

**Definition 1.** Let  $X$  be a system of sets.  $X$  is *closed under powersets* iff  $\mathcal{P}(U) \in X$  for every  $U \in X$ .