



# Models of early visual perception

**Advanced Graphics**

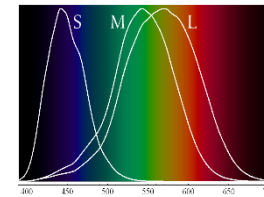
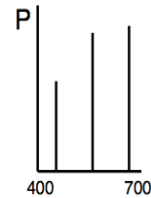
Rafal Mantiuk

*Computer Laboratory, University of Cambridge*

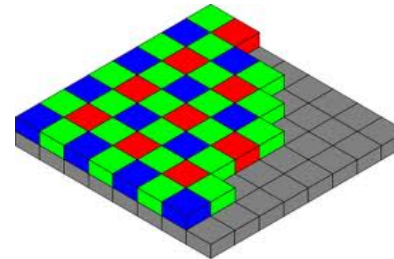
# Many technical solutions are motivated by visual perception



Image & video compression



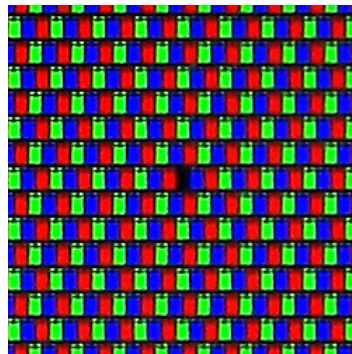
Display spectral emission - metamerism



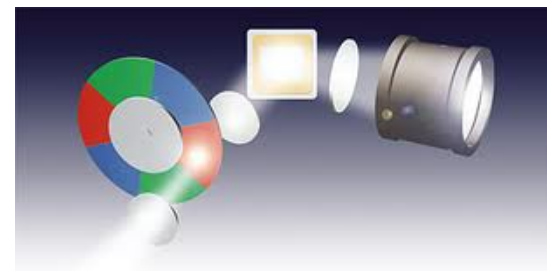
Camera's Bayer pattern



Halftoning



Display's subpixels



Color wheel in DLPs



# Perceived brightness of light

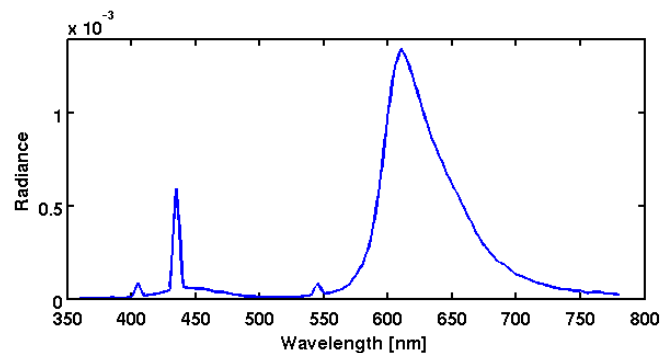
# Luminance

- ▶ Luminance – how bright the surface will appear regardless of its colour. Units:  $\text{cd}/\text{m}^2$

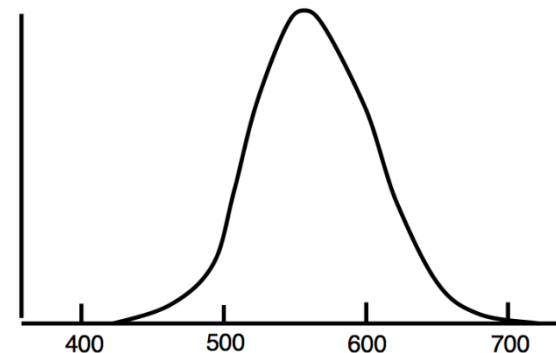
Luminance

$$L_V = \int_0^{\infty} L(\lambda) \cdot V(\lambda) d\lambda$$

Light spectrum (radiance)



Luminous efficiency function (weighting)



# Luminance and Luma

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## ▶ Luminance

- ▶ Photometric quantity defined by the spectral luminous efficiency function
- ▶  $L \approx 0.2126 R + 0.7152 G + 0.0722 B$
- ▶ Units:  $\text{cd}/\text{m}^2$

## ▶ Luma

- ▶ Gray-scale value computed from LDR (gamma corrected) image
- ▶  $Y = 0.2126 R' + 0.7152 G' + 0.0722 B'$
- ▶  $R'$  – prime denotes gamma correction

$$R' = R^{1/\gamma}$$

- ▶ Unitless

# Gamma correction (reminder – Color lecture)

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- ▶ Gamma correction is used to encode luminance or tristimulus color values (RGB) in imaging systems (displays, printers, cameras, etc.)

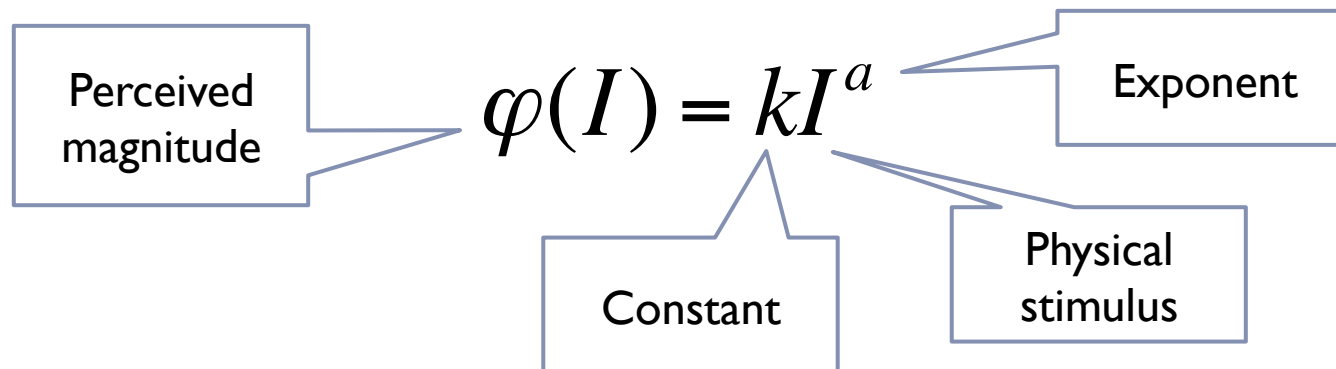
The diagram shows the equation  $V_{out} = a \cdot V_{in}^{\gamma}$  with four callout boxes: 'Gain' pointing to 'a', 'Gamma (usually =2.2)' pointing to the exponent 'gamma', 'Luminance' pointing to 'V\_out', and 'Luma' pointing to 'V\_in'.

For color images:  $R = a \cdot (R')^{\gamma}$  and the same for green and blue

# Steven's power law for brightness

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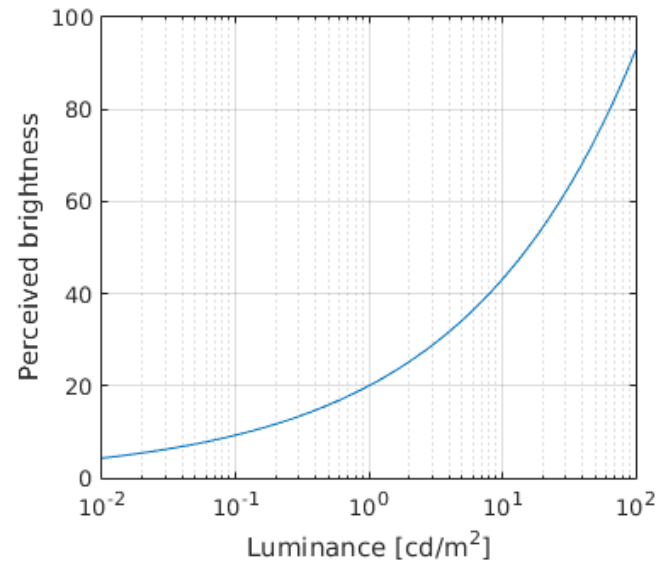
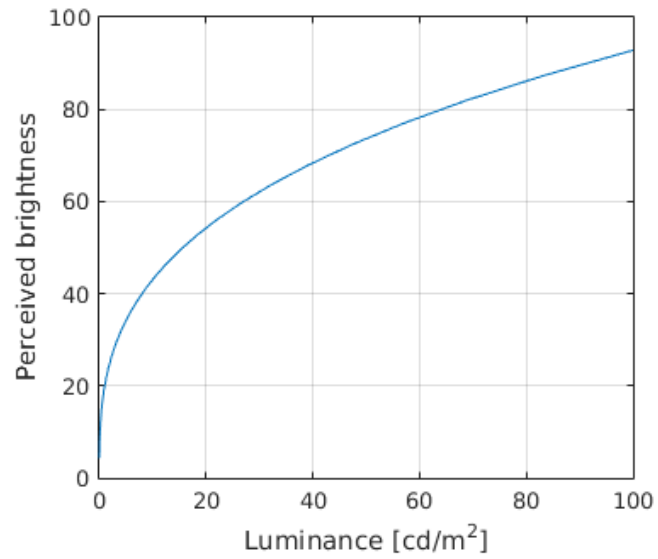
- ▶ Stevens (1906-1973) measured the perceived magnitude of physical stimuli
  - ▶ Loudness of sound, tastes, smell, warmth, electric shock and brightness
  - ▶ Using the magnitude estimation methods
    - ▶ Ask to rate loudness on a scale with a known reference
- ▶ All measured stimuli followed the power law:



- ▶ For brightness (5 deg target in dark),  $a = 0.3$

# Steven's law for brightness

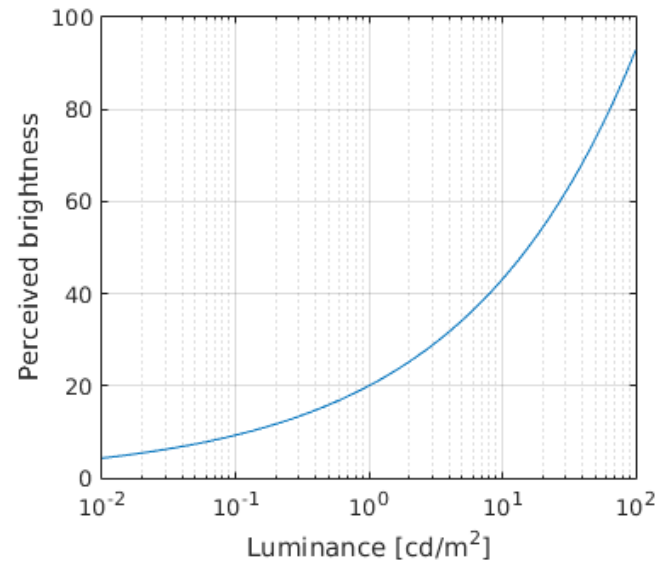
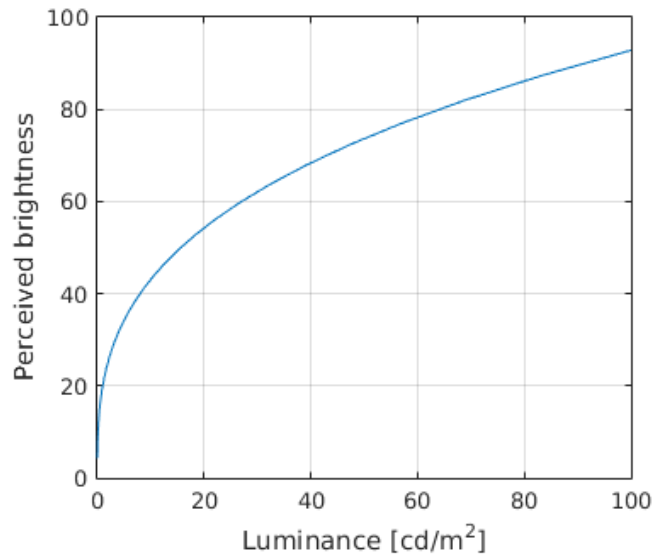
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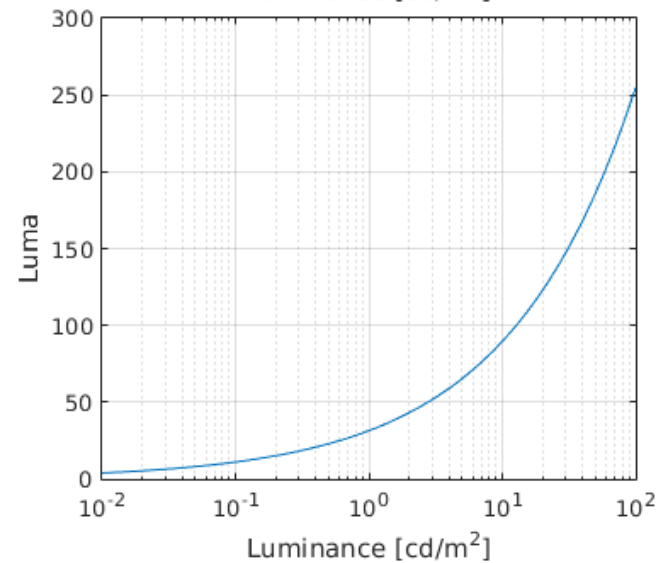
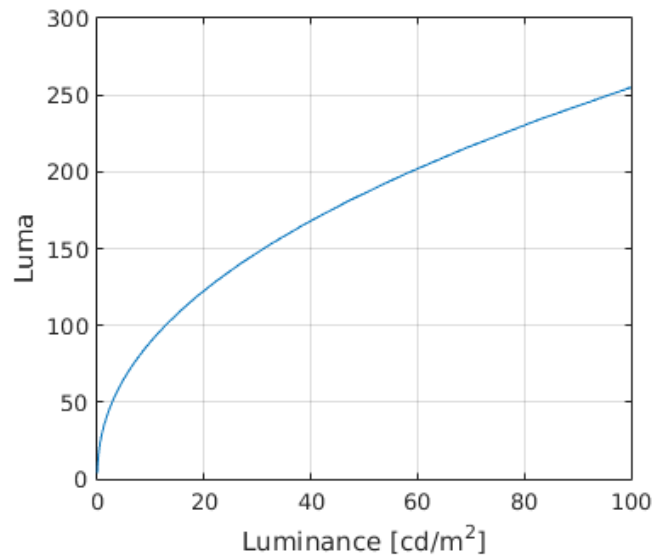


# Steven's law vs. Gamma correction

Stevens' law  
 $a=0.3$



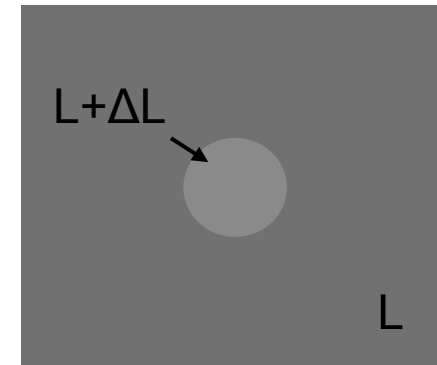
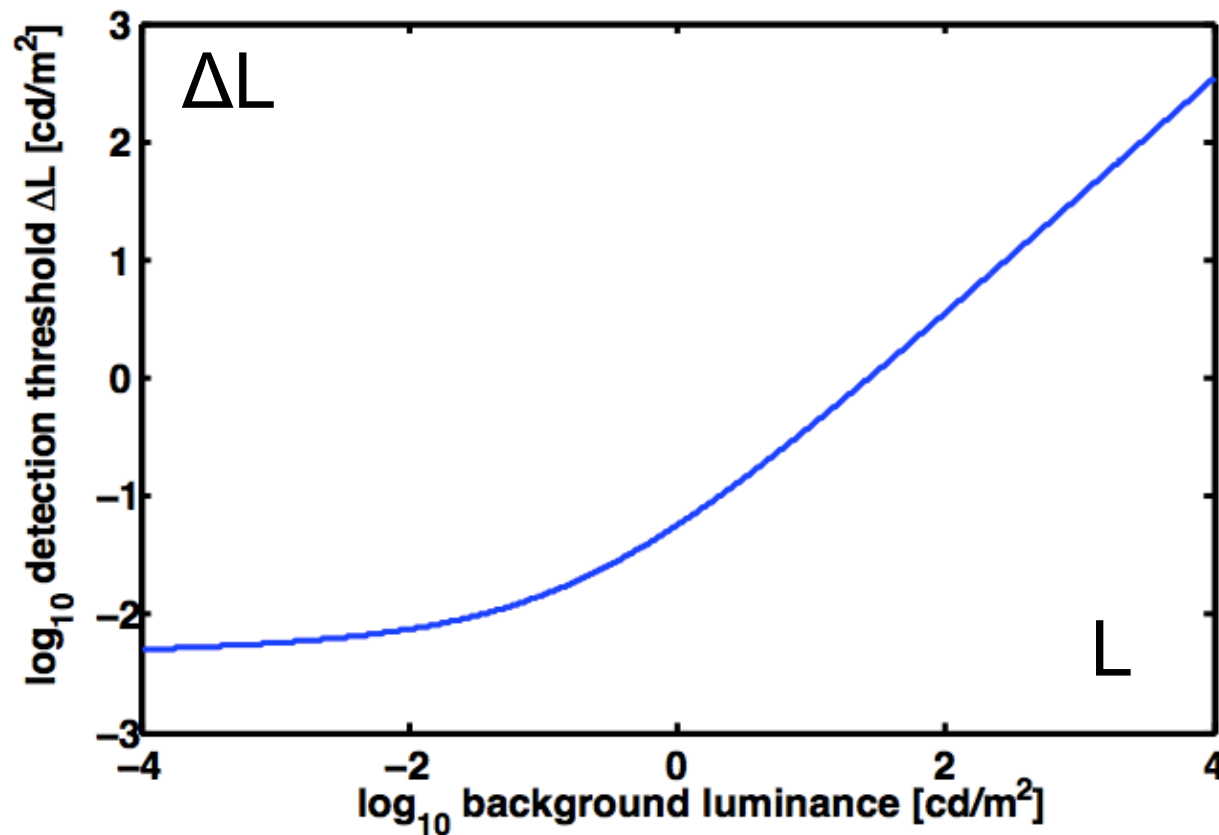
Gamma function  
Gamma = 2.2



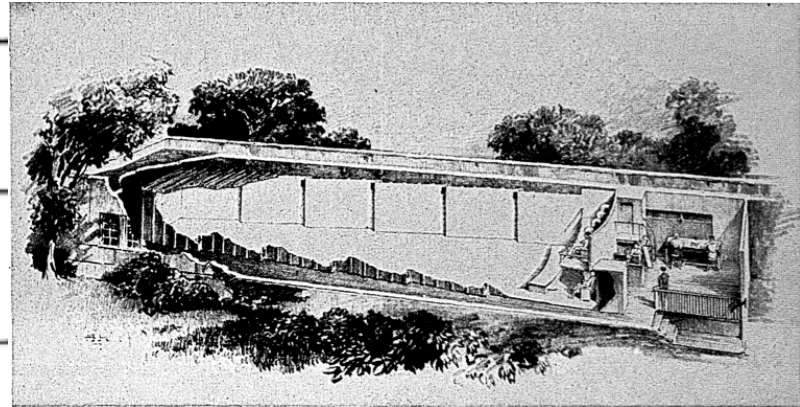
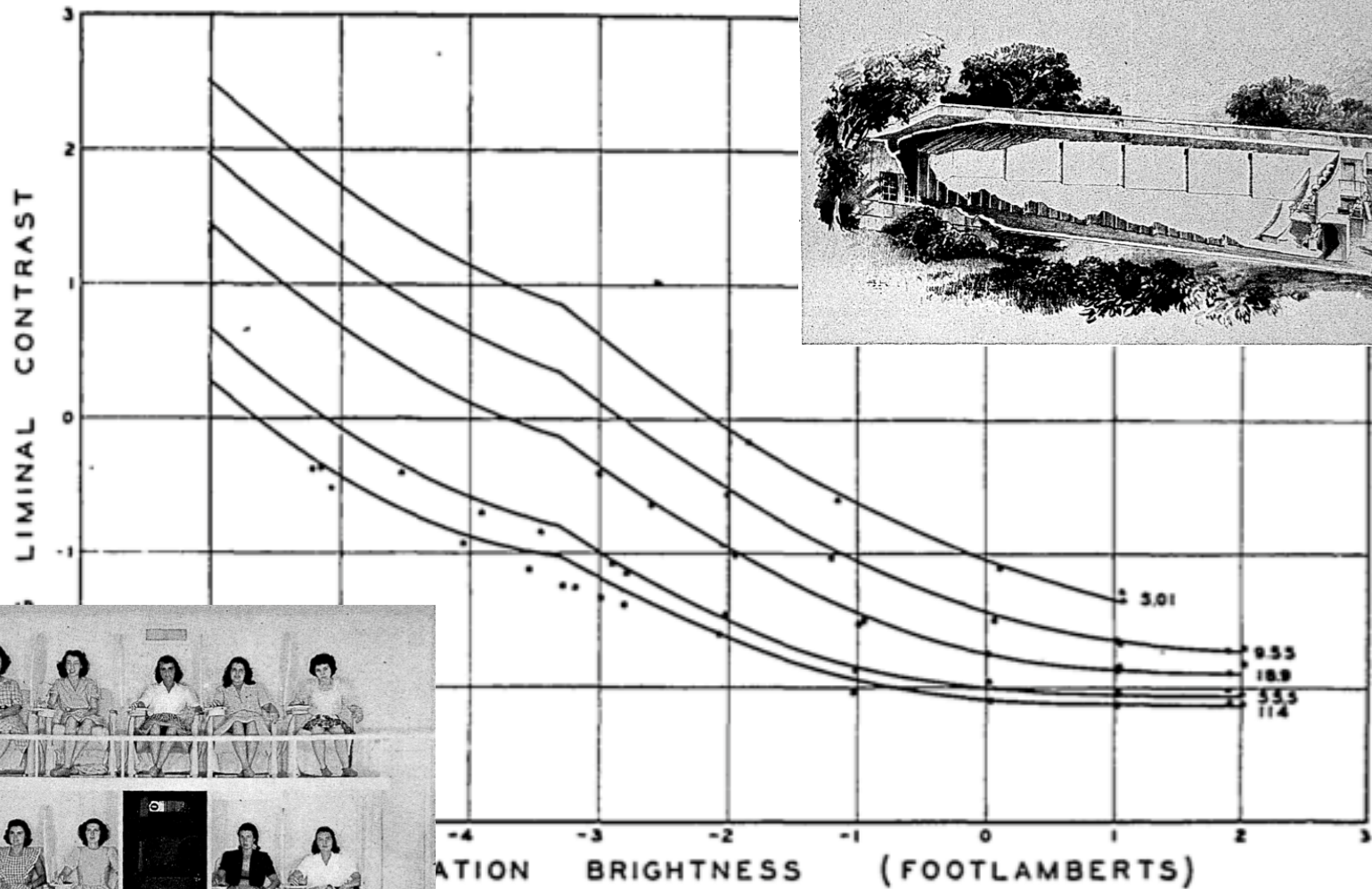
# Detection and discrimination

# Threshold versus intensity (t.v.i.) function

- ▶ The smallest detectable difference in luminance for a given background luminance

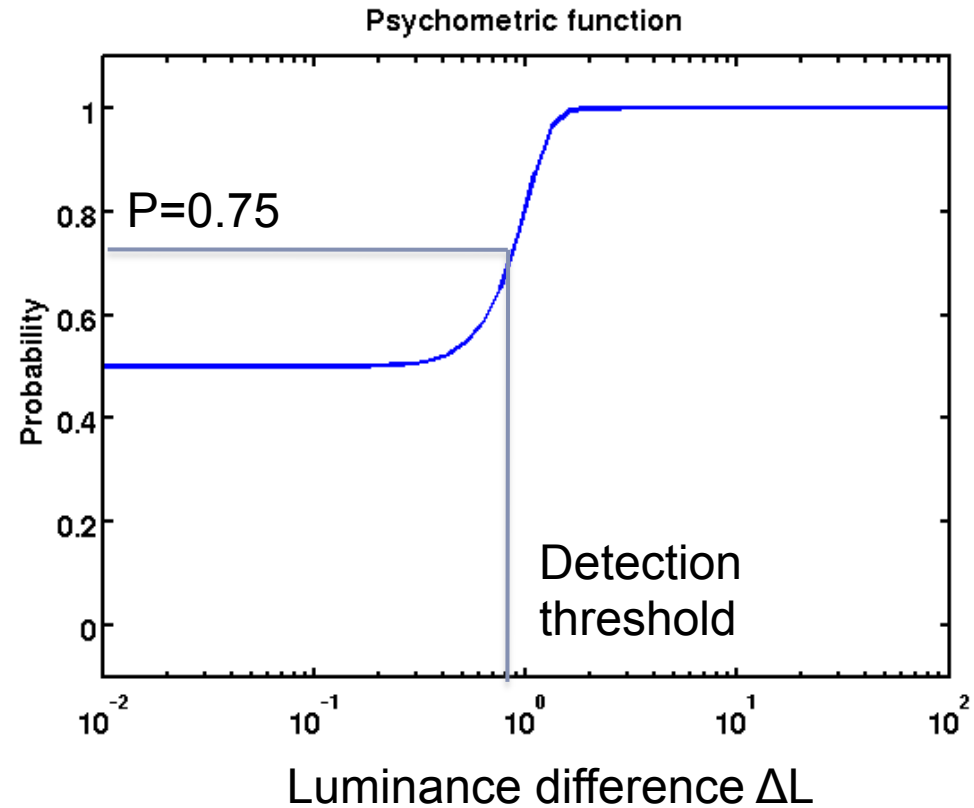
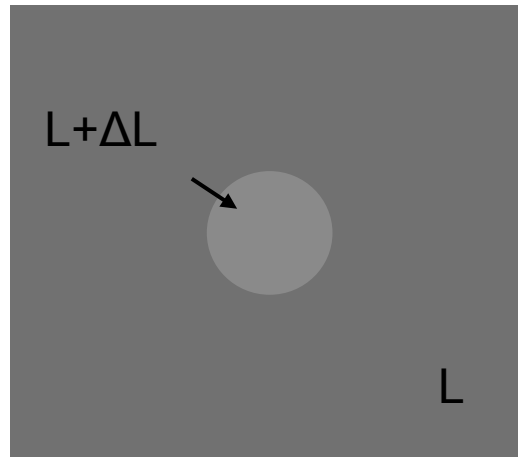


