

# Solution Progress

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Easter 2016

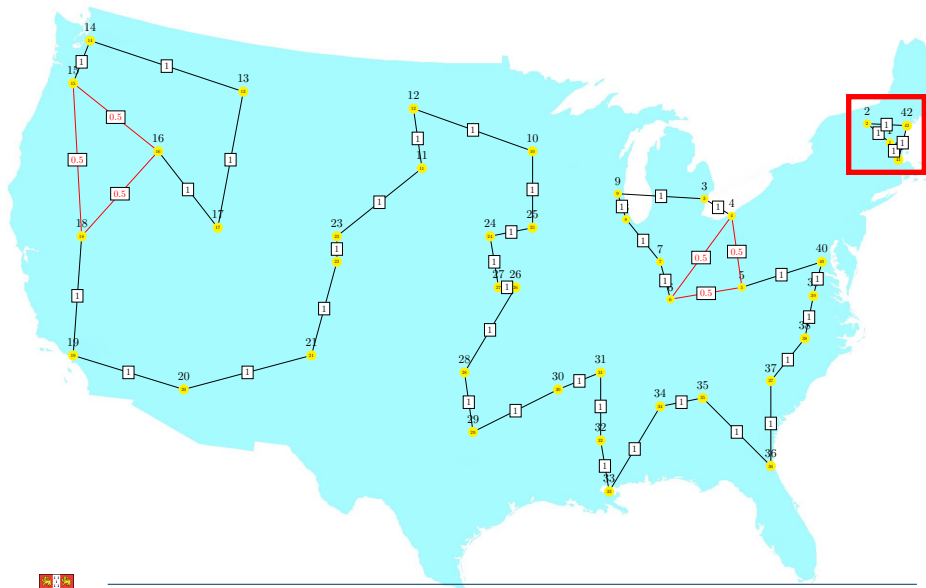


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## Iteration 1: Eliminate Subtour 1, 2, 41, 42

Objective value:  $-641.000000$ , 861 variables, 945 constraints, 1809 iterations

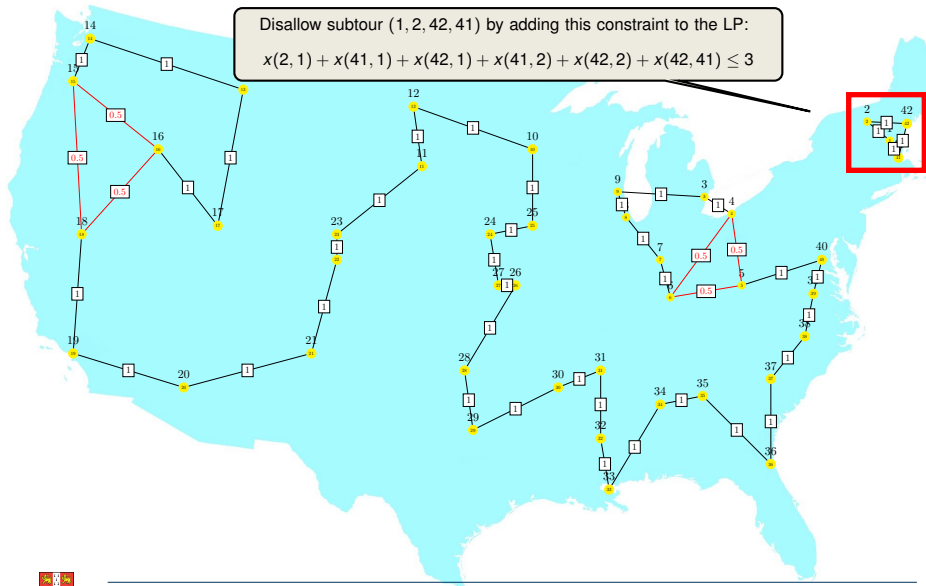


## Iteration 1: Eliminate Subtour 1, 2, 41, 42

Objective value:  $-641.000000$ , 861 variables, 945 constraints, 1809 iterations

Disallow subtour (1, 2, 42, 41) by adding this constraint to the LP:

$$x(2, 1) + x(41, 1) + x(42, 1) + x(41, 2) + x(42, 2) + x(42, 41) \leq 3$$



## Iteration 1: Eliminate Subtour 1, 2, 41, 42

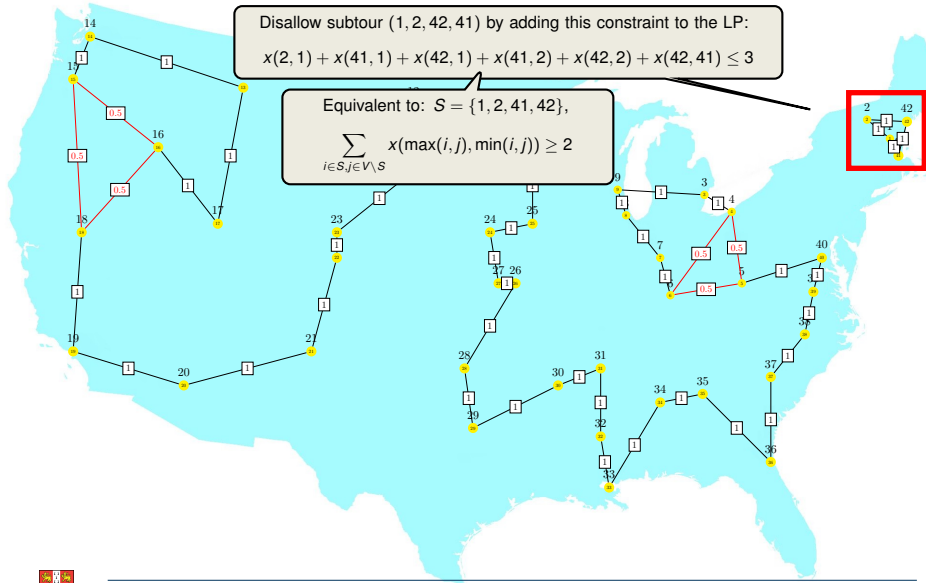
Objective value:  $-641.000000$ , 861 variables, 945 constraints, 1809 iterations

Disallow subtour (1, 2, 42, 41) by adding this constraint to the LP:

$$x(2, 1) + x(41, 1) + x(42, 1) + x(41, 2) + x(42, 2) + x(42, 41) \leq 3$$

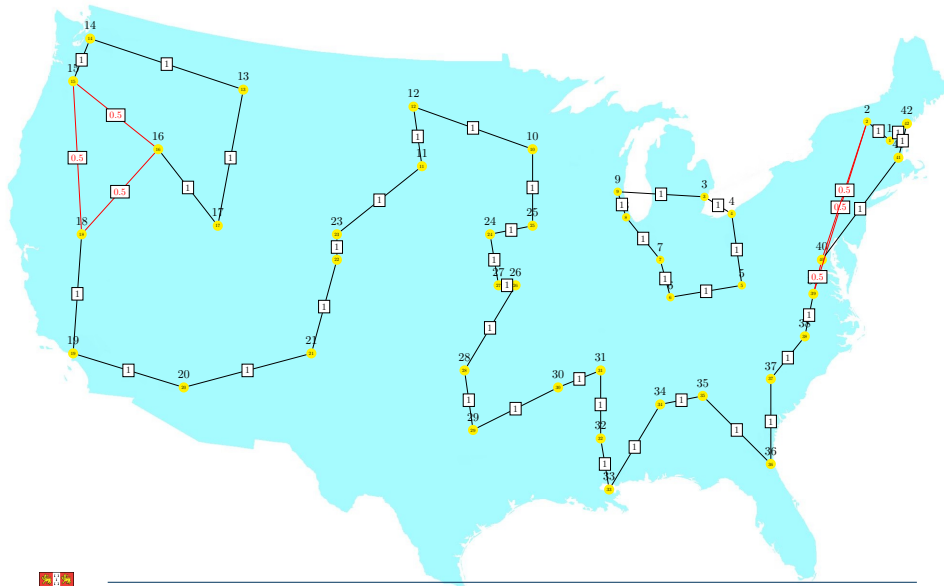
Equivalent to:  $S = \{1, 2, 41, 42\}$ ,

$$\sum_{i \in S, j \in V \setminus S} x(\max(i, j), \min(i, j)) \geq 2$$



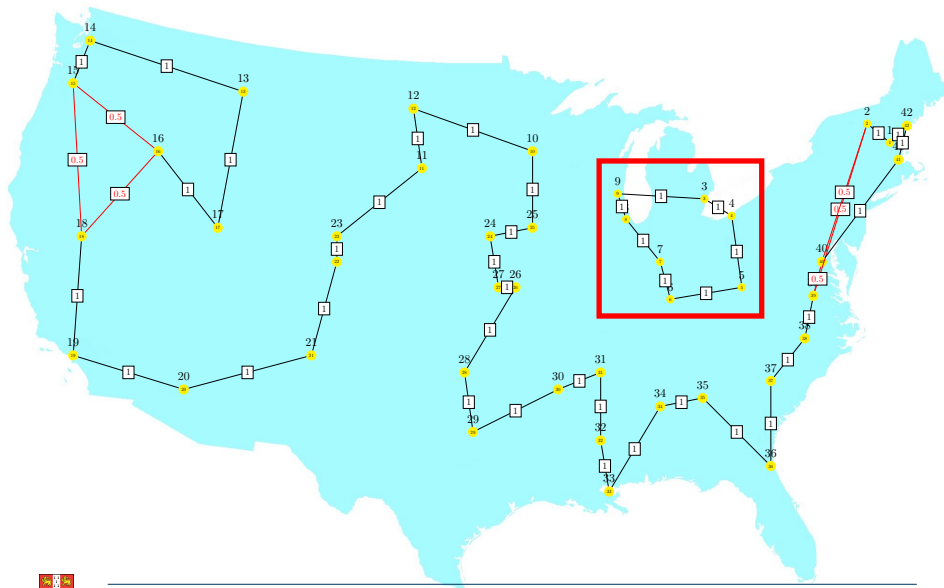
## Iteration 2:

Objective value:  $-676.000000$ , 861 variables, 946 constraints, 1802 iterations



## Iteration 2: Eliminate Subtour 3 – 9

Objective value:  $-676.000000$ , 861 variables, 946 constraints, 1802 iterations

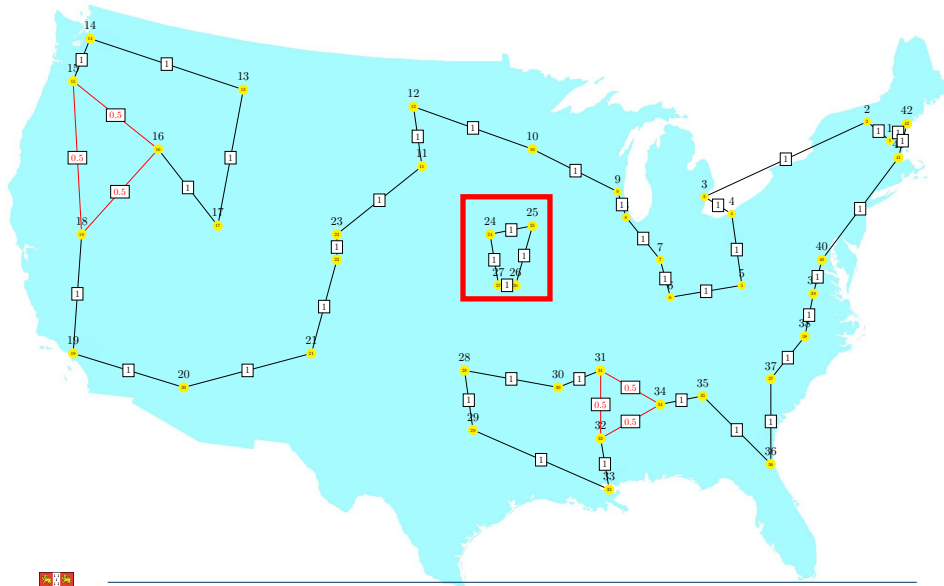






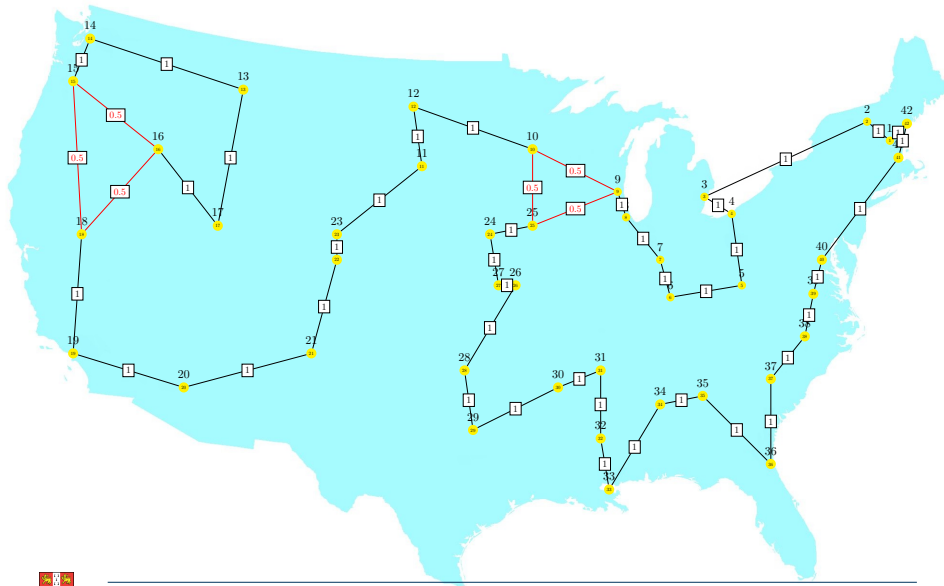
### Iteration 3: Eliminate Subtour 24, 25, 26, 27

Objective value:  $-681.000000$ , 861 variables, 947 constraints, 1984 iterations



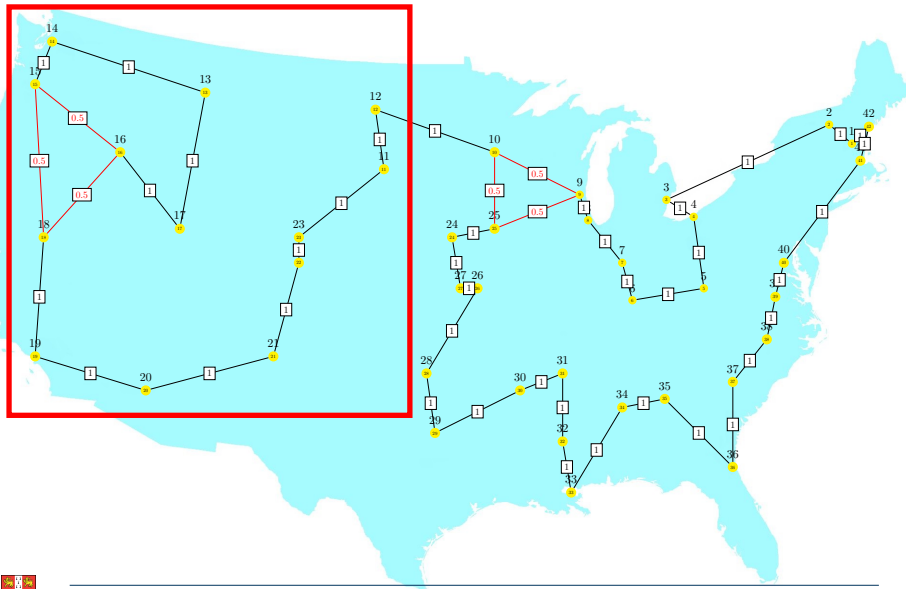
## Iteration 4:

Objective value:  $-682.500000$ , 861 variables, 948 constraints, 1492 iterations



