Secure Compilation of a Multi-Tier Web Language

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Abstract
Storing state in the client tier (in forms or cookies, for example) improves the efficiency of a web application, but it also renders the secrecy and integrity of stored data vulnerable to untrustworthy clients. We study this general problem in the context of the LINKS multi-tier programming language. Like other systems, LINKS stores unencrypted application data, including web continuations, on the client tier; hence, LINKS is open to attacks that expose secrets, and modify control flow and application data. We characterise these attacks as failures of the general principle that security properties of multi-tier applications should follow from review of the source code (as opposed to the detailed study of the files compiled for each tier, for example). We eliminate these threats by augmenting the LINKS compiler to encrypt and authenticate any data stored on the client. We model this compilation strategy as a translation from a core fragment of the language to a concurrent \(\lambda\)-calculus equipped with a formal representation of cryptography. To formalize source-level reasoning about LINKS programs, we define a type-and-effect system for our core language; our implementation can machine-check various integrity properties of the source code.

By appeal to a recent system of refinement types for secure implementations, we show that our compilation strategy guarantees all the properties provable by our type-and-effect system.

Categories and Subject Descriptors D.3.1 [Formal Definitions and Theory]: Formal Methods; D.4.6 [Security and Protection]: Cryptographic controls; F.3.1 [Specifying and Verifying About Programs]: Specification techniques

General Terms Languages, Security, Design, Verification

Keywords Integrity, type systems, compilers, cryptography, web programming, web application security.

1. Introduction
1.1 The Background Trend: Toward Multi-Tier Languages
Nobody would question the success of the web, but people do question the need for so many different web programming languages.

One must be well versed in a multiplicity of languages to write even trivial web applications. Code for the server tier may be in JSP (Sun Microsystems 2006), PHP (The PHP Group 2006), or ASP (Microsoft 2006), for example; queries running on the database tier may be in SQL or XQuery; and code for the client tier (the browser) may use HTML (W3C 1999), CSS (W3C 2007), and JavaScript (ECMA International 1999), and so on.

This multiplicity gives rise to the problem of impedance mismatch (Meijer et al. 2003): data exchanged between the different tiers of the same application often comes in incompatible shapes and formats. Each language defines its own type system and data structures. Coordination between different languages requires many conversion functions; these are error prone and obscure the essential algorithm. Another problem of language multiplicity is that security reviews of web applications (Scambay and Shema 2002; Howard and LeBlanc 2003) require detailed knowledge of the languages on each tier.

In contrast to the various single-tier languages mentioned previously, a multi-tier programming language is a high level web programming language that compiles to code split between each of the tiers of a web application. Given minimal user input, the compiler automatically performs the partitioning of the code between client, server, and database, the translation into other languages, and the linking of the components with each other. By raising the level of abstraction, multi-tier languages allow the developer to focus on the algorithms and logics of the web application, while leaving the details of data and code partitioning, and data conversion, to the compiler. Several languages adopt such an approach: LINKS is a strongly typed, multi-tier, functional programming language for the web (Cooper et al. 2006); HOP (Serrano et al. 2006) is a Scheme-based language for creating interactive applications across the web; Hilda (Yang et al. 2006) is a declarative language for developing data-driven web applications; MLS (Murphy VII et al. 2008) is a distributed language with a prototype for web programming that enables code to run on different tiers; the Google Web Toolkit (Google 2006) simplifies the construction of client-side code by compiling Java to JavaScript; LINQ (Microsoft 2005) is a set of extensions to the .NET framework that provides language-level syntax and libraries to express database queries.

1.2 Source-Based Security for Multi-Tier Web Applications
It is worth returning to first principles, by recalling what we mean by a high-level language, so as to see the implications for security. To say a language is high-level means that it supports a programming model that abstracts from the details of the lower-level code to which the language is compiled. The ideal is that one may reason about program correctness and performance solely in terms of the abstract programming model, without recourse to the details of compilation. Multi-tier languages are high-level languages for the web; they offer various programming models that abstract from the details of the target single-tier languages to which they compile. LINKS in particular abstracts from the details of JavaScript and SQL and supports a high-level model based on call-by-value functional programming with XML literals.
Security is an aspect of correctness, so high-level languages should allow security reasoning in terms of the abstract programming model. Hence, security reviews may be conducted efficiently at the source-level. Unfortunately, this ideal is seldom completely achieved; Abadi (1999), for example, describes how some security properties obtained by reasoning about Java programs are not preserved by compilation to JVM code. Still, the high-level ideal remains a desirable goal, which may be stated as follows.

**Principle of Source-Based Reasoning.** Security properties of compiled code should follow from review of the source code and its source-level semantics.

Our objective in this paper is to allow security reasoning about multi-tier LINKS programs at the source level, and to formalize security properties in the context of LINKS. LINKS was not designed with security in mind. As we see next, its implementation needs to be adapted because it places too much trust in the browser tier.

### 1.3 Some Violations of Source-Based Security and a Solution

LINKS programs maintain state either in the browser or database, but not in the middle tier, the web server. To keep state in the browser, LINKS relies on the idea of embedding continuations in HTML pages (Hughes 2000; Queinnec 2000) as first implemented in the PLT Scheme Web Server (Graunke et al. 2001). LINKS represents continuations as closures (expression identifier plus values of free variables) in hidden fields within HTML pages or as URL parameters. This creates a security risk as a malicious client may modify these continuation strings and force unexpected computations on the server.

When discussing security, we need to specify the threat model so as to design suitable protection against possible attacks. The focus of this paper is the threat model where the client (as opposed to some third party) attempts to attack the web server running a LINKS program. Our main concern is securing code or data that must legitimately be stored in a browser controlled by the attacker.

We want to protect our application against rogue clients and to guarantee that the implementation corresponds to the source level semantics.

In what follows, we assume an untrustworthy client browser controlled by the attacker, who may run software to capture, decode, and modify web pages received from the server. We assume that transport layer security (SSL/TLS) protects against attacks by a third party. We only consider LINKS programs that keep no mutable state in a database, and where all functions reside on the server. In general, we assume that the source code of both the application program and the LINKS system itself are public (and hence implementation mechanisms such as encoding formats are known to the attacker). The only exception to this rule is that for the purpose of writing examples we assume there may be some secret data embedded within the source of the application program, such as a database password.

Given this threat model, the following attacks on the LINKS system show failures of the Source-Based Reasoning principle.

1. The client may learn secret data that is held in a closure embedded in a web page; for example, they may learn server data such as a password.
2. The client may break the integrity of server data by modifying a closure embedded in a web page so as to change future behaviour of the application; for example, the client may change the price of an item in a shopping cart.
3. The client may change the control flow of the program by discovering an unreachable function held in one closure, and then modifying a function value held in another closure.

The problem of untrustworthy clients is not new (for example, Krishnamurthi et al. (2007) discuss it in the context of the PLT Scheme Web Server), and indeed the solution in our setting, without mutable state, is quite simple; still, we believe we are the first to formalize and implement the solution. We propose to apply authenticated encryption to closures to fix these problems. Authenticated encryption is a combination of secrecy and integrity protection where we initially hash the data and subsequently encrypt the data itself along with the hash. We need randomised encryption to prevent failures of secrecy such as point (1). We need the encryption to be authenticated (in our case, by including a hash) to prevent failures of integrity such as points (2) and (3). We have coded our proposal as a small modification of the LINKS system.

### 1.4 TinyLINKS and Formalizing a Secure Implementation

To enable a precise description and a security proof, we introduce TinyLINKS, an extended fragment of the LINKS language.

Our development makes use of a concurrent λ-calculus (RCF), and its implementation in the practical typechecker F7 (Bengtson et al. 2008). RCF and F7 rely on refinement types (Xi and Pfening 1999; Flanagan 2006), to check a range of security properties by typing F7 checks programs in the ML dialect F# (Syme et al. 2007) against interface files enhanced with refinement types.

