

Optimising Compilers 2012–2013

Exercise Sheet 3

The purpose of this exercise is to gain familiarity with *constraint-based analyses*, particularly *0CFA* (zeroth-order control-flow analysis) from Lecture 11.

1. (a) What is a higher-order function?
- (b) How do higher-order functions make it harder to predict control flow within a program?
- (c) How does the 0CFA help to predict control flow?
- (d) Do object-oriented programs have analysis issues related to higher-order functions?

Consider the following simple λ -calculus like language, call it \mathcal{L} :

$$e ::= v \mid c \mid \lambda v. e \mid e_1 e_2 \mid \text{let } v = e_1 \text{ in } e_2 \mid \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \mid e_1 \oplus e_2$$

where v ranges over variables, c ranges over integer constants, and \oplus ranges over binary operations.

0CFA computes information about control flow in a program by computing a subset of a program's data flow: the flow of functions (or function pointers). In the following, the data flow of integer constants will also be tracked to aid understanding.

2. (a) Define informally the notion of a *binding site* and *use site* and indicate the binding and use sites in the syntax of \mathcal{L} .
- (b) The following expression has a single *program point* labelling the formal parameter x of f :

$$\text{let } f = (\lambda x^0. x + x) \text{ in } f\ 2 + f\ 3$$

Label the remaining program points (it may help to write the expression as a tree).

- (c) Given *flow variables* α_i associating sets to each program point, what is the value of set α_0 following a 0CFA? What integer values flow out of the body of the λ ?
- (d) Write down and explain the rule for generating constraints for **let**-bindings and variables v .
- (e) Consider the following expression with a partial labelling of program points:

$$\text{let } f = (\lambda x. x^1\ 0) \text{ in } (\text{let } g = (\lambda y^0. y + 1) \text{ in } (f\ g) + (g\ 1))$$

Compute the flow sets for α_1 and α_0 .

3. (a) Calculate a full 0CFA (tracking just function values, not integer values) for the following expression:

$$\text{let } f = (\lambda x. x\ 0) \text{ in } (h\ (\lambda y. y * 3)) + (h\ (\lambda z. z + 1))$$

- (b) Write down and explain the rule for generating constraints for functions and function application.

4. Answer the following past paper questions:

- 2004 Paper 9 Question 3
- 2007 Paper 9 Question 16 (using the constraint-based analysis approach for part (b))

In question 2007, by escaping we mean that some part of a list passed as an input may be returned as part of the result. For example, given $f(x) = tl(x)$, the argument x may escape (even though it will be just some cons cell and whenever the list x is non-empty).

Think for example:

```
L = cons(..., []);
x = f(L);
...
use(x)
...
```

If we know that argument of f does not escape and the list L is not used after the function call, then we can free all memory allocated for L (because we know that x cannot point there). We have to be more careful if `[]` above is some pre-existing list.

Past exam questions can be found at:

<http://www.cl.cam.ac.uk/teaching/exams/pastpapers/t-OptimisingCompilers.html>