# t.v.i. measurements – Blackwell 1946



# Psychophysics

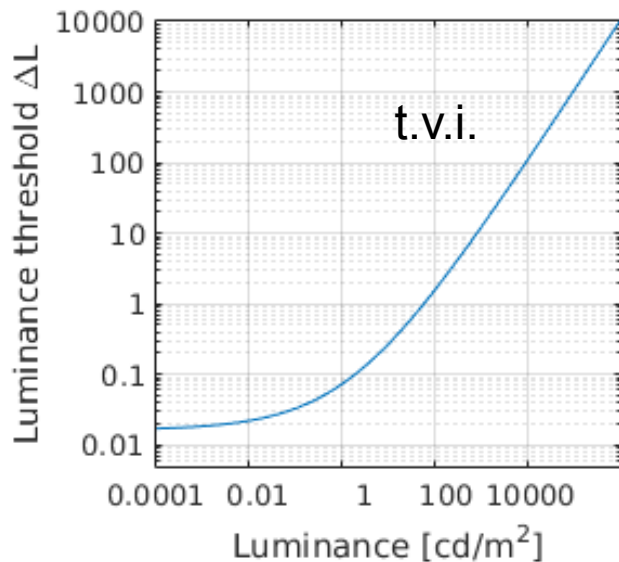
## Threshold experiments



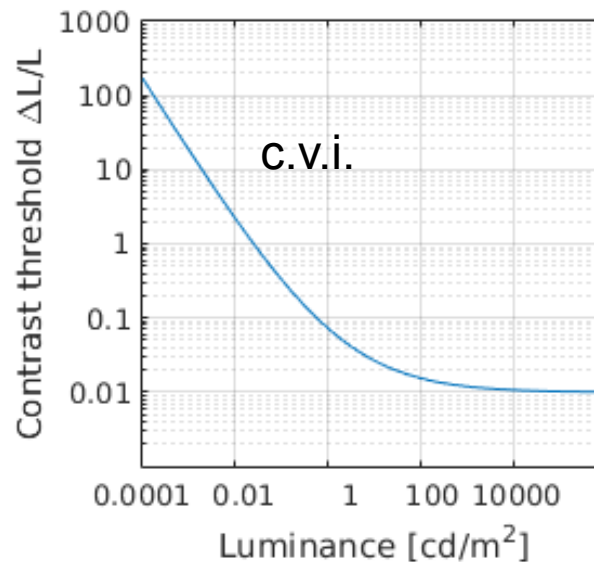
# t.v.i function / c.v.i. function / Sensitivity

- ▶ The same data, different representation

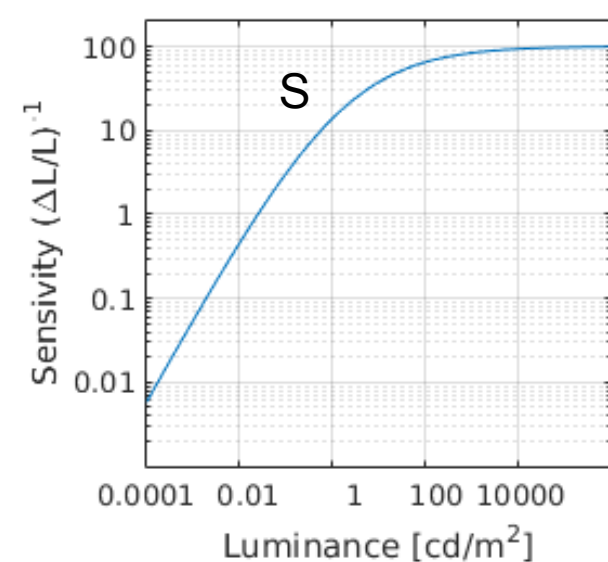
Threshold vs. intensity



Contrast vs. intensity



Sensitivity



$$\Delta L = L_{disk} - L_{background}$$

$$T = \frac{\Delta L}{L}$$

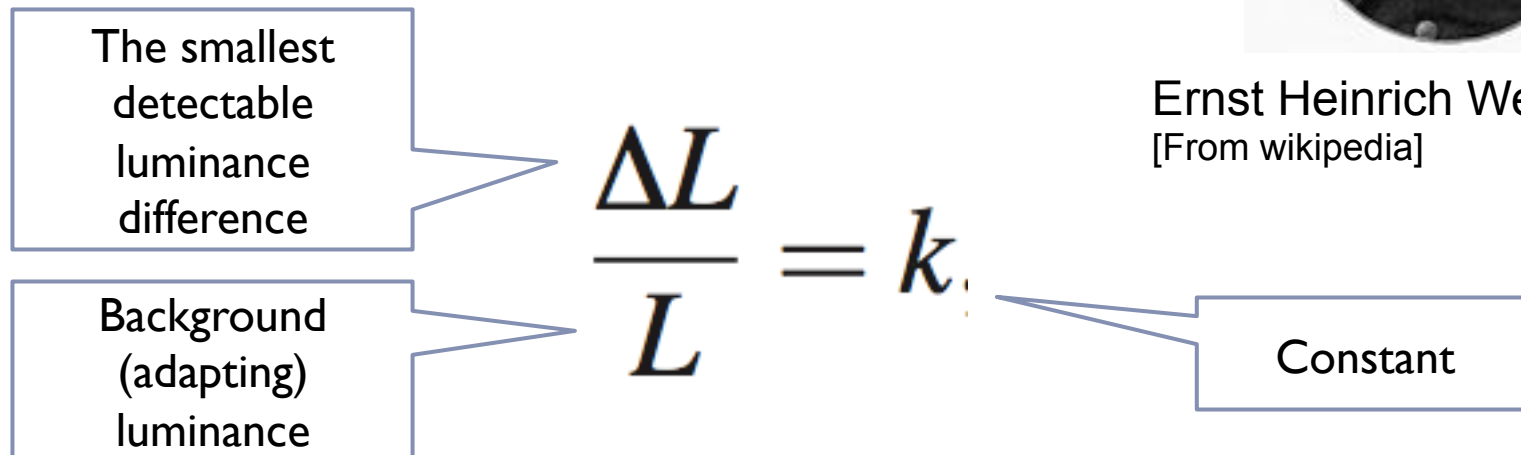
$$S = \frac{1}{T} = \frac{L}{\Delta L}$$

# Sensitivity to luminance

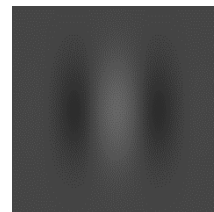
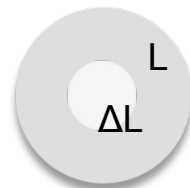
- ▶ Weber-law – the just-noticeable difference is proportional to the magnitude of a stimulus



Ernst Heinrich Weber  
[From wikipedia]



Typical stimuli:



# Consequence of the Weber-law

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- ▶ Smallest detectable difference in luminance

$$\frac{\Delta L}{L} = k$$

L	ΔL
100 cd/m <sup>2</sup>	1 cd/m <sup>2</sup>
1 cd/m <sup>2</sup>	0.01 cd/m <sup>2</sup>

- ▶ Adding or subtracting luminance will have different visual impact depending on the background luminance
- ▶ Unlike LDR luma values, luminance values are **not** perceptually uniform!



# How to make luminance (more) perceptually uniform?

- ▶ Using “Fechnerian” integration

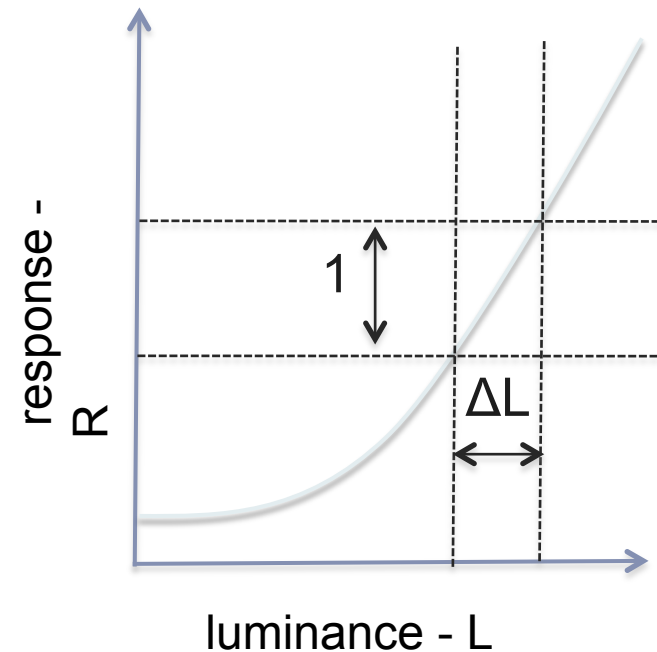
$$\frac{dR}{dl}(L) = \frac{1}{\Delta L(L)}$$

Derivative of response

Detection threshold

Luminance transducer:

$$R(L) = \int_0^L \frac{1}{\Delta L(l)} dl$$



## Assuming the Weber law

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$$\frac{\Delta L}{L} = k.$$

- ▶ and given the luminance transducer

$$R(L) = \int_0^L \frac{1}{\Delta L(l)} dl$$

- ▶ the response of the visual system to light is:

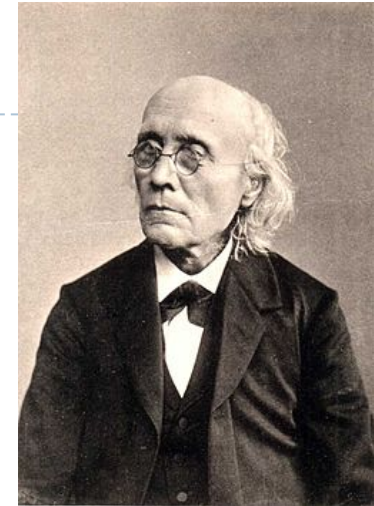
$$R(L) = \int \frac{1}{kL} dL = \frac{1}{k} \ln(L) + k_1$$

## Fechner law

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$$R(L) = a \ln(L)$$

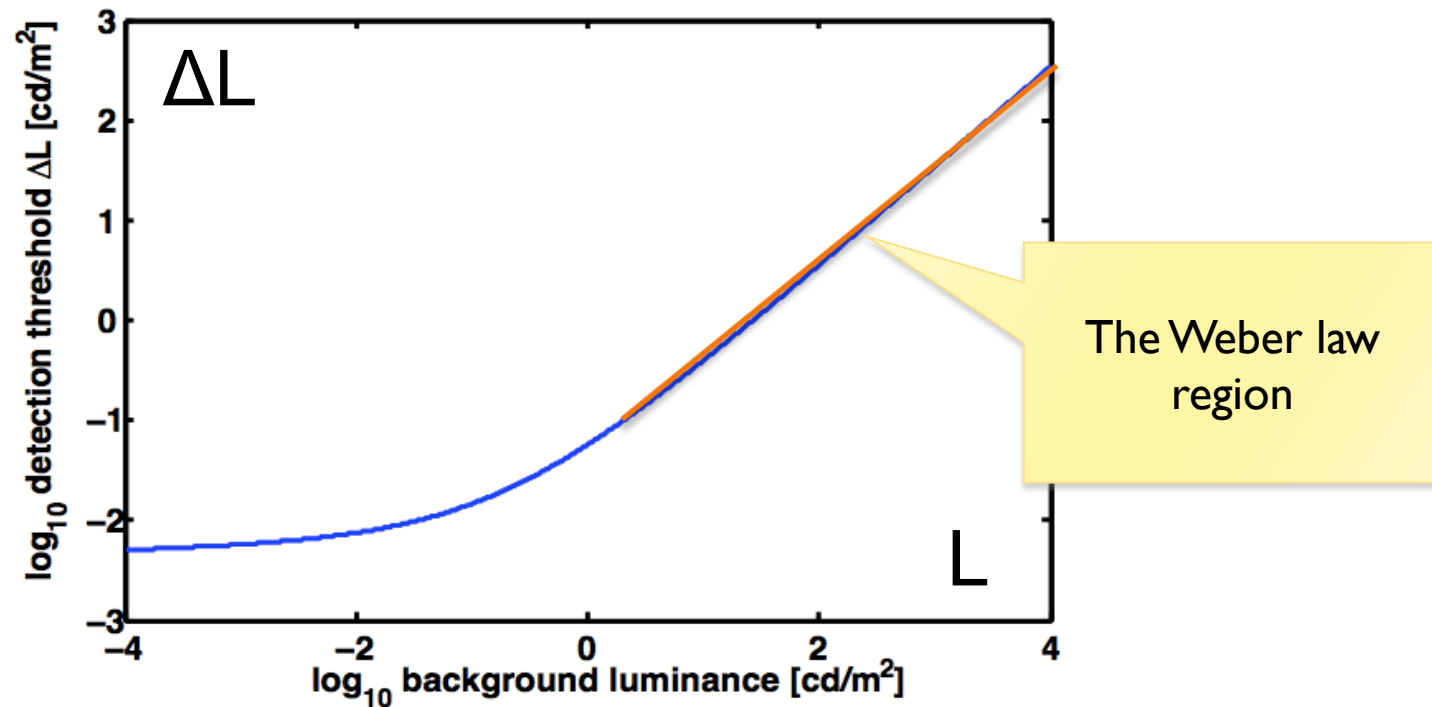
- ▶ Response of the visual system to luminance is **approximately** logarithmic



Gustav Fechner  
[From Wikipedia]

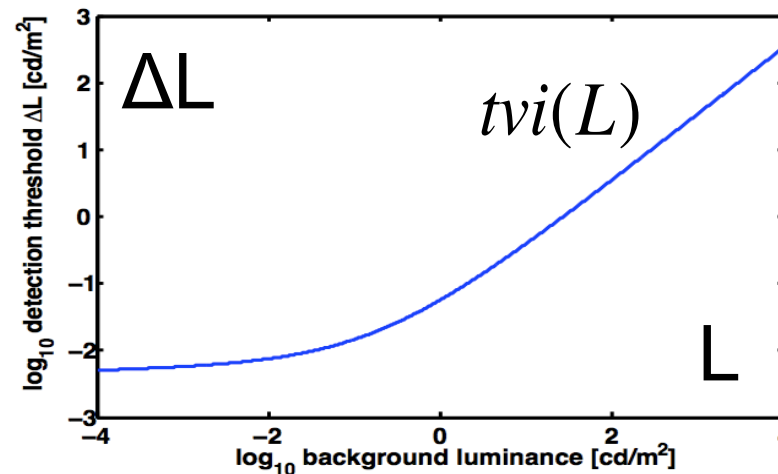
# But...the Fechner law does not hold for the full luminance range

- ▶ Because the Weber law does not hold either
- ▶ Threshold vs. intensity function:



# Weber-law revisited

- ▶ If we allow detection threshold to vary with luminance according to the t.v.i. function:



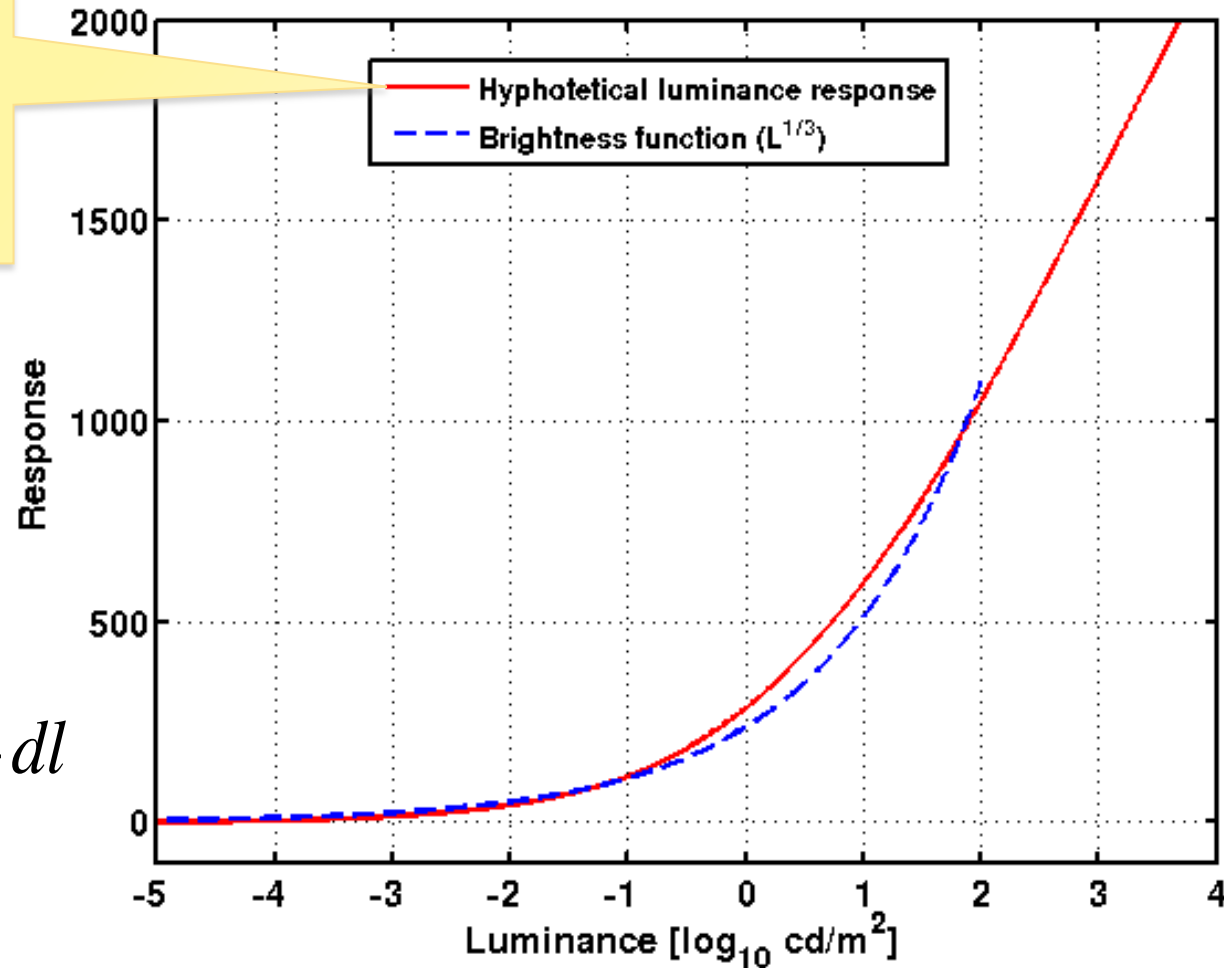
- ▶ we can get more accurate estimate of the “response”:

$$R(L) = \int_0^L \frac{1}{tvi(l)} dl$$

# Fechnerian integration and Stevens' law

R(L) - function derived from the t.v.i. function

$$R(L) = \int_0^L \frac{1}{tvi(l)} dl$$



# Applications of JND encoding – R(L)

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- ▶ **DICOM grayscale function**
  - ▶ Function used to encode signal for medical monitors
  - ▶ 10-bit JND-scaled (just noticeable difference)
  - ▶ Equal visibility of gray levels
- ▶ **Dolby Vision – Perceptual Quantizer**
  - ▶ To encode pixels for high dynamic range images and video



The Future of Vision

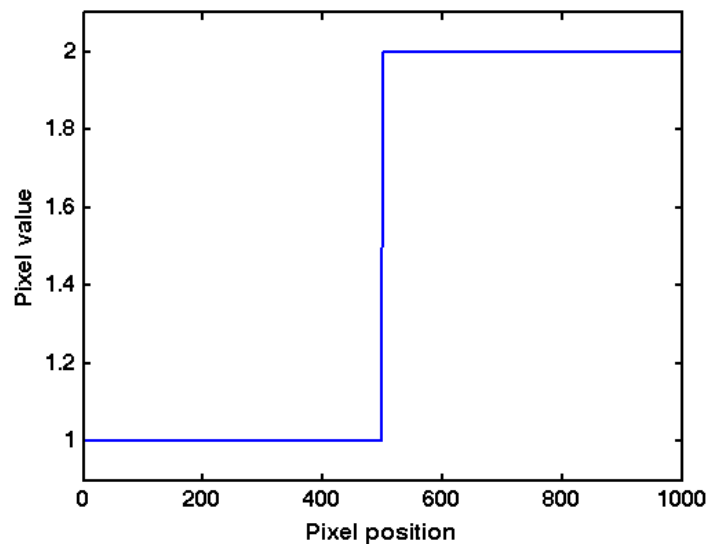
# Spatial contrast sensitivity



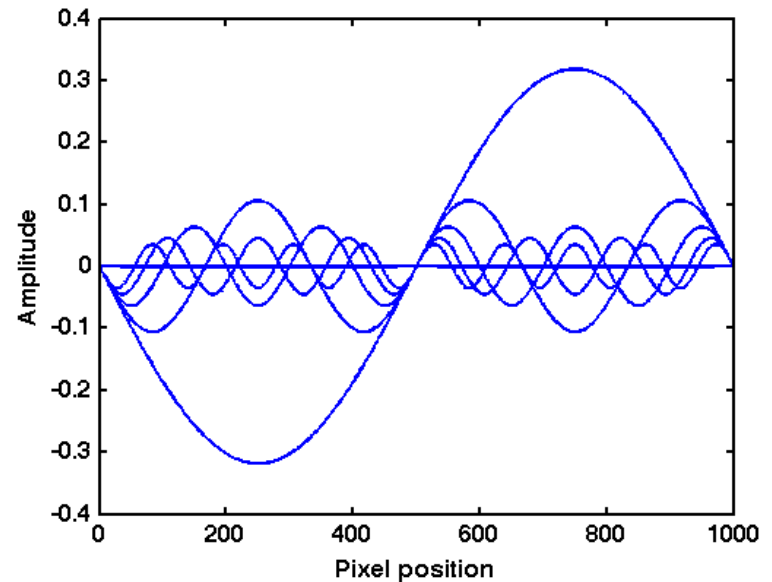
# Fourier analysis

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- ▶ Every N-dimensional function (including images) can be represented as a sum of sinusoidal waves of different frequency and phase



$$= \sum$$

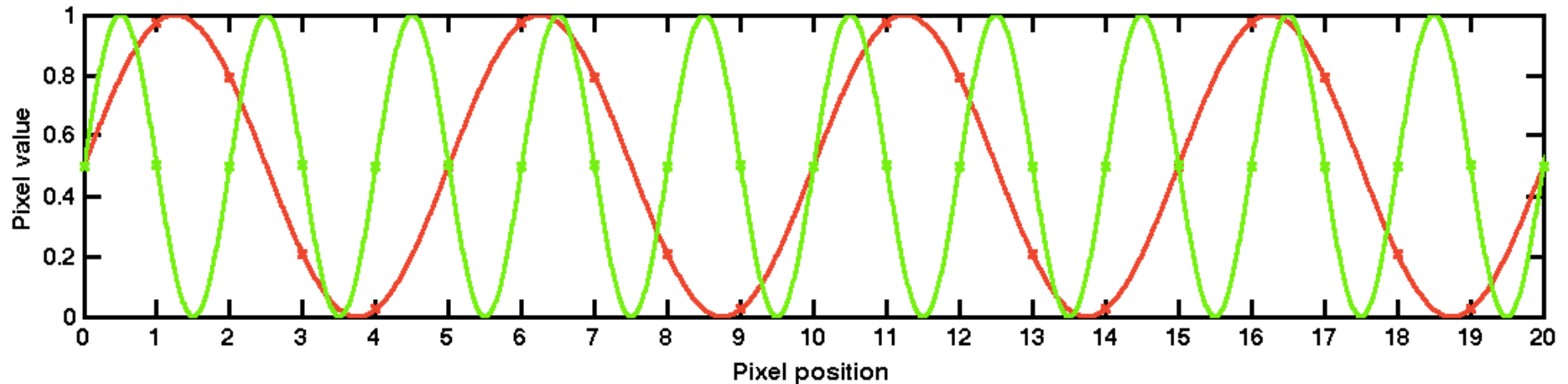


- ▶ Think of “equalizer” in audio software, which manipulates each frequency

# Spatial frequency in images

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- ▶ Image space units: cycles per sample (or cycles per pixel)

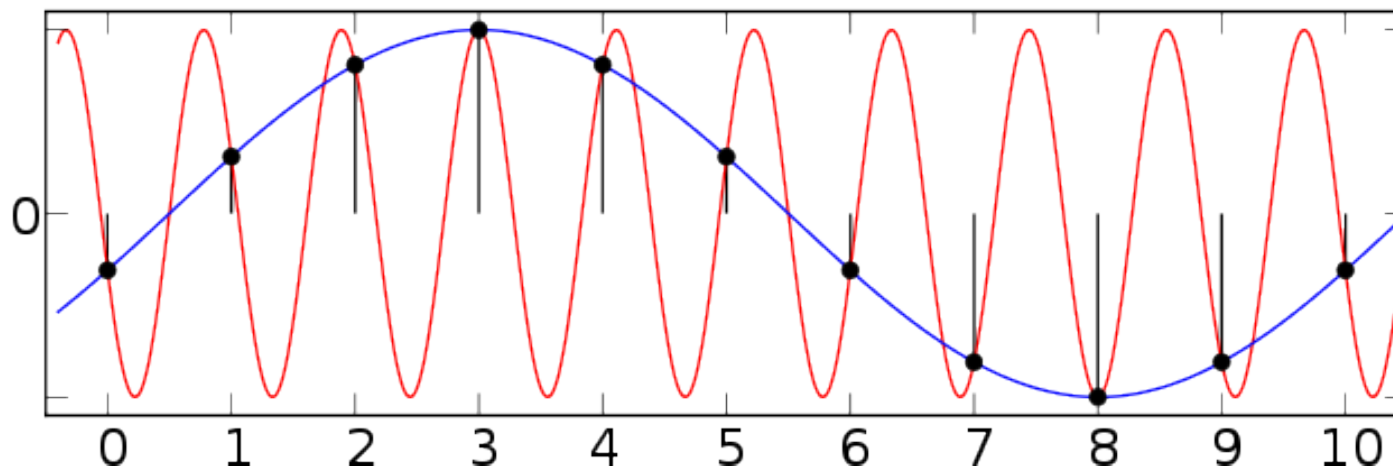


- ▶ What are the screen-space frequencies of the red and green sinusoid?
- ▶ The visual system units: cycles per degree
  - ▶ If the angular resolution of the viewed image is 55 pixels per degree, what is the frequency of the sinusoids in cycles per degree?

