

1

# The ML family

ML is not a single language. Apart from Standard ML, which we use here, there are many descendants of the original ML used as the metalanguage of Edinburgh LCF, e.g.

- CAML Light an excellent lightweight system developed at INRIA.
- Objective CAML a new version of CAML Light including object-oriented features.
- Lazy ML a version from Gothenburg using *lazy evaluation*.
- Standard ML an agreed 'standard version'

Standard ML has two parts: the *Core* language and the *Modules*. We will not cover the module system at all.



John Harrison

Starting up ML

4

Moscow ML is already installed on Thor. In order to start it up, type:

/group/clteach/jrh/mosml/'arch'/bin/mosml

This will invoke the appropriate version, depending on the machine architecture.

The system should start up and present its prompt.

\$ /group/clteach/jrh/mosml/'arch'/bin/mosml
Moscow ML version 1.42 (July 1997)
Enter 'quit();' to quit.

If you want to install Moscow ML on your own computer, see the Web page:

http://www.dina.kvl.dk/~sestoft/mosml.html

# Interacting with ML

We will run ML as an interpreter, rather like a sophisticated calculator. You just type an expression into it, terminated by a semicolon, and it prints the result of evaluating it, e.g.

-10+5;

> val it = 15 : int

ML not only prints the result, but also infers the *type* of the expression, namely **int**. If ML cannot assign a type to an expression then it is rejected:

```
-1 + true;
```

! .... Type clash: ....

ML knows the type of the built-in operator +, and that is how it makes its type inference.

We'll treat the type system more systematically next time; for the moment, it should be intuitively clear.

# Loading from files

We have just been typing things into ML and thinking about the results. However one doesn't write real programs in this way.

Typically, one writes the expressions and declarations in a file. To try them out as you go, these can be inserted in the ML window using cut and paste.

You can cut and paste using X-windows and similar systems, or an editor like Emacs with multiple buffers.

For larger programs, it's convenient simply to load them from file into the ML session. This can be done using the **use** command in ML, e.g:

```
use "myprog.ml";
```

Programs can also include comments written between (\* and \*). These are ignored by ML, but are useful for people reading the code.

#### Using functions

Since ML is a functional language, expressions are allowed to have function type. The ML syntax for a function taking x to t[x] is fn x => t[x]. For example we can define the successor function:

- fn x => x + 1;

Again, the type of the expression, this time int -> int, is inferred and displayed. However the function itself is not printed; the system merely writes fn.

Functions are applied by juxtaposition, with or without bracketing:

### Curried functions (1)

Every function in ML takes a single argument. One way to get the effect of multiple arguments is to use a *pair* for the argument — we'll discuss this next time.

Another way, often more powerful, is to use *Currying*, making the function take its arguments one at a time, e.g.

- fn x => (fn y => x + y); > val it = fn : int -> (int -> int)

This function takes the first argument and gives a new function. For example:

-  $(fn x \Rightarrow (fn y \Rightarrow x + y)) 1;$ 

is just the successor function again, e.g.

> val it = 7 : int

John Harrison

### **Curried functions (2)**

Because curried functions are so common in functional programming, ML fixes the rules of association to avoid the need for many parentheses.

When one writes  $E_1 E_2 E_3$ , ML associates it as  $(E_1 E_2) E_3$ . For example, all the following are equivalent:

- ((fn x => (fn y => x + y)) 1) 6; > val it = 7 : int

John Harrison

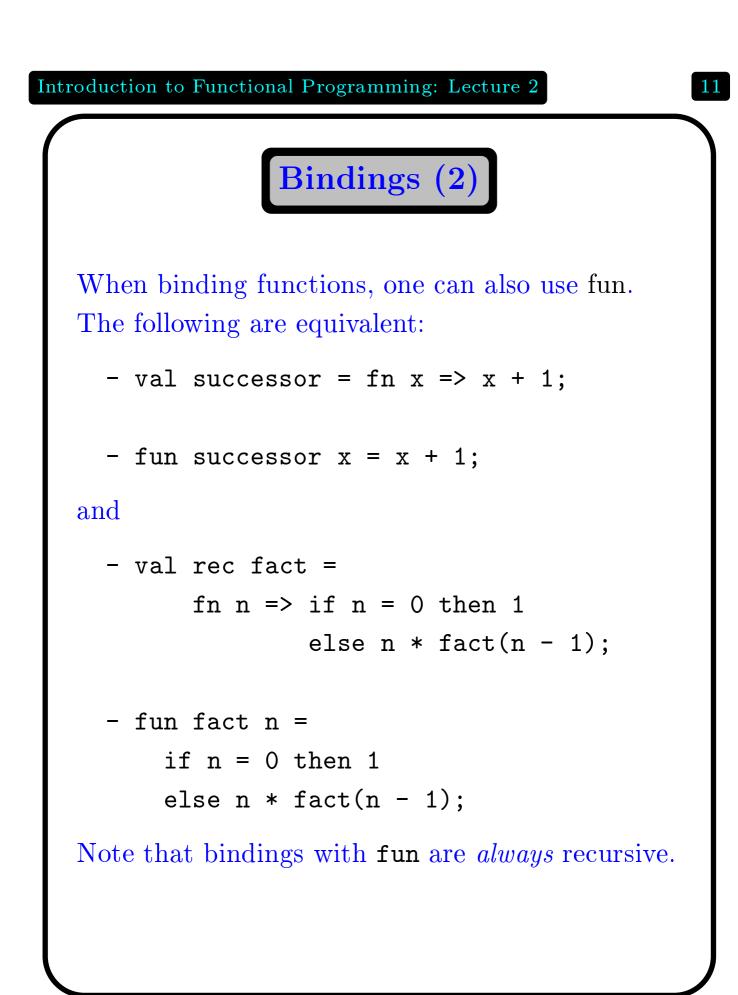
Bindings (1)