We developed a typed, formal model of a server implementing TinyLINKS as a function from HTTP requests to XML responses. Our model is within F7 (that is, within F# but with typing enhanced with refinement types). Given this model, we define the *standard implementation* (as used by the LINKS system) as a translation from TinyLINKS expressions into F7. Moreover, by appeal to existing formal models of cryptography within F7, we describe our *secure implementation* strategy as a simple modification of the standard implementation.

We annotate TinyLINKS programs with event-based assertions so as to express correctness properties. We enhance the usual LINKS type system with effects as a technique for proving assertion safety. Hence, we can state and prove expected safety properties, including the integrity properties violated by the attacks on (2) and (3), within TinyLINKS. The main theorem of the paper, Theorem 2, is that the class of properties provable with our type-and-effect system is preserved by the secure implementation.

Assuming our F7 model of the secure implementation corresponds to our secure modification of the LINKS system, this result amounts to a formal instance of our principle of source-based reasoning: any property proved by running our typechecker as a review of a LINKS program (with TinyLINKS type annotations), actually applies to the implementation of the program as a web application. Hence, for example, we may rule out attacks (2) and (3). (Although we believe that our encryption rules out attack (1) on data secrecy, our formal results do not yield secrecy properties.)

### 1.5 Contributions

- We propose a secure compilation strategy, based on cryptography, for client-side continuations and implement it as a modification of the LINKS system.
- We define a formal semantics for a subset, TinyLINKS, and develop a type-and-effect system that allows source level reasoning about integrity.
- We formalize both the standard and the secured compilation strategy as type-directed translations from TinyLINKS programs to F7 expressions.
- We prove a correctness result for the secure strategy, Theorem 2: if a LINKS program is well typed using the type-and-effect system, then the properties proved are respected by the secure compilation strategy at the F7 level.
2. Introducing the LINKS Multi-Tier Language

A LINKS program is a top-level expression, \( E_{\text{top}} \) (which typically consists of a series of \texttt{var}-bound functions, ending with an XML expression for the top-level page) located at an implicit URL. A client browser initiates the execution of the program by requesting a URL and receives an (XML-encoded) HTML value, the result of evaluating the top-level expression in the program associated with the URL. From the perspective of the user, the computation proceeds by interacting with the page: clicking on links, filling in forms, and submitting them. From the perspective of the LINKS system, the computation consists of receiving and responding to a series of requests following the HTTP protocol.

2.1 The HTTP Protocol (Review)

The HyperText Transfer Protocol (HTTP) is a stateless, request-response protocol that uses a client-server model. An HTTP client opens a connection and sends a request message to an HTTP server. The requested resource (a static or dynamic page) is identified by a URI. The server returns a response message, usually containing the resource that was requested, and closes the server connection. For creating dynamic pages, a web server can use the Common Gateway Interface (CGI) to run any server-side program to produce responses on its behalf. The protocol defines several possible request messages (methods) that might produce side-effects on the server. In this paper, we consider only the GET and POST methods, because LINKS is built on top of just these two primitives.

The GET method instructs the browser to retrieve the resource associated with the URL. The resource may be statically or dynamically generated but its production should cause no side-effects. In the case of dynamic resources, the URI supplied by the GET method might contain an additional query string that contains data to be passed to a web application. A question mark in the URI acts as a separator between the host and directory, and the query string. This query string is composed of a series of field-value pairs separated by ampersand characters. The POST method is used to send data to the server, potentially updating server state. The request URI indicates which program is to process the data, with the body of the message containing the encoded data of the form.

2.2 LINKS and its Implementation

The LINKS system is called by the web server as a CGI program, to process an HTTP request and produce an XML response.

Once the source code is uploaded to the server, a user executes the program by entering its URL; this corresponds to a GET request with no query string. The LINKS interpreter receives the incoming request and translates the program into XML. During the translation of client-tier code with embedded LINKS expressions to plain HTML and JavaScript, the suspended expressions embedded inside links and forms need to be transformed, along with their environment bindings, into a continuation string. These continuation strings replace the embedded LINKS expressions in the translated code. To achieve this, the system generates a unique label (a pointer) for each expression that occurs inside the program and thereafter maintains an association list between every sub-expression and its label. When constructing a response, LINKS applies a base64 encoding to the hashed expression label and the environment bindings, representing them as a list of pairs.

An important design decision in implementing web continuations for stateful interactions over the stateless HTTP protocol is where to store the continuation object (server or client) and for how long. LINKS takes the approach of storing the serialised continuation in a field named \( \_k \), either a hidden field inside a form or in a URL itself. During a subsequent GET or POST request, the system checks if such a field exists, and continues the execution from the sub-expression corresponding to the encoded label.

The serialised continuation includes the expression pointer along with the required environment bindings. A malicious user, using simple tools and some knowledge of the encoding used by the LINKS system, can modify these serialised pointers that are passed between the browser and the server. The system upon receiving a subsequent request is unable to determine if a modification has taken place, leaving it exposed to rogue clients.

2.3 TINYLINKS, a Fragment of LINKS

The compilation process followed by LINKS is formalized in an extended fragment of the language that we call TINYLINKS. TINYLINKS is an extension of the simply-typed, call-by-value \( \lambda \)-calculus with XML values for representing web pages. The syntax of TINYLINKS goes beyond LINKS for two reasons.

First, so that we may represent the browsing behaviour of users as code within TINYLINKS, we include \texttt{get} and \texttt{post} expressions that use HTTP to fetch links and fill in forms. Second, so that we may specify expected trace-based properties within code, we include \texttt{event} and \texttt{assert} expressions. We have purposefully left out several LINKS features like database queries, concurrency, forms and tier splitting from our formalization. Our simplification is justified because the security anomalies we are studying can be observed even without these features, which would distract from and complicate our theory.

The original (LINKS) program goes through a sequence of transformations (recreating links and forms, \( \lambda \)-lifting, naming intermediate results) to generate an expression in TINYLINKS. The syntax is given in the display below; it is in a minimal style, reminiscent of \( A \)-normal form (Sahry and Felleisen 1993), where the \texttt{var} expression is the principal way of sequencing computations. Phrases of syntax are identified up to \( \alpha \)-conversion, that is, up to consistent renaming of bound variables.

### Values and Expressions of TINYLINKS:

<table>
<thead>
<tr>
<th>Expression</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f, y, x )</td>
<td>Variables</td>
</tr>
<tr>
<td>( p )</td>
<td>Predicate symbol</td>
</tr>
<tr>
<td>( W )</td>
<td>Annotation, see Section 4</td>
</tr>
<tr>
<td>( c ::= )</td>
<td>Data type constructor</td>
</tr>
<tr>
<td>Unit</td>
<td>unit constructor</td>
</tr>
<tr>
<td>Zero</td>
<td>integer constructors</td>
</tr>
<tr>
<td>Succ</td>
<td>string constructor</td>
</tr>
<tr>
<td>Nil</td>
<td>list constructors</td>
</tr>
<tr>
<td>Cons</td>
<td>tuples</td>
</tr>
<tr>
<td>Tuple</td>
<td>HTML constructors</td>
</tr>
<tr>
<td>( g ::= )</td>
<td>Primitive functions</td>
</tr>
<tr>
<td>(</td>
<td>+</td>
</tr>
<tr>
<td>intToXml</td>
<td>type conversions</td>
</tr>
<tr>
<td>( L ::= p(V_1, \ldots, V_n) )</td>
<td>Event: tag ( p ) with a list of values</td>
</tr>
<tr>
<td>( V, U ::= )</td>
<td>Value</td>
</tr>
<tr>
<td>( x )</td>
<td>variable</td>
</tr>
<tr>
<td>( c(V_1, \ldots, V_n) )</td>
<td>constructor</td>
</tr>
<tr>
<td>( \lambda x_1, \ldots, x_n \cdot E )</td>
<td>abstraction</td>
</tr>
<tr>
<td>( \text{href}(E) )</td>
<td>link</td>
</tr>
<tr>
<td>( \text{form}([f_1, \ldots, f_n], E) )</td>
<td>form</td>
</tr>
<tr>
<td>( E ::= )</td>
<td>Expression</td>
</tr>
<tr>
<td>( V )</td>
<td>value</td>
</tr>
<tr>
<td>( (E: W) )</td>
<td>type-and-effect annotation</td>
</tr>
<tr>
<td>( \text{var} x = E_1; E_2 )</td>
<td>variable binding</td>
</tr>
<tr>
<td>( V(U_1, \ldots, U_n) )</td>
<td>primitive application</td>
</tr>
<tr>
<td>( V(U_1, \ldots, U_n) )</td>
<td>function application</td>
</tr>
<tr>
<td>( \text{switch}(V) { )</td>
<td></td>
</tr>
<tr>
<td>( \quad \text{case} c(x_1, \ldots, x_n) \rightarrow E_1 )</td>
<td>pattern matching</td>
</tr>
<tr>
<td>( \quad \text{case} _ \rightarrow E_2 )</td>
<td></td>
</tr>
<tr>
<td>} )</td>
<td>get request</td>
</tr>
</tbody>
</table>
The syntactic category of values includes variables, constructor applications, λ-abstractions and two HTML constructs for creating forms and links. Booleans, integers and strings are not taken as primitive but are recovered through standard encodings using data type constructors and constructor applications. We have Zero and Succ to represent integers, and similarly, we represent lists of values using Nil and Cons. Strings become lists of characters, and characters are mapped to integers.