# Nyquist frequency

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- ▶ What is the highest frequency that can be reconstructed for a given sampling density?
  - ▶ Sampling density – how many pixels per image/visual angle/...



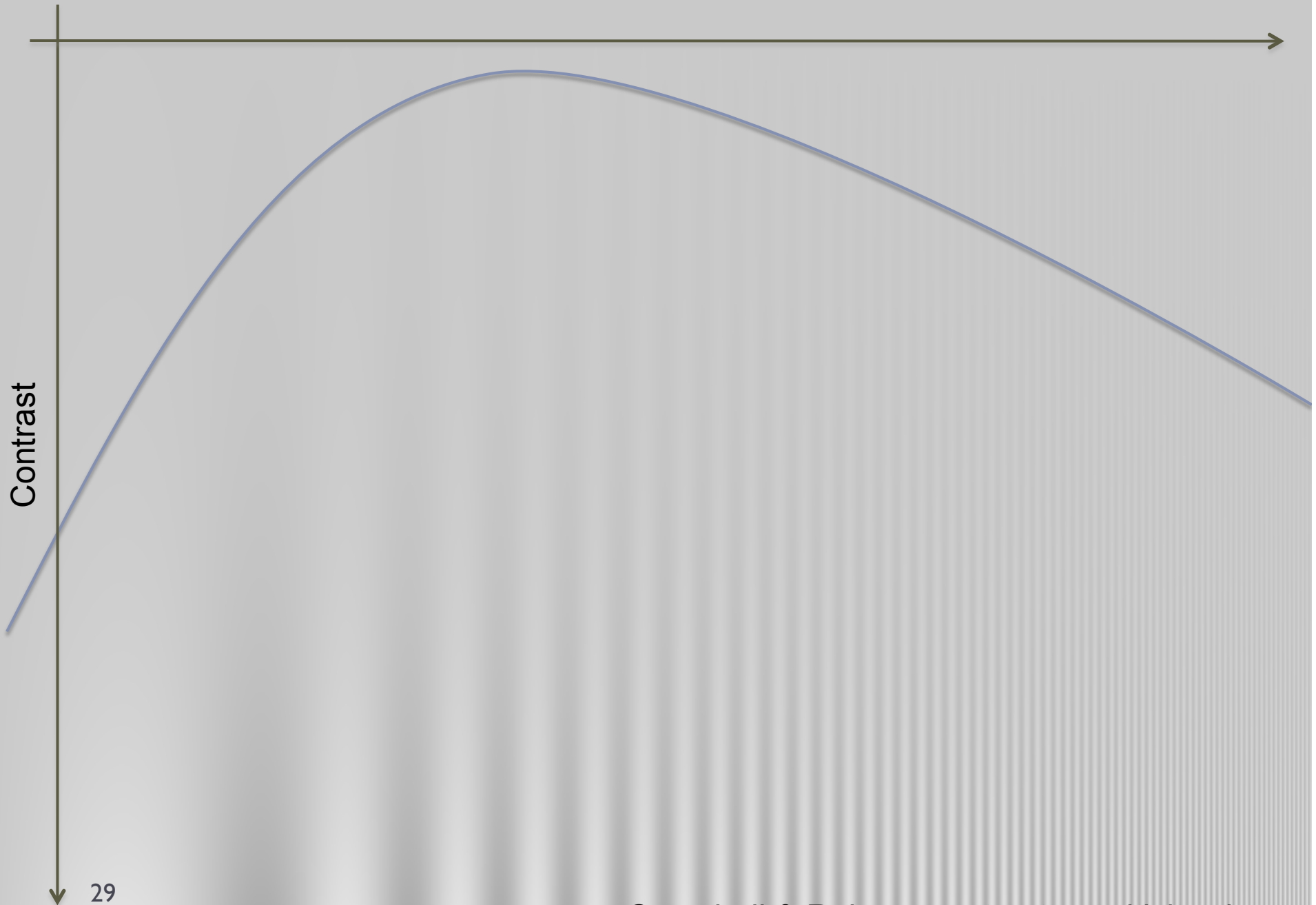
- ▶ Two different sinusoids can be fitted to this set of samples
- ▶ It is possible to fit an infinite number of sinusoids if we allow infinitely high frequency

# Nyquist frequency / aliasing

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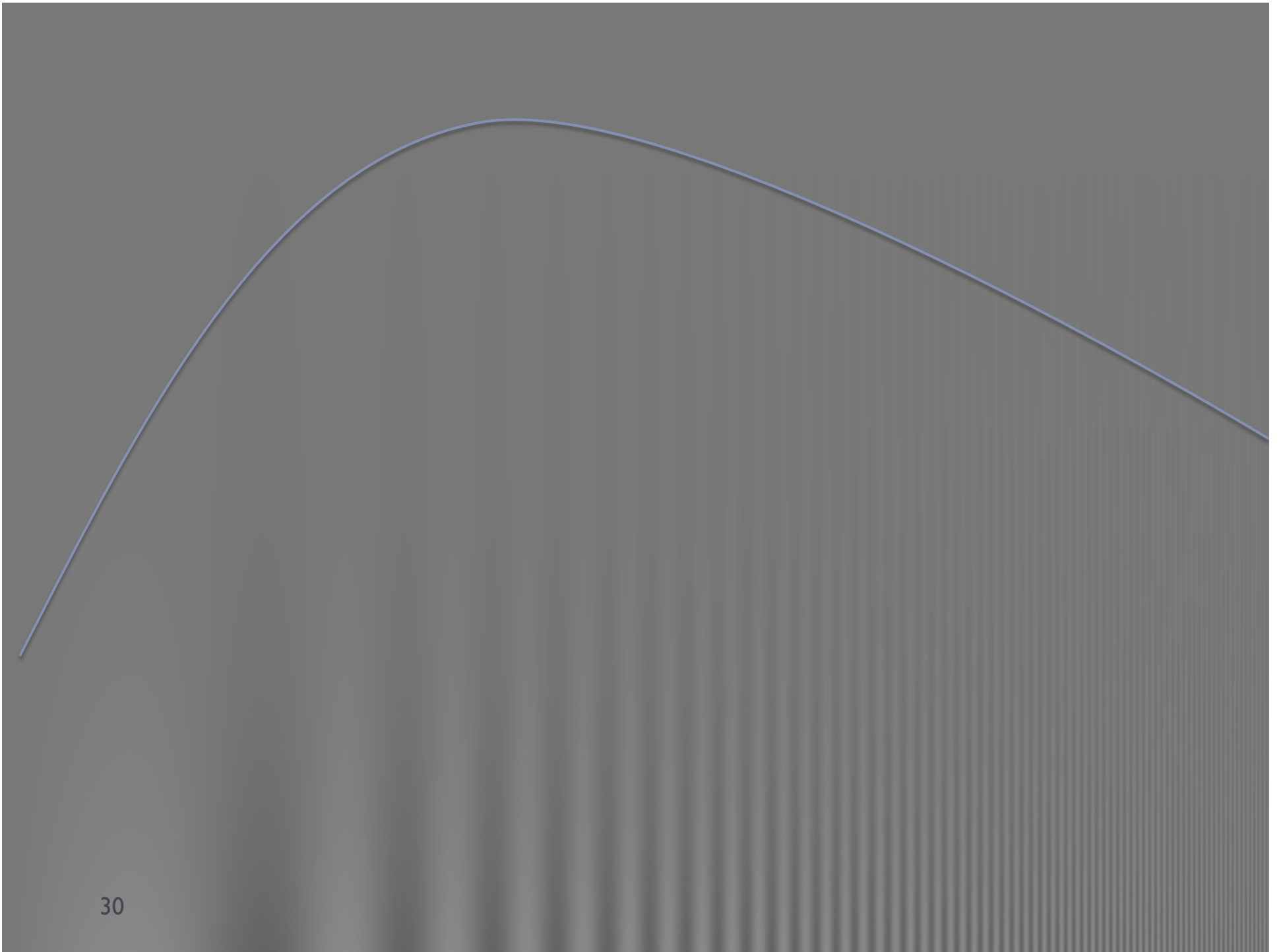
- ▶ Nyquist frequency is the highest frequency that can be represented by a discrete set of uniform samples (pixels)
- ▶ Nyquist frequency = 0.5 sampling rate
  - ▶ For audio
    - ▶ If the sampling rate is 44100 samples per second (audio CD), then the Nyquist frequency is 22050 Hz
  - ▶ For images (visual degrees)
    - ▶ If the sampling rate is 60 pixels per degree, then the Nyquist frequency is 30 cycles per degree
- ▶ When resampling an image to lower resolution, the frequency content above the Nyquist frequency needs to be removed (reduced in practice)
  - ▶ Otherwise **aliasing** is visible

Spatial frequency [cycles per degree]



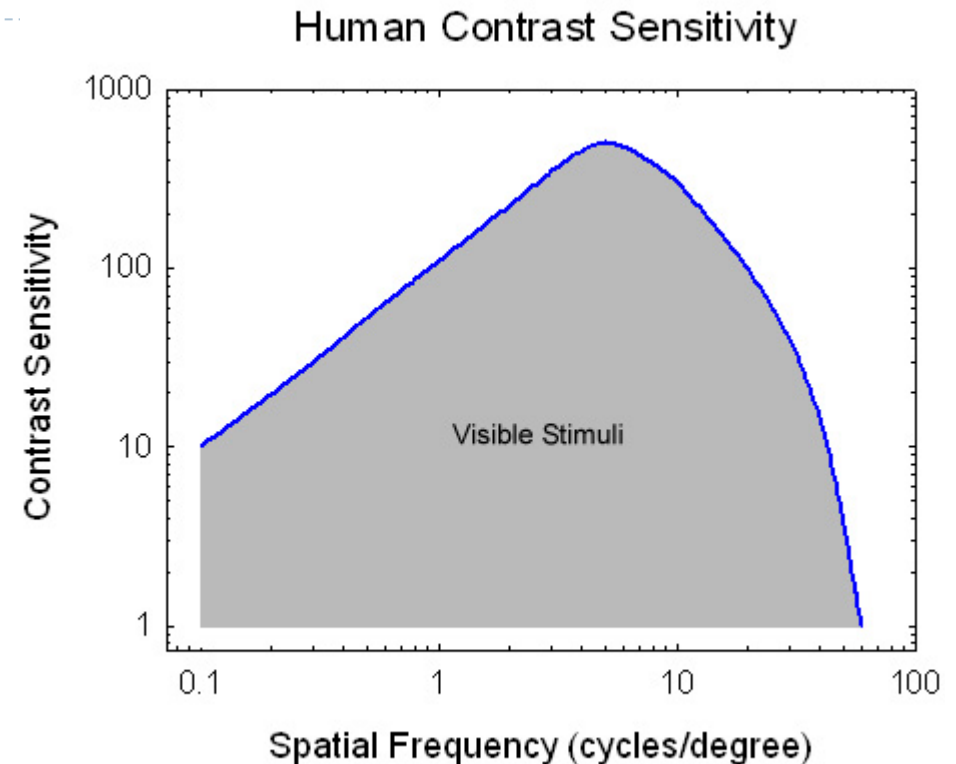
29

Campbell & Robson contrast sensitivity chart



# Contrast Sensitivity

- ▶ Sensitivity:  
I / threshold contrast
- ▶ Contrast =  $\Delta L/L$
- ▶ Maximum acuity 2-5 cycles/degree (0.2 %)
  - ▶ Decrease toward low frequencies: lateral inhibition
  - ▶ Decrease toward high frequencies
  - ▶ Upper limit: 60-70 cycles/degree



Rationale: if we were sensitive to low frequencies, the vision would be affected by changes of illumination. There are physical limitations to the perception of high frequencies.

# Implications of CSF

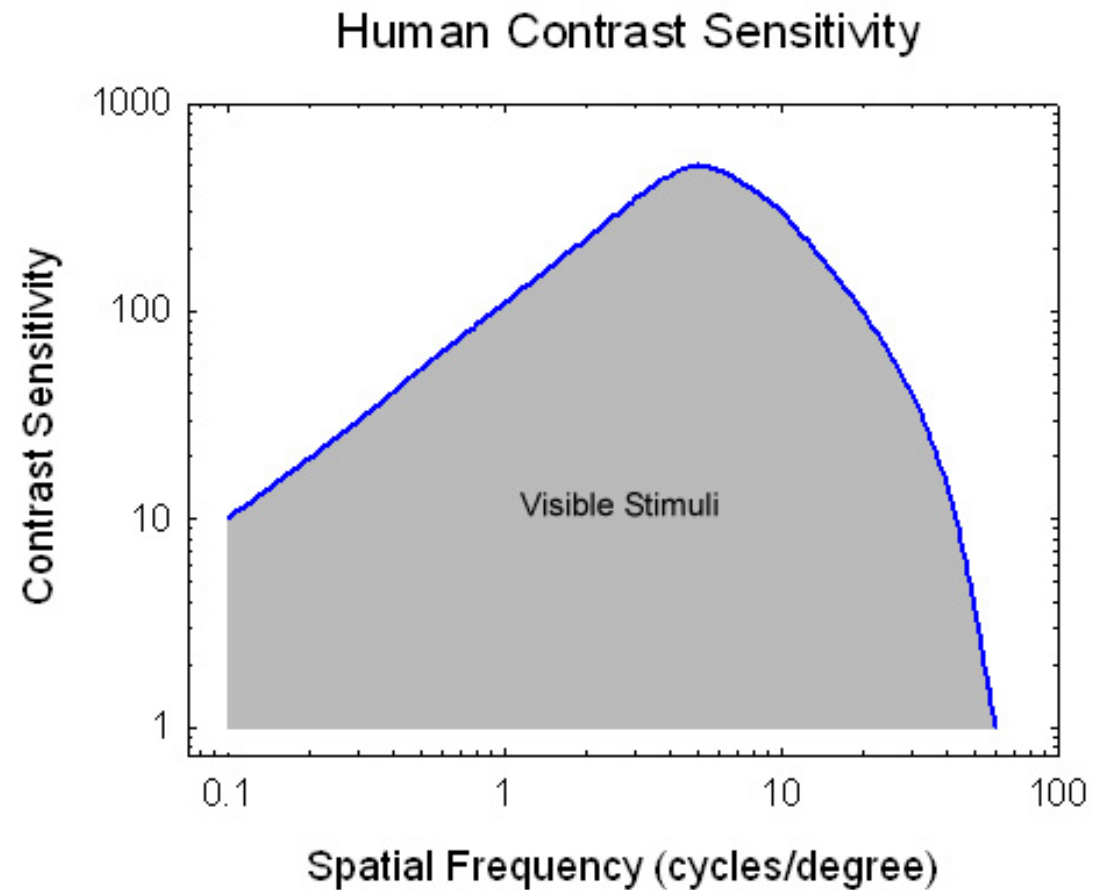
- ▶ As objects get further away, they get smaller; spatial frequencies get higher
  - ▶ At some point we cannot see the details
  - ▶ That is the upper limit of the CSF (60-70 cpd)
- ▶ When we get too close to low frequency patterns, they seem to be constant
  - ▶ The background of this slide contains a smooth gradient
  - ▶ It is well visible when you look at it from a normal viewing distance
  - ▶ Now enlarge the slide to full screen and move your head very close
  - ▶ The gradient should disappear



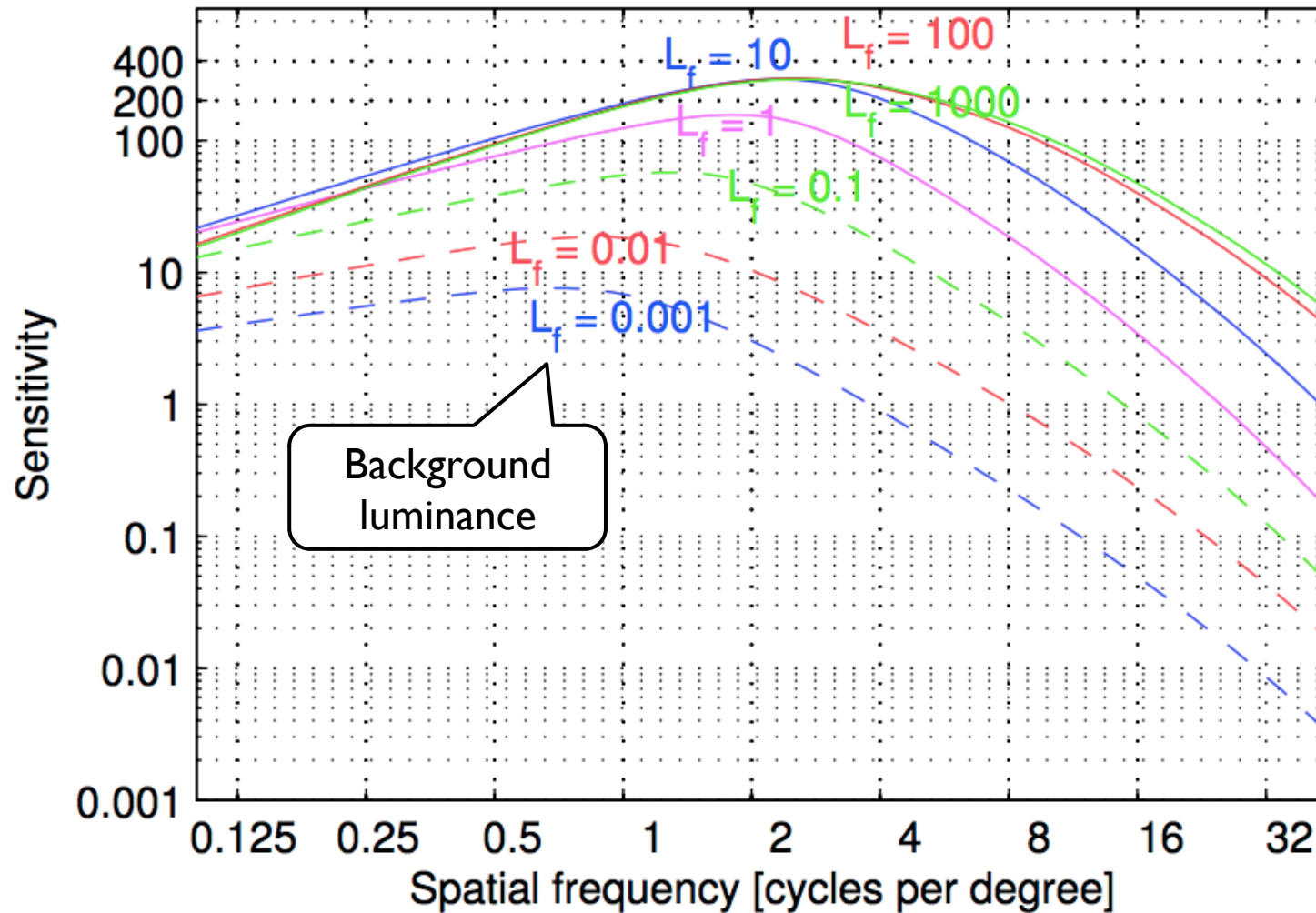
# Explaining the effects with CSF

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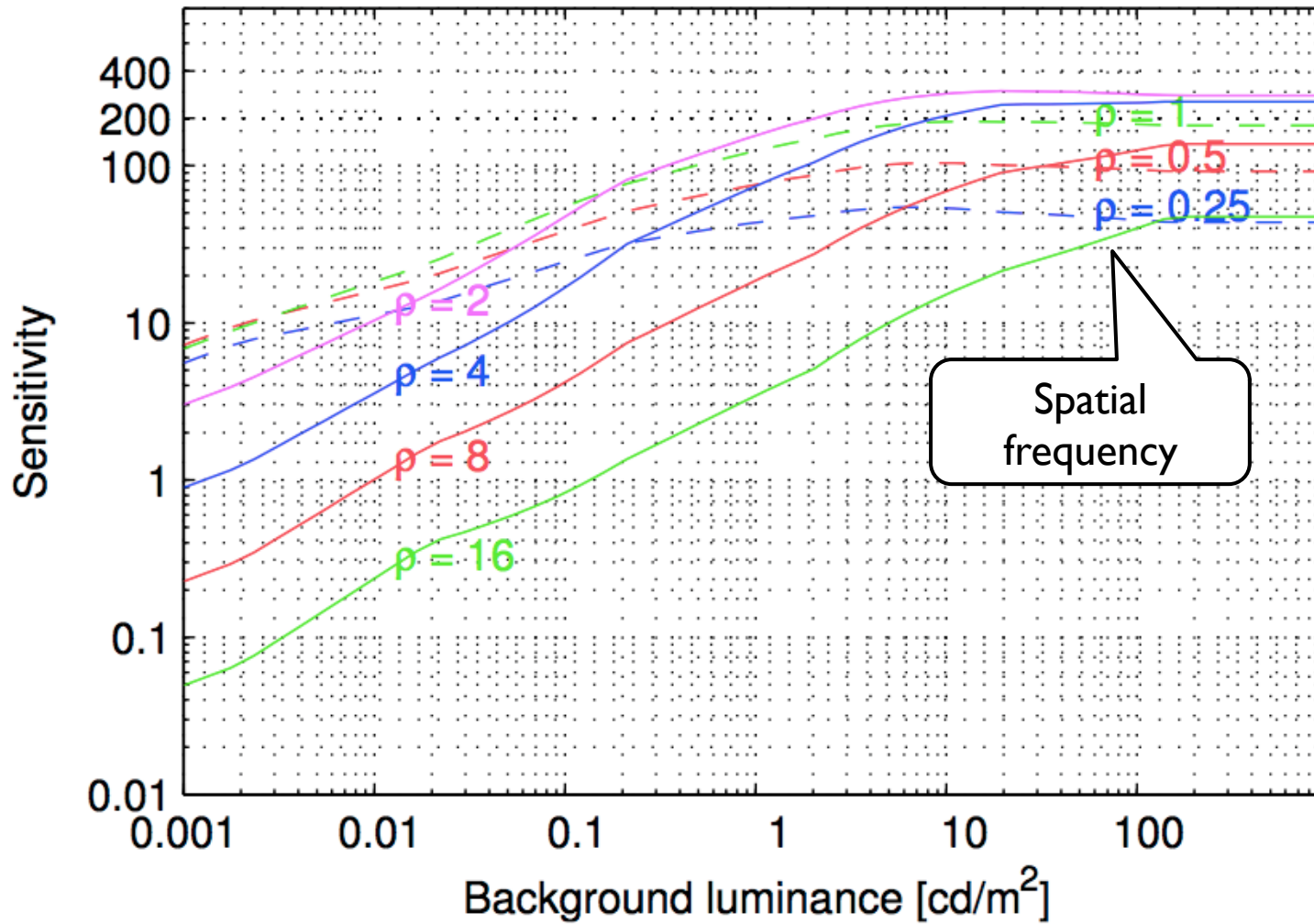
- ▶ Can you explain the effects described on the previous slide using the CSF plot?



