

<i>location, x, m</i>	address
<i>integer, n</i>	integer
<i>thread_id, t</i>	thread id
<i>memory, M</i>	::= memory (function from addresses to integers)
<i>expression, e</i>	::= expression
	n integer literal
	x read from address x
	$x = e$ write value of e to address x
	$e; e'$ sequential composition
	$e + e'$ plus
	lock x lock mutex at address x
	unlock x unlock mutex at address x
<i>process, p</i>	::= process
	$t:e$ thread
	$p p'$ parallel composition
<i>state, s</i>	::= state
	$\langle p, M \rangle$ process p and memory M
<i>label, l</i>	::= label
	W $x=n$ write
	R $x=n$ read
	LOCK x lock
	UNLOCK x unlock
	τ internal action (tau)
<i>thread_label, t : l</i>	::= thread label
	$t:l$ label

$\boxed{e \xrightarrow{l} e'}$ e does l to become e'

$$\begin{array}{c}
\frac{}{x \xrightarrow{\text{R } x=n} n} \text{ READ} \\
\frac{}{x = n \xrightarrow{\text{W } x=n} n} \text{ WRITE} \\
\frac{e \xrightarrow{l} e'}{x = e \xrightarrow{l} x = e'} \text{ WRITE_CONTEXT} \\
\frac{}{n; e \xrightarrow{\tau} e} \text{ SEQ} \\
\frac{e_1 \xrightarrow{l} e'_1}{e_1; e_2 \xrightarrow{l} e'_1; e_2} \text{ SEQ_CONTEXT} \\
\frac{n = n_1 + n_2}{n_1 + n_2 \xrightarrow{\tau} n} \text{ PLUS} \\
\frac{e_1 \xrightarrow{l} e'_1}{e_1 + e_2 \xrightarrow{l} e'_1 + e_2} \text{ PLUS_CONTEXT_1}
\end{array}$$

$$\frac{e_2 \xrightarrow{l} e'_2}{n_1 + e_2 \xrightarrow{l} n_1 + e'_2} \quad \text{PLUS_CONTEXT_2}$$

$$\frac{}{\text{lock } x \xrightarrow{\text{LOCK } x} 0} \quad \text{LOCK}$$

$$\frac{}{\text{unlock } x \xrightarrow{\text{UNLOCK } x} 0} \quad \text{UNLOCK}$$

$\boxed{p \xrightarrow{t:l} p'}$ p does $t : l$ to become p'

$$\frac{e \xrightarrow{l} e'}{t:e \xrightarrow{t:l} t:e'} \quad \text{THREAD}$$

$$\frac{p_1 \xrightarrow{t:l} p'_1}{p_1 | p_2 \xrightarrow{t:l} p'_1 | p_2} \quad \text{PAR_CONTEXT_LEFT}$$

$$\frac{p_2 \xrightarrow{t:l} p'_2}{p_1 | p_2 \xrightarrow{t:l} p_1 | p'_2} \quad \text{PAR_CONTEXT_RIGHT}$$

$\boxed{M \xrightarrow{t:l} M'}$ M does $t : l$ to become M'

$$\frac{M(x) = n}{M \xrightarrow{t:\text{R } x=n} M} \quad \text{MREAD}$$

$$\frac{}{M \xrightarrow{t:\text{W } x=n} M \oplus (x \mapsto n)} \quad \text{MWRITE}$$

$$\frac{M(x) = 1}{M \xrightarrow{t:\text{LOCK } x} M \oplus (x \mapsto 0)} \quad \text{MLOCK}$$

$$\frac{}{M \xrightarrow{t:\text{UNLOCK } x} M \oplus (x \mapsto 1)} \quad \text{MUNLOCK}$$

$\boxed{s \xrightarrow{t:l} s'}$ s does $t : l$ to become s'

$$\frac{\frac{p \xrightarrow{t:l} p'}{M \xrightarrow{t:l} M'}}{\langle p, M \rangle \xrightarrow{t:l} \langle p', M' \rangle} \quad \text{SSYNC}$$

$$\frac{p \xrightarrow{t:\tau} p'}{\langle p, M \rangle \xrightarrow{t:\tau} \langle p', M \rangle} \quad \text{STAU}$$

Definition rules: 19 good 0 bad

Definition rule clauses: 32 good 0 bad