

Joint Channel Sensing and Power Control Scheme for Cognitive Radio Wireless Sensor Networks

Ziqiang Feng, Ian Wassell
Computer Laboratory
University of Cambridge, UK
Email: {zf232, ijw24}@cam.ac.uk

Abstract—In this paper, we investigate channel sensing and power control problems in a cluster-based cognitive radio wireless sensor network (CRWSN). We first propose three channel sensing algorithms to solve the channel sensing problem including availability constraints. Then a joint channel sensing and power control scheme (JCSPCS) is proposed to solve the power control problem including quality of service (QoS) constraints. We prove that all our algorithms are probably approximately correct (PAC) algorithms that can correctly identify a bad channel with high probability. We show that our algorithms are suitable for QoS-constrained applications as they all terminate in a finite time with a finite error rate. The performance of our channel sensing algorithms and the joint channel sensing and power control scheme is shown in the simulation results.

I. INTRODUCTION

In a traditional wireless sensor network (WSN), sensors usually operate in the Industrial, Scientific and Medical (ISM) unlicensed bands and have a limited energy supply. However, the development of the internet of things (IoT) and the high demand in the unlicensed bands has given rise to the problem of coexistence of heterogeneous systems. It is thus challenging to deploy WSN in busy unlicensed bands, especially for QoS-constrained applications. On the other hand, most licensed spectrum is underutilized and stays unoccupied for most of the time [1]. Cognitive radio (CR) is thus considered as a method to improve the spectrum efficiency for QoS-constrained applications in a WSN [2].

CR allows secondary users (unlicensed users) to opportunistically access the vacant channels of primary users (licensed users). However, secondary users must not interfere with the primary users. Since the channel availability statistics are generally unknown to the secondary users, they have to sense the available vacant channels before transmitting any data. The problem of channel sensing and access in cognitive radio networks has been widely investigated. Some of the literature has modeled the channel sensing problem as a multi-armed bandit problem [3]. In [4], the author models the opportunistic spectrum access problem as a restless multi-armed bandit problem and propose a regenerative cycle algorithm to track the best channel, i.e., that with the best availability statistics. A traditional exploration and exploitation problem is thus investigated. In [5], a decentralized online learning algorithm is proposed to find available channels for multiple users. The algorithm is designed based on the well known Upper Confidence Bound (UCB) [3] policy that yields logarithmic regret over time without requiring any information on channel availability statistics.

Cognitive wireless sensors can only afford to sense part of the spectrum at a time. Cooperative sensing is thus needed for joint channel sensing. In addition, the detected available channels in a CRWSN must be coordinated to avoid collisions. Therefore, a cluster-based CRWSN architecture is proposed. For a QoS-constrained application in a CRWSN, a channel must be assigned as soon as possible if a node makes a data transmission request. Instead of tracking the good channels, sensor nodes in our model sense their pre-assigned part of the spectrum and only eliminate the bad channels, but with high confidence. We show that our algorithms can always assign an available channel to a sensor node that has a data transmission request. Furthermore, our channel sensing algorithms terminate in a finite time and with a limited error rate. In order to maximize the lifetime of each sensor nodes and meet the QoS constraints such as maximum delay and minimum data rate, a joint channel sensing and power control scheme (JCSPCS) is proposed in this paper that can improve the energy efficiency of sensors in the network without violating the QoS constraints.

II. SYSTEM MODEL AND PROBLEM FORMULATION

Consider the cluster-based CRWSN in Fig. 1 with K licensed orthogonal channels allocated to PUs for slotted transmission. Cognitive radio wireless sensors can transmit their data to the corresponding cluster head through licensed channels that are sensed idle in each time slot. In each cluster, each channel is pre-assigned to a sensor for channel sensing. Let $\mathcal{S} = \{S_1, S_2, \dots, S_K\}$ and $\mathcal{C} = \{C_1, C_2, \dots, C_K\}$ denote the set of sensors and the corresponding pre-assigned channels in one cluster respectively. We use $\mathcal{T} = \{T_1, T_2, \dots\}$ to represent the set of time slots in the network. At the beginning of each time slot, the wireless sensors in \mathcal{S} sense their pre-assigned channels and report the sensing results as well as their data transmission request (if any) to the cluster head via a control channel. The cluster head then notifies the sensors with their assigned channels for transmission. Note that for each sensor with a data transmission request, the assigned channel for transmission is selected from the available channels and does not necessarily have to be the same as the pre-assigned one.