# CSF as a function of spatial frequency



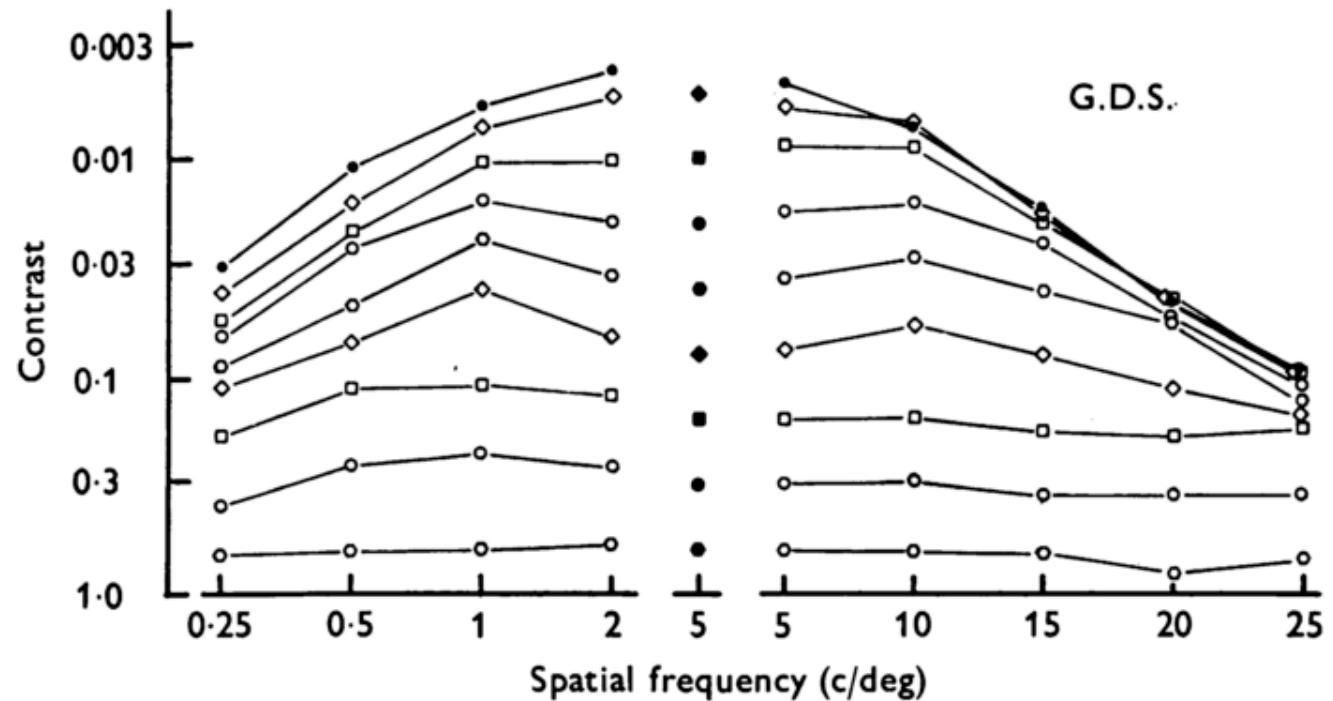
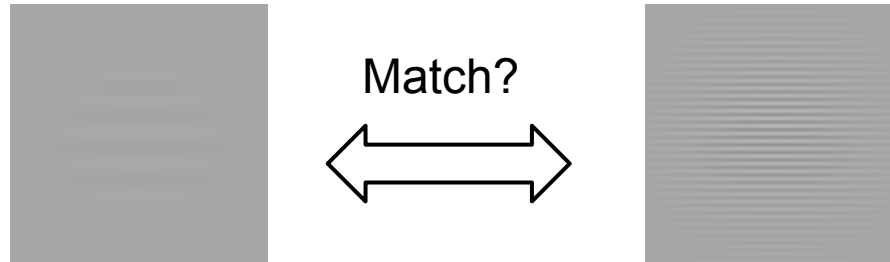
# CSF as a function of background luminance



# Contrast constancy

# Contrast constancy

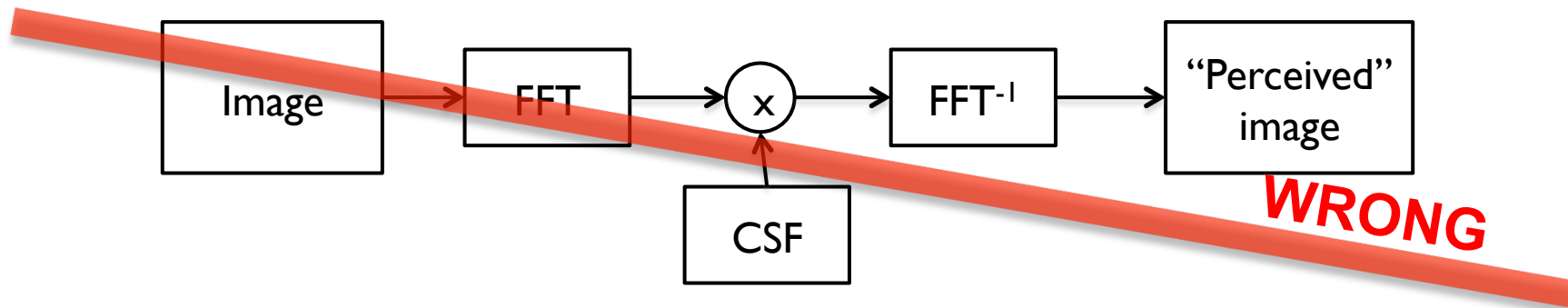
Experiment: Adjust the amplitude of one sinusoidal grating until it matches the perceived magnitude of another sinusoidal grating.



Contrast constancy  
No CSF above the detection threshold

# Contrast constancy

- ▶ For high (supra-threshold) contrast, the perceived magnitude of contrast does not change with spatial frequency
- ▶ The CSF gets “flat” above the detection threshold
- ▶ A common mistake - use CSF as a linear filter:



- ▶ why CSF cannot be used as a linear filter?

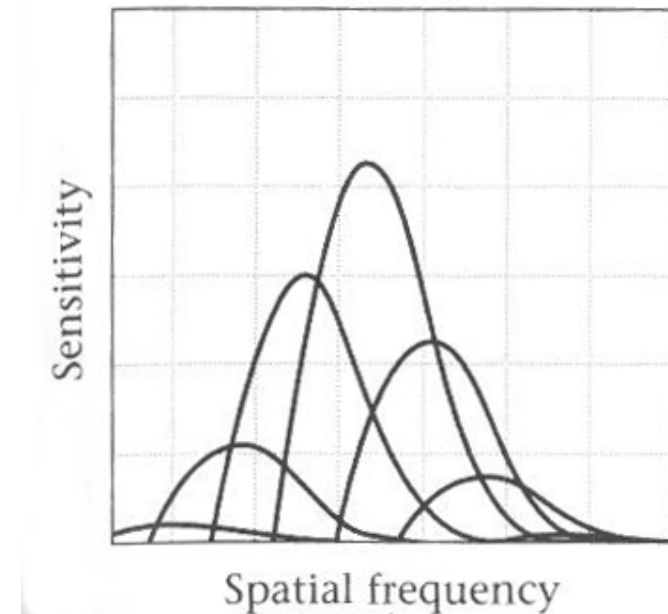
# Multi-resolution models



# Spatial-frequency selective channels

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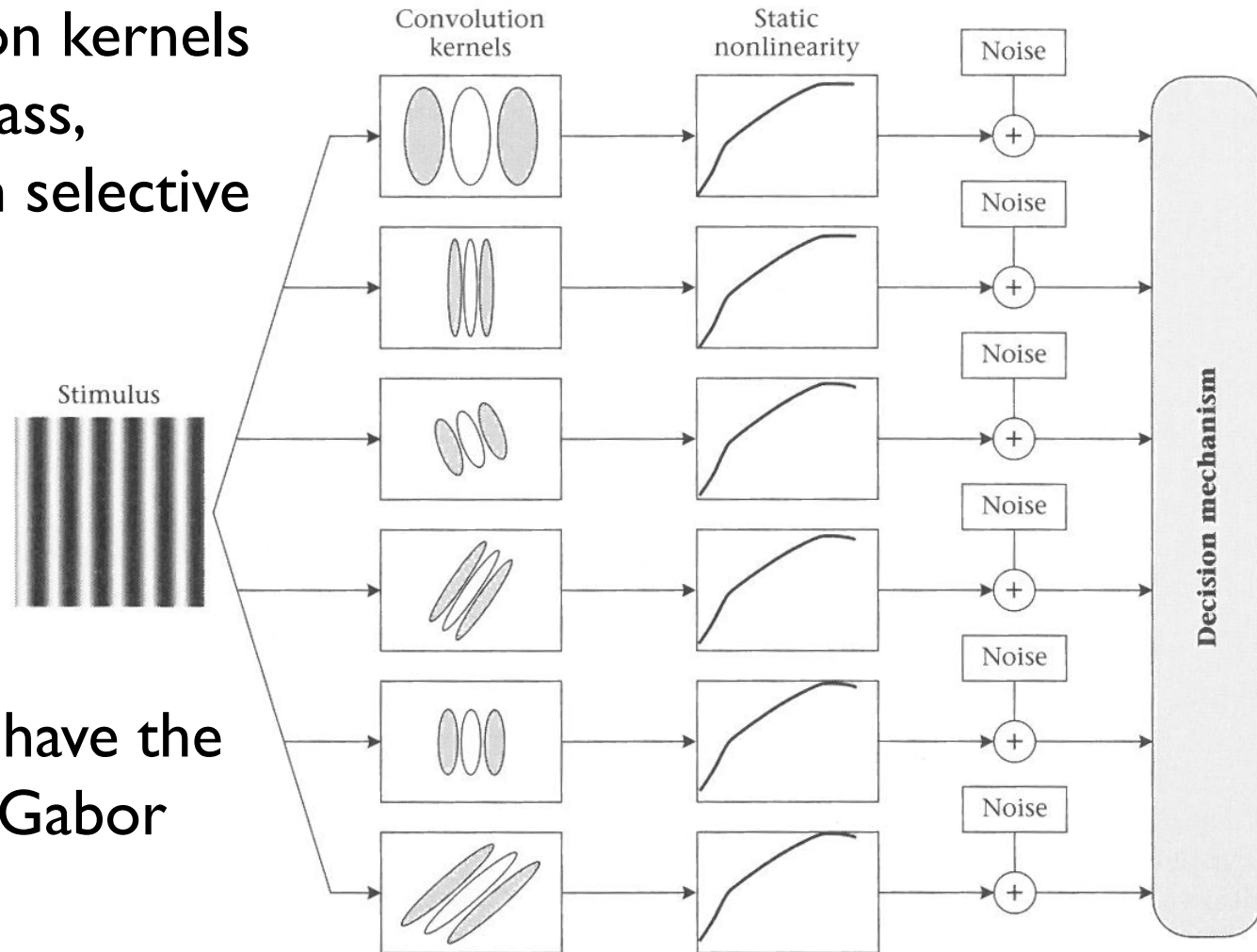
- ▶ The visual information is passed to the visual cortex in multiple channels
  - ▶ The channels are selective to spatial frequency, temporal frequency and orientation
  - ▶ Each channel is affected by different „noise” level
  - ▶ The CSF is the net result of information being passed in noise-affected visual channels



From: Wandell, 1995

# Multi-resolution visual model

- ▶ Convolution kernels are band-pass, orientation selective filters

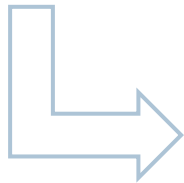


- ▶ The filters have the shape of a Gabor function

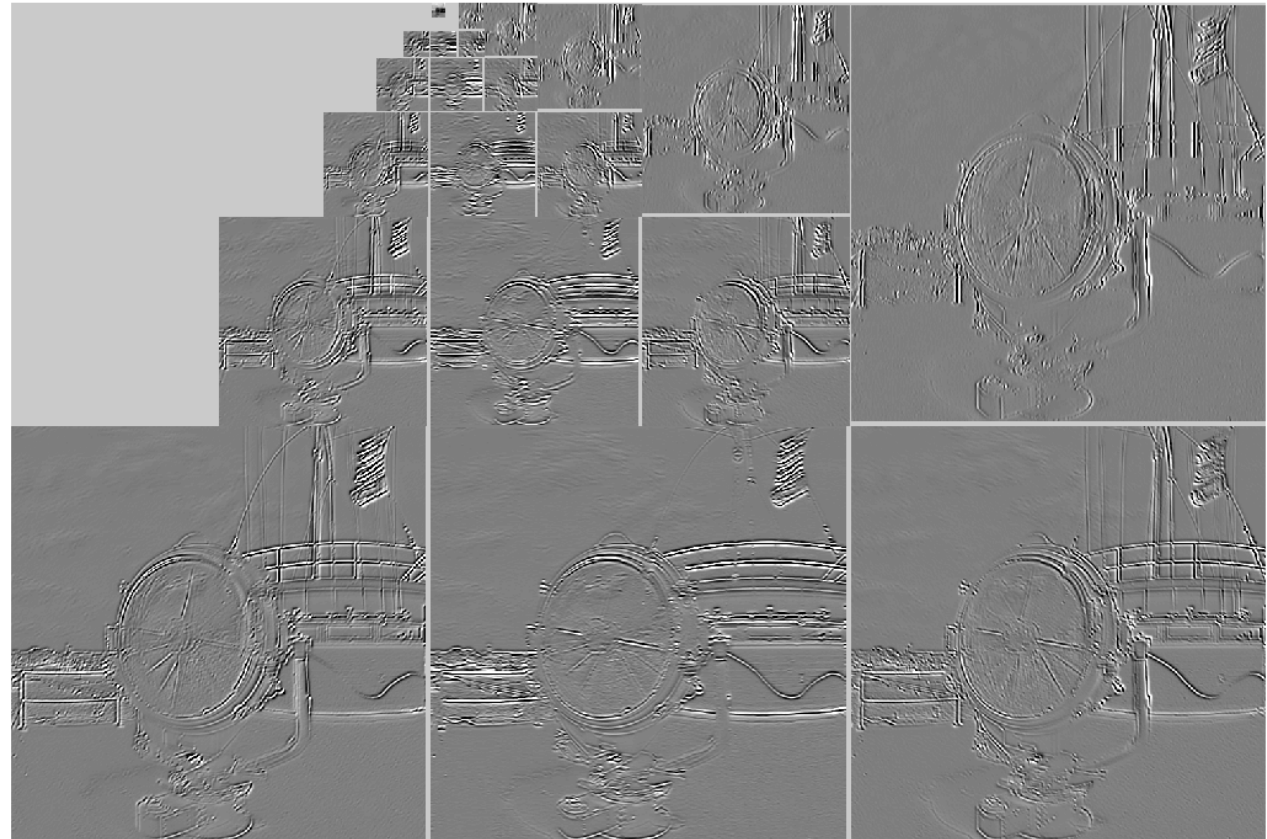
From: Wandell, 1995

# Multi-scale decomposition

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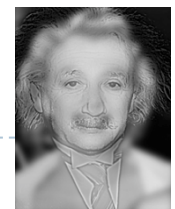
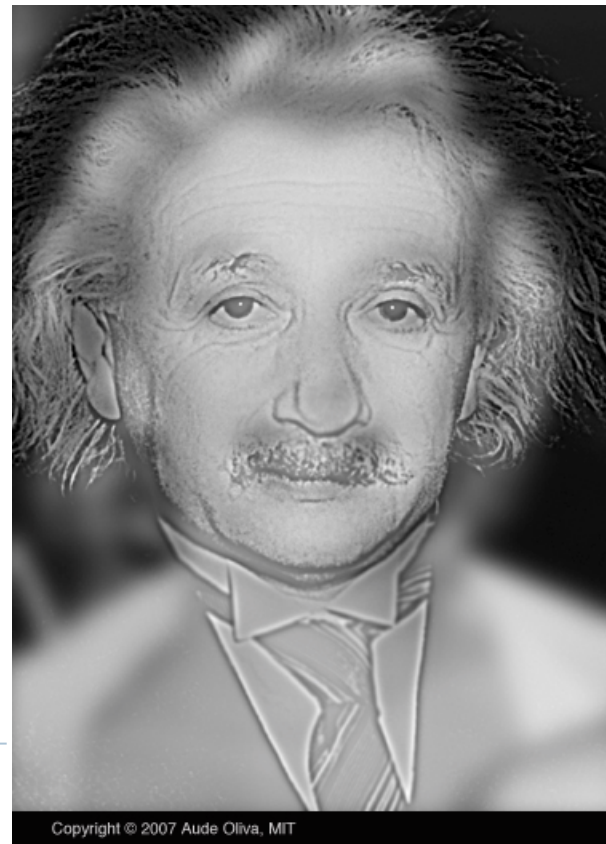
Steerable pyramid  
decomposition



# Applications of multi-scale models

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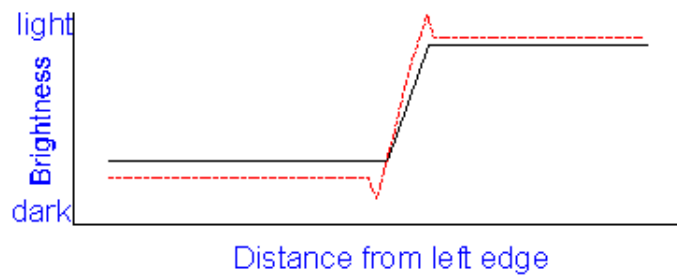
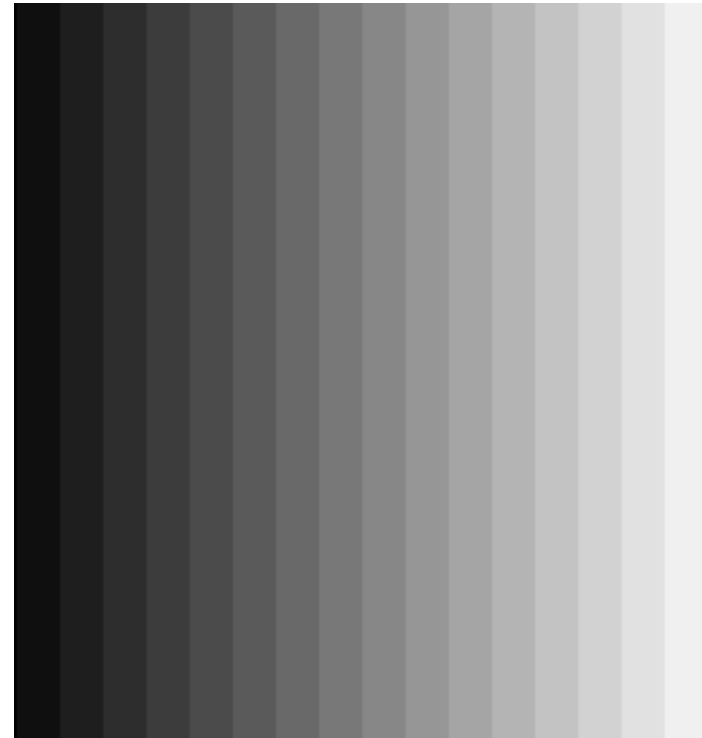
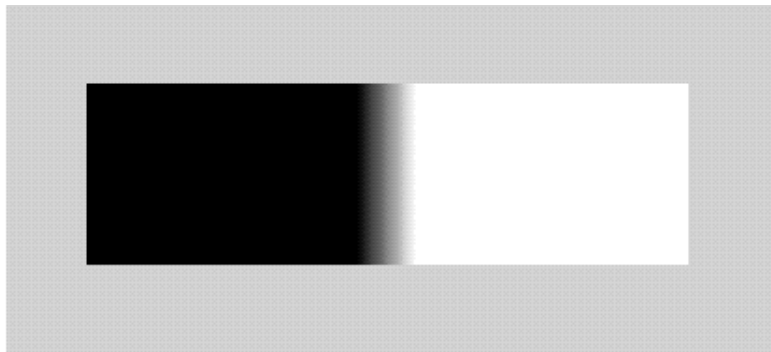
- ▶ **JPEG2000**
  - ▶ Wavelet decomposition
- ▶ **JPEG / MPEG**
  - ▶ Frequency transforms
- ▶ **Image pyramids**
  - ▶ Blending & stitching
  - ▶ Hybrid images



# Mach Bands – evidence for band-pass visual processing

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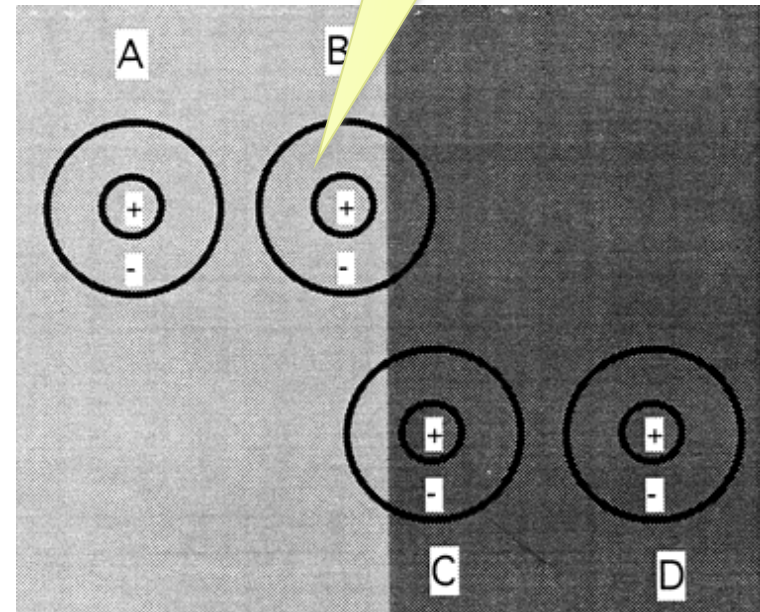
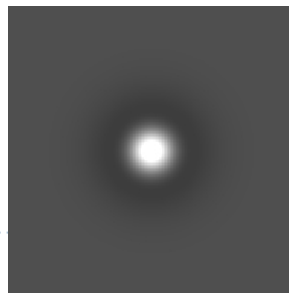
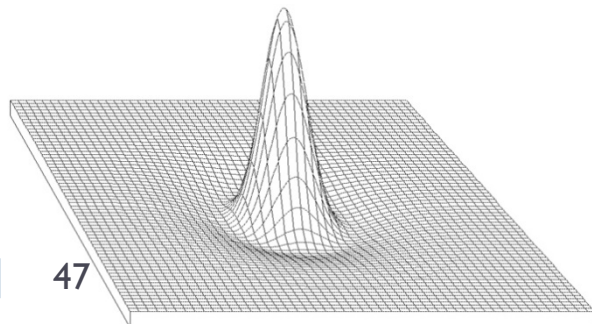
- “Overshooting” along edges
  - Extra-bright rims on bright sides
  - Extra-dark rims on dark sides
- Due to “Lateral Inhibition”



# Centre-surround (Lateral Inhibition)

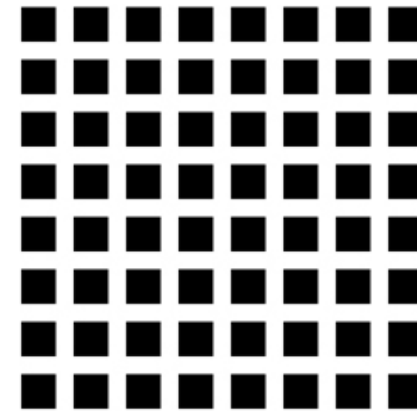
- ▶ “Pre-processing” step within the retina
  - ▶ Surrounding brightness level weighted negatively
    - ▶ A: high stimulus, maximal bright inhibition
    - ▶ B: high stimulus, reduced inhibition & stronger response
    - ▶ D: low stimulus, maximal inhibition
    - ▶ C: low stimulus, increased inhibition & weaker response

Center-surround receptive fields (groups of photoreceptors)



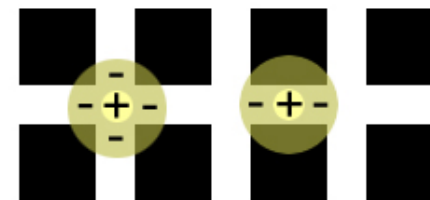
# Centre-surround: Hermann Grid

- Dark dots at crossings
- Explanation
  - Crossings (A)
    - More surround stimulation (more bright area)
    - ⇒ Less inhibition
    - ⇒ Weaker response
  - Streets (B)
    - Less surround stimulation
    - ⇒ More inhibition
    - ⇒ Greater response
- Simulation
  - Darker at crossings, brighter in streets
  - Appears more steady
  - What if reversed ?