We express HTML pages as values created by applying data constructors (Elem, Text) to value arguments that may contain suspended expressions as follows:

- An href value represents a link which, when clicked, evaluates the suspended expression E. The evaluation request for the expression is implemented using a GET message.
- A form value represents an HTML form with a suspended computation that requires additional user input to proceed. The labels represent the available input fields a client can provide or modify, both visible and hidden; we treat $\ell_i$ as bound variables which are pairwise distinct with scope E. The evaluation request for a form is implemented using a POST message.

Next, we informally describe the semantics of TinyLinks.

A value V is fully evaluated.

An expression with a type-and-effect annotation behaves as the expression on its own.

To evaluate a variable binding, we first evaluate the expression $E_1$ until it yields a value $V$ and we subsequently substitute $V$ for the variable $x$ in the expression $E_2$.

To evaluate a function application $V(U_1, \ldots, U_n)$, we first ensure that $V$ is a $\lambda$-abstraction of the form $\lambda x_1, \ldots, x_n. E$. The application evaluates to $E$ with the $U_i$ substituting for the free occurrences of the variable $x_i$ in the expression.

To evaluate a pattern match, we unify the value $V$ with the pattern $c(x_1, \ldots, x_n)$. If $V$ is a matching constructor applied to the same number of values, $c(V_1, \ldots, V_n)$, the whole switch expression evaluates to the expression $E_1$ with the corresponding values $V_i$ substituting the free variables $x_i$. If the unification fails the whole expression evaluates to $E_2$.

To evaluate a get expression, we check that the value provided is an href(E) and we evaluate the expression E.

To evaluate a post expression, we check that the value provided is a form, form([\ell_1, \ldots, \ell_n], E). We then proceed to evaluate the embedded expression E with the values $V_i$ being substituted for the free labels $\ell_i$.

The annotations assert L and event L return Unit at once.

The annotations assert L and event L have no computational significance, and are included in TinyLinks simply to express certain safety properties. We say an expression is safe to mean that whenever an assertion assert L occurs in an execution, there is a previous occurrence within the execution of an event event L. Such properties are known as (non-injective) correspondences (Woo and Lam 1993), for example. They are widely used for specifying integrity properties of security mechanisms (Gollmann 2003). Here, we use correspondences in Section 4 to express integrity properties of web applications.

In subsequent sections, we treat the language syntax liberally by relying on special derived forms. Unit, lists and tuples are written using conventional shorthand notation but it is understood that the underlying implementation makes use of the corresponding constructors. We lift expressions occurring inside constructor applications and we bind them to freshly generated variables. Tuple projection uses pattern matching and sequencing of expressions is defined by binding to a freshly generated anonymous variable. Multi-case switch expressions are derived by nested uses of the core syntax.

2.4 An Example Web Application and a Client

We introduce programming in Links through an example: even this simple example is susceptible to attacks. The following program represents, in abstract, the process of selling an item at an agreed price. A user requests the web page and is presented with a single button. We assume the price is pre-agreed and thus is hard-coded in the source code. Once the user clicks the buy button the subsequent page is fetched displaying the price to be paid.

The program example declares two functions running on the server. The sellAt function represents the sale offer page; it takes an integer value as its input and produces a web page, containing a form with a button. The onsubmit attribute of the form tag is annotated with the 1 namespace, to instruct the compiler that the text contained in the curly braces is not a literal string but rather a Links expression. Furthermore, this expression is not to be evaluated immediately, but only after the form is submitted. The buy function represents the confirmation page that a user sees after clicking the buy button. It receives an integer price value and a database password argument, does a simple conversion to XML and returns the XML value as its output.

A Simple Web Application: Sale

```ocaml
fun buy(value, dbpass) server {
  intToXml(value) # omitting actual call to the database
}

fun sellAt(price) server {
  var dbpass = "secret";
  <form onsubmit="(buy(price,dbpass))" method="POST">
    <button type="submit">Buy</button>
  </form>
  sellAt(42)
}
```

After the initial request for the program which is implemented as a GET request, the server returns a response with the required web page containing an empty form with a single button. Clicking the button generates a PGST request that includes a hidden variable x and the user is finally presented with the result, 42. It is clear, even by inspecting the source code, that if the program terminates, the only possible output of any interaction with it would be the number 42 being displayed in a web page.

We have included get and post expressions within TinyLinks so we may formally express the browsing behaviour of users as TinyLinks expressions. Let a client be any expression context $E_{\text{client}}$ within TinyLinks containing a hole of the form href(·). The hole represents the web application with which the client interacts. The idea is that the value href($E_{\text{url}}$) represents a link to the main page of the web application $E_{\text{url}}$. The expression $E_{\text{client}[E_{\text{url}}]}$ obtained by filling the hole $E_{\text{client}}$ with $E_{\text{url}}$ is a formal representation of the client $E_{\text{client}}$ browsing the web application $E_{\text{url}}$.

For example, here is a client for our example that requests the main page, which consists of a single form, and submits it.

An Example of a Client Within TinyLinks:

```ocaml
var app = href(·)
var p = get(app)
post(p)
```
The reason we model web clients as expression contexts is to reduce source-based reasoning about the security properties of a web application \( E_{\text{url}} \) to a formal question: for all client contexts \( E_{\text{client}} \), does \( E_{\text{client}}[E_{\text{url}}] \) enjoy the intended property.

As a very simple example, we expect that for all client contexts \( E_{\text{client}} \), whenever \( \text{intToXml}(\text{value}) \) occurs in any execution of \( E_{\text{client}}[E_{\text{url}}] \), value is 42. Given the simple functional semantics of LINKS this sort of property may easily be established by inspection or by some suitable static analysis (such as in Section 4). Unfortunately, as we discuss next, such source-based reasoning is not preserved by LINKS.

3. Some Attacks on the LINKS System

With sufficient knowledge about how the system works, a rogue client working at the HTTP level can examine and modify the continuation strings embedded within web pages to mount at least three kinds of attack: the client (1) may obtain hidden information stored by LINKS in pages on the client, (2) may modify such information, and (3) may construct function calls that did not exist in the source program. Point (1) is a failure of secrecy, and points (2) and (3) are failures of integrity. We distinguish points (2) and (3) as failures of data integrity and control integrity.

3.1 An Attack on Secrecy

We demonstrate an attack on secrecy using the sale example from Section 2.4. A client makes an initial request for the example using the GET method. The server responds with the intermediate page that contains a single form with the buy button. The following figure contains the generated HTML.

**Translation of the Form in the Sale Example:**

```html
<form method="post" action="#">
  <input type="hidden" name="k" 
    value="base64((hash(buy)(price,dbpass))),[price=42,
    dbpass="secret"]") />
  <button type="submit">Buy</button>
</form>
```

The translation is straightforward: forms are directly translated to their corresponding HTML elements and the hidden variable \( k \) holds the continuation string. For clarity we represent the continuation string symbolically; it is a base64 encoding of the expression hash of the onsubmit attribute, along with an environment that binds price to 42 and dbpass to “secret”. The implementation stores the secret value of dbpass in plain text inside the serialised environment. Hence, the attacker may simply decode the secret.