For sensor S_i sensing C_i at time slot T_j , we use a random variable $\theta_{i,j}$ to represent whether C_i is idle ($\theta_{i,j} = 1$) or not ($\theta_{i,j} = 0$). We also use $\omega_{i,j}$ to represent the data transmission request of sensor S_i at time slot T_j , where $\omega_{i,j} = 1$ represents that S_i has data to send and $\omega_{i,j} = 0$ otherwise. A message containing $(\theta_{i,j}, \omega_{i,j})$ is sent to the cluster head via a control channel after channel sensing.

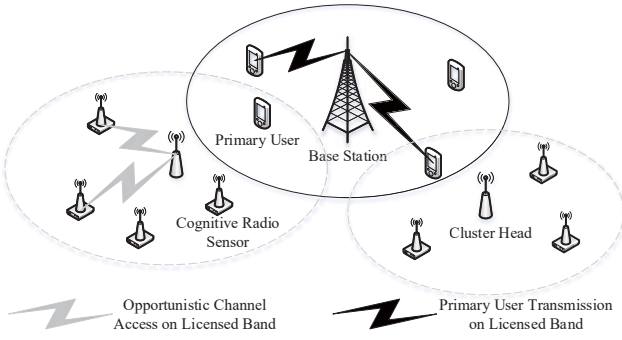


Fig. 1: Cluster-based cognitive radio wireless sensor network

A. Channel Sensing with Availability Constraints

In the CRWSN, sensors are only allowed to access the idle channels. The availability of the licensed channels is determined by the primary users' behavior. Therefore, we can improve the channel sensing efficiency if we can predict the channel availability by utilizing the channel sensing history. As each channel only has two states (busy or idle), we assume that the availability of channels in \mathcal{C} follows independent identical Bernoulli distributions over different time slots with parameters $\mu = \{\mu_1, \mu_2, \dots, \mu_K\}$ which are unknown to the sensors. The empirical mean availability of channel C_i after the channel sensing in time slot T_n is expressed as

$$\hat{\mu}_{i,n} = \frac{1}{n} \sum_{j=1}^n \theta_{i,j}. \quad (1)$$

Assuming that we have a channel availability requirement μ^* for all channels, we define the good channel set as $C_G = \{C_i \in \mathcal{C} : \mu_i \geq \mu^*\}$ and the bad channel set as $C_B = \{C_i \in \mathcal{C} : \mu_i < \mu^*\}$ respectively. Sensors have to estimate the mean availability via (1). We assume that sensor S_i use energy $\eta_i E_i$ for channel sensing where E_i is the total energy of S_i and $\eta_i \in [0, 1]$ is the fraction of energy used for channel sensing. For simplicity and without loss of generality, we assume that all sensors have the same total energy E and ratio η .

With the sensing energy constraint ηE , we use an arbitrary algorithm $\rho \in \Omega$ to classify the channels into an empirical good set ($\hat{C}_G(\rho, \eta)$) and bad set ($\hat{C}_B(\rho, \eta)$) based on the past channel sensing results where Ω is the set of algorithms we use. We define the set of misclassified channels with algorithm ρ and energy ratio η as $C_E(\rho, \eta) = \{C_i \in \hat{C}_G(\rho, \eta) : \mu_i < \mu^*\}$. The error rate is thus defined as $\varepsilon(\rho, \eta) = \frac{|C_E(\rho, \eta)|}{|\mathcal{C}|}$.

We aim at finding an algorithm $\rho^* \in \Omega$ that can find the good and bad channels in a limited time with high confidence and with a minimum error rate which is expressed as

$$\rho^* = \arg \min_{\rho \in \Omega} \varepsilon(\rho, \eta) = \arg \min_{\rho \in \Omega} \left(\frac{|C_E(\rho, \eta)|}{K} \right), \quad (2)$$

$$s.t. \quad (P_{i,c} + P_{i,s}) \alpha T N_{i,\max} \leq \eta E, \forall i \in \{1, 2, \dots, K\}.$$

where $P_{i,c}$ is the circuit power consumption of S_i , $P_{i,s}$ is the channel sensing power consumption of S_i , T is the length of each time slot, α is the fraction of time used for channel

sensing in each time slot and $N_{i,\max}$ is the maximum number of time slots for S_i to spend on channel sensing. According to (2), the maximum number of time slots N is expressed as

$$N = \min_i N_{i,\max} = \min_i \left(\left\lfloor \frac{\eta E}{\alpha T (P_{i,c} + P_{i,s})} \right\rfloor \right). \quad (3)$$