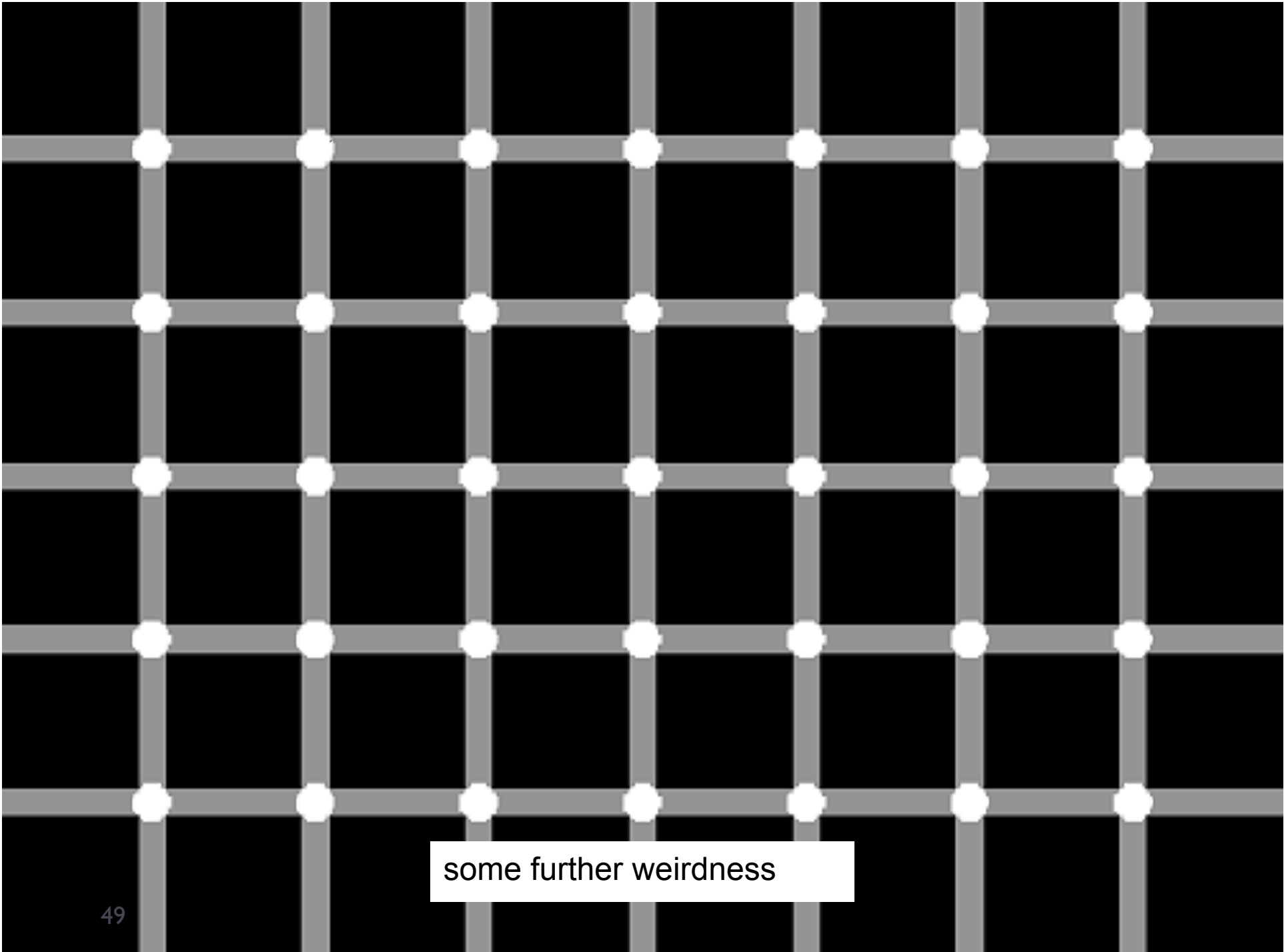


A

B



Simulation



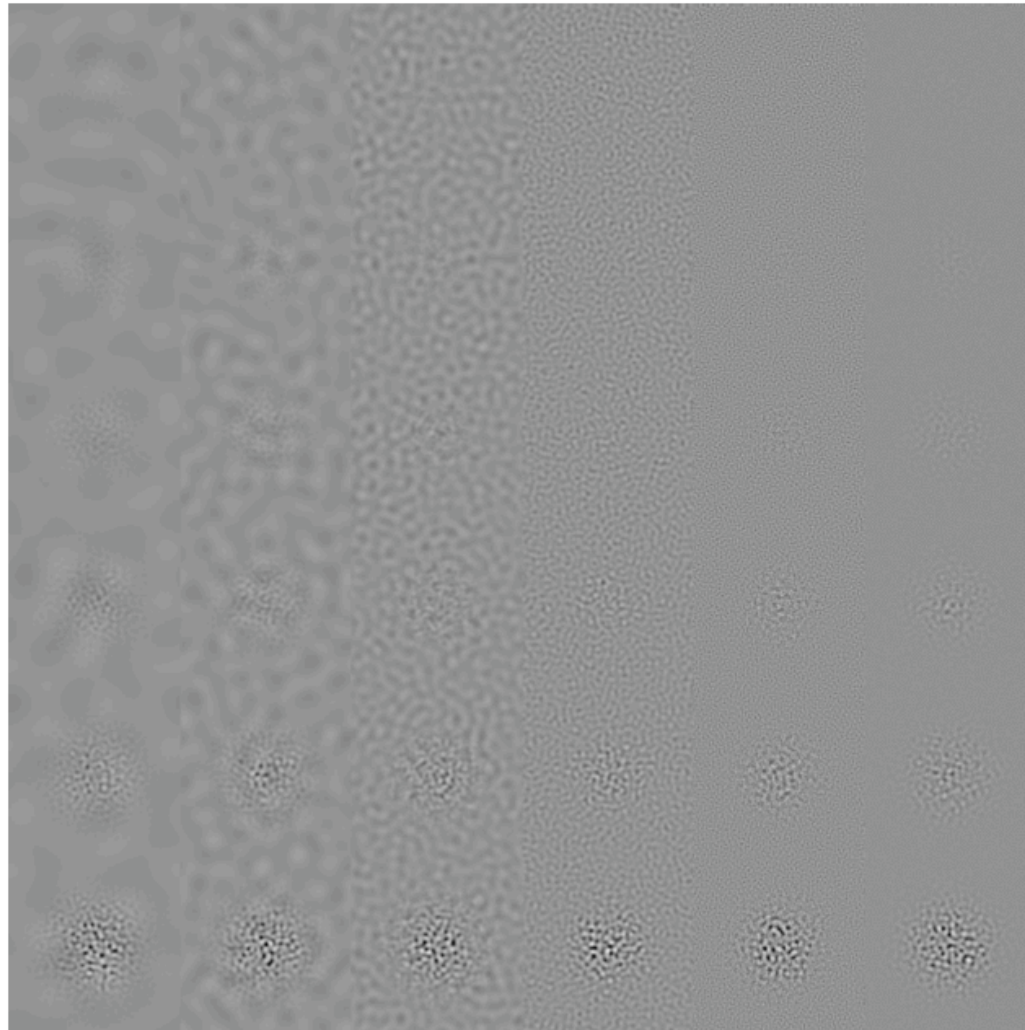
some further weirdness



# Contrast masking

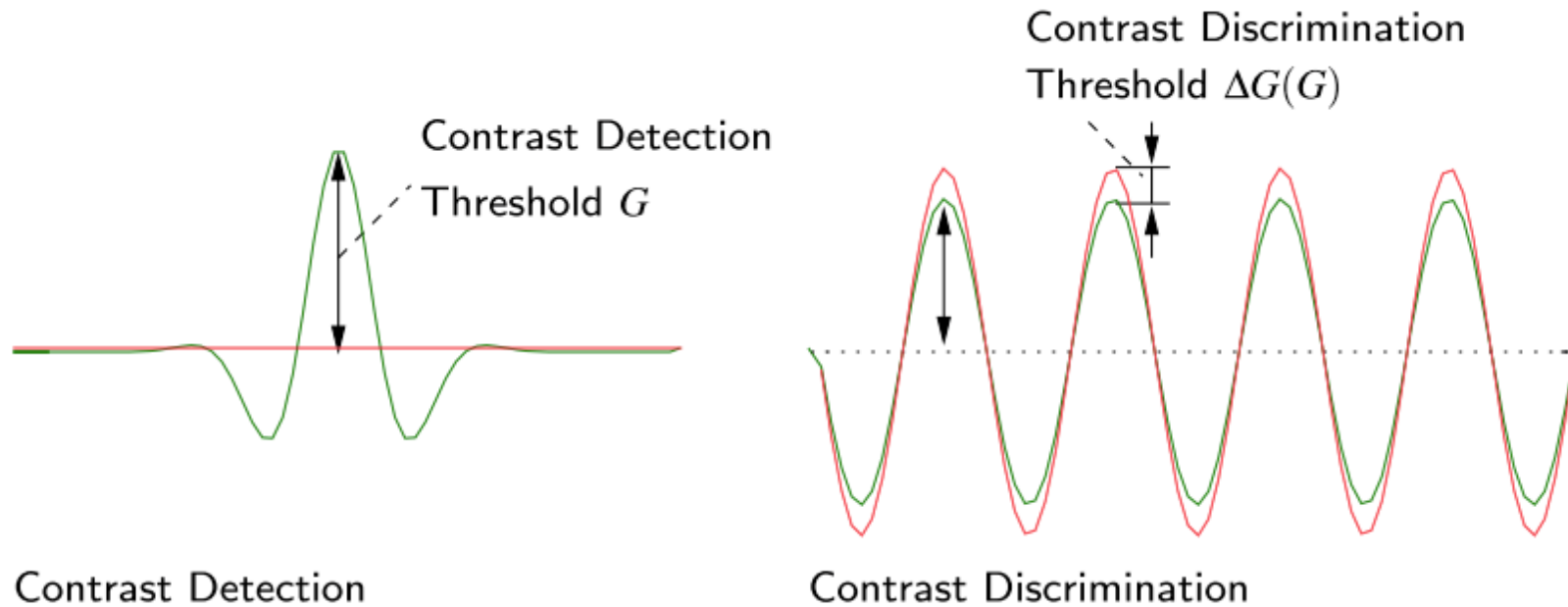
In which vertical bar is the pattern the most and the least visible?

---



# Detection vs. discrimination

---



# Definitions of contrast

Simple Contrast

$$C_s = \frac{L_{max}}{L_{min}}$$

Weber Fraction

$$W = \frac{\Delta L}{L_{min}}$$

Logarithmic Ratio

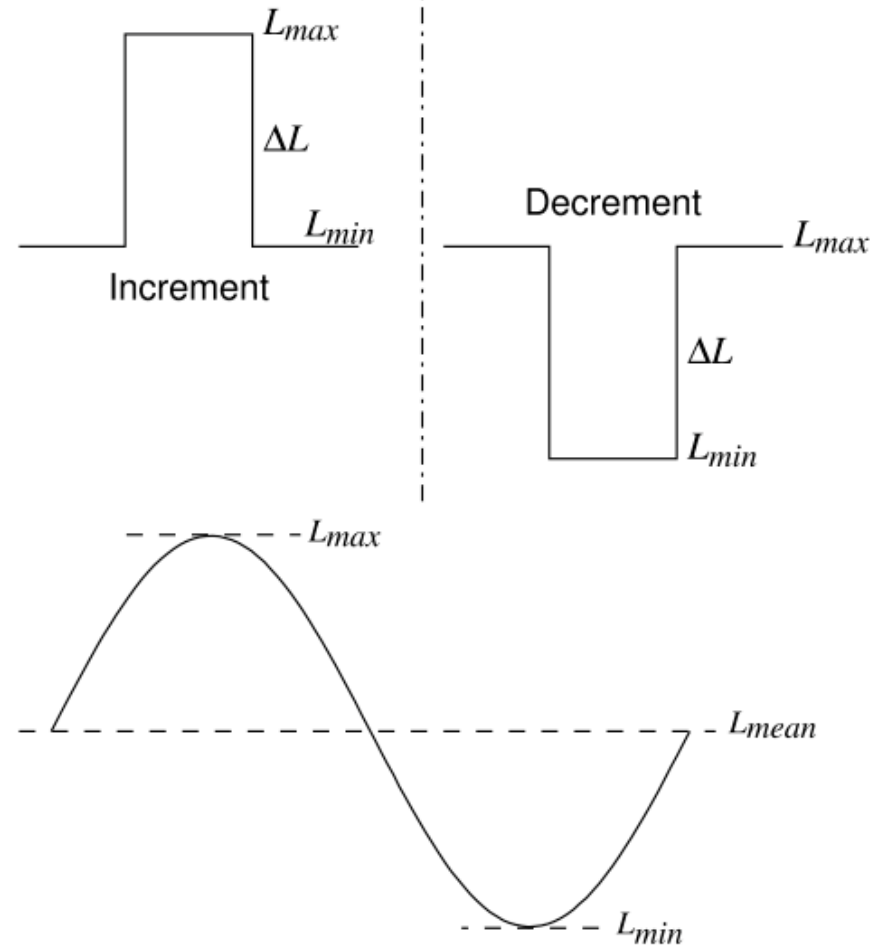
$$G = \log_{10}\left(\frac{L_{max}}{L_{min}}\right)$$

Michelson Contrast

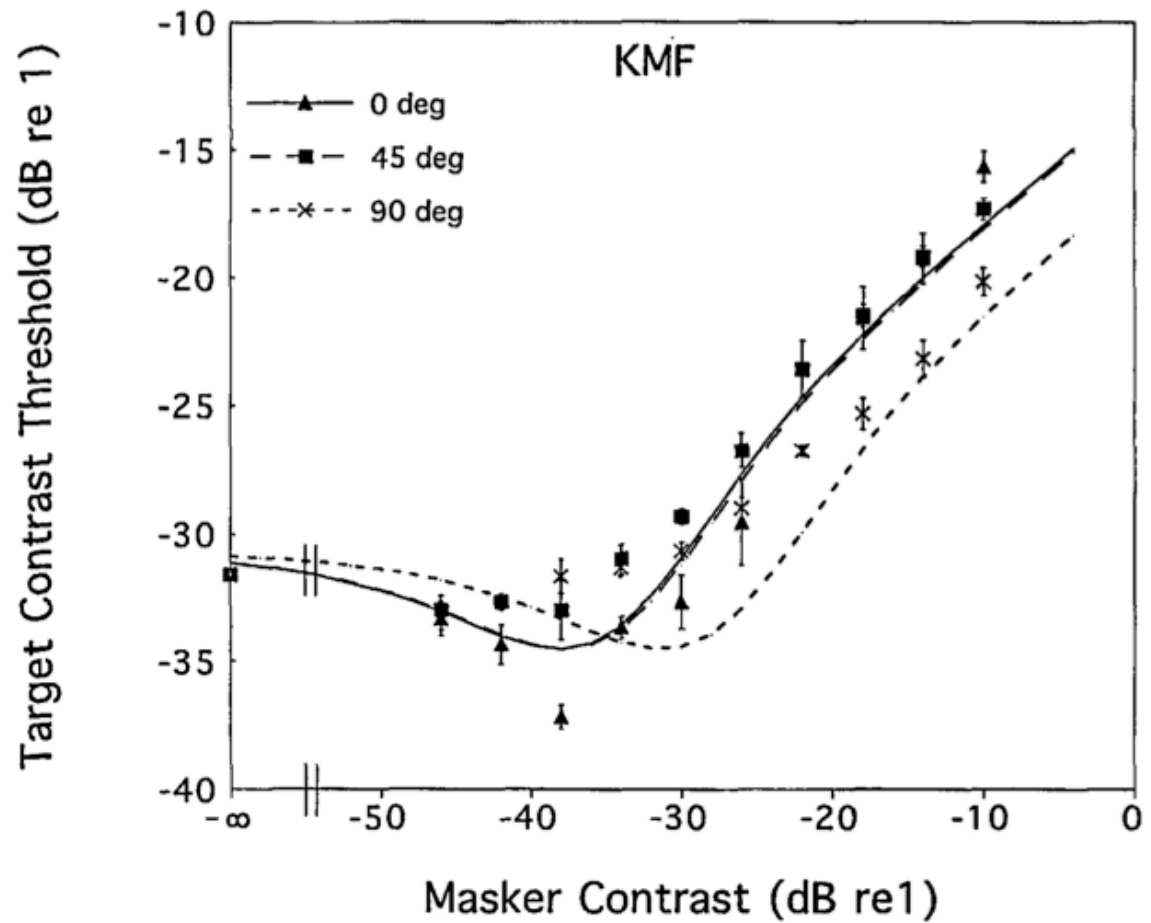
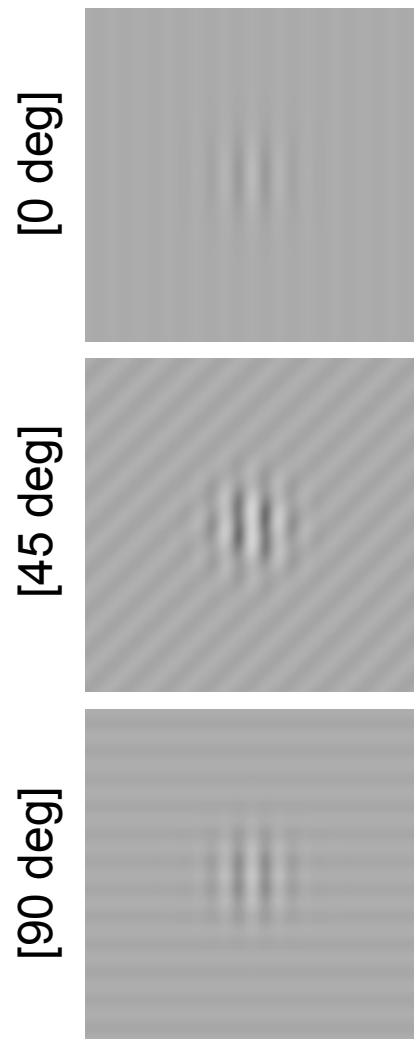
$$M = \frac{|L_{max} - L_{min}|}{L_{max} + L_{min}}$$

Signal to Noise Ratio

$$SNR = 20 \cdot \log_{10}\left(\frac{L_{max}}{L_{min}}\right)$$



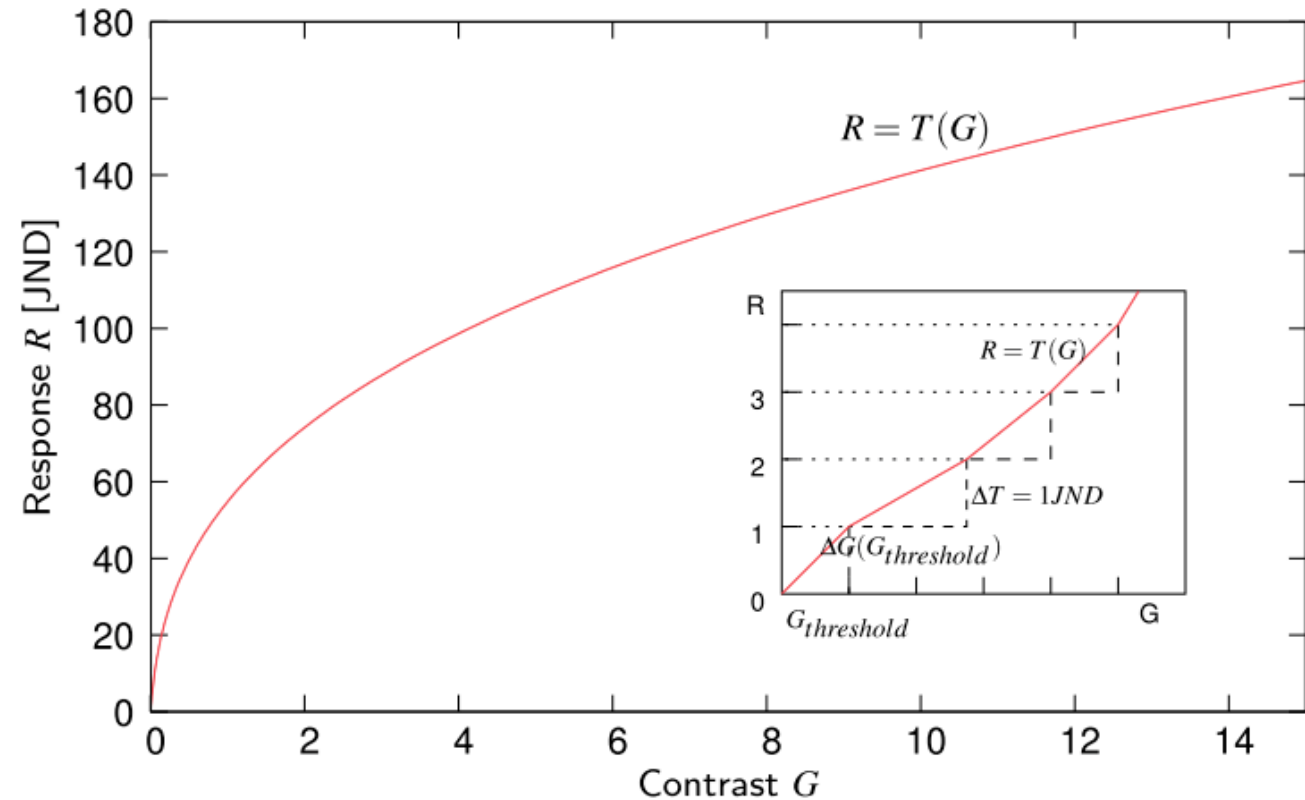
# Visual masking experiments - discrimination



[Foley, JOSAA, 1994]

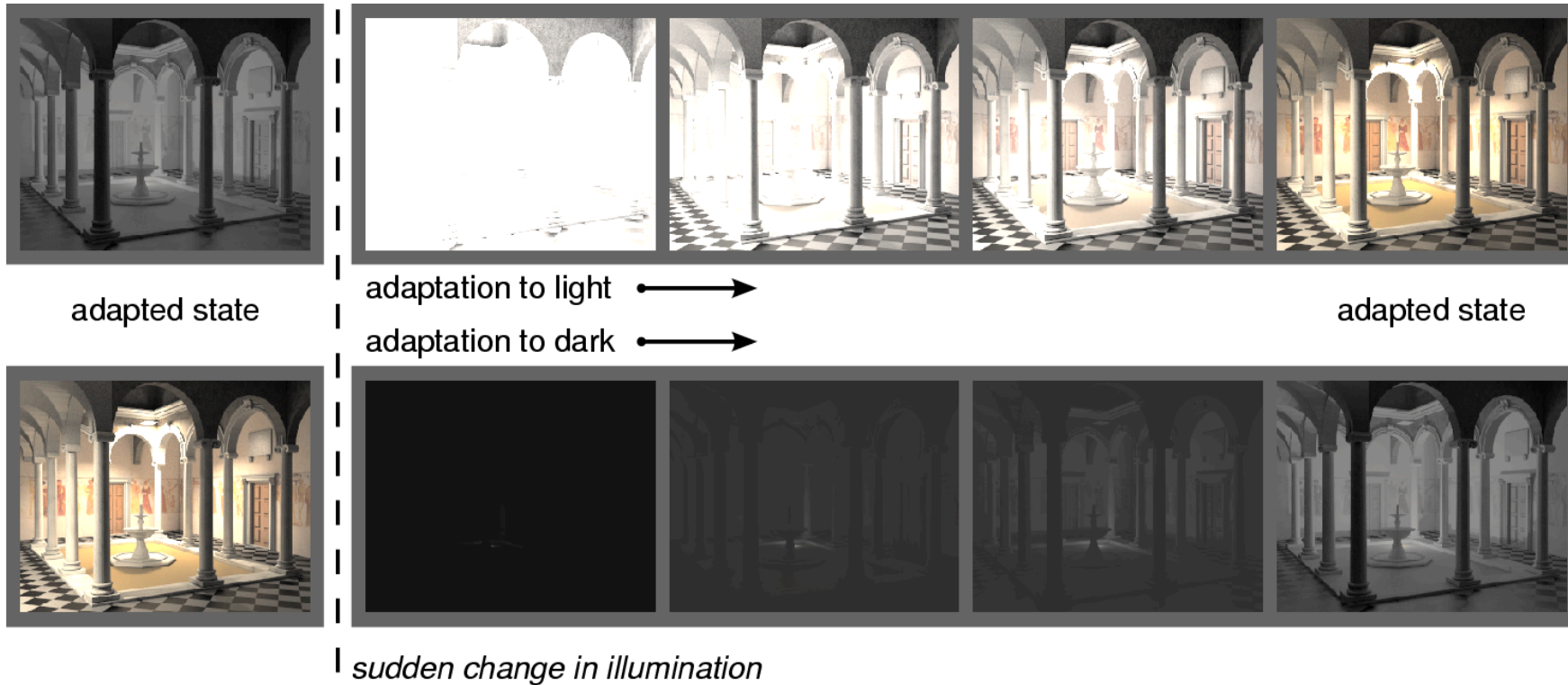
# Contrast transducer

- ▶ Similar to JND encoding
- ▶ Trans. from physical contrast into “perceived” contrast



# Light and dark adaptation

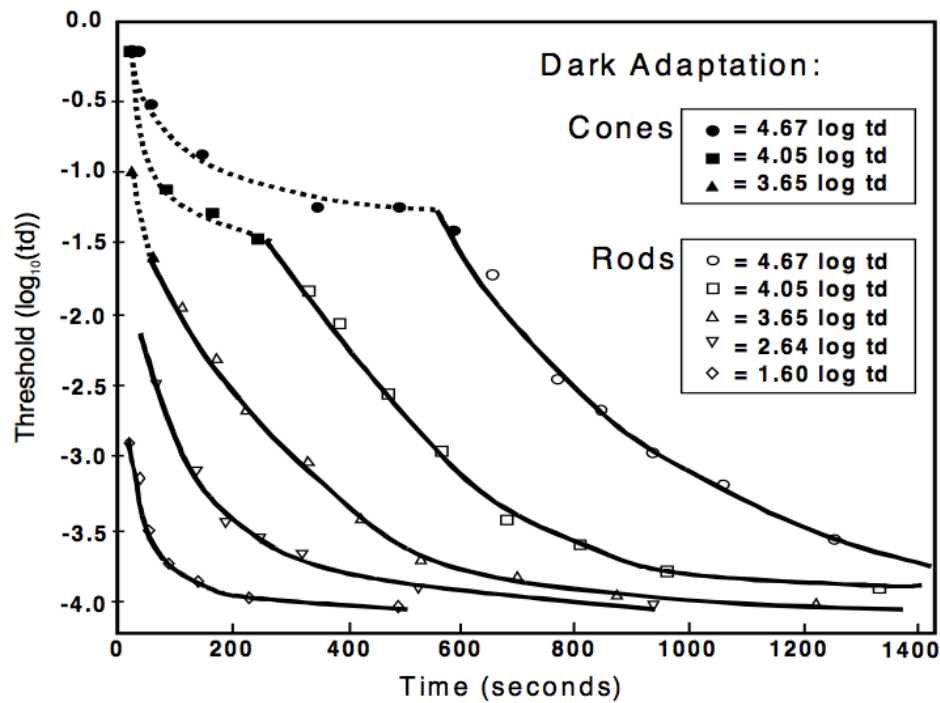
# Light and dark adaptation



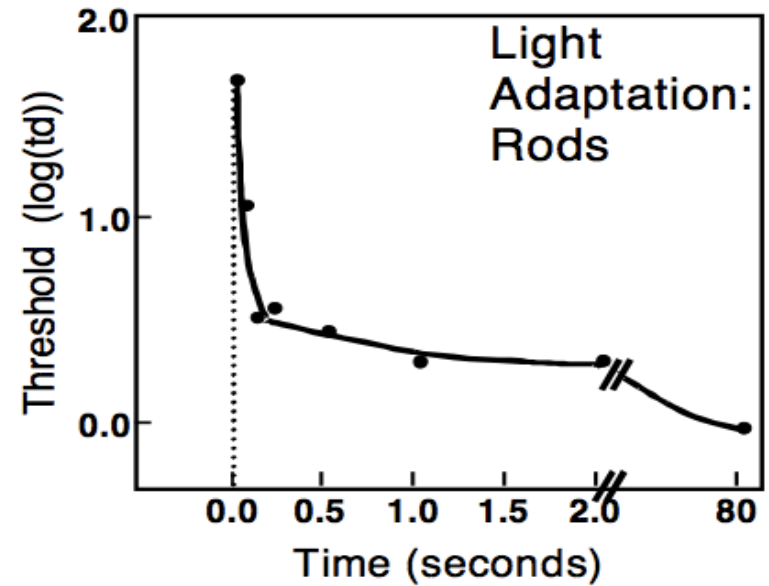
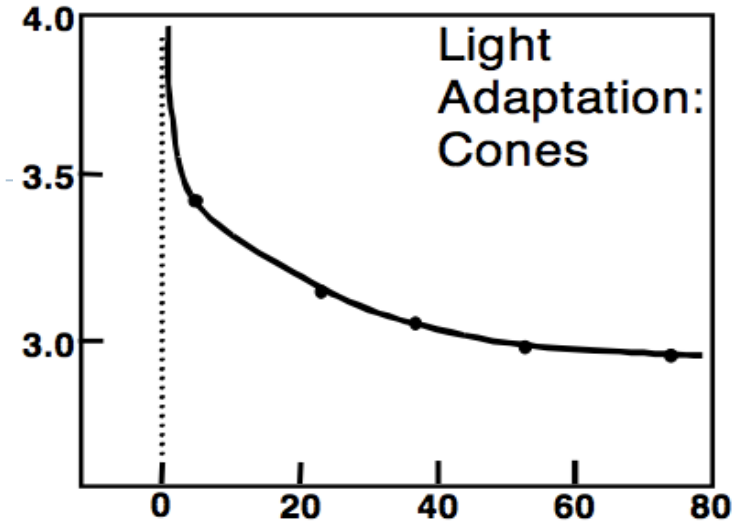
- ▶ Light adaptation: from dark to bright
- ▶ Dark adaptation: from bright to dark (much slower)