It is not necessary to evaluate an expression all in one piece. You can *bind* an expression to a name using val:

- val successor = fn  $x \Rightarrow x + 1$ ;
- > val successor = fn : int -> int
- successor(successor(successor 0));
- > val it = 3 : int

Note that this isn't an assignment statement, merely an abbreviation. But bindings can be recursive: just add rec:

- val rec fact =
 fn n => if n = 0 then 1
 else n \* fact(n - 1);
> val fact = fn : int -> int
- fact 3;
> val it = 6 : int



### **Higher order functions**

Curried functions are an example of a function that gives another function as a result.

We can also define functions that take other functions as arguments. This one takes a positive integer n and a function f and returns  $f^n$ , i.e.  $f \circ \cdots \circ f$  (n times):



Local declarations

13

Bindings can be made local using

let decs in expr end

#### For example:

This binding is now invisible beyond the terminating end. Similarly one can make a declaration local to another *declaration* by:

local decs in decs end

# ML's evaluation strategy

Execution of an ML program just means evaluating an expression. You can think of this evaluation as happening by a kind of syntactic unfolding of the program.

- Constants like 1 and + evaluate to themselves.
- Evaluation stops immediately at something of the form fn x => ... and does not 'look inside' the ....
- When evaluating a combination s t, then first both s and t are evaluated to s' and t'. If s' is not of the form fn x => u[x] then things stop there. Otherwise u[t'], the result of replacing the dummy variable x by the evaluated form of t is evaluated.

It is important to grasp this evaluation strategy in order to understand ML properly.

#### Which evaluation strategy

But does evaluation order actually matter? One might guess not. For example:

$$(1 + 2) + (3 + 4) = 3 + (3 + 4)$$
  
= 3 + 7 = 10

and

$$(1 + 2) + (3 + 4) = (1 + 2) + 7$$
  
= 3 + 7 = 10

give the same answer. Does this generalize? In fact, for 'pure' functional programs, if two different evaluation orders terminate, they give the same answer. (This is roughly the *Church-Rosser theorem.*)

But there are still reasons to care about evaluation order: termination, efficiency, and imperative features.

# Lazy evaluation

ML's evaluation strategy is called *eager* or *call-by-value* because the argument to a function is evaluated even if it never ends up being used.

An alternative would be, when evaluating (fn x => u[x]) t, to evaluate u[t] without yet evaluating t. This is *call-by-name* evaluation.

The advantage is: we avoid evaluating t if it isn't actually used, and this evaluation might be very costly or even fail to terminate.

The disadvantage of a naive implementation is that one would re-evaluate t if it's used more than once. So one needs a clever sharing implementation — *lazy evaluation*.

Lazy evaluation seems better in principle, and many functional languages, even ML's relative Lazy ML, use it. But it's harder to implement efficiently and doesn't seem to fit with imperative features. Hence ML's choice.

ML evaluation examples

4 -8

John Harrison

# The conditional

Consider evaluating a factorial (as defined earlier) where the conditional is evaluated eagerly. To evaluate fact(0) we unfold it to:

if 0 = 0 then 1 else 0 \* fact(0 - 1)

We need to cut this down to 1. But under the standard eager rules, we would first evaluate all three subexpressions, including fact(0 - 1). This leads to an infinite loop.

So we can't regard the conditional as an ordinary function of three arguments: it has to have its own 'lazy' reduction strategy.

The test expression is evaluated first, and according to its value, precisely one of the arms, never both,