B. Power Control with QoS Constraints

Although increasing the transmission power level generally increases the data rate, it also decreases the lifetime of the sensor node. In this paper, we aim at finding the transmission power level that can maximize the total number of transmitted bits for QoS-constrained applications. We assume that all sensors have the same set of transmission power levels denoted by $P = \{P_1, P_2, \dots, P_M\}$ in ascending order.

We use $R_{i,j,k} = f_i(P_j, C_k)$ to denote the maximum data rate of sensor S_i with power P_j at channel C_k . For simplicity, we assume that the maximum data rate of sensor $S_i \in \mathcal{S}$ with power P_j at channel C_k is a logarithmic function denoted as $f_i(P_j, C_k) = W \log_2(1 + P_j g_{i,k})$ where W is the channel bandwidth and $g_{i,k}$ is the instantaneous channel gain to noise ratio of C_k for S_i . The total number of transmitted bits for sensor S_i with transmission power P_j at channel C_k is expressed as

$$L_{i,j,k} = \frac{(1 - \eta) E W \log_2(1 + P_j g_{i,k})}{(P_j + P_{i,c})}. \quad (4)$$

Assuming that S_i has a minimum data rate requirement denoted by R_i^* , the optimal transmission power for C_k that can maximize the total number of transmitted bits is expressed as

$$P_{i,k}^* = \arg \max_{P_j \in P} L_{i,j,k} = \arg \max_{P_j \in P} \left(\frac{R_{i,j,k}(1 - \eta) E}{P_j + P_{i,c}} \right), \quad (5)$$

$$s.t. \quad R_{i,j,k} \geq R_i^*, \forall S_i \in \mathcal{S}, C_k \in \mathcal{C}; \quad \eta \geq \eta^*;$$

where η^* is the minimum energy ratio for reliable channel sensing. We use $L_{i,k}^*$ to denote the optimal total number of transmitted bits for S_i on C_k using power $P_{i,k}^*$. Let $\lambda_{i,k} = 1$ if C_k is accessed by S_i and $\lambda_{i,k} = 0$ otherwise. The maximum number of transmitted bits in the each cluster is expressed as

$$L^* = \max \sum_{i=1}^K \sum_{k=1}^K \lambda_{i,k} L_{i,k}^*, \quad (6)$$

$$s.t. \quad \sum_{k=1}^m \lambda_{i,k} = 1, \forall i; \quad \sum_{i=1}^n \lambda_{i,k} \leq 1, \forall k.$$

III. ALGORITHMS

In this section we introduce algorithms to solve the channel sensing problem with availability and power constraints.

A. Passive Rejection Algorithm

Under a passive rejection algorithm, sensor S_i always senses its corresponding channel C_i until it has high confidence that μ_i is less than the minimum channel availability requirement μ^* . We first propose a simple reject algorithm (SRA) denoted by ρ_{SRA} as detailed in Algorithm 1. SRA is an ε -PAC algorithm that can correctly identify a bad channel with probability at least $1 - \varepsilon$. An algorithm is an ε -probably approximately correct (PAC) algorithm if it outputs the correct result with probability at least $1 - \varepsilon$. The proof is omitted due to the space limit.

Algorithm 1 Simple Reject Algorithm (SRA)

Input the value of μ^* , η and T . Calculate N based on (2) and (3).
Initialization: $\hat{C}_G(\rho_{SRA}, \eta) \leftarrow \mathcal{C}$, $\hat{C}_B(\rho_{SRA}, \eta) \leftarrow 0$.
for $1 \leq n \leq N$ **do**
 for each $C_i \in \hat{C}_G$ **do**
 Calculate $\hat{\mu}_{i,n}$ based on (1).
 if $\gamma_{i,n} = \mu^* - \hat{\mu}_{i,n} \geq \sqrt{\frac{1}{2n} \ln(\frac{1}{\varepsilon})}$ **then**
 $\hat{C}_G \leftarrow \hat{C}_G - \{C_i\}$, $\hat{C}_B \leftarrow \hat{C}_B \cup \{C_i\}$.
 end if
 end for
end for
Output $\hat{C}_G(\rho_{SRA}, \eta)$.