# Time-course of adaptation



Bright -> Dark



Dark -> Bright

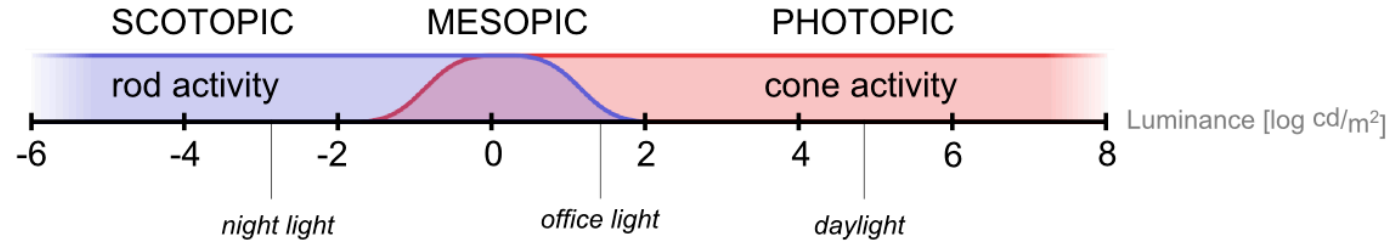
# Temporal adaptation mechanisms

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- ▶ **Bleaching & recovery of photopigment**
  - ▶ Slow asymmetric (light → dark, dark → light)
  - ▶ Reaction times (1-1000 sec)
  - ▶ Separate time-course for rods and cones
- ▶ **Neural adaptation**
  - ▶ Fast
  - ▶ Approx. symmetric reaction times (10-3000 ms)

# Night and daylight vision

Vision mode:

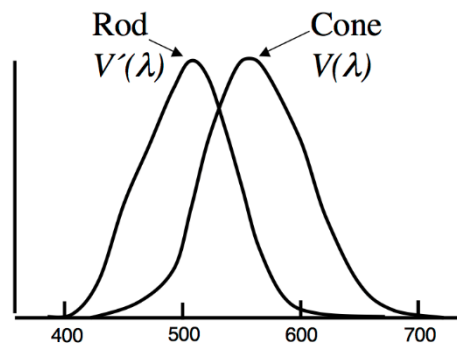


Mode properties: monochromatic vision  
limited visual acuity

good color perception  
good visual acuity



Luminous efficiency

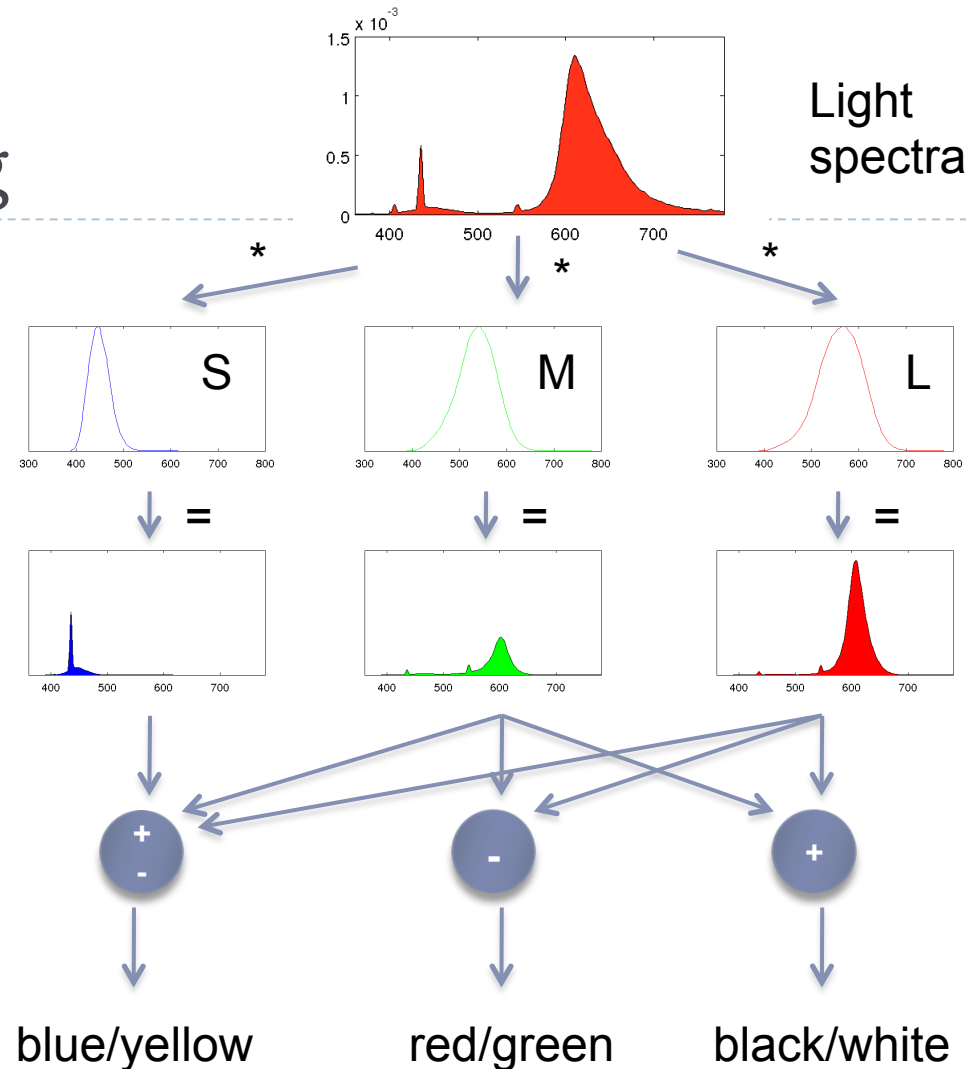




# Opponent colours and spatial colour vision

# Colour processing

- ▶ Light is sensed by L, M and S, cones
  - ▶ Each cone type is sensitive to different wavelengths
- ▶ Responses from L, M and S cones are combined into three opponent pathways
  - ▶ achromatic (black/white) pathway – luminance
  - ▶ 2 colour opponent pathways
- ▶ Rationale: improve coding efficiency for natural scenes

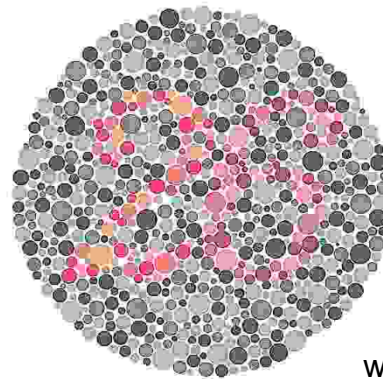
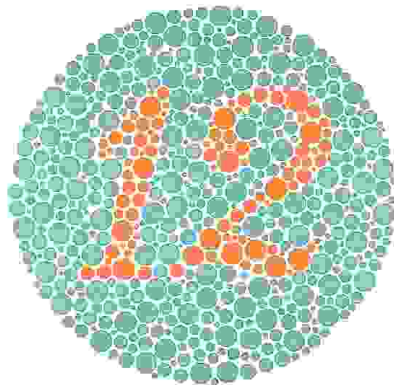


# Colour perception

- ▶ **Di-chromaticity (dogs, cats)**
  - ▶ Yellow & blue-violet
  - ▶ Green, orange, red indistinguishable
- ▶ **Tri-chromaticity (humans, monkeys)**
  - ▶ Red, green, blue
  - ▶ Colour-blindness
    - ▶ Most often men, green-red colour-blindness

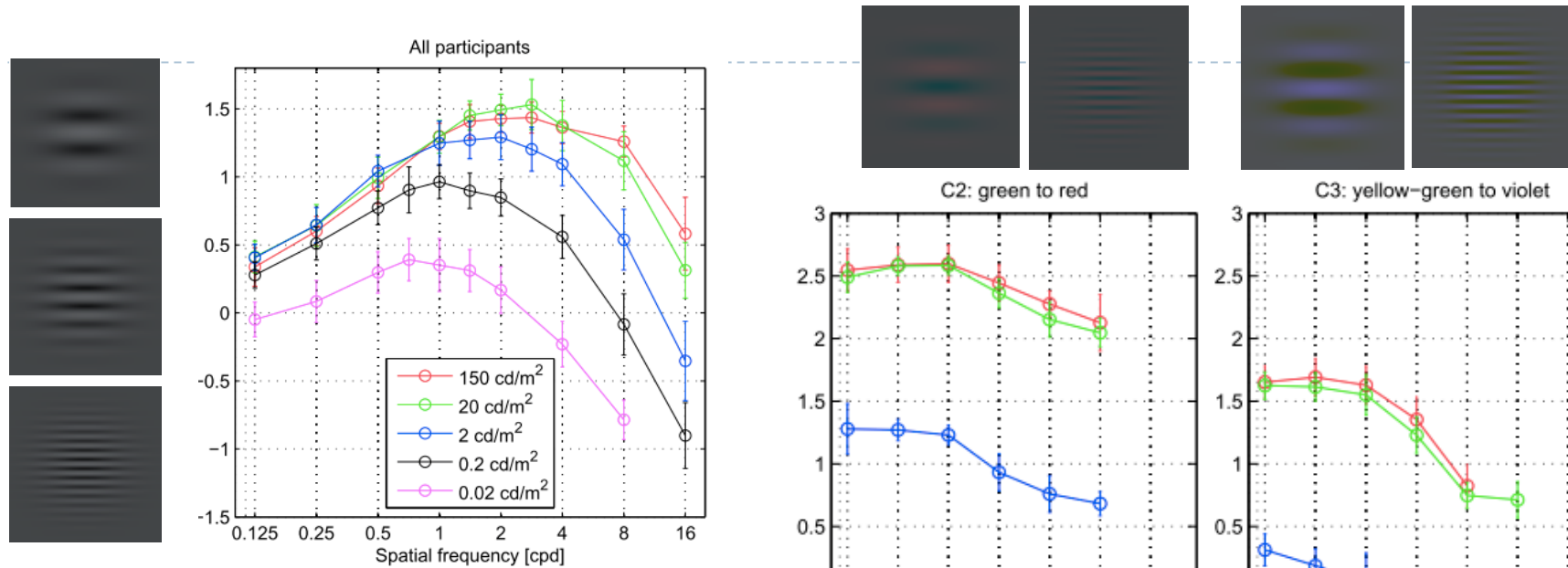


[www.lam.mus.ca.us/cats/color/](http://www.lam.mus.ca.us/cats/color/)

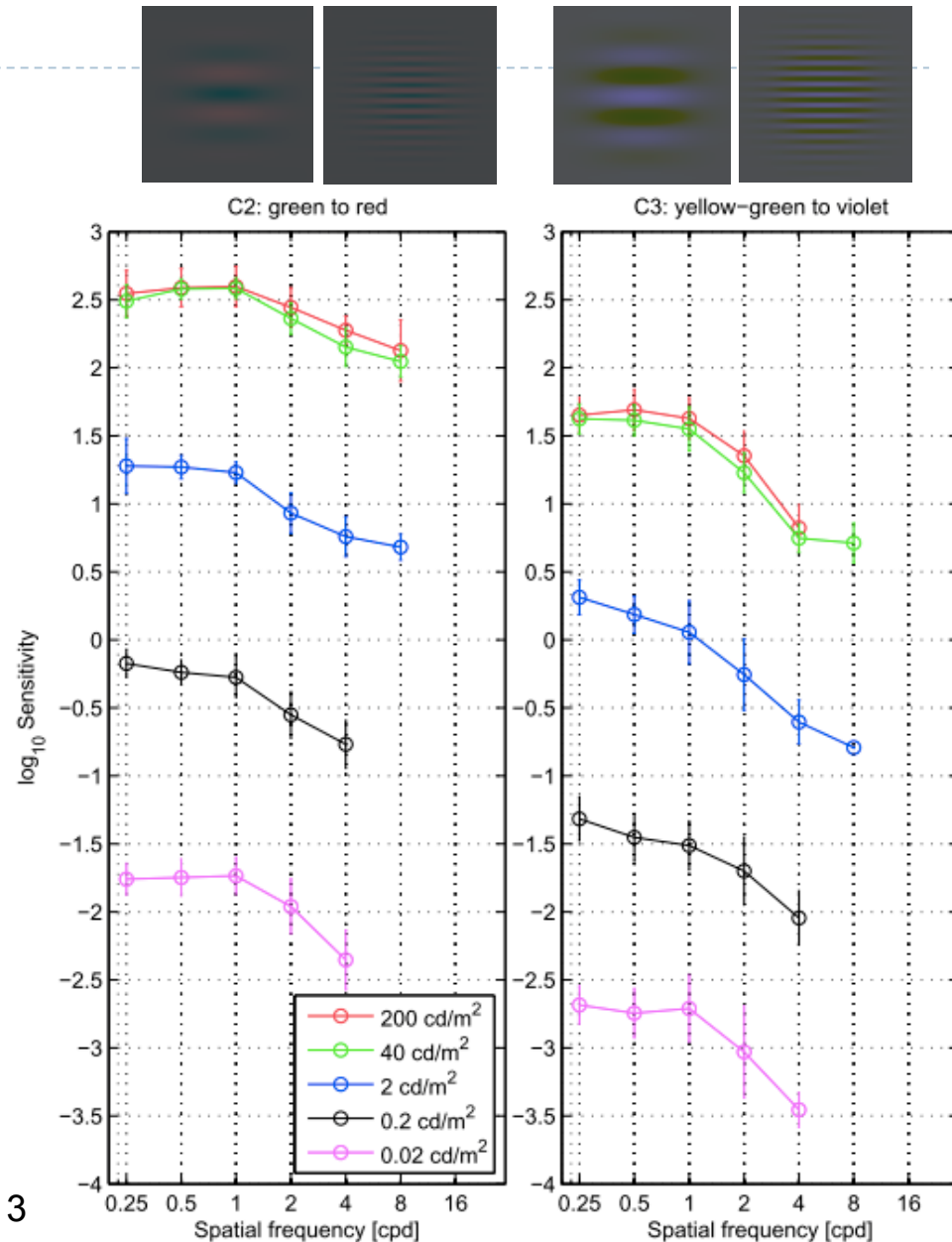


[www.colorcube.com/illusions/clrblind.html](http://www.colorcube.com/illusions/clrblind.html)

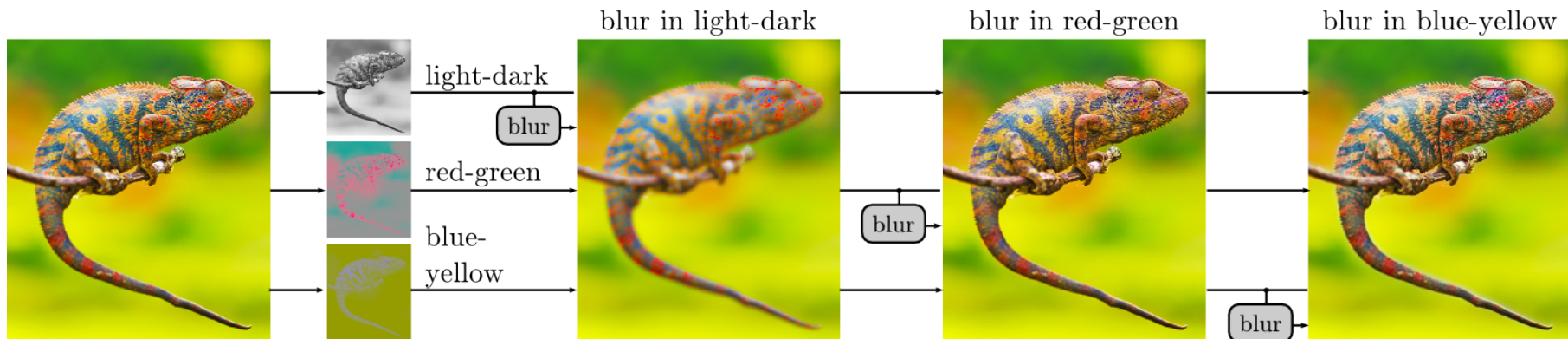
# Colour Contrast Sensitivity



- ▶ **Colour vs. luminance vision system**
  - ▶ Higher sensitivity at lower frequencies for colour
  - ▶ High frequencies less visible



# Visibility of blur



- ▶ The same amount of blur was introduced into light-dark, red-green and blue-yellow colour opponent channels
- ▶ The blur is only visible in light-dark channel
- ▶ This property is used in image and video compression
  - ▶ Sub-sampling of colour channels (4:2:1)



# Depth perception

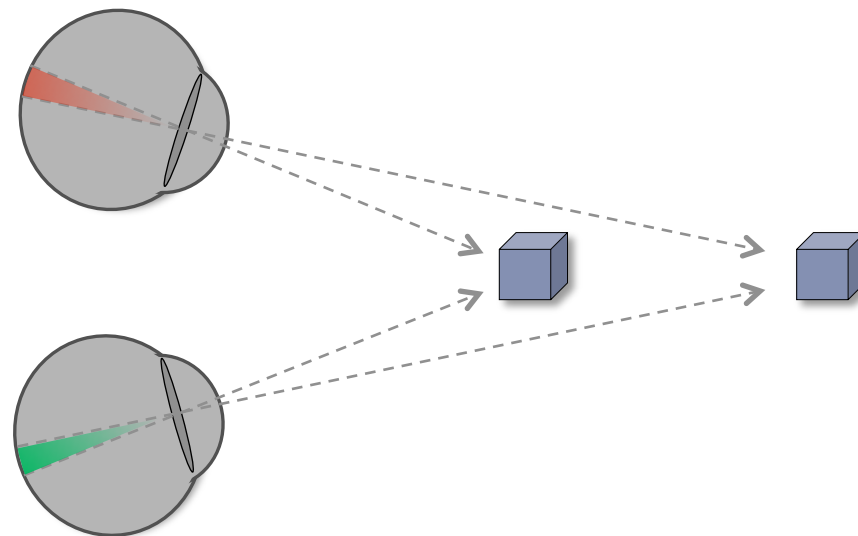
The slides in this section are the courtesy of Piotr Didyk (<http://people.mpi-inf.mpg.de/~pdidyk/>)

# Depth perception

---

**We see depth due to depth cues.**

**Stereoscopic depth cues:**  
binocular disparity



# Depth perception

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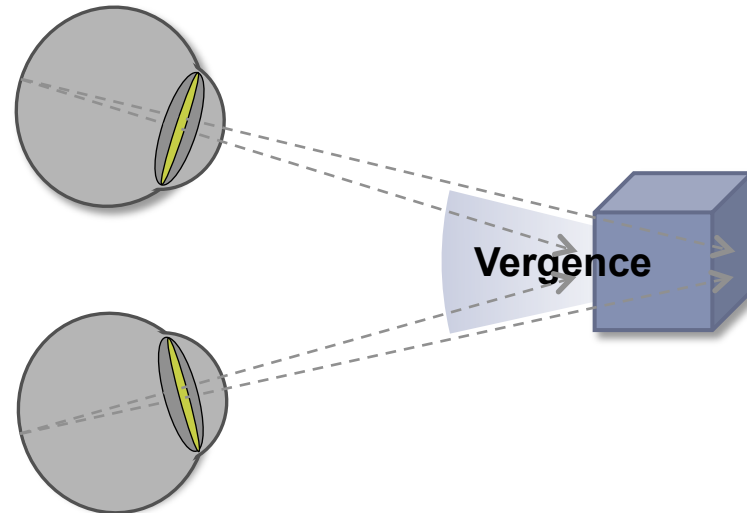
**We see depth due to depth cues.**

**Stereoscopic depth cues:**

binocular disparity

**Ocular depth cues:**

accommodation, vergence



# Depth perception

---

**We see depth due to depth cues.**

**Stereoscopic depth cues:**

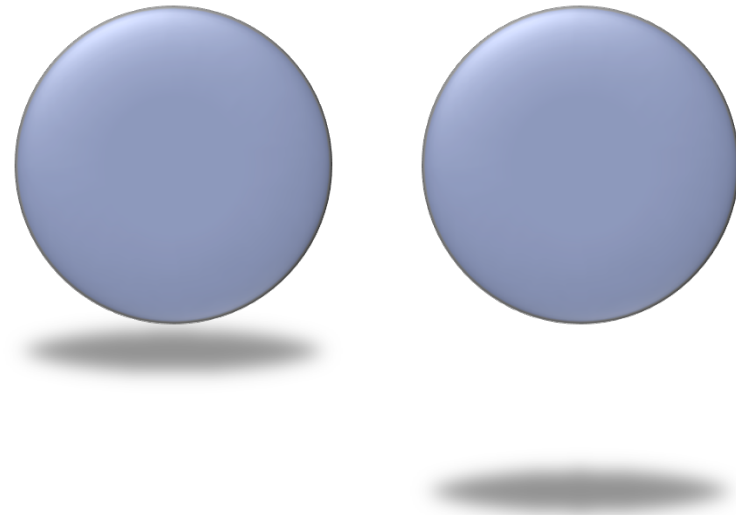
binocular disparity

**Ocular depth cues:**

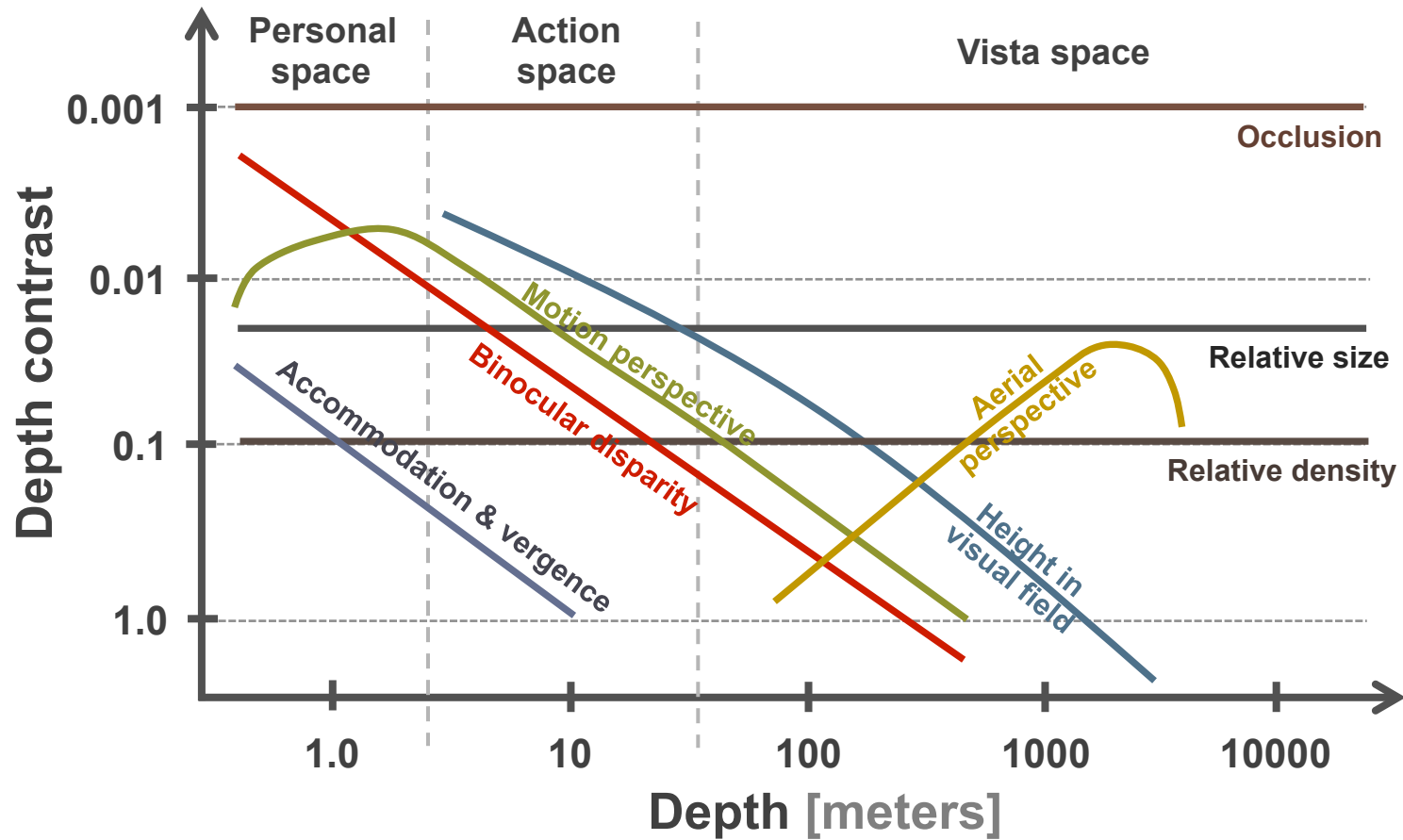
accommodation, vergence

**Pictorial depth cues:**

occlusion, size, shadows...