3.2 An Attack on Data Integrity

A more sophisticated attack on the previous program might involve modifying parts of the continuation string. We can rewrite the continuation replacing it with the following one, in which the binding of price is 0 in the environment (e.g. \([\text{price}=0,\text{dbpass}="\text{secret}"]\)). By clicking on the buy button, we submit a POST request with the updated continuation and force the server to evaluate the original expression under the counterfeit environment.

3.3 An Attack on Control Integrity

The next example demonstrates how an attacker can make calls that are not possible in the source level program. The following program presents the user with a link to click, and subsequently displays a page with a number. The implementation declares a function page with two local functions \( f \) and \( \text{g} \) corresponding to a reachable page and an unreachable one. It also contains a link that upon clicking will display the reachable page. The variable \( \text{g} \) corresponding to the unreachable page is bound to \( w \) inside the link’s expression but never used subsequently in the body of the \( \text{var} \)-expression.

**Unreachable Page Example:**

```haskell
fun page(x) server {
  var \( f = \text{fun} \) {} <html> A page with \( \text{intToXml}(x) \) </html> };
  var \( g = \text{fun} \) {} 
  <html> An unreachable page with \( \text{intToXml}(x) \) </html> ;
  \text{a.href}=*{\text{var w=\text{g} } ; \text{f}()}*" Click for reachable page */a>
}<a href="hash(\text{var w=g; f()})"> Click for reachable page */a>
```

The attack on the example would still be possible even without the binding of \( g \) to \( w \). Given that an attacker has access to both the source code of the program being executed and the interpreter, they may forge a call to \( g \) by constructing a valid code pointer.

4. Source-Based Reasoning about LINKS

In subsequent sections, Sections 5 and 6, we formalize the HTTP-based implementation described and attacked above, and also a simple cryptographic mechanism intended to protect against these attacks. We aim not just to show that a few specific attacks fail, but to show that the cryptography protects whole classes of properties provable at the source-level.

The purpose of this section is to define an exemplary source-based analysis that is preserved by the secure translation. We describe a dependent type-and-effect system for proving the assertion-based safety properties described in Section 2, that whenever an assertion \( \text{assert} L \) occurs in an execution, there is a previous occurrence of an event \( \text{event} L \). Data integrity and control integrity properties, such as those attacked in the previous section, are provable within our system.

4.1 A Type-and-Effect System

The design of our type-and-effect system is inspired by a simple system for typing correspondences in a process calculus (Gordon and Jeffrey 2003); we expect our results could be extended to more sophisticated program analyses or logics. For the sake of a simple presentation, our system lacks parametric polymorphism, a feature of LINKS itself, but it could easily be added.

The syntax of types and effects is as follows. The intention is that a type describes a value, and a type-and-effect describes an expression.

**Syntax of Types, Effects, and Environments:**

\[
\begin{align*}
F & ::= L_1, \ldots, L_m & \text{Effect: a set of events} \\
W & ::= \{x:T\}F & \text{(monadic) Type-Effect} \\
P & ::= \{x_1:T_1, \ldots, x_n:T_n\}F & \text{polymadic Type-Effect} \\
B & ::= \text{unit} | \text{int} | \text{string} | \text{xml} & \text{Base Types} \\
S, T, H & ::= B & \text{Types} \\
B & ::= \text{base type} \\
[T] & ::= \text{list} \\
T_1 \times \cdots \times T_n & ::= \text{tuple} \\
P & \rightarrow W & \text{polymadic function}
\end{align*}
\]
Types consist of base types, lists, tuples and function types. A type-and-effect expression is formed by a sequence of monomorphic types along with an effect. Intuitively, it captures the evaluation properties of expression $E$ which may have the observable effect in $W$. In a (monadic or polyadic) type-and-effect expression $\langle \mathbf{x} ; T \rangle \{F\}$ a variable $\mathbf{x}$ is bound with scope $T_{i+1}, \ldots, T_n$ and $F$. In function types $\langle \mathbf{x} ; (T_1 \times \cdots \times T_m) \{F\} \rightarrow (x : T) \{F_2\} \rangle$ the variables $x_1, \ldots, x_n$ are bound with scope $F_1$ and $F_2$, whereas the variable $x$ is bound with scope $F$. An environment is a list of variables along with their associated types. We write $\text{dom} (\Gamma)$ for the domain of an environment and $\emptyset$ for the empty one.

The type-and-effect system consists of a set of inductively defined algorithmic judgments, relative to a typing environment, $\Gamma$, and an effect, $F$. Assigning a type-and-effect $W = \langle \mathbf{x} ; T \rangle \{F'\}$ to an expression means that, assuming that the set of events in $T$ have occurred, evaluation of the expression is safe, and if the expression yields a value $v$, it has type $T$, and afterwards we may assume the events in $F'$ have occurred. Hence, the effect $F$ is a precondition, a set of events assumed to have occurred before execution, and the effect $F'$ is a postcondition, a set of events safe to assume after execution. The rules are in bidirectional style (Pierce and Turner 1998) and correspond directly to our implementation.

Judgments:

\[
\begin{align*}
\Gamma \vdash \emptyset & \quad \text{\textbf{G is well-formed}} \\
\Gamma; F \vdash V \Downarrow T & \quad \text{\textbf{value } V \text{ synthesises output type } T} \\
\Gamma; F \vdash V \Updownarrow T & \quad \text{\textbf{value } V \text{ type-checks against input type}} \\
\Gamma; F \vdash E \Uparrow W & \quad \text{\textbf{expression } E \text{ synthesises output } W} \\
\Gamma; F \vdash E \Downarrow W & \quad \text{\textbf{expression } E \text{ type-checks against input } W} \\
\end{align*}
\]

The following tables contain the typing rules for the type-and-effect system.

Well-formed Environment: $\Gamma \vdash \emptyset$

\[
\begin{align*}
\begin{array}{c}
\text{(Env } \emptyset \text{)} \\
\emptyset \vdash \emptyset \\
\text{(Env Ext)} \\
\Gamma \vdash \emptyset \quad x \notin \text{dom}(\Gamma) \\
\Gamma \vdash x : T \vdash \emptyset \\
\end{array}
\end{align*}
\]

According to these rules, in a well-formed environment the variables in the domain of the environment are distinct and every variable occurring free in a type is mentioned in the domain.

The constructors in our language have a fixed arity and type. We formalize this by providing a relation with the relevant types.

Constructor Instances:

\[
c : (T_1, \ldots, T_n) \rightarrow T
\]

\[
\begin{align*}
\text{Nil : } & (\text{List}) \rightarrow T \\
\text{Cons : } & (T_1 \times \cdots \times T_n, T) \rightarrow T \\
\text{Zero : } & \text{int} \rightarrow T \\
\text{Succ : } & \text{int} \rightarrow \text{int} \\
\text{String : } & \text{string} \rightarrow \text{XML} \\
\text{Tuple : } & (T_1, \ldots, T_n) \rightarrow (T_1 \times \cdots \times T_n) \\
\text{Unit : } & () \rightarrow \text{unit} \\
\text{Elem : } & \{\text{string}, \text{XML}\} \rightarrow \text{XML} \\
\text{Text : } & \{\text{string}\} \rightarrow \text{XML}
\end{align*}
\]

Next, we present the synthesis and checking rules for values.

Algorithmic Typing Rules for Expressions (Synthesis):

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

By (T-Var), to type check a $\lambda$-abstractions against an arrow type, we ensure that the body of the abstraction typechecks against the result type of the arrow, in an extended environment with function arguments given the respective types from the arrow argument and the effect being extended with the corresponding effect from the type. By (T-Const-S), during type checking of a type constructor that has a polymorphic return type (Nil, Cons, Tuple), we can infer the source types and subsequently type check the applied values against this inferred type. By (T-Swap), the last rule type checking for values, turns the type checking problem into a type synthesis one. This saves duplication of inter-derivable rules in both type checking and the type synthesis definitions.