We also propose an improved reject algorithm (IRA) denoted by ρ_{IRA} as detailed in Algorithm 2, which is also an ε -PAC algorithm.

Algorithm 2 Improved Reject Algorithm (IRA)

Input the value of μ^* , η and T . Calculate N based on (2) and (3). Let $B_\varepsilon(n, p)$ denote the quantile of order ε for the binomial distribution with parameter n and p .
Initialization: $\hat{C}_G(\rho_{IRA}, \eta) \leftarrow \mathcal{C}$, $\hat{C}_B(\rho_{IRA}, \eta) \leftarrow 0$.
for $1 \leq n \leq N$ **do**
 for each $C_i \in \hat{C}_G$ **do**
 Calculate $\hat{\mu}_{i,n}$ based on (1).
 if $n\hat{\mu}_{i,n} \leq B_\varepsilon(n, \mu^*)$ **then**
 $\hat{C}_G \leftarrow \hat{C}_G - \{C_i\}$, $\hat{C}_B \leftarrow \hat{C}_B \cup \{C_i\}$.
 end if
 end for
end for
Output $\hat{C}_G(\rho_{IRA}, \eta)$.

B. Active Elimination Algorithm

Although passive rejection algorithms can identify bad channels with high confidence, classifying channels with mean value close to μ^* still remains non-trivial. In addition, it is not energy efficient to sense most channels every time slot if there are only a small amount of sensors having data transmission requests. Thus, we propose an active elimination algorithm (AEA) denoted by ρ_{AEA} that can find the m best channels in \mathcal{C} with a finite time horizon and low error rate.

Without loss of generality, we assume that μ is ordered and $\mu_1 > \mu_2 > \dots > \mu_K$. Let $\mu_m = \mu^*$. We use $\Delta_{i,j} = \mu_i - \mu_j$ to denote the gap between μ_i and μ_j . For the m best channels in \mathcal{C} we define Δ_i^m as

$$\Delta_i^m = \begin{cases} \Delta_{i,m+1}, & 1 \leq i \leq m \\ \Delta_{m,i}, & m+1 \leq i \leq K. \end{cases} \quad (7)$$

At round i , the probability that $C_n \in C_G$ is eliminated is at most $6 \exp\left(-\frac{(\Delta_i^m)^2 t}{2}\right)$ where $t = \left\lfloor \frac{N}{\lceil \log_2(\frac{K}{m}) \rceil} \right\rfloor$. AEA is thus an ε -PAC algorithm that can correctly identify the m best channels with probability at least $1 - \varepsilon$ where $\varepsilon = \frac{6mN}{t} \exp\left(-\frac{(\Delta_i^m)^2 t}{2}\right)$. The proof is omitted due to the space limit.

Algorithm 3 Active Elimination Algorithm (AEA)

Input the value of μ^* , η , m and T . Calculate N based on (2) and (3).
Initialization: $G_0 \leftarrow \mathcal{C}$.
for round i , $1 \leq i \leq \lceil \log_2(\frac{K}{m}) \rceil$ **do**
 Sensing each channel $C_j \in G_{i-1}$ for $t = \left\lfloor \frac{N}{\lceil \log_2(\frac{K}{m}) \rceil} \right\rfloor$
 time slots. Let G_i be the set of $\left\lfloor \frac{|G_{i-1}|}{2} \right\rfloor$ channels in G_{i-1}
 with largest empirical mean value.
end for
Output $\hat{C}_G(\rho_{AEA}, \eta) \leftarrow G_{\lceil \log_2(\frac{K}{m}) \rceil}$.