# Cues sensitivity



*"Perceiving layout and knowing distances: The integration, relative potency, and contextual use of different information about depth"*  
by Cutting and Vishton [1995]

# Depth perception

---

**We see depth due to depth cues.**

**Stereoscopic depth cues:**

binocular disparity

**Ocular depth cues:**

accommodation, vergence

**Pictorial depth cues:**

occlusion, size, shadows...



**Challenge:**  
Consistency is  
required!

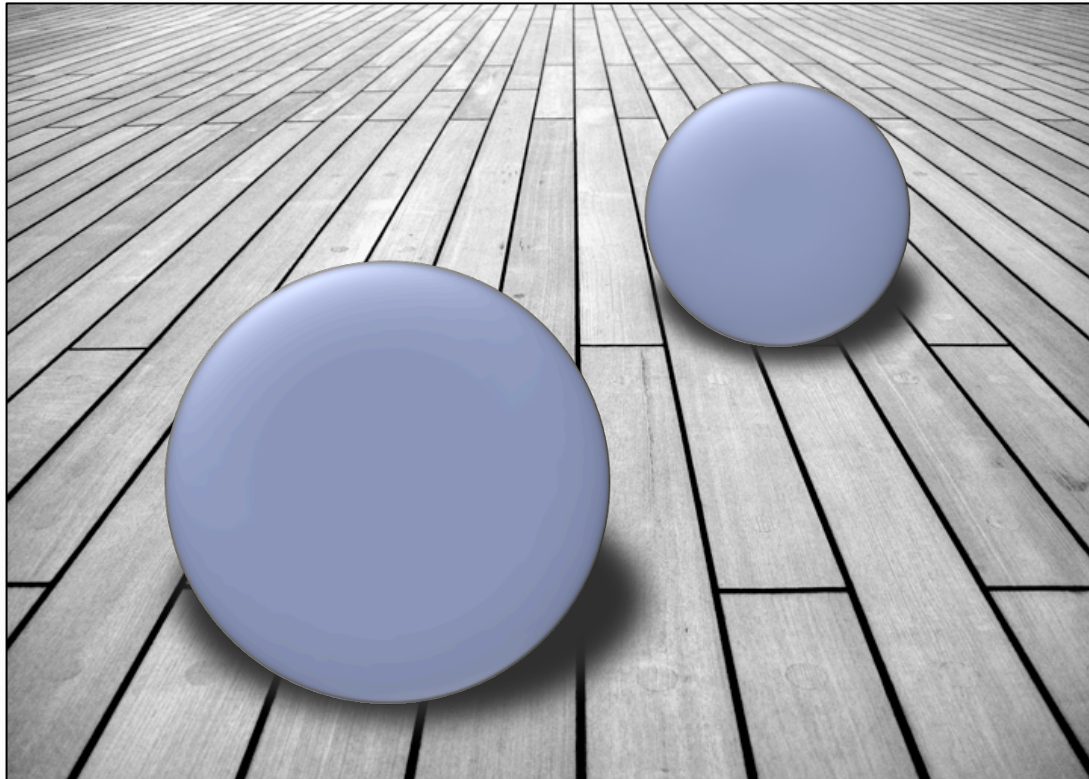


# Simple conflict example

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## Present cues:

- Size
- Shadows
- Perspective
- **Occlusion**



# Disparity & occlusion conflict

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**Objects in front**





# Disparity & occlusion conflict

---

**Disparity & occlusion conflict**



# Depth perception

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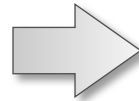
**We see depth due to depth cues.**

**Stereoscopic depth cues:**

binocular disparity

**Ocular depth cues:**

accommodation, vergence

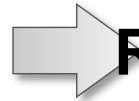


**Require 3D space**

**We cheat our Human Visual System!**

**Pictorial depth cues:**

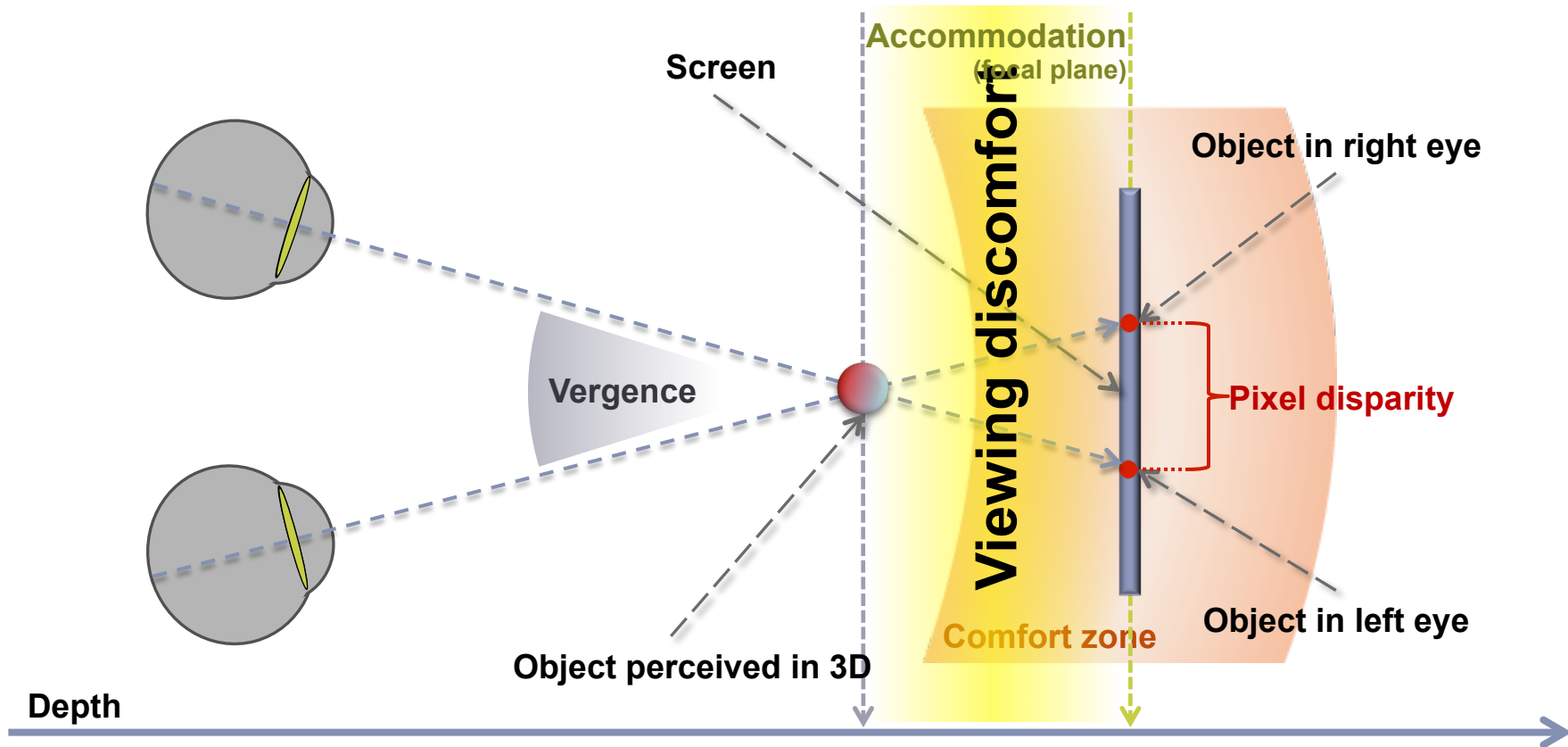
occlusion, size, shadows...



**Reproducible on a flat displays**

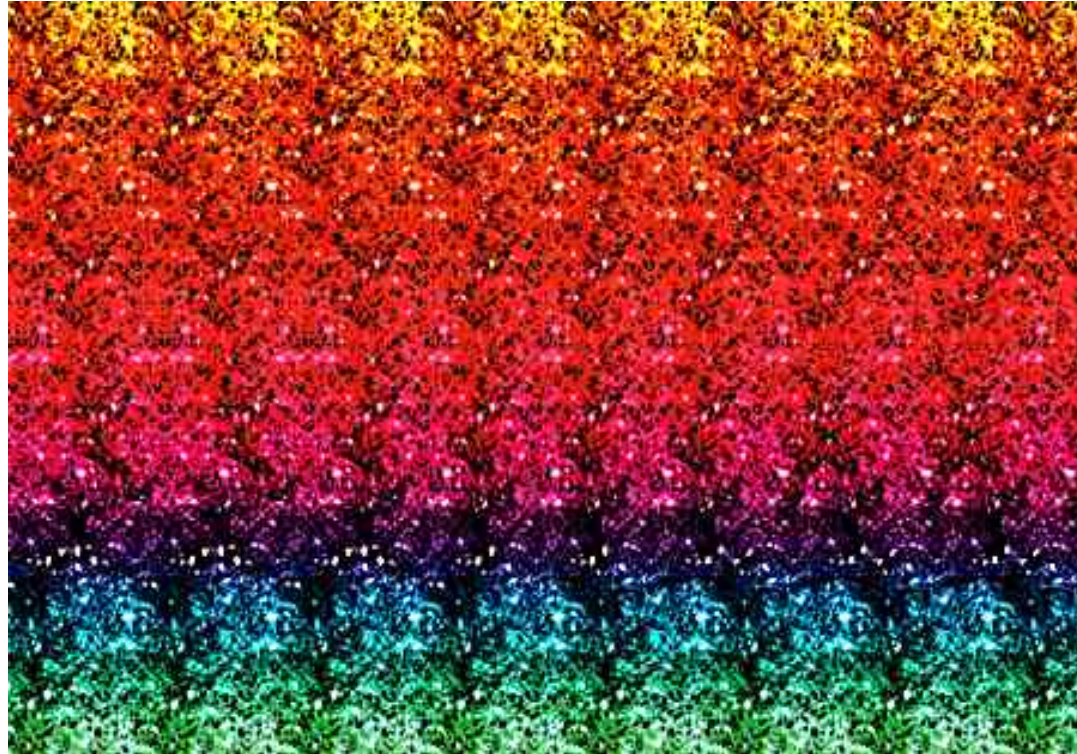


# Cheating our HVS



# Single Image Random Dot Stereograms

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- ▶ Fight the vergence vs. accommodation conflict to see the hidden image

# Viewing discomfort

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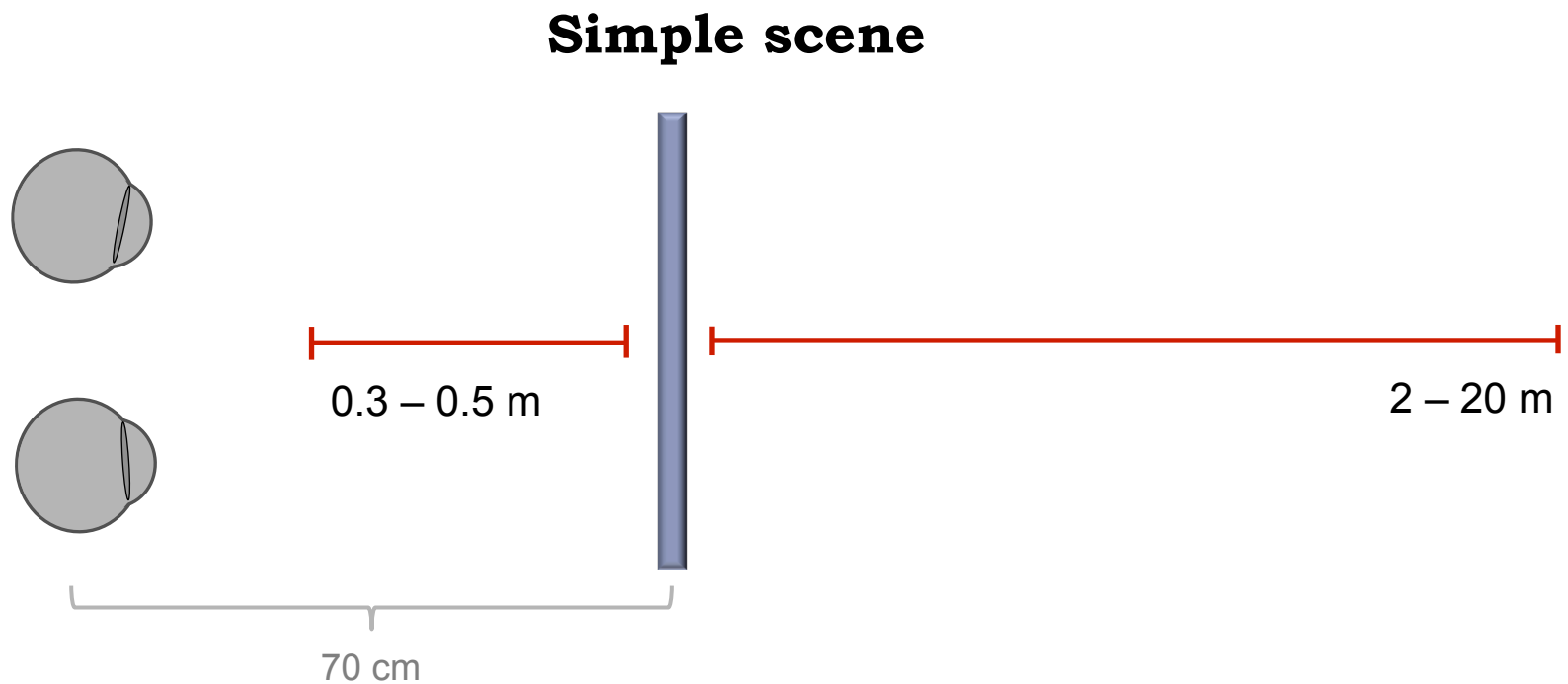


# Comfort zones

---

## Comfort zone size depends on:

- Presented content
- Viewing condition



“Controlling Perceived Depth in Stereoscopic Images” by Jones et al. 2001

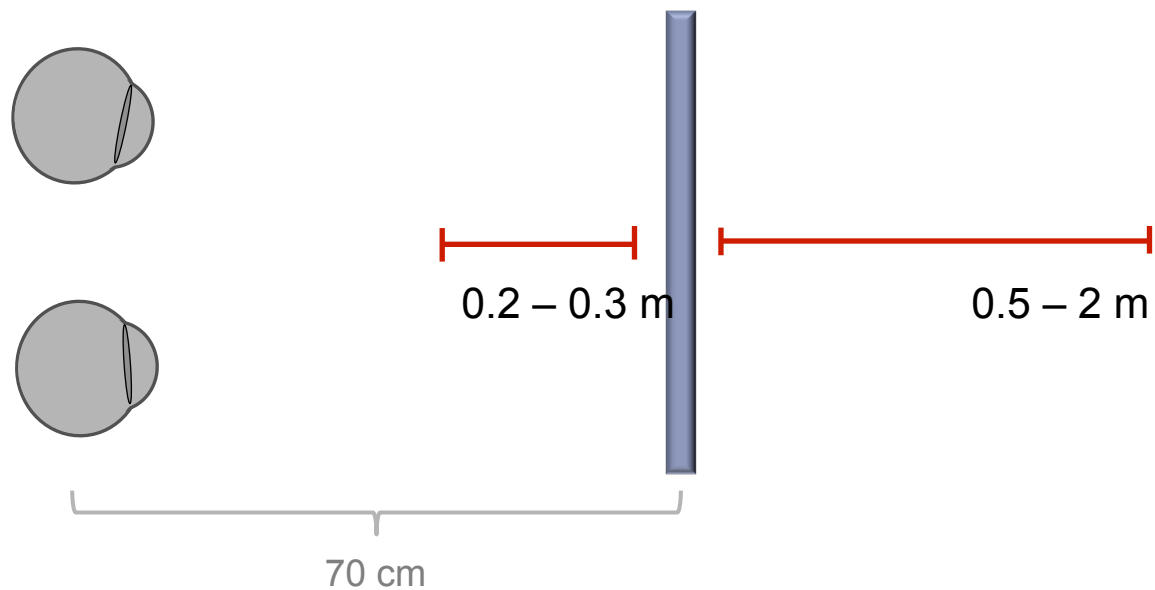
# Comfort zones

---

## Comfort zone size depends on:

- Presented content
- Viewing condition

**Simple scene, user allowed to look away from screen**



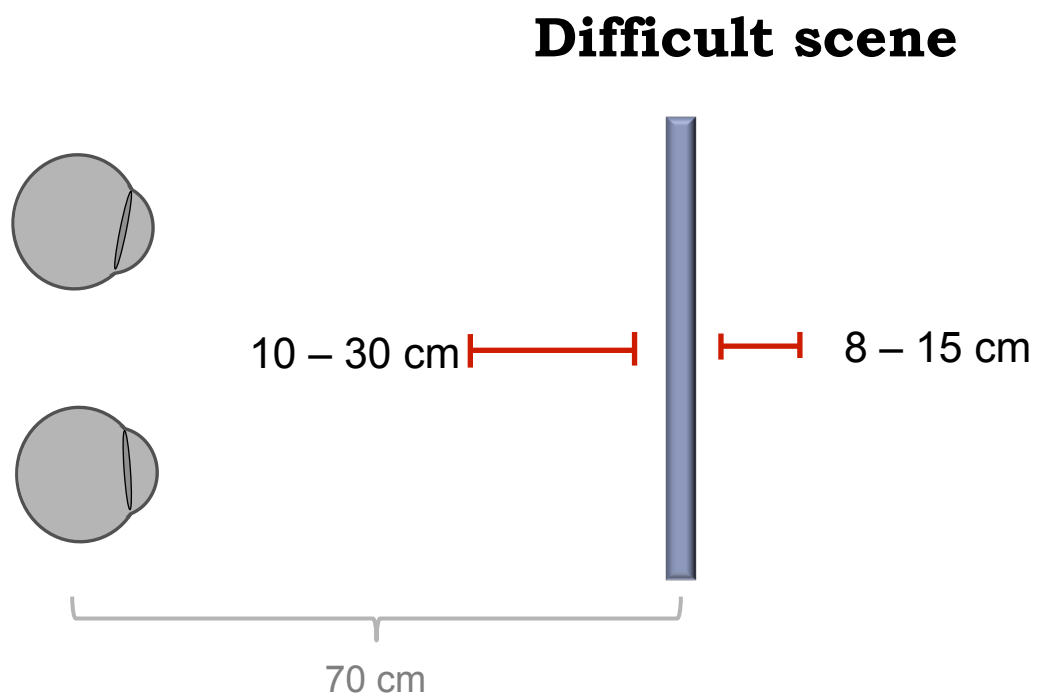
▶ *“Controlling Perceived Depth in Stereoscopic Images” by Jones et al. 2001*

# Comfort zones

---

## Comfort zone size depends on:

- Presented content
- Viewing condition



▶ *“Controlling Perceived Depth in Stereoscopic Images” by Jones et al. 2001*



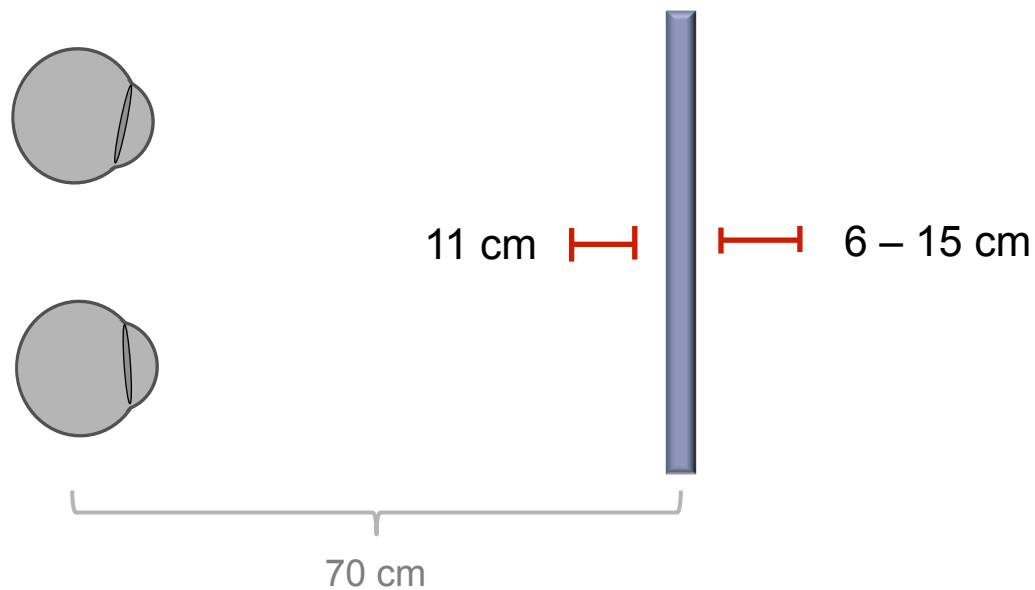
# Comfort zones

---

## Comfort zone size depends on:

- Presented content
- Viewing condition

## Difficult scene, user allowed to look away from screen



“Controlling Perceived Depth in Stereoscopic Images” by Jones et al. 2001

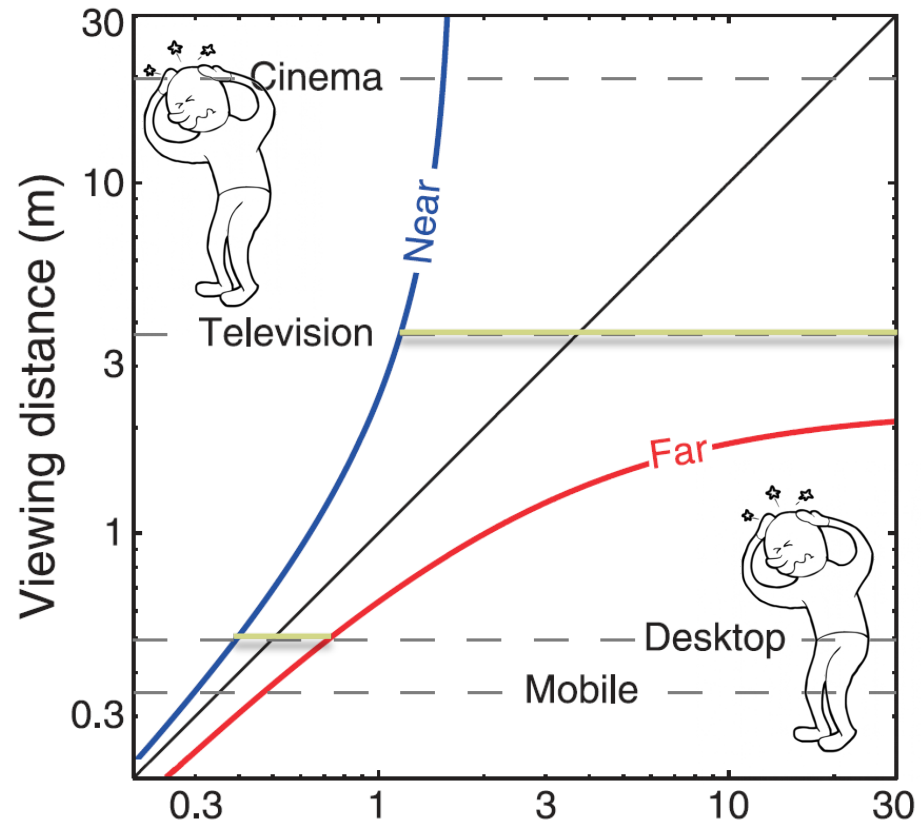
# Comfort zones

## Comfort zone size depends on:

- Presented content
- Viewing condition
- Screen distance

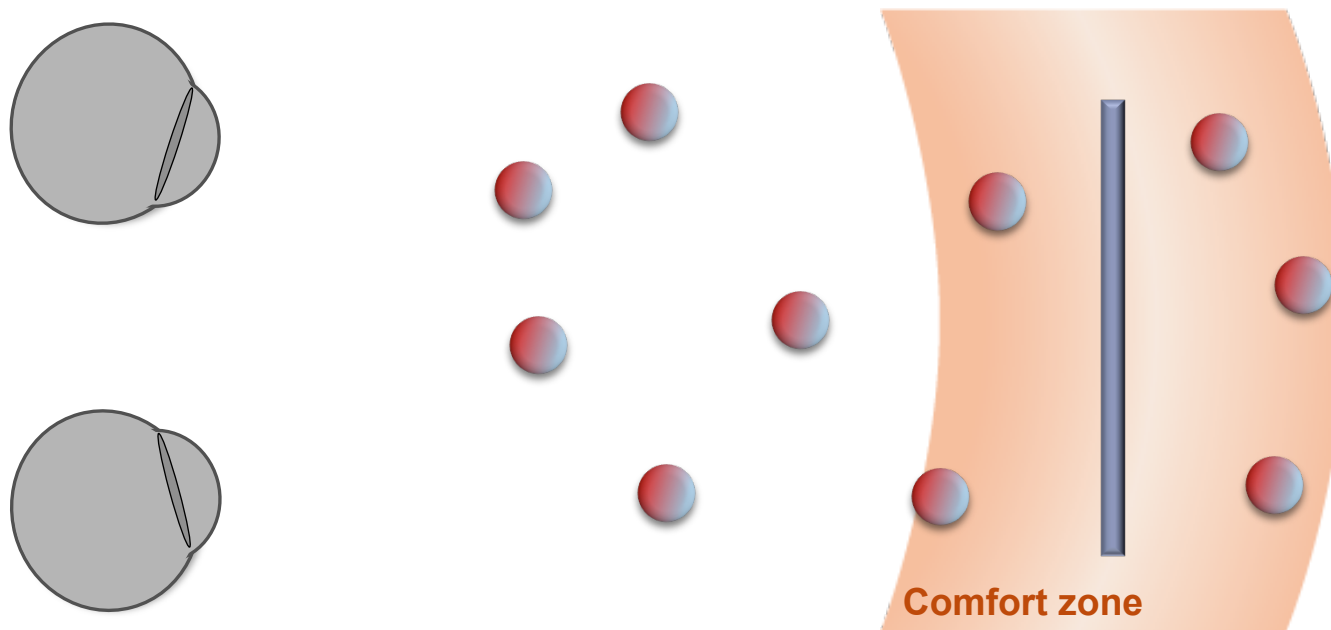
## Other factors:

- Distance between eyes
- Depth of field
- Temporal coherence



# Depth manipulation

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Scene manipulation  
~~Viewing discomfort~~ Viewing comfort

---



High(er) level vision

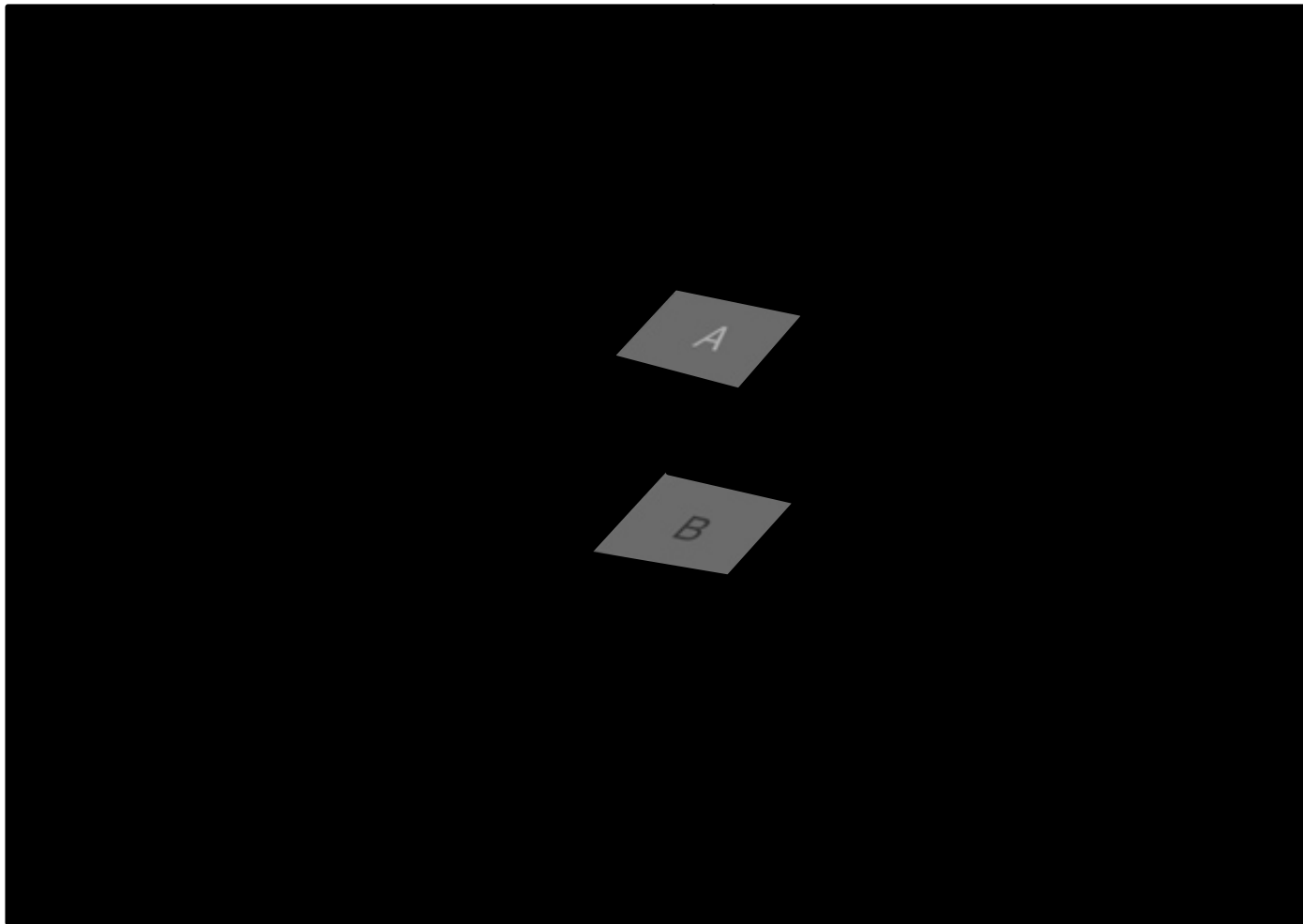
# Simultaneous contrast

---



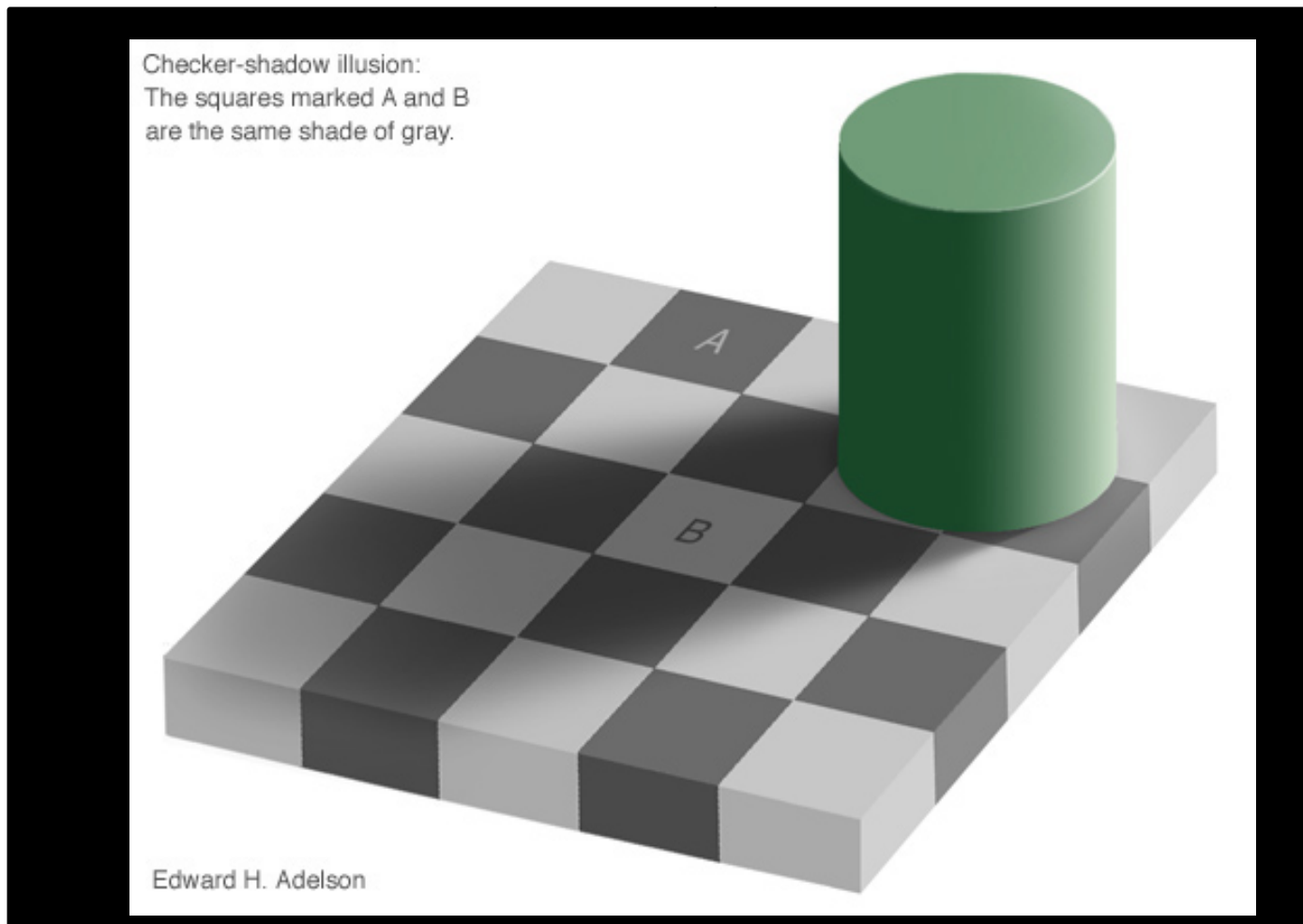
# High-Level Contrast Processing

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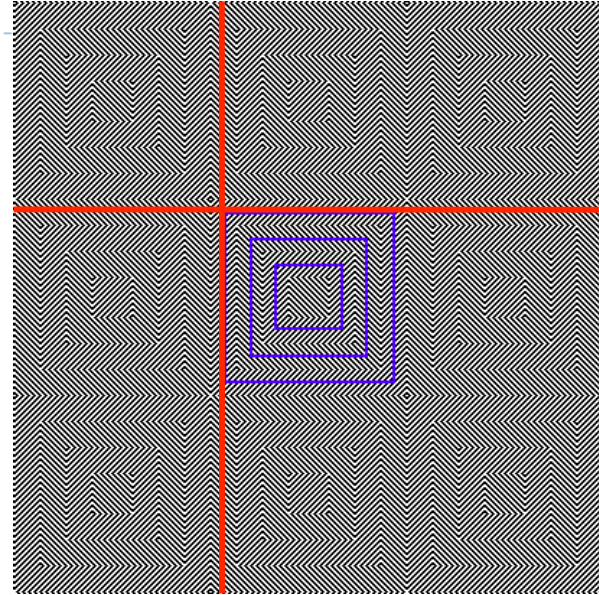
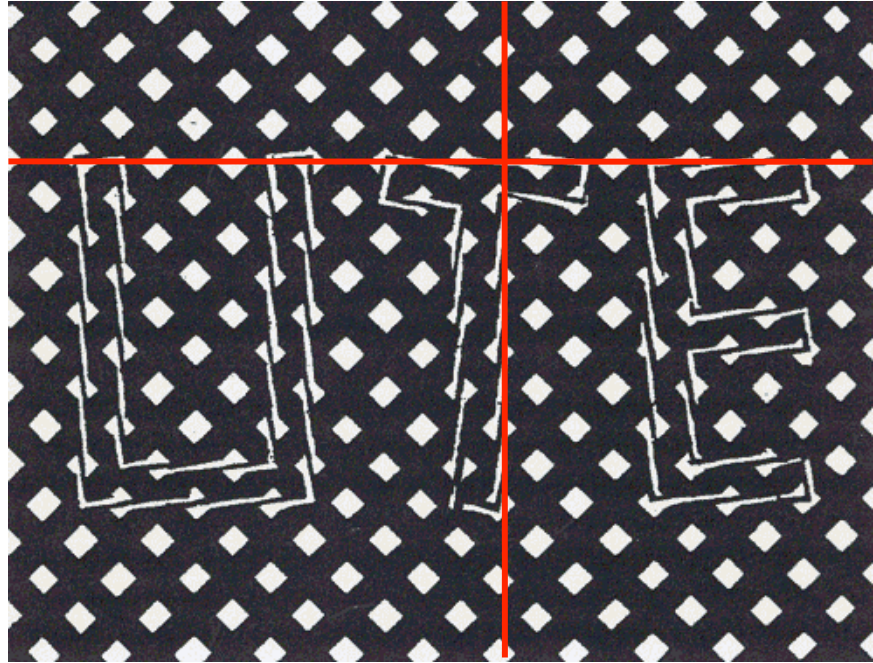


# High-Level Contrast Processing

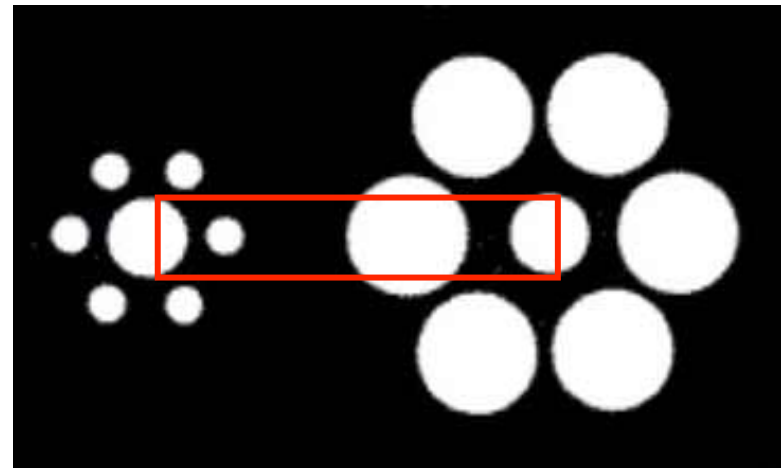
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# Shape Perception

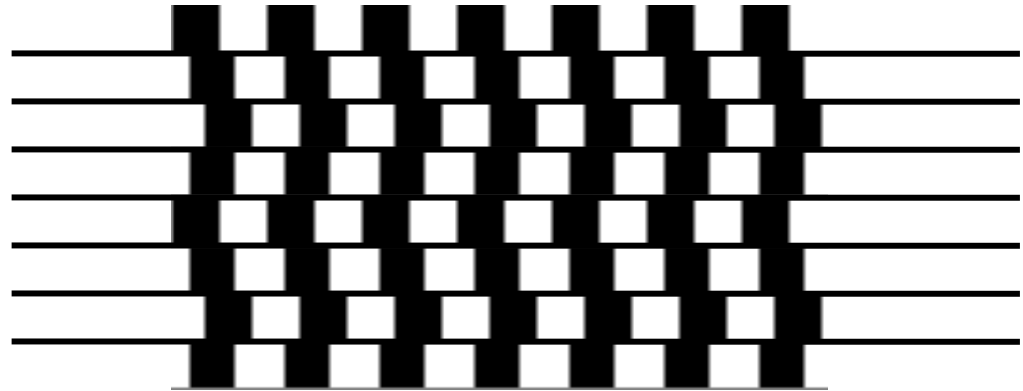
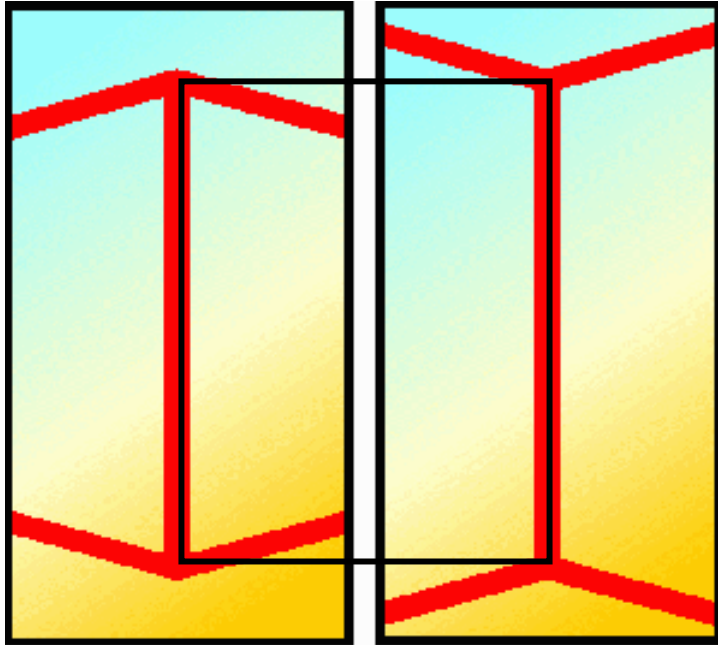


- Depends on surrounding primitives
  - Directional emphasis
  - Size emphasis





# Shape Processing: Geometrical Clues

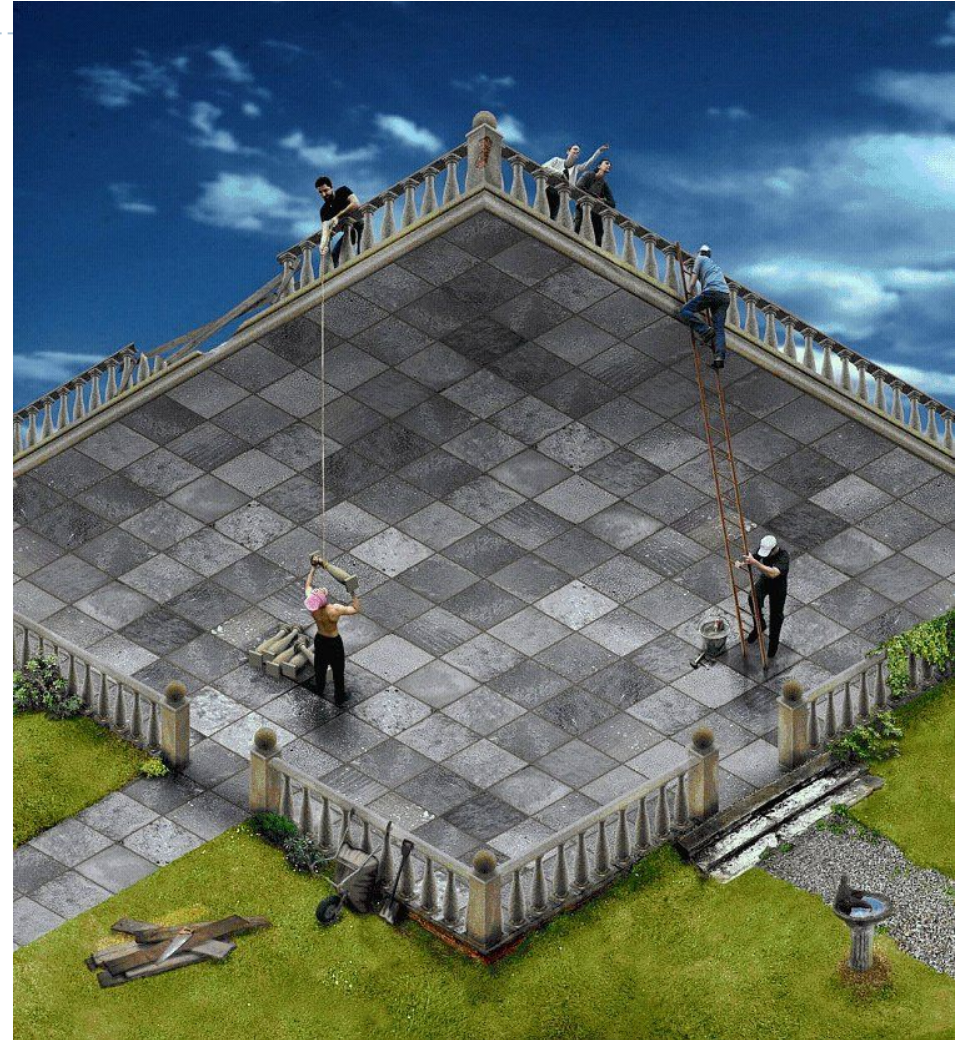
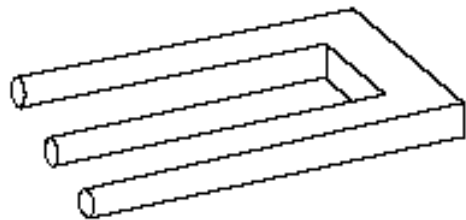
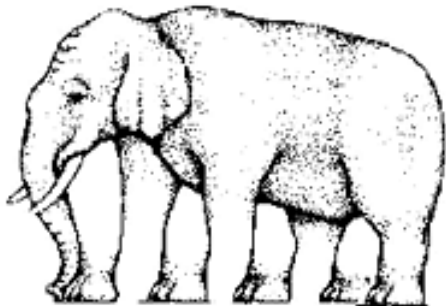


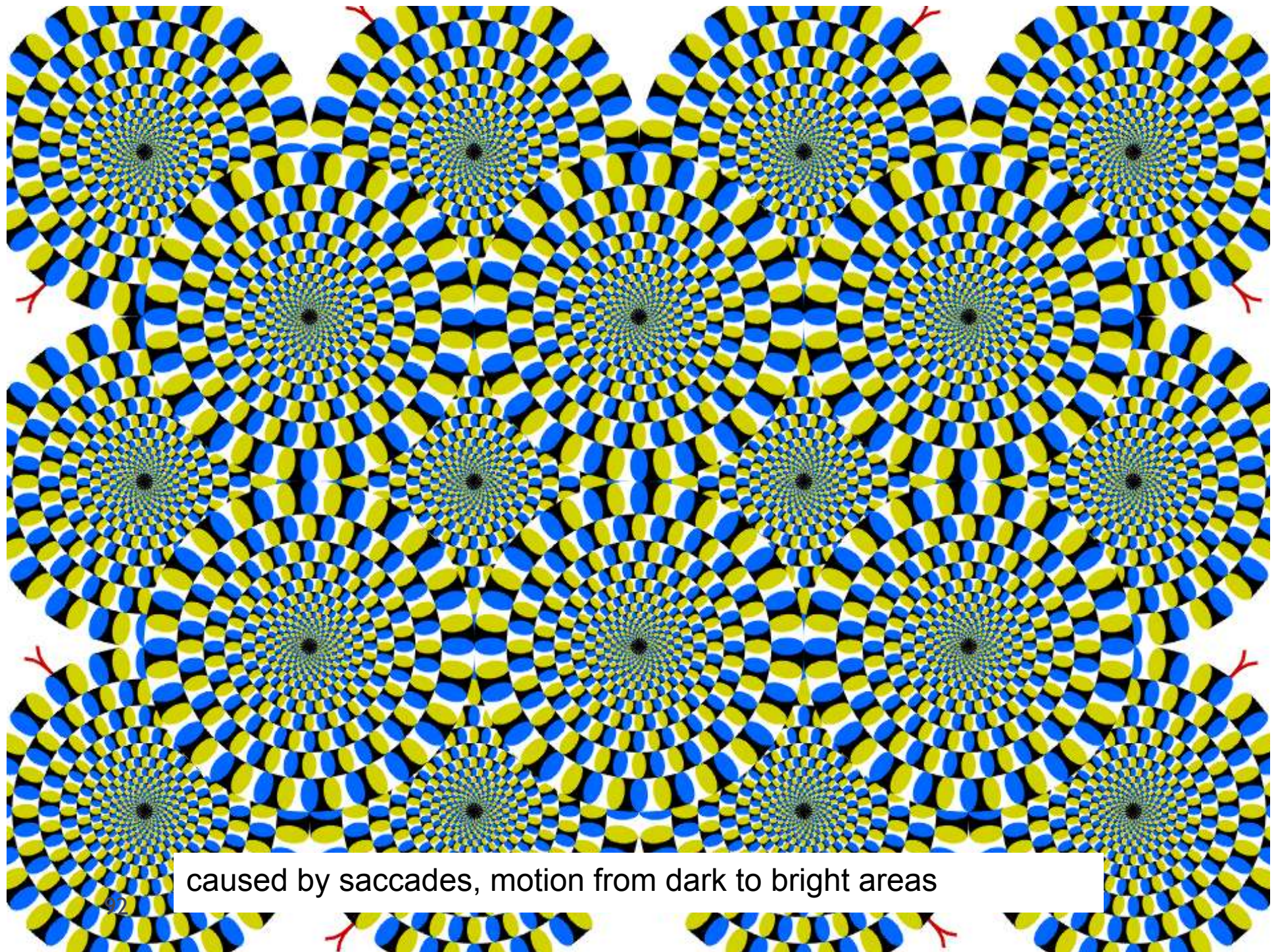
<http://www.panoptikum.net/optischetaeusungen/index.html>

- Automatic geometrical interpretation
  - 3D perspective
  - Implicit scene depth

# Impossible Scenes

- Escher et.al.
  - Confuse HVS by presenting contradicting visual clues
  - Local vs. global processing





caused by saccades, motion from dark to bright areas

# Law of closure

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# Another Optical Illusion

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- ▶ If you stare for approx. 20 seconds some of you will actually see a giraffe.

# References

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- ▶ Wandell, B.A. (1995). *Foundations of vision*. Sinauer Associates.
- ▶ Mantiuk, R. K., Myszkowski, K., & Seidel, H. (2015). High Dynamic Range Imaging. In *Wiley Encyclopedia of Electrical and Electronics Engineering*. Wiley.
  - ▶ Section 2.4
  - ▶ Available online:  
[http://www.cl.cam.ac.uk/~rkm38/hdri\\_book.html](http://www.cl.cam.ac.uk/~rkm38/hdri_book.html)