We present the algorithmic typing rules to associate expressions with types-and-effects.

Algorithmic Rules for Expressions (Synthesis):

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Var)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]

\[
\begin{align*}
\Gamma, F \vdash E \Downarrow W & \quad \text{(T-Swap)} \\
\Gamma \vdash \emptyset & \quad \text{fv} (F) \subseteq \text{dom}(\Gamma) \\
\Gamma' = \Gamma, x : T, \Gamma'' & \quad \Gamma \vdash x \Updownarrow T
\end{align*}
\]
The rule (T-Source) synthesises a type-and-effect W for an annotated expression by checking that the expression type checks against the source level annotation. Rule (T-Val) synthesises a type-and-effect by combining the synthesised type during type synthesis with the effect used as an assumption for the judgment. To synthesise a type for a switch expression we type check the value V against the result type of the constructor c. We then ensure that the expressions of both branches synthesise the same type-and-effect, which is the synthesised type of the entire expression. In the case of variable binding (T-Bind), we synthesise a type-and-effect for E₁. We then synthesise one for E₂ while extending the typing environment with a type for the bound variable and the overall effect with the effect of E₁. The rule (T-App) synthesises a type-and-effect from a polyadic function application. By (T-Get), the type for the get operation is always of type xml with an empty effect, provided that the embedded value is of type xml. By (T-Post), the post operation always has type xml with an empty effect, provided that the values associated with the submission labels are of type string and the embedded value of type xml. The rules (T-Event) for event L and (T-Assert) for assert L are the same, except that (T-Assert) requires L ∈ F, where F is the precondition on the judgment.

### Algorithmic Rules for Expressions (Checking):

\[ \Gamma; F \vdash E \xrightarrow{\text{syn}} W \]

(T-Bind)
\[ \Gamma; F \vdash E₁ \xrightarrow{\text{syn}} \langle x; T₁ \rangle \{ F₁ \} \quad \Gamma; x; T₁; F₁; F₂ \vdash E₂ \xrightarrow{\text{syn}} W \quad x \notin \text{fv}(W) \]

(T-App)
\[ \Gamma; F \vdash U \xrightarrow{\text{syn}} T \quad T = \langle x₁; T₁ \ldots xₙ; Tₙ \rangle \{ F₁ \} \rightarrow W \quad T \text{ closed} \]
\[ \Gamma; F \vdash V₁ \xrightarrow{\text{syn}} T_i \quad \forall i \in 1..n \quad F₁[Vᵢ/x₁] \ldots [Vᵢ/xₙ] \subseteq F \]
\[ \Gamma; F \vdash U(V₁, \ldots, Vₙ) \xrightarrow{\text{syn}} W[V₁/x₁] \ldots [Vₙ/xₙ] \]

(T-Get)
\[ \Gamma; F \vdash V \xrightarrow{\text{syn}} \text{xml} \]
\[ \Gamma; F \vdash \text{get}(V) \xrightarrow{\text{syn}} \langle \_ : \text{xml} \rangle \{ \} \]

(T-Post)
\[ \Gamma; F \vdash V \xrightarrow{\text{syn}} \text{xml} \]
\[ \Gamma; F \vdash \langle \text{post}((a = V_i) \forall i \in 1..n, U) \rangle \xrightarrow{\text{syn}} \langle \_ : \text{xml} \rangle \{ \} \]

(T-Assert)
\[ \Gamma \vdash \text{assert } \langle T \rangle \xrightarrow{\text{syn}} \langle \_ : \text{xml} \rangle \{ \} \]

The idea is that a web application is a closed expression that yields a page of type xml, and that no assert involved in creating this page, or any subsequent page, may fail.

### 4.2 Expressing Data and Control Integrity with Assertions

Our working example, sale, consists of two pages; one is an offer to sell if the button is clicked and the other is confirmation of the sale at the pre-agreed price. The required security property is that, if the confirmation page is ever reached with a price, the same price was offered in the previous page. To express that, we add an event expression with the PricesIs event to the page making the offer for the item, and an assert expression with the same event in the confirmation page. We ask for is that, for all possible execution paths of this program, whenever an assert PricesIs(value) occurs, there is a previous occurrence of the event event PricesIs(price) with the arguments value and price being equal. The following figure shows concretely the annotated program that we use as input to our typechecker.

---

**Data Integrity with Assertions: Sale**

```latex
\text{sig} \text{buy} : \langle \text{value:int, dbpass:string} \rangle \{ \text{PricesIs(value)} \} \rightarrow \langle r: \text{xml} \rangle \{ \}
\text{fun} \text{buy(value, dbpass)} \text{server} \{ \text{assert} \text{PricesIs(value)}; \text{intToXml(value)} \# \text{omitting actual call to the database} \}
\text{sig} \text{sellAt} : \langle \text{price:int} \rangle \rightarrow \langle r: \text{xml} \rangle \{ \}
\text{fun} \text{sellAt(price)} \text{server} \{ \text{var} \text{dbpass} = "\text{secret}"; \text{event} \text{PricesIs(price)}; \text{<form} \text{onsubmit=\"(buy(price, dbpass))\" method=\"POST\">\text{<button} \text{type=\"submit\">Buy</button>\text{</form>}} \}
\text{sellAt(42)} \}
```

Similarly, the unreachable function example consists of two pages. The first page presents a link and the second one presents a message that the page was reachable. The required security property is that the additional function g declared in the source code in never called, despite being in scope inside the href expression. To express this property we assert an impossible event Unreachable() inside the body of the unreachable function. Since there is no corresponding event in the program and the function g is never called, the program typechecks correctly.

---

**Control Integrity with Assertions: Unreachable**

```latex
\text{fun} \text{page(s) server} \{ \text{var} \text{f = fun 0} \{ \langle<html> \text{A page with} \{ \text{intToXml(s)} \} \langle<html\rangle \}; \text{var} \text{g : \langle x:unit\rangle(\text{Unreachable()} \rightarrow \langle r: \text{xml} \rangle \{ \} \# \text{fun} 0 \{ \text{assert} \text{Unreachable()}\}; \text{<html> An unreachable page with} \{ \text{intToXml(s)} \} \langle<html\rangle \}; \text{<a href="(var u=g(f()))"}>Click for reachable page</a>\}
```

page(42)
If we change \( f() \) to \( g() \) inside the body of the \texttt{href}, then the program is no longer typeable (because the precondition on \( g() \) is not satisfied) and indeed no longer safe (because assert Unreachable() is reachable with no prior Unreachable() event)

5. A Semantics for the Standard Implementation
We give a semantics for the standard implementation of \textsc{Links} by translating a provably safe \textsc{TinyLinks} web application \texttt{Eart} to an F7 expression \([E_{\text{art}}]_a\).

5.1 Interlude: Refinement Types and Safety in F7
Saying \([E_{\text{art}}]_a\) is an F7 expression means that is a directly executable F# program, while also being an expression in the concurrent \(\lambda\)-calculus that underpins F7 (Bengtson et al. 2008). F7 allows any type to be refined with a formula of first-order logic; for example, the refinement type \((x : T)(C)\) consists of the values \(x\) of type \(T\) such that formula \(C\) holds (\(C\) may contain \(x\)).

The purpose of refinement types in F7 is to type check safety properties induced by \texttt{assume} C and \texttt{assert} C expressions, where \(C\) is a formula. An F7 expression is \textit{safe} if and only if, whenever \texttt{assert} C occurs in an execution, the formula \(C\) follows from a set \(C_1, \ldots, C_n\) of formulas where, for each \(i\), \(C_i\) has previously occurred in the execution. The \textit{safety-by-typing theorem} for F7 is that whenever a closed expression is well-typed, it is safe. The F7 typechecker makes use of an external theorem prover to ensure statically that each asserted formula will be provable. The F7 type system is rather more flexible than the one for \textsc{TinyLinks}, and hence we can directly interpret the \texttt{event} and \texttt{assert} expressions of \textsc{TinyLinks} using \texttt{assume} and \texttt{assert}.