C. Joint Channel Sensing and Power Control Scheme

We now propose the joint channel sensing and power control scheme (JCSPCS) to maximize the amount of transmitted data of each sensor. With channel availability constraints and data transmission requests, we use the AEA to find the m best channels for n sensors ($n \leq m \leq K$) to regularly transmit their data. Let ε^* be the maximum acceptable error rate of AEA. We have $\varepsilon = \frac{6mN}{t} \exp\left(-\frac{(\Delta_i^m)^2 t}{2}\right) \leq \varepsilon^*$. We assume $t = \frac{N}{\log_2(\frac{K}{m})}$ for simplicity. Thus, we have

$$N \geq \frac{2 \log_2(\frac{K}{m})}{(\Delta_i^m)^2} \ln\left(\frac{6m \log_2(\frac{K}{m})}{\varepsilon^*}\right). \quad (8)$$

We also assume that each sensor $S_i \in \mathcal{S}$ has the same circuit power consumption $P_{i,c} = P_c$ and channel sensing power consumption $P_{i,s} = P_s$. According to (2), (3), (5) and (8), the minimum energy ratio for reliable channel sensing denoted as

$$\eta \geq \frac{2\alpha T (P_c + P_s) \log_2(\frac{K}{m})}{(\Delta_i^m)^2 E} \ln\left(\frac{6m \log_2(\frac{K}{m})}{\varepsilon^*}\right) = \eta^*. \quad (9)$$

From (5), we know that $\frac{(1-\eta^*)E}{P_j + P_c}$ is bounded and inversely proportional to P_j while $\log_2(1 + P_j g_{i,k})$ is bounded and logarithmically proportional to P_j . According to the extreme value theorem, for each S_i transmitting data on C_k , there exists a $P_{i,k}^*$ that maximizes the total number of transmitted bits.

We propose the joint channel sensing and power control scheme (JCSPCS) shown in Algorithm 4.

Algorithm 4 Joint Channel Sensing and Power Control Scheme

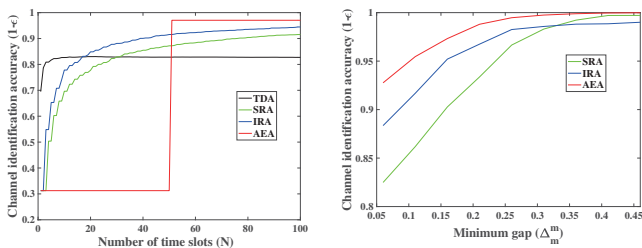
Input the value of n , m , K , T , Δ_i^m and ε^* .
Initialization: Find the m best channels using AEA. Calculate η^* according to (9).
for $1 \leq i \leq n$ **do**
 for $1 \leq k \leq m$ **do**
 Calculate $P_{i,k}^*$ and $L_{i,k}^*$ based on (5). $L \leftarrow L_{i,k}^*$.
 end for
end for
Solve (6) using the Hungarian algorithm [6].
Output λ^* and L^* , where λ^* is the $n \times m$ matrix with element $\lambda_{i,k}$ that maximizes L^* in (6).

IV. SIMULATION RESULTS

In our simulation, we assume that the channels are slow fading channels. The channel state information (CSI) is available to the transmitter and receiver. The transmission power ranges from 0 to 100 mW and is equally divided into $M = 10$ levels. For channel C_k assigned to sensor S_i , the normalized channel gain $g_{i,k}$ is randomly generated. Some parameters in the simulation are given in TABLE I.

TABLE I: Parameters for simulation

Symbol	Description	Value
P_c	circuit power consumption	10 mW
P_s	sensing power consumption	30 mW
T	length of each time slot	1 s
α	fraction of time for channel sensing	0.1
E	total energy	500 J
W	channel bandwidth	200 kHz
M	transmission power levels	10
R^*	minimum data rate requirement	100 kbps



(a) CIA with different channel sensing algorithms. (b) CIA with different minimum channel availability gap (Δ_m^m).

Fig. 2: Channel identification accuracy (CIA)

We first consider the channel sensing problem with availability constraints. We set $K = 16$, $m = 5$, $N = 100$, and $\mu^* = 0.7$. Elements in $\mu = \{\mu_1, \mu_2, \dots, \mu_K\}$ are ordered and equally spaced in the interval $[0.05, 0.95]$. In the beginning, all channels are assumed to be good channels. We compared our algorithms with a threshold detection algorithm (TDA). In TDA, we say a channel C_i is bad if in any time slot T_n we have $\hat{\mu}_{i,n} < \mu^*$. The performance of algorithms is averaged over 1000 simulation runs. Fig. 2a shows that all our algorithms correctly identify the good channels with higher accuracy (above 90%) compared to that of TDA (82%). For the final error rate, we have $\varepsilon(\rho_{SRA}, \eta) > \varepsilon(\rho_{IRA}, \eta) > \varepsilon(\rho_{AEA}, \eta)$. Unlike SRA and IRA that gradually identify bad channels with high confidence, AEA achieves the lowest error rate as it keeps sensing channels until it has high confidence to eliminate at most half of the existing channels. We then investigate how $\Delta_{i,j}$ affects the error rate ε for our channel sensing algorithms. According to the definition in (7), we have $\Delta_m^m = \Delta_{m+1}^m = \min_i \Delta_i^m$. We set $K = 16$, $m = 5$, $N = 30$, and $\mu^* = 0.7$. We gradually change Δ_m^m from 0.05 to 0.45. We compare the error rates of our algorithms with different values of Δ_m^m . From Fig. 2b, we show that for all algorithms the error rates ε decrease with increasing Δ_m^m . Under the same parameter settings, AEA always has the lowest error rate.

