkm38/hdri\\_book.html](http://www.cl.cam.ac.uk/~rkm38/hdri_book.html)
- ▶ Review of recent video tone-mapping
  - ▶ A comparative review of tone-mapping algorithms for high dynamic range video  
*Gabriel Eilertsen, Rafal K. Mantiuk, Jonas Unger*, Eurographics State-of-The-Art Report 2017.
- ▶ Selected papers on tone-mapping:
  - ▶ G.W. Larson, H. Rushmeier, and C. Piatko, “A visibility matching tone reproduction operator for high dynamic range scenes,” *IEEE Trans. Vis. Comput. Graph.*, vol. 3, no. 4, pp. 291–306, 1997.
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  - ▶ Ritschel, T. et al. 2009. Temporal Glare: Real-Time Dynamic Simulation of the Scattering in the Human Eye. Computer Graphics Forum. 28, 2 (Apr. 2009), 183–192
  - ▶ ...