5.2 Well-Typed Web Applications
We share as much functionality as possible between the standard semantics \([E_{\text{art}}]_a\), of this section, and the secure semantics \([E_{\text{art}}]_s\), explained in Section 6. The two translation algorithms are similar with the differences being mentioned in this section and explained in the next.

Throughout the two translations, we consider some fixed well-typed \textsc{TinyLinks} expression \texttt{Eart}, and a structure \(\mathcal{W} = (\texttt{Eart}, J, \mathcal{J})\). The expression \texttt{Eart} represents the main entry point to the web application; \texttt{Eart} is a closed expression of type xml. The set \(J\) identifies all functions, links, and forms occurring in \texttt{Eart}, together with their types and effects. The set \(\mathcal{J}\) records a distinct type constructor \texttt{Hf} for each member \(j \in J\); each \texttt{Hf} corresponds in the implementation to the hashed expression label for the expression part of \(J\) (recall Section 2.2).

Well-Typed Web Application: \(\mathcal{W} = (\texttt{Eart}, J, \mathcal{J})\)

There is a typing derivation \(\mathcal{D} : \emptyset \vdash \texttt{Eart} : \xi : \text{xml}\{1\}\) for \texttt{Eart}. Set \(J\) records all instances of \(\langle\text{Abs} \rangle\), \(\langle\text{Href} \rangle\), and \(\langle\text{Form} \rangle\) in the typing derivation; we have \(J \in J\) if and only if \(\Gamma; F : E \rightarrow W\) occurs in the typing derivation for \texttt{Eart} and \(J = (\Gamma; F; E; W)\). Set \(\mathcal{J} = \{\texttt{Hf} : J \in \mathcal{W}\}\) is a set of distinct constructor names.

As a shorthand for referring to the global typing derivation \(\mathcal{D}\), we sometimes write a subexpression of \texttt{Eart} with a type subscript to indicate the type assigned by \(\mathcal{D}\); for example, we may write \(U_T(V_1, \ldots, V_n)\) for an application where function \(U\) has type \(T\).

5.3 Modelling a Web Server hosting \textsc{Links}
We begin by formalizing the client’s view of a \textsc{Links}-based web application as a function type \((g, p)\) \texttt{webapp}, which sends HTTP requests to XML-encoded \(\textsc{HTML}\). The type parameters \(g\) and \(p\) refer to the type of continuations attached to \texttt{GET} and \texttt{POST} methods, as discussed in Section 2.2. In the standard implementation, the continuation types are algebraic types \texttt{linkclos} and \texttt{funclos} (given subsequently) representing possible closures of subexpressions of \texttt{Eart}. (In the next section, continuations are encrypted closures.)

(M1) Types for HTTP, XHTML, and Web Applications:

<table>
<thead>
<tr>
<th>Type</th>
<th>((g, p)) \texttt{req} =</th>
</tr>
</thead>
<tbody>
<tr>
<td>GET</td>
<td>\texttt{of } \texttt{g} option</td>
</tr>
<tr>
<td>POST</td>
<td>\texttt{of } \texttt{p} \ast \texttt{string list}</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Type</th>
<th>((g, p)) \texttt{xml} =</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elem</td>
<td>\texttt{of } \texttt{string } \ast \texttt{(g', p)} \texttt{xml list}</td>
</tr>
<tr>
<td>Text</td>
<td>\texttt{of } \texttt{string}</td>
</tr>
<tr>
<td>Href</td>
<td>\texttt{of } \texttt{g}</td>
</tr>
<tr>
<td>FormElem</td>
<td>\texttt{of } \texttt{p} \ast \texttt{string list}</td>
</tr>
</tbody>
</table>

\((g, p)\) \texttt{webapp} = \((\texttt{g}, \texttt{p})\) \texttt{req} \rightarrow (\texttt{g'}, \texttt{p}) \texttt{xml}

Values of type \((g, p)\) \texttt{xml} are abstract representations of XML (in fact, XHTML) web pages. A value \texttt{Elem}(s, \texttt{xs}) represents an XML element named \texttt{s}, with \texttt{children} \texttt{xs}. A value \texttt{Text}(\texttt{s}) represents actual text \texttt{s}. A value \texttt{Href}(\texttt{g}) represents an HTML link to a \textsc{TinyLinks} expression encoded by the continuation \texttt{g}. A value \texttt{FormElem}(\texttt{p}, \texttt{ls}) represents an HTML form, with parameters \texttt{ls}, and that when submitted produces a page from a \textsc{TinyLinks} expression encoded by the continuation \texttt{p}. (For full \textsc{Links} we would need a more accurate XML model, but this suffices for \textsc{TinyLinks}.)

The algebraic type \((g, p)\) \texttt{req} models HTTP requests. A message \texttt{Get}(\texttt{None}) is a GET for the main page, that is, the one obtained by evaluating \texttt{Eart}. A message \texttt{Get}(\texttt{Some}(\texttt{g})) is a GET for a page referenced by a link \texttt{Href}(\texttt{g}), that is itself contained within a previously obtained page, such as the main page. A message \texttt{Post}(\texttt{p}, \texttt{ls}) is a POST on a form \texttt{FormElem}(\texttt{p}, \texttt{ls}), filling in the values \texttt{xs} for the parameters \texttt{ls}. We can omit any explicit URL from these messages, as all the pages described by a web application \texttt{Eart} are at the same base URL on the same server.

5.4 The Standard Semantics
The translation algorithm proceeds as follows:

- The first step is to perform type-directed closure conversion on all the \(\lambda\)-abstractions, forms and links occurring in the source and generate suitable datatypes for representing them in F7.
- Generate mutually recursive function instances (\(Hf\)); each corresponding to the closures that were generated previously.
- Finally, translate the top level web server listener.

We begin with a translation of \textsc{TinyLinks} types and the generation of the following F7 types for closures: \texttt{funclos}_{p \ast W} has a constructor \texttt{Hf} for each \(\lambda\)-abstraction of type \(P \rightarrow W\) occurring in \texttt{Eart}; \texttt{formclos} has a constructor \texttt{Hf} for each \texttt{form}-expression occurring in \texttt{Eart}; and \texttt{linkclos} has a constructor \texttt{Hf} for each \texttt{form}-expression occurring in \texttt{Eart}.

Translation of Types, Effects, and Environments:

\[
\begin{align*}
\text{int} & = \text{int} \\
\text{string} & = \text{string} \\
\text{unit} & = \text{unit} \\
\text{xml} & = \langle\text{linkclos, funclos}\rangle\text{xml} \\
\text{[T]} & = \text{[T]}\text{list} \\
\text{[T]}_1 \times \cdots \times \text{[T]}_n & = \text{[T]}_1 \times \cdots \times \text{[T]}_n \\
\text{P} \rightarrow \text{W} & = \text{funclos}_{p \ast W} \\
\text{[x_1; T_1 \ldots x_n; T_n]} & = \text{[x_1; T_1]} \ast \cdots \ast \text{x_n; T_n]} \\
\text{[Γ]} & = \text{x_1; T_1 \ldots x_n; T_n} \\
\text{[Γ; F]} & = \text{x_1; T_1 \ast \cdots \ast x_n; T_n]} \\
\end{align*}
\]
(M2) Generated datatypes:

\[ \text{type funclos} \mapsto W = \sum \left\{ \lambda J : (\Gamma, F, (\lambda x_1, \ldots, x_n, E), P \rightarrow W) \land J \in \mathcal{J} \right\} \]

and formcloes = \[
\sum \left\{ \lambda J : (\Gamma, F, \text{formo}((f_1, \ldots, f_m), E), \text{xml}) \land J \in \mathcal{J} \right\}
\]

and linkcloes = \[
\sum \left\{ \lambda J : (\Gamma, F, \text{href}(E), \text{xml}) \land J \in \mathcal{J} \right\}
\]

We rely on F7 refinement types to record effects. We regard a TinyLinks effect \(F\) as an F7 formula: the conjunction of the formulas obtained by interpreting each event \(L = p(V_1, \ldots, V_n)\) in \(F\) as a predicate \(p\) with parameters \(V_1, \ldots, V_n\). The F7 translation \((x_1: [T_1], \ldots, x_n: [T_n]) \{F\}\) of a type-and-effect is an \(n\)-ary tuple refined with \(F\) treated as a formula. The F7 translation \([\Gamma; F]\) of an environment with a pre-condition is similar.

Next, we define the translation of values and expressions. When a value \(V\) is a \(\lambda\)-abstraction, link or form, we emit the data type constructor \(H_J\) where \(J\) is the typing judgment for \(V\); the constructor \(H_J\) corresponds to the hashed expression label for \(V\) in the actual implementation. The function \(\mathcal{C}[V]\) defines how each constructor takes a record argument representing the environment.

**Translation of Values:** \([V]\)

\[
\begin{align*}
[x] &= x \\
\text{Unit} &= () \\
\text{Zero} &= 0 \\
\text{Suc}(V) &= V + 1 \\
\text{Nil} &= \text{n}l \\
\text{Cons}(V, V') &= V :: [V'] \\
\text{Tuple}(V_1, \ldots, V_n) &= [V_1, \ldots, V_n] \\
\text{c}(V_1, \ldots, V_n) &= \text{c}(V_1, \ldots, V_n) \\
\text{hreff}(E) &= \text{hreff}(E) \\
\text{form}(f_1, \ldots, f_n, E) &= \text{FormElem}(\text{form}((f_1, \ldots, f_n), E), (f_1, \ldots, f_n)) \\
\end{align*}
\]

The translation of expressions \([E]\) for \(J = ((x; U_i)^{e_1, n}, F, V, T) \land J \in \mathcal{J}\)

\[
\begin{align*}
\mathcal{E}[V] &= [V] \\
\mathcal{E}[\text{var} x := E_1; E_2] &= \text{let } x = \mathcal{E}[E_1] \text{ in } \mathcal{E}[E_2] \\
\mathcal{E}[g(U_1, \ldots, U_n)] &= g[U_1] \ldots [U_n] \\
\mathcal{E}[\text{let } x = E_1 \text{ in } \text{(match } x \text{ with } \sum \left\{ \lambda J : (\Gamma, F, \text{href}(E), \text{xml}) \land J \in \mathcal{J} \right\} \right\} \left\{ \lambda J : (\Gamma, F, \text{form}(f_1, \ldots, f_n, E), \text{xml}) \land J \in \mathcal{J} \right\} \right\} \\
\mathcal{E}[\text{match } V \text{ with } \sum \left\{ \lambda J : (\Gamma, F, \text{href}(E), \text{xml}) \land J \in \mathcal{J} \right\} \right\} \\
\mathcal{E}[\text{if } c(x_1, \ldots, x_n) \rightarrow E_1 \text{ else } E_2] &= \text{switch}(V) \left\{ \begin{array}{ll}
\text{case } c(x_1, \ldots, x_n) \rightarrow E_1 \\
\text{case } E_2 \\
\end{array} \right. \\
\mathcal{E}[\text{hreff}(E)] &= \text{match } V \text{ with } \text{hreff}(E) \rightarrow \text{webserver}(\text{Get}(\text{Some}(E))) \\
\mathcal{E}[\text{post}(f_1, \ldots, f_n, U)] &= \text{match } V \text{ with } \text{FormElem}(f_1, f_2) \rightarrow \text{webserver}(\text{Post}(f_1, [U])^{e_1, n}) \\
\mathcal{E}[\text{event } L] &= \text{assert } L \\
\mathcal{E}[\text{assert } L] &= \text{assert } L
\end{align*}
\]

The translation of expressions assumes the following functions \(f_H\), for unpacking and evaluating closures, and also a top-level function webserver defined below.

**Translation from \([E_{url}]\) to \([E_{url}]\) in F7:**

Let \([E_{url}]\) be the F7 module obtained from \(E_{url}\) by concatenating the type and function definitions displayed previously: (M1) fixed datatypes; (M2) generated datatypes; (M3) generated functions; (M4) top-level webserver function. Let the interface of the module be: \(\text{val webserver : (linkcloes, formcloes)webapp}\).

**Lemma 1.** If \(E_{url}\) is provably safe then \([E_{url}]\) is a closed expression of F7 of type: \([E_{url}]\)(linkcloes, formcloes)webapp.

**Theorem 1.** If \(E_{url}\) is provably safe at the source level, then the (standard) webserver \([E_{url}]\) is safe.
6. Semantics of a Secure Implementation

Of course, it is naïve to imagine that your opponent across the network is so polite as to obey typing rules. A better model of a potentially untrustworthy HTTP-level client in F7 is as an arbitrary (not necessarily well-typed) expression context (as in the spi calculus (Abadi and Gordon 1999) and subsequent work). Although our semantics \([E_{url}]\) abstracts some low level details, we still can express each of the attacks from Section 3 as untyped F7 contexts.

This section formalizes our use of cryptography to protect against these attacks, and establishes our main result, that the secured model \([E_{url}]\) is safe even when placed in an untyped context.

6.1 Interlude: Public Types and Robust Safety in F7

Let an opponent be an arbitrary F7 expression context. We say an F7 expression is robustly safe if it is safe whenever it is placed within any opponent context. A significant result concerning F7 is the robust-safety-by-typing theorem: that a closed well-typed expression is robustly safe, provided its type satisfies conditions for being public. A function type is public, roughly, when there are no non-trivial preconditions (refinements) on its arguments. We cannot expect an untyped context to respect such preconditions. In particular, the function type (linkclos,formclos)webapp is not public, because of the refinements on types for the constructors \(H_{1}\) of linkclos and formclos. The attacks (2) and (3) can be seen as an attacker failing to respect the integrity constraints expressed by these refinements.

6.2 Protecting Continuations with Authenticated Encryption

The make and check functions, to construct and deconstruct the authenticated encryption of a continuation, are programmed as follows in F7. If a continuation is modified, the call to check will fail; in particular, the call to hmacsha1Verify will raise an exception.

**Authenticated Encryption:**

```plaintext
let mkKey: unit → 'a symkey = Crypto.mkEncKey // encryption key
let mkHKey: unit → 'a hkey = Crypto.mkHKey // hashing key

let make (ek: (hmac * 'a) symkey) (hk: 'a hkey) (s: 'a): cipher =
    aesEncrypt ek (pickl hmac hk (pickl s) s)

let check (ek: (hmac * 'a) symkey) (hk: 'a hkey) (m: cipher): 'a =
    let hs = unpickle aesDecrypt ek m in
    let sv = hmacsha1Verify hk (pickl s) h in s

let tHKey: linkclos hkey = mkHKey()
let fHKey: formclos hkey = mkHKey()
let lSKey: (hmac * linkclos) symkey = mkKey()
let fSKey: (hmac * formclos) symkey = mkKey()
```

Key management is a concern in the case of different versions of the same application or for long running applications. When a new version is deployed, the keys should be refreshed to prevent confusion between versions. For long-lived keys, we can encrypt new pages with a new key, but we retain the old keys to decrypt old pages.

6.3 The Secure Semantics

The following table describes the changes to the definitions of the previous section to obtain our formal model \([E_{url}]\) of the secure translation. The modifications are to the translation of the xml type, the translation of href and form values, and the top-level web server listener.

**Modifications for the Secure Translation:**

\[
[E_{url}]_s = (cipher, cipher)xml
\]

\[
 hinges(E) = \begin{cases} 
 \text{let ciphertext = make lSKey lHKey (Hhref(E)) in Hhref(cipher),} \\
 \text{form([f1, ..., fn], E) = \} \\
 \text{let ciphertext = make fSKey fHKey \{ \text{form([f1, ..., fn], E) in FormElement(cipher, [f1, ..., fn])} \}} 
\end{cases}
\]

\[
\text{let webserver (req: (cipher, cipher)req) \rightarrow (cipher, cipher)xml = match req with} \\
\text{Get(None) \rightarrow E[E_{url}]} \\
\text{Get(Some(cipher)) \rightarrow \} \\
\text{match (check lSKey HKey cipher) with} \\
\text{\{f \in \text{\}} in J.f href(E, T) \} \\
\text{match (check fSKey fHKey cipher) \{f \in \} with} \\
\text{\{h \in \} in J.h form([f1, ..., fn], E, T) \} \\
\text{\} \} \}
\]

The encryption occurs during the translation of the href and form, the values which construct continuations that may flow to the potential opponent. The code to dispatch on incoming requests in a webserver is the same as before, except that the encrypted continuations need to be decrypted.

The function type (cipher,cipher)webapp is public, because there are no refinement types in its argument type. (None of the continuations in the argument (cipher,cipher)req are acted upon until they have been dynamically validated by the cryptographic operations used by the check function. In F7, the type cipher of byte arrays acts somewhat like a dynamic type.) Hence, our main theorem is a corollary, given the robust-safety-by-typing theorem of F7, of Lemma 2.

**Lemma 2.** Suppose that \(\emptyset;\emptyset \vdash E_{url} \{ xml \}. \) Then \([E_{url}]_s\) is a closed expression of F7 of type: \([E_{url}]_s\) is a closed expression of F7 of type: \(cipher, cipher)webapp\.

**Theorem 2.** If \(E_{url}\) is provably safe at the source level, then the (secure) webserver \([E_{url}]_s\) is robustly safe.

The secure implementation is independent of any specific integrity properties proved at the source level; the same implementation works for all provable properties.

7. Implementations

Our implementations consist of a modification to the Edinburgh LINKS system to support our secure compilation strategy, a type checker corresponding to the system presented in Section 4, and a compiler implementing the straightforward and secure translation rules from Section 5 and Section 6.
7.1 Modifications to the Edinburgh LINKS System

The Edinburgh LINKS system is written in Objective Caml and consists of an interpreter that is called from a web server as a CGI program to process GET or POST requests. For our modifications we used the latest public release of the system which is version 0.4. To implement our solution based on cryptography, we used the Cryptokit library for OCaml which provides a variety of cryptographic primitives to implement security-sensitive applications.

The LINKS system defines clear interfaces between the interpreting loop and the marshalling and unmarshalling of requests and results, which are all collected in the Result module. Our modification amounts to extending the functions responsible for marshalling and unmarshalling continuations, expressions and environments, by adding a call to our custom authenticated encryption and decryption functions between the pickling, and the base64 encoding/decoding stages. Since our implementation requires only local modifications in a single module, we anticipate these changes are applicable to later versions of the system (including SELINKS system (Swamy et al. 2008)). As a basic validation, we tested that our original attacks on the modified system are no longer realisable.

7.2 A Certified (But Symbolic) Implementation of LINKS

There are always discrepancies of some sort between formal calculi like TINYLINKS and actual programming languages; we have implemented our results so as to validate them experimentally as well as theoretically. Our source level analysis is implemented in a certifying compiler, that, given a program with a security policy expressed by source level type annotations, checks that the program satisfies the particular policy, and not only produces executable F# code using the secure translation, but also produces machine checkable evidence that the translated code respects the policy.

The TINYLINKS implementation consists of 4500 lines of F# code divided between the parser, the type checker and the compiler. While we could have used the Edinburgh LINKS code as a basis, we chose not to do so for two reasons: (1) we want to understand better the security related details and abstract away from the complexity of the language implementation, (2) we intend to study the effect of language features to security in isolation, and progressively combine them with other novel language features.

The certified compiler works in two phases; the compilation phase and the verification phase. The compilation phase takes a TINYLINKS program that contains type-and-effect annotations, event, and assert, expressing the required security property, type checks it and produces an F# program along with an F7 interface as output. For the verification phase, we employ a type checker with refinement types (F7), that is part of the trusted computing base, to automatically check the certificate. Having executable formal semantics for LINKS gives us the opportunity for a fully interoperable but certified web server using the resulting F# program as a concrete implementation in a web server. Currently our translation cannot communicate with a browser but is a promising direction for further work.

8. Related Work

\( \lambda \)-calculi with locations.\ The technique we developed for LINKS programs can also be applied to other multi-tier languages to protect the application state.

HOP (Serrano et al. 2006) is a language similar to LINKS that uses a stratified approach in writing interactive applications across the web. It defines two strata: the computational one that carries out the computations of the graphical user interface. As in LINKS, the compiler transforms expressions in forms or links into CPS and closure converts them. These continuations can float freely between the client and the server and are not encrypted.

Neubauer and Thiemann (2005) propose a programming framework consisting of a calculus, a static analysis that performs an assignment of code to locations, and a range of program transformations that automatically insert communication primitives, perform resource pooling and finally split the program into separate processes to run at separate locations.

The implementation of the PLT Scheme Web Server (Krishnamurthi et al. 2007), provides web-specific core primitives for writing applications that are able to interact with a database. The main contribution is the advanced control flow mechanisms that are exposed through the core primitives. Actual continuations are stored on the server, and only continuation identifiers are shipped to the client, with their corresponding threads being suspended, waiting for input on a channel.

ML5 (Murphy VII et al. 2008) extends the HOP approach to a fully distributed multi-tier language focusing on mobility, and develops a type system that ensures that mobile resources are used in a type safe manner. The implementation shares several of the ideas (CPS, closure conversion) used in LINKS and HOP, but there is no explicit study of protection against a rogue client.

Security for multi-tier languages.\ The closest work to ours is SELINKS (Swamy et al. 2008), an enhancement of LINKS with user-defined label-based security policies. SELINKS expands on the original goal of LINKS by allowing the web server and the database to collaboratively enforce application specific security policies. The security strategy of SELINKS relies on a trusted database tier. The SELINKS type system ensures that labelled data can never flow to client code (to address secrecy) and also that labelled data cannot be created on the client (to address integrity). In contrast, the security strategy of this paper relies on cryptography to protect the secrecy and integrity of encrypted data stored on the untrusted client. A shortcoming of our work compared to SELINKS is that we do not support the database tier. On the other hand, our use of cryptography supports a programming style where trusted or secret data can be offloaded onto the client. The SELINKS security policy would forbid this programming style, unless no security policy is applied, in which case the attacks that we have described on the original Edinburgh version would still apply. Clearly, a combination of our security strategies would be beneficial.

Swift (Chong et al. 2007) uses Java and GWT to write web applications expressing integrity and confidentiality properties as type annotations. The compiler statically analyses these annotations and decides where data and code will be placed to guarantee the security constraints. Location annotations are at the statement level and subexpressions of a compound expression are allowed to execute at different hosts. To ensure control flow integrity, the client and the server runtime systems maintain a stack of closures that communicate with each other with control transfer messages. A client is not allowed to execute a high integrity closure, unless it was pushed from the server and it happens to be at the top of the closure stack. The server checks that these conditions hold and can detect violations.

Source-level security by target-level cryptographic typing.\ There are a few similar approaches where high level security properties are preserved through a translation to a lower-level target language that uses cryptography. Gordon and Pucaella (2005) show via a typed translation to the spi-calculus that a cryptographic implementation of a SOAP-based secure RPC mechanism correctly authenticates web service requests and responses. In the context of a distributed cryptographic implementation for an asynchronous \( \pi \)-calculus, Abadi et al. (2006) obtain computational secrecy guarantees by translating to a language with concrete cryptographic prim-
9. Conclusion

We have obtained practical and theoretical results demonstrating that it is possible to perform source-based security analysis in a multi-tier web programming language. In the context of TINYLINKS, we have formalized an example type-and-effect system that can guarantee data and control flow integrity properties of programs. Our results show that through a secure, type-directed translation we can ensure that properties proved at the source level are preserved by the actual implementation. To further validate our approach, we have implemented both a type-and-effect checker and our secure translation producing executable semantics in F#, that can form part of a certified web server.

In future work, we intend to extend our results to support server-side state and client-side functions. Additionally, we intend to extend our compiler and the theoretical framework developed in this paper to handle secrecy properties.

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