#### 14: Clique Finding Machine Learning and Real-world Data

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Lent 2017

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- You implemented betweenness centrality.
- This let you find "gatekeeper" nodes in the Facebook network.
- We will now turn to the task of finding clusters in networks.

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You will test this on a small network derived from one Facebook user.

# Clustering in networks

- clustering: automatically grouping data according to some notion of closeness or similarity.
- agglomerative clustering works bottom-up.
- **divisive clustering** works top-down, by splitting.
- Newman-Girvan method a form of divisive clustering.
- Criterion for breaking links is edge betweenness centrality.
- When to stop?
  - Prespecified (today's tick): use prior knowledge to decide when to stop, based on number of clusters.
  - Inherent 'goodness of clustering' metric: today's starred tick uses modularity (Newman 2004).

### Step 1: Code for determining connected components

- Today's graph is disconnected: there are five connected components.
- Finding connected components: depth-first search, start at an arbitrary node and mark the other nodes you reach.

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- Repeat with unvisited nodes, until all are visited.
- Implementation hint: depth-first, so use recursion (the program stack stores the search state).

- Previously: σ(s, t|v) the number of shortest paths between s and t going through node v.
- Now: σ(s, t|e) the number of shortest paths between s and t going through edge e.
- Algorithm only changes in the bottom-up (accumulation) phase: δ(v) much as before, but c<sub>B</sub>[(v, w)]

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#### Brandes (2008) pseudocode

```
 \begin{array}{l} \blacktriangledown \ \mathbf{accumulation} \ // - \texttt{back-propagation of dependencies} \\ \mathbf{for} \ v \in V \ \mathbf{do} \ \delta[v] \leftarrow 0 \\ \mathbf{while} \ S \ not \ empty \ \mathbf{do} \\ \\ pop \ w \leftarrow S \\ \mathbf{for} \ v \in Pred[w] \ \mathbf{do} \ \delta[v] \leftarrow \delta[v] + \frac{\sigma[v]}{\sigma[w]} \cdot (1 + \delta[w]) \\ \\ \mathbf{if} \ w \neq s \ \mathbf{then} \ c_B[w] \leftarrow c_B[w] + \delta[w] \\ \end{array}
```

#### Edge betweenness

**output**: betweenness  $c_B[q]$  for  $q \in V \cup E$  (initialized to 0)

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\left[\begin{array}{c} \mathbf{for} \ v \in V \ \mathbf{do} \ \delta[v] \leftarrow 0 \\ \mathbf{while} \ S \ not \ empty \ \mathbf{do} \\ pop \ w \leftarrow S \\ \mathbf{for} \ v \in Pred[w] \ \mathbf{do} \\ \left[\begin{array}{c} c \leftarrow \frac{\sigma[w]}{\sigma[w]} \cdot (1 + \delta[w]) \\ c_B[(v,w)] \leftarrow c_B[(v,w)] + c \\ \delta[v] \leftarrow \delta[v] + c \\ \mathbf{if} \ w \neq s \ \mathbf{then} \ c_B[w] \leftarrow c_B[w] + \delta[w] \end{array}\right]
```

ignore last line

**while** number of connected subgraphs < specified number of clusters (and there are still edges):

- **1** calculate edge betweenness for every edge in the graph
- 2 remove edge(s) with highest betweenness
- 3 recalculate number of connected components

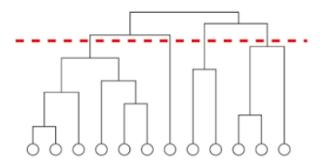
Note:

Treatment of tied edges: either remove all (today) or choose one randomly.

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#### Visualization as dendrogram

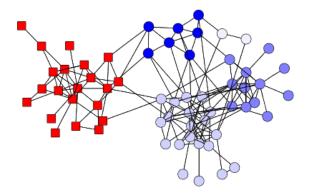
- Either: stop at prespecified level (tick).
- Or: complete process and choose best level by 'modularity' (starred tick).



Newman and Girvan (2004)

#### Dolphin data: different clustering layers

- squares vs circles: first split
- different colours: further splits

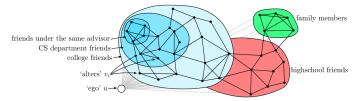


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# Facebook circles dataset: McAuley and Leskovec (2012)

- Designed to allow experimentation with automatic discovery of circles: Facebook friends in a particular social group.
- Profile and network data from 10 Facebook ego-networks (networks emanating from one person: referred to as an ego).
- Gold-standard circles, manually identified by the egos themselves.
- Average: 19 circles per ego, each circle with average of 22 alters.
- Complete network consists of 4,039 nodes in 193 circles.

Requires more sophisticated methods than Newman-Girvan: a) nodes may be in multiple circles, b) not just network data.



25% of circles are contained completely within another circle50% overlap with another circle25% have no members in common with any other circle

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## Evaluating simple clustering

- Assume data sets with gold standard or ground truth clusters.
- But: unlike classification, we don't have labels for clusters, number of clusters found may not equal true classes.
- **purity**: assign label corresponding to majority class found in each cluster, then count correct assignments, divide by total elements (cf accuracy).

http://nlp.stanford.edu/IR-book/html/
htmledition/evaluation-of-clustering-1.html

But best evaluation (if possible) is extrinsic: use the system to do a task and evaluate that.

- Classification (e.g., sentiment classification): assigning data items to predefined classes.
- Clustering: groupings can emerge from data, unsupervised.
- Clustering for documents, images etc: anything where there's a notion of similarity between items.
- Most famous technique for hard clustering is k-means: very general (also variant for graphs).
- Also soft clustering: clusters have graded membership

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#### Schedule

#### Task 12:

- Implement the Newman-Girvan method.
- Discover clusters in the network provided.
- Ticking: Tick 7 or earlier ticks.

Final sessions:

- Tick 8: task 11 and task 12 (Friday, unless demonstrators have spare time today).
- Friday March 10: last lecture (catch up) and ticking.
- Monday March 13: demonstrators available for final ticks, but no lecture.