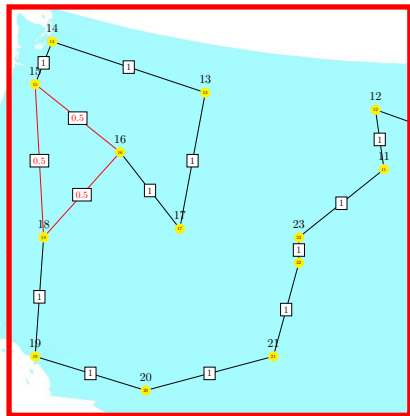
## Iteration 4: Eliminate Cut 11 – 23

Objective value:  $-682.500000$ , 861 variables, 948 constraints, 1492 iterations



## Iteration 4: Eliminate Cut 11 – 23

Objective value:  $-682.500000$ , 861 variables, 948 constraints, 1492 iterations



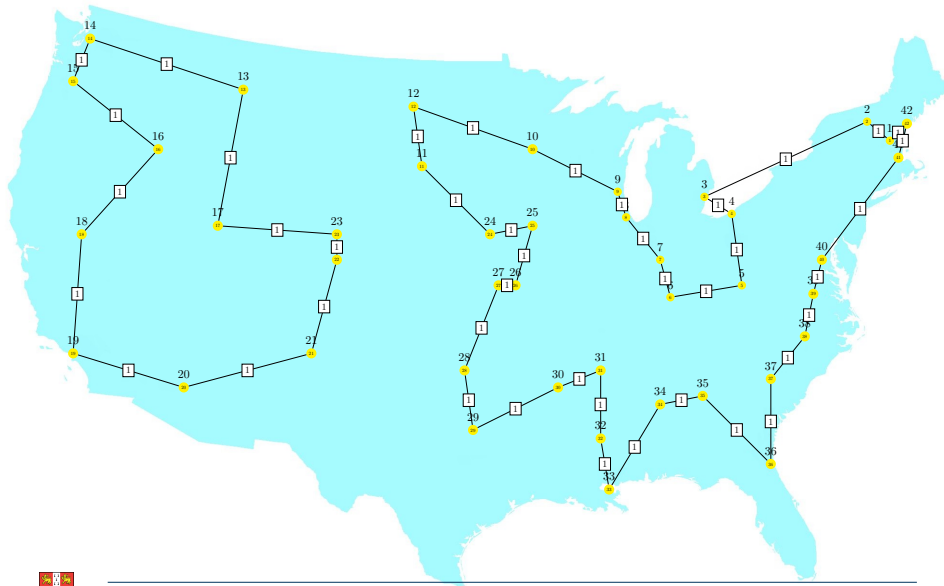
Tour has to include at least two edges between  $S = \{11, 12, \dots, 23\}$  and  $V \setminus S$ :

$$\sum_{i \in S, j \in V \setminus S} x(\max(i, j), \min(i, j)) \geq 2.$$



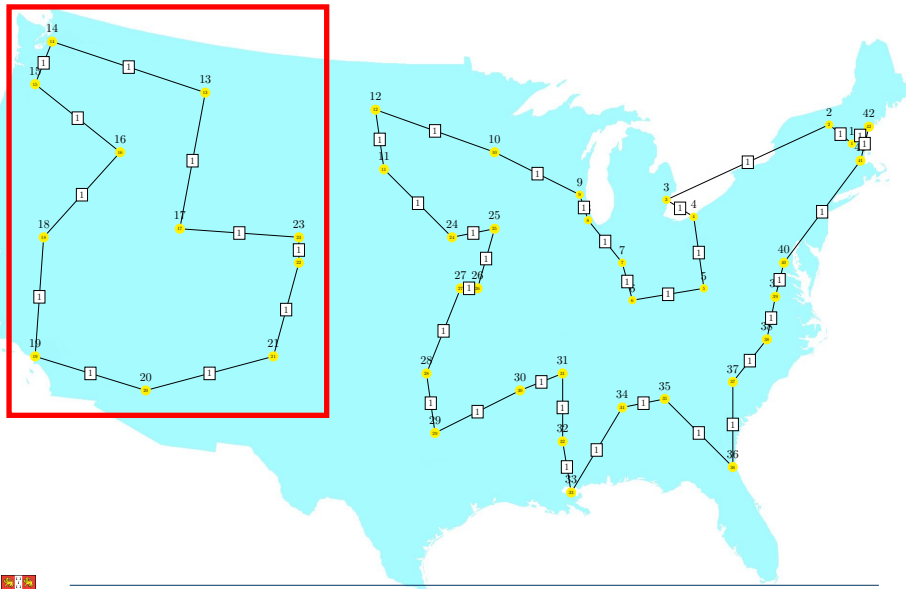
## Iteration 5:

Objective value:  $-686.000000$ , 861 variables, 949 constraints, 2446 iterations



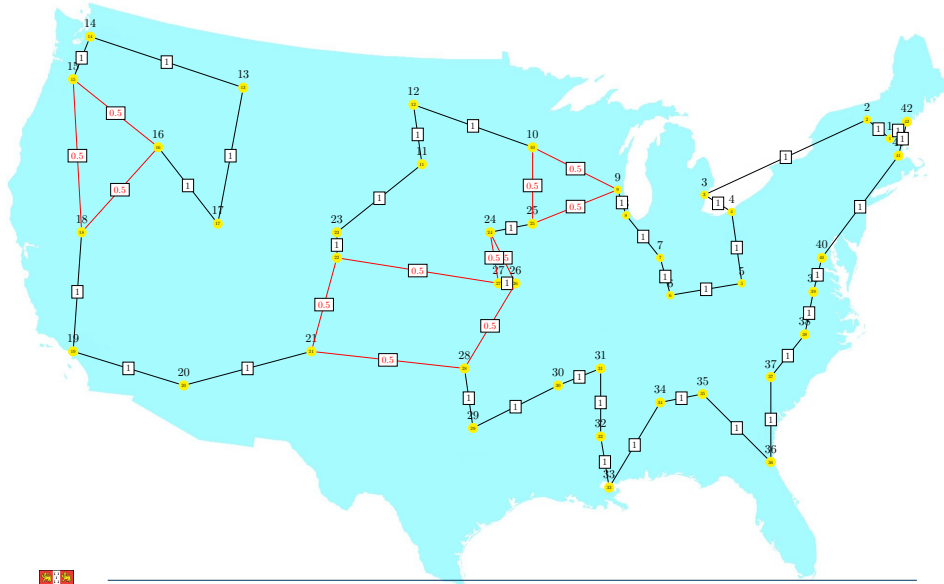
## Iteration 5: Eliminate Subtour 13 – 23

Objective value:  $-686.000000$ , 861 variables, 949 constraints, 2446 iterations



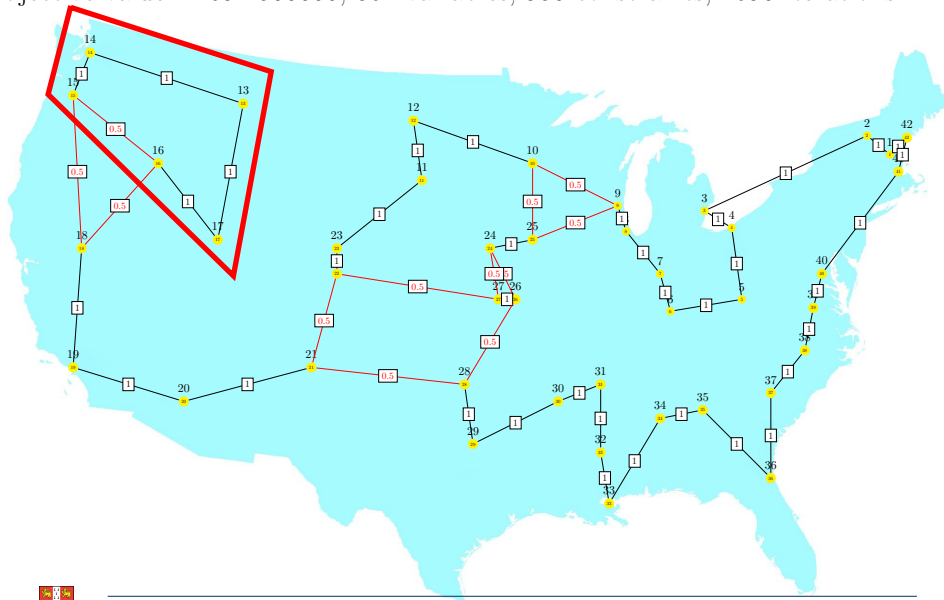
## Iteration 6:

Objective value:  $-694.500000$ , 861 variables, 950 constraints, 1690 iterations



## Iteration 6: Eliminate Cut 13 – 17

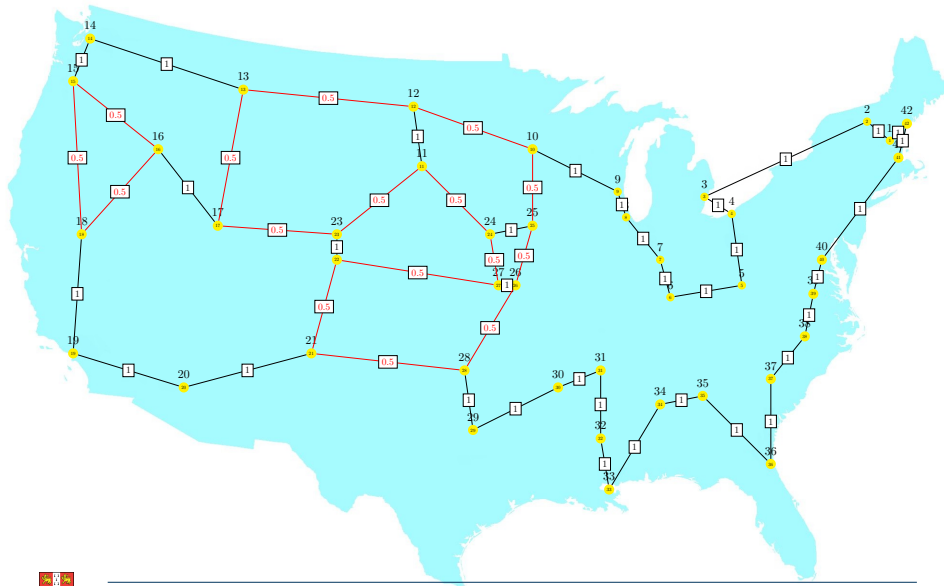
Objective value:  $-694.500000$ , 861 variables, 950 constraints, 1690 iterations





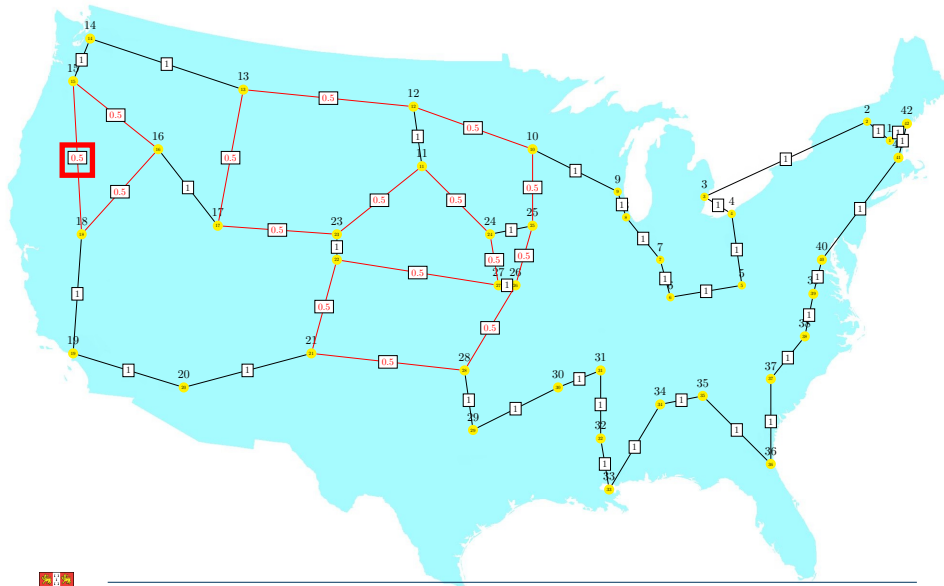
## Iteration 7:

Objective value:  $-697.000000$ , 861 variables, 951 constraints, 2212 iterations



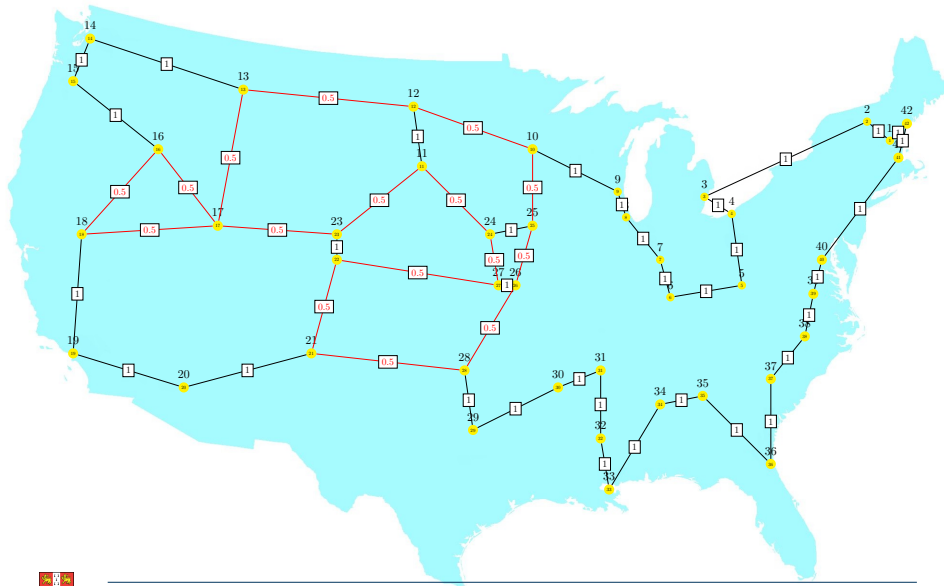
## Iteration 7: Branch 1a $x_{15,18} = 0$

Objective value:  $-697.000000$ , 861 variables, 951 constraints, 2212 iterations



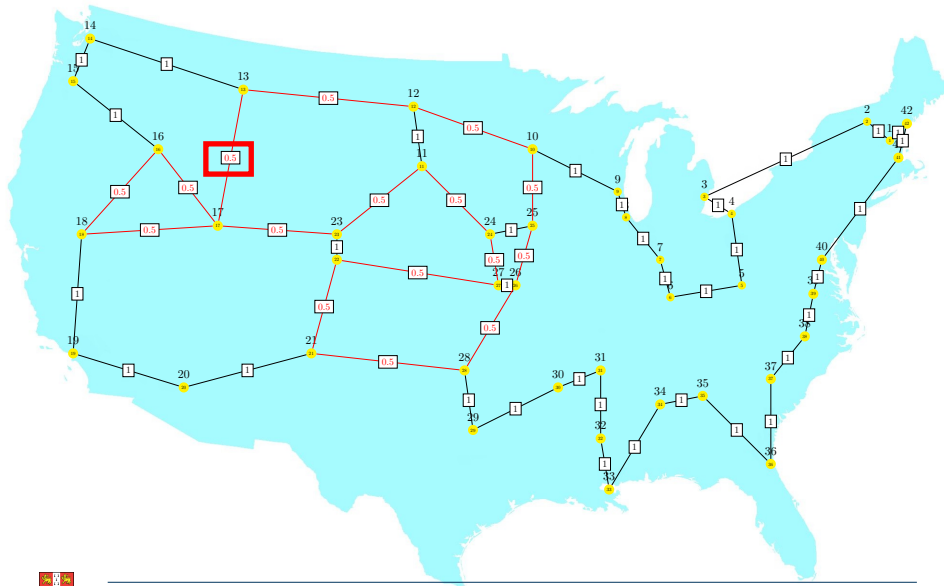
## Iteration 8:

Objective value:  $-698.000000$ , 861 variables, 952 constraints, 1878 iterations



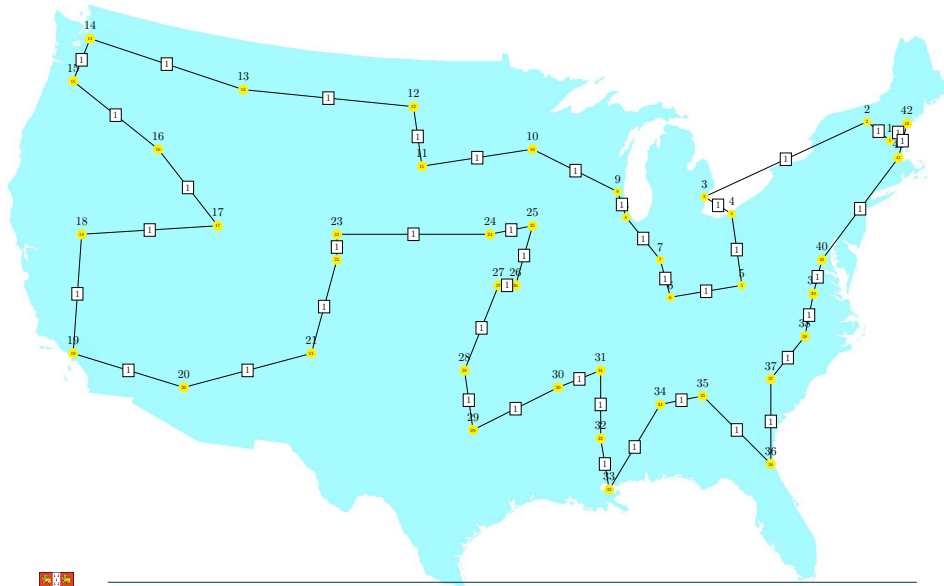
## Iteration 8: Branch 2a $x_{13,17} = 0$

Objective value:  $-698.000000$ , 861 variables, 952 constraints, 1878 iterations



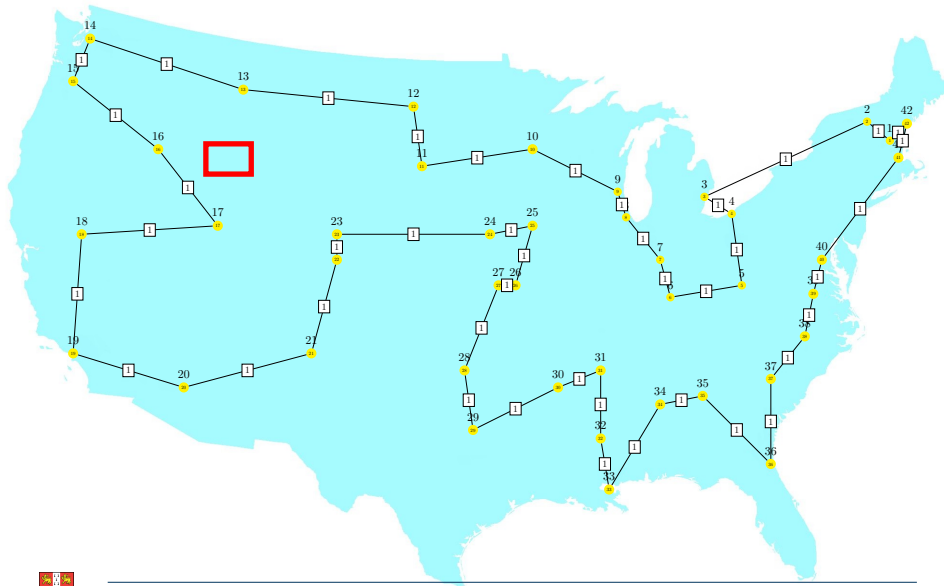
## Iteration 9:

Objective value:  $-699.000000$ , 861 variables, 953 constraints, 2281 iterations



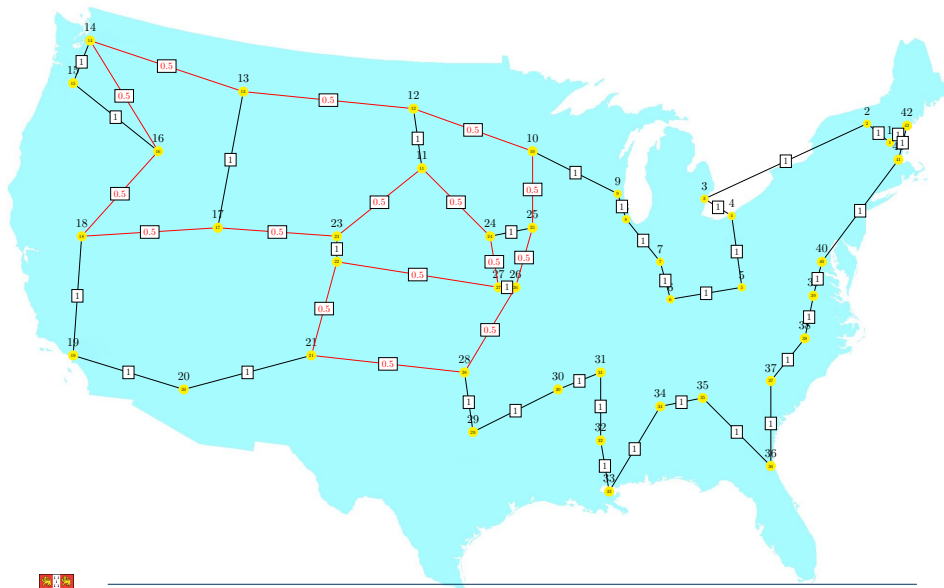
## Iteration 9: Branch 2b $x_{13,17} = 1$

Objective value:  $-699.000000$ , 861 variables, 953 constraints, 2281 iterations



## Iteration 10:

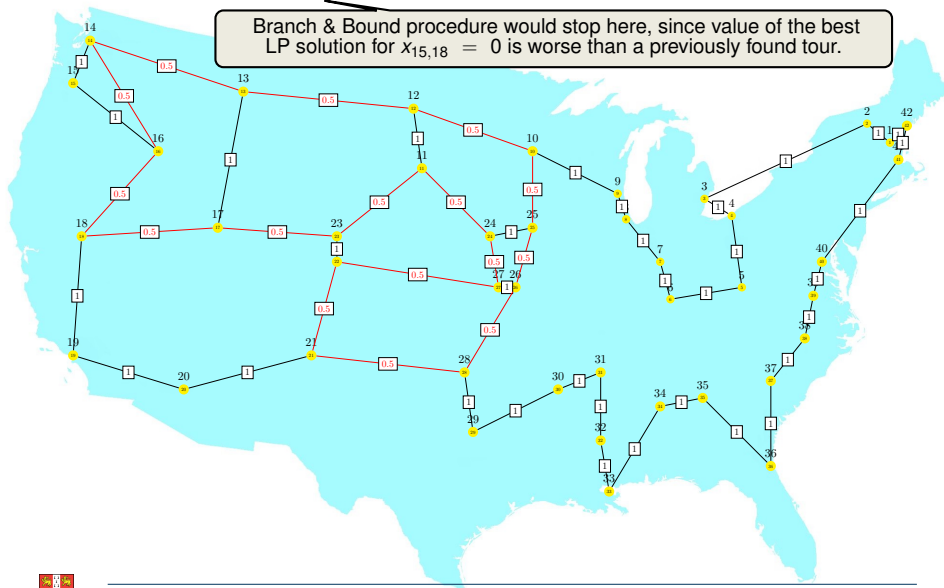
Objective value:  $-700.000000$ , 861 variables, 954 constraints, 2398 iterations



## Iteration 10:

Objective value:  $-700.000000$ , 861 variables, 954 constraints, 2398 iterations

Branch & Bound procedure would stop here, since value of the best LP solution for  $x_{15,18} = 0$  is worse than a previously found tour.

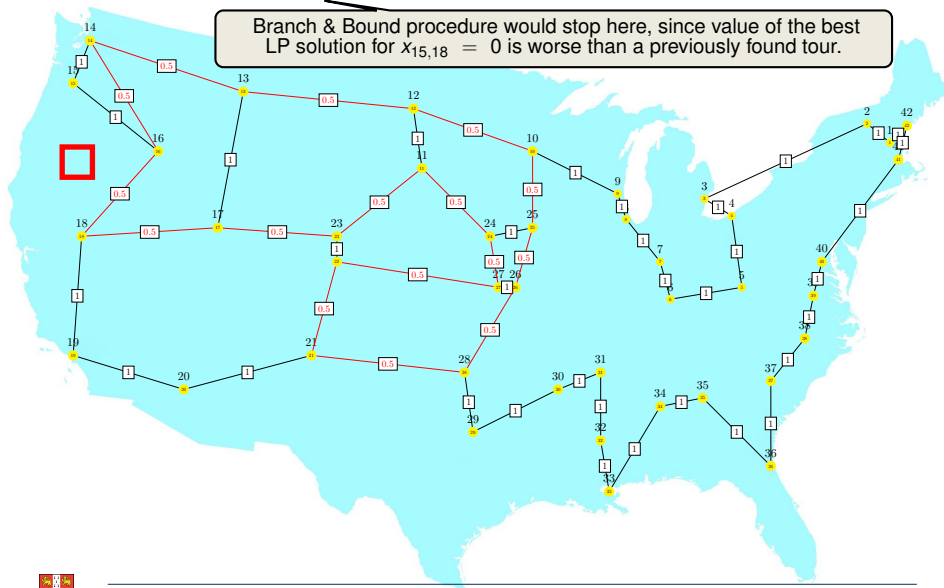




## Iteration 10: Branch 1b $x_{15,18} = 1$

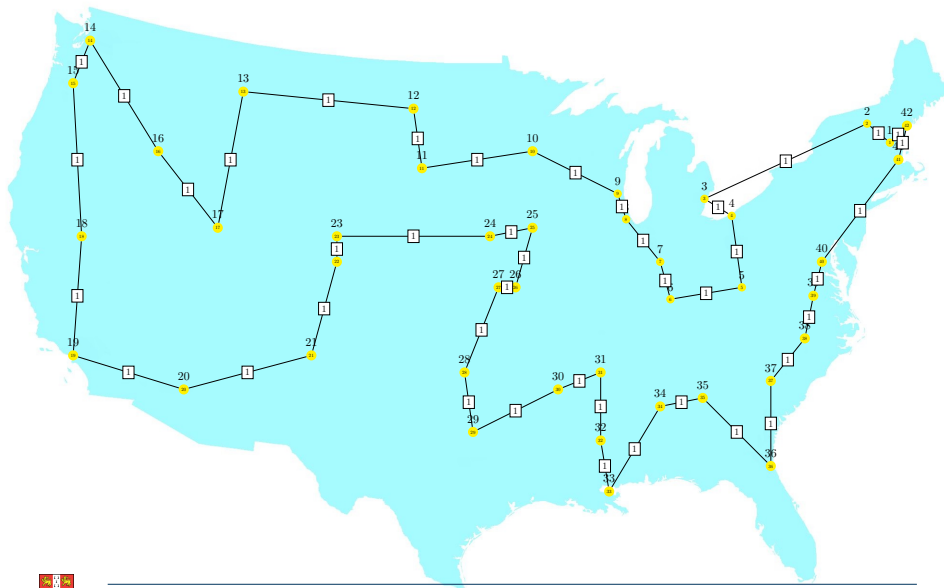
Objective value:  $-700.000000$ , 861 variables, 954 constraints, 2398 iterations

Branch & Bound procedure would stop here, since value of the best LP solution for  $x_{15,18} = 0$  is worse than a previously found tour.



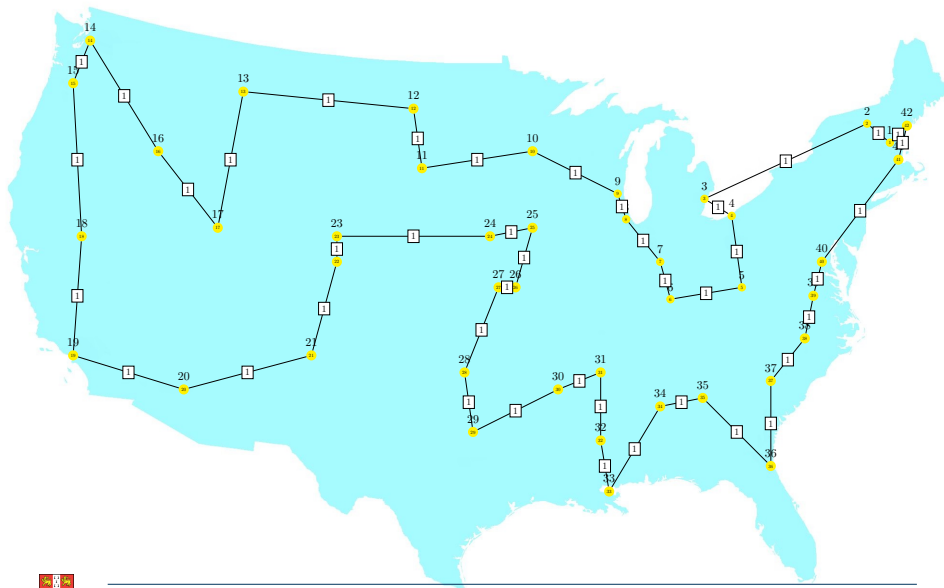
## Iteration 11:

Objective value:  $-701.000000$ , 861 variables, 953 constraints, 2506 iterations



## Iteration 11: Branch & Bound terminates

Objective value:  $-701.000000$ , 861 variables, 953 constraints, 2506 iterations



## Branch & Bound Overview

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1: LP solution 641



## Branch & Bound Overview

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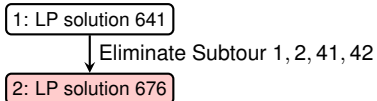
1: LP solution 641

↓ Eliminate Subtour 1, 2, 41, 42



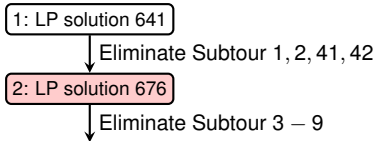
## Branch & Bound Overview

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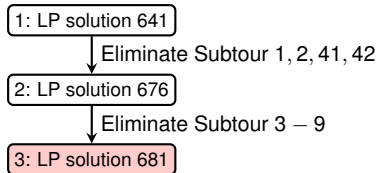
## Branch & Bound Overview

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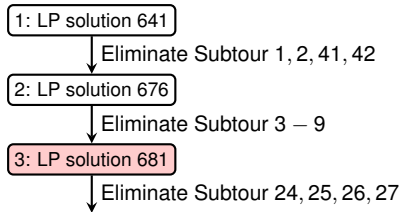
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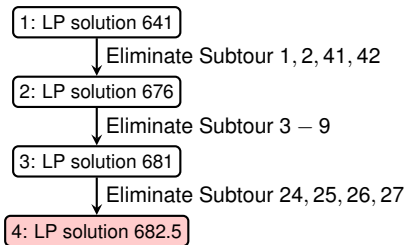
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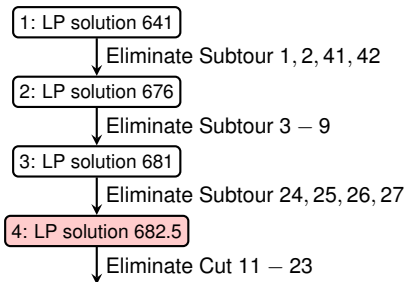
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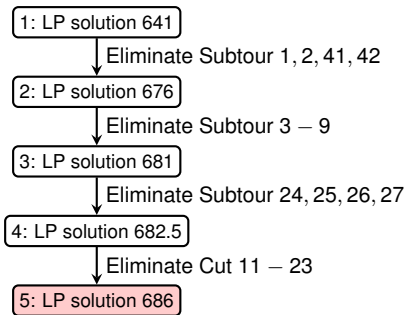
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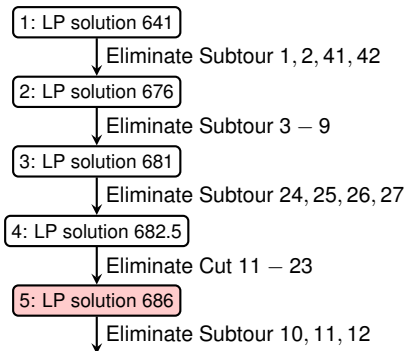
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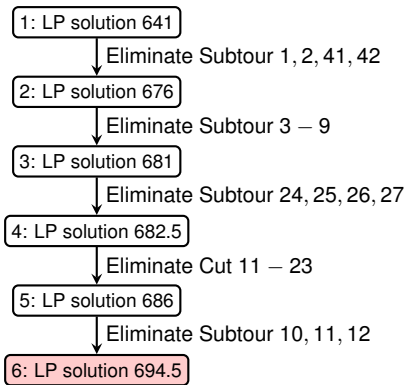
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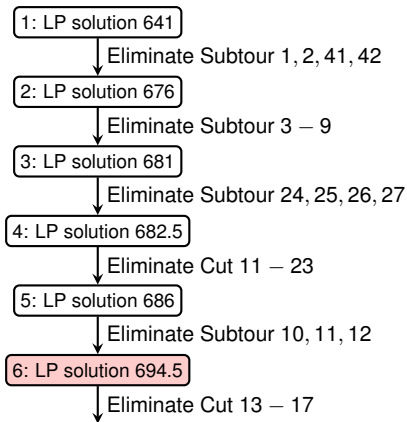


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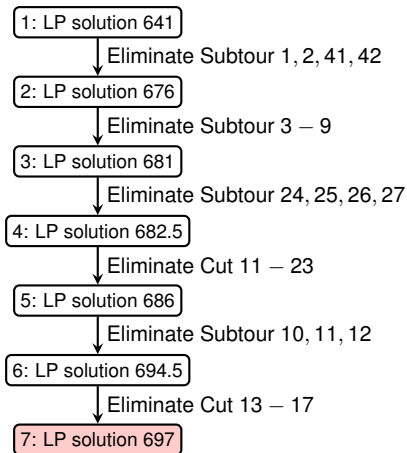
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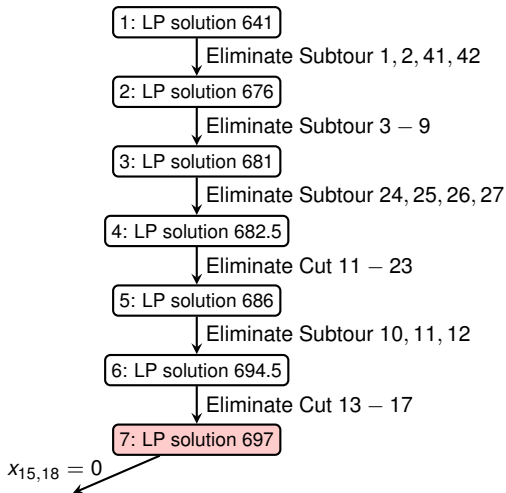


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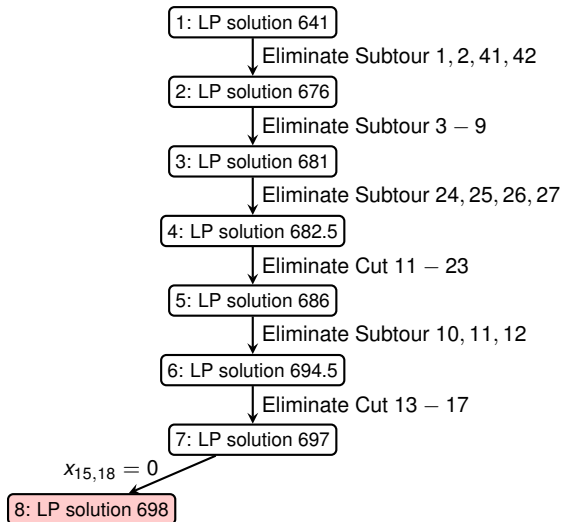




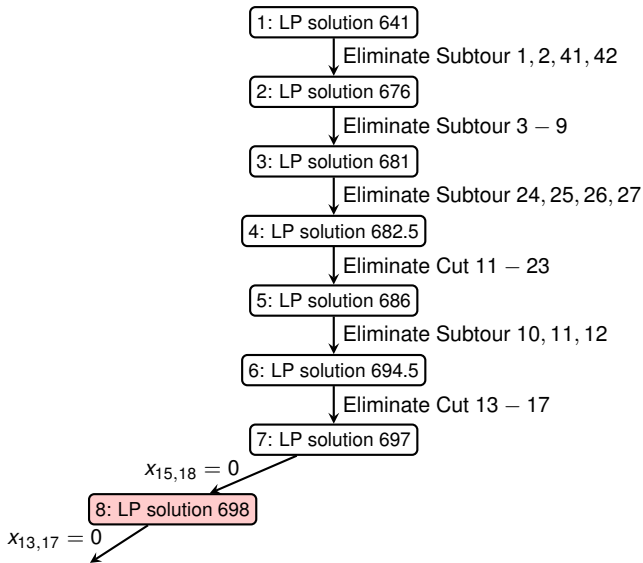
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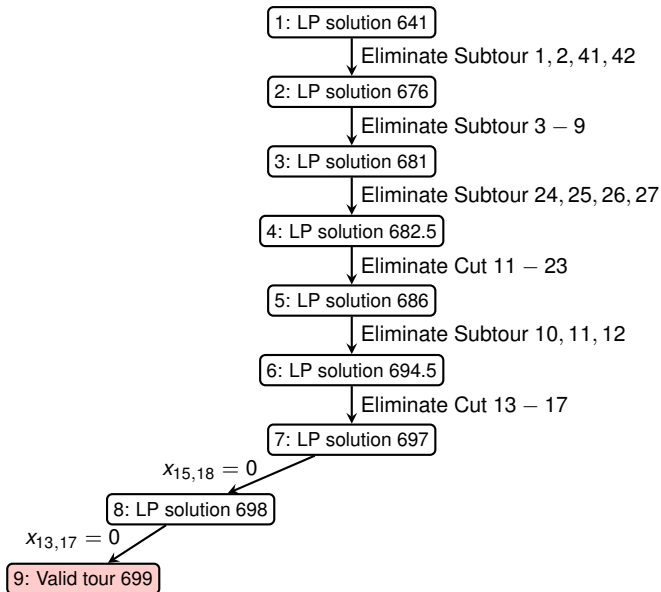
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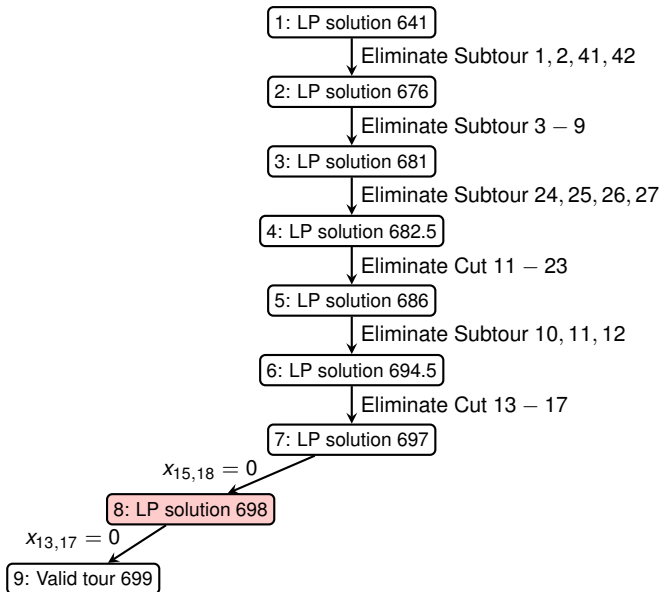
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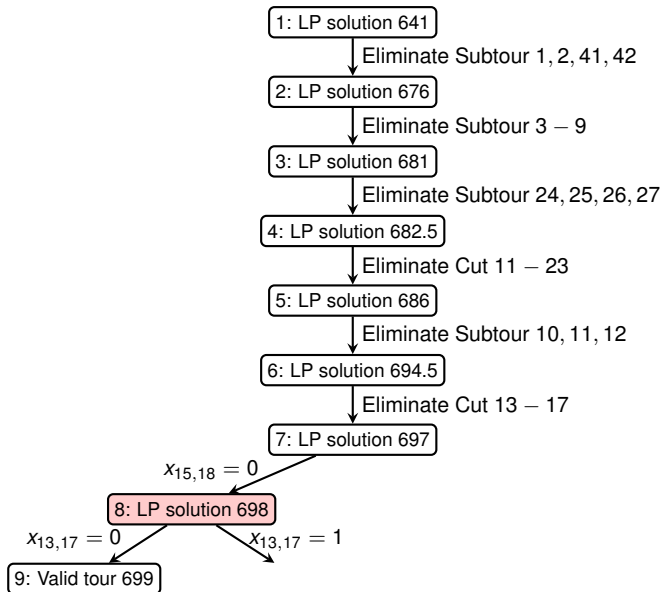
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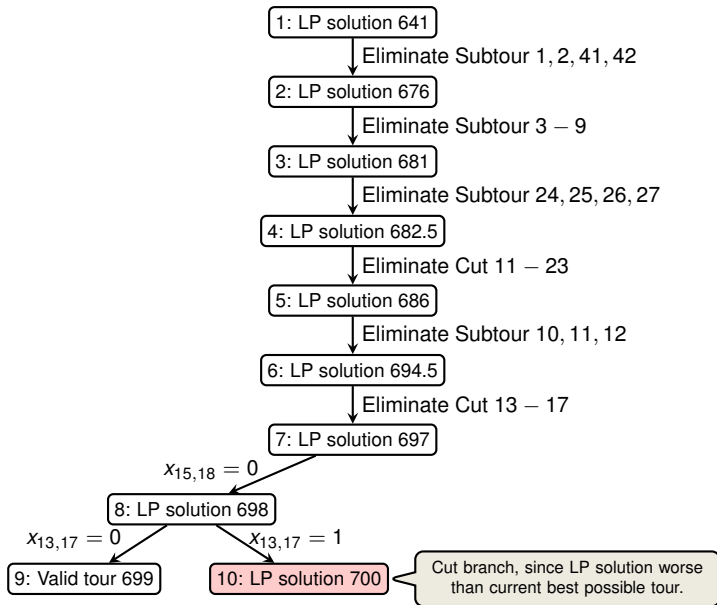
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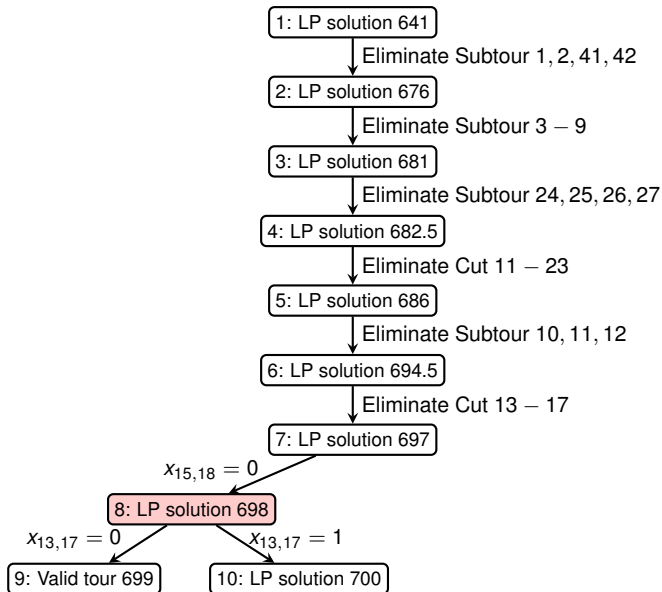
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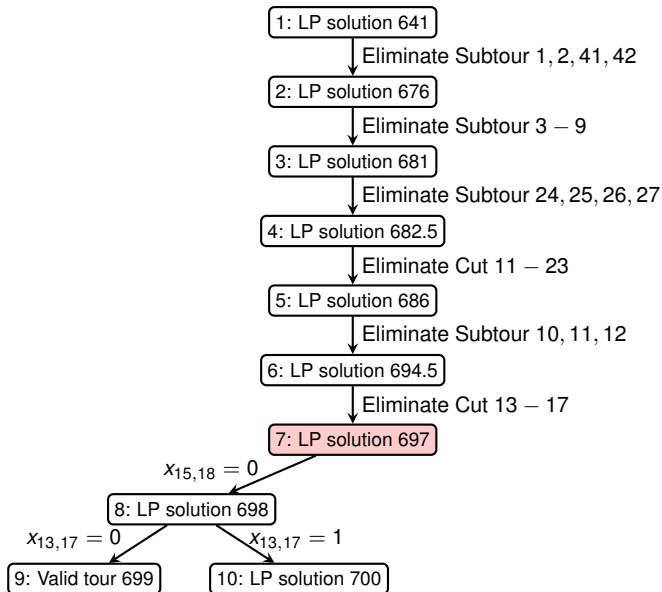


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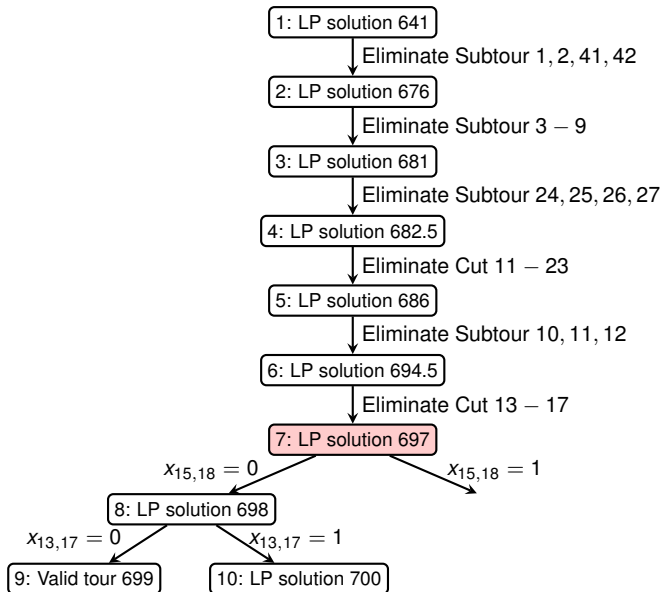




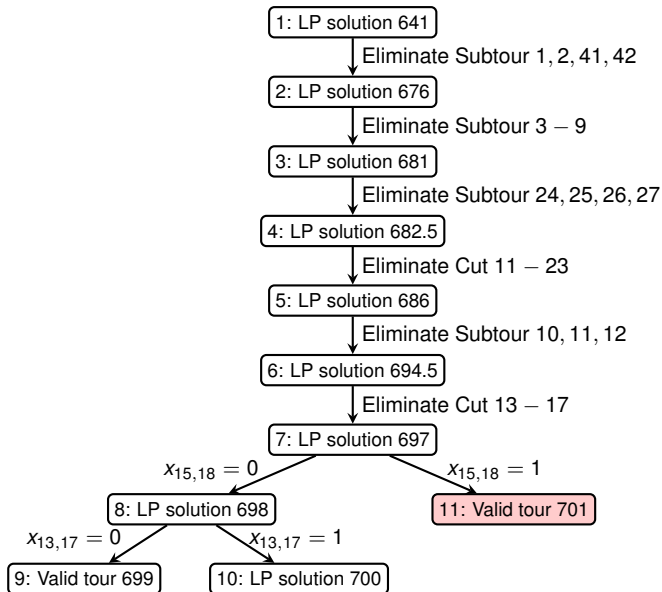
## Branch & Bound Overview



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