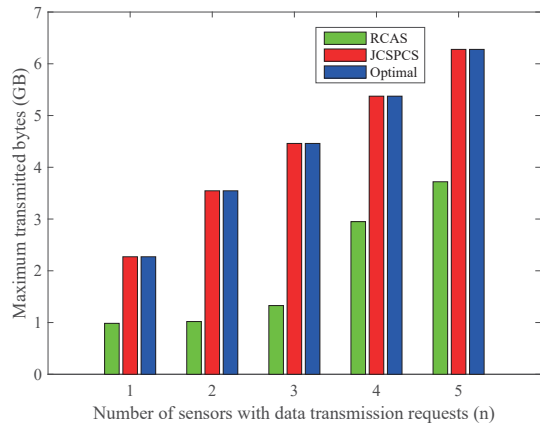


Fig. 3: Maximum number of transmitted bits in the cluster vs. different number of sensors with data transmission requests.

Finally, we show the efficiency of JCSPCS in Fig. 3. Here, we investigate JCSPCS with different n . We set $K = 16$, $m = 5$, $\varepsilon^* = 0.1$, $\Delta_m^m = 0.06$ and $\mu^* = 0.7$. Fig. 3 shows that JCSPCS outperforms the random channel access scheme (RCAS) with different n in our simulation and JCSPCS is the optimal solution. Note that Hungarian algorithm [6] has $O(n^4)$ time complexity. However, this is not a problem in practice since the number of sensors with data transmission requests in each cluster is small ($n \sim 10^1$).

V. CONCLUSION

In this paper, we considered power control and channel sensing problem in a CRWSN. We proposed three ε -PAC algorithms to solve the channel sensing problem with availability constraints. Then we considered the power control problem with QoS constraints and aimed at maximizing the total number of transmitted bits in the cluster. A joint channel sensing and power control scheme (JCSPCS) is proposed to optimize the total data transmission. Simulation results showed that our ε -PAC algorithms can correctly identify good channels with low error rate. We also showed that JCSPCS maximized the number of transmitted bits in the cluster.

REFERENCES

- [1] M. McHenry, E. Livsics, T. Nguyen, and N. Majumdar, "Xg dynamic spectrum access field test results [topics in radio communications]," *IEEE Communications Magazine*, vol. 45, no. 6, pp. 51–57, June 2007.
- [2] O. B. Akan, O. B. Karli, and O. Ergul, "Cognitive radio sensor networks," *Netw. Mag. of Global Internetwkg.*, vol. 23, no. 4, pp. 34–40, Jul. 2009. [Online]. Available: <http://dx.doi.org/10.1109/MNET.2009.5191144>
- [3] P. Auer, N. Cesa-Bianchi, and P. Fischer, "Finite-time analysis of the multiarmed bandit problem," *Machine learning*, vol. 47, no. 2-3, pp. 235–256, 2002.
- [4] C. Tekin and M. Liu, "Online learning in opportunistic spectrum access: A restless bandit approach," in *INFOCOM, 2011 Proceedings IEEE*, April 2011, pp. 2462–2470.
- [5] Y. Gai and B. Krishnamachari, "Decentralized online learning algorithms for opportunistic spectrum access," in *Global Telecommunications Conference (GLOBECOM 2011), 2011 IEEE*. IEEE, 2011, pp. 1–6.
- [6] H. W. Kuhn, "The hungarian method for the assignment problem," *Naval Research Logistics Quarterly*, vol. 2, pp. 83–97, 1955.