

SWIFT MAC Protocol: HOL Specification

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June 12, 2006

Abstract

This document is typeset from a HOL specification. Further details of the model described in this document can be found in the paper “Rigorous Protocol Design in Practice: An Optical Packet-Switch MAC in HOL”, available on the web at <http://www.cl.cam.ac.uk/users/pes20/optical/root.pdf>.

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Chapter 1

Basic Types and Definitions

1.1 Types

1.1.1 Summary

type_abbrev_mac
type_abbrev_port
type_abbrev_pingid
type_abbrev_fabric_state
type_abbrev_data

1.1.2 Rules

```
— :  
type_abbrev mac : word16
```

```
— :  
type_abbrev port : word16
```


– :
type_abbrev *pingid* : *word32*

– :
type_abbrev *fabric_state* : (port#port)set

– :
type_abbrev *data* : string

1.2 Continuous Time

1.2.1 Summary

type_abbrev_time
NSEC
USEC
MSEC
SEC

1.2.2 Rules

– :
type_abbrev *time* : *real*

– :
(NSEC : time) = 1/1000000000

Rule version:

REMOVE1

3

|

|

– :
(USEC : time) = 1/1000000

|

|

– :
(MSEC : time) = 1/1000

|

|

– :
(SEC : time) = 1

|

1.3 Library Functions

1.3.1 Summary

INTERVAL
REMOVE1

1.3.2 Rules

|

– :
 $\text{INTERVAL}(\text{lower} : \text{time}, \text{upper}) = \{x \mid \text{lower} \leq x \wedge x \leq \text{upper}\}$

|

|

Rule version:

```

- :
(REMOVE1 x[] = []) ^
(REMOVE1 x(CONS y ys) = if x = y then ys else REMOVE1 x ys)

```

1.4 Parameters

1.4.1 Summary

```

TRANSMISSION_TIME
SLOP_TIME
MIN_PING_REUSE_TIME
CONNECTED_PING_REPEAT_TIME
UNCONNECTED_PING_REPEAT_TIME
MAX_HOST_THINKING_TIME
ARBITER_WRITEOFF_TIME
REQUEST_REISSUE_TIME
TIMER_GRAININESS

```

1.4.2 Rules

```

- :
TRANSMISSION_TIME = 9 * USEC

```

Description The time taken for a packet of data to pass through the switch.

```

- :
SLOP_TIME = 500 * NSEC

```

Description

The fabric state is guaranteed by the arbiter for at least a period of $\text{TRANSMISSION_TIME} + 2 * \text{SLOP_TIME}$.

Rule version:

– :
MIN_PING_REUSE_TIME : time = 0 * NSEC

Description The amount of time which must pass before a pingid can be reused on the same port.

– :
CONNECTED_PING_REPEAT_TIME = 10 * MSEC

Description The interval between pings sent to a host which the arbiter believes is connected.

– :
UNCONNECTED_PING_REPEAT_TIME = 10 * USEC

Description The interval between 'speculative' pings sent to a port on which the arbiter does not know of a host.

– :
MAX_HOST_THINKING_TIME = 200 * NSEC

Description The maximum 'logic delay' before a host responds to a ping or data-grant message.

– :
ARBITER_WRITEOFF_TIME : time = 100 * MSEC

Description The amount of time which must pass for a host without a ping arriving before the host decides to assume the arbiter has crashed.

– :
REQUEST_REISSUE_TIME = 500 * USEC

Description The amount of time which must pass before a host retransmits a data-request on the assumption that it previously got lost.

– :
TIMER_GRAININESS = 200 * NSEC

Description This is the maximum time which can elapse between when a timer should go off and when it actually does go off (on the next clock cycle).

Chapter 2

Arbiter/ Arbiter

2.1 Messages, Labels

2.1.1 Summary

a2h_msg
h2a_msg
type_abbrev_arbiter_trace

2.1.2 Rules

```
— :  
a2h_msg =  
  A2H_DATA_GRANT of mac  
| A2H_PING of pingid  
| A2H_MAC_GRANT of mac  
| A2H_MASTER_IS of mac
```

```
— :  
h2a_msg =  
  H2A_DATA_REQUEST of mac  
| H2A_PONG of pingid
```

```
| H2A_MAC_REQUEST(* no info needed *)
| H2A_WHO_IS_MASTER
```

```
– :
type_abbrev arbiter_trace : num → arbiter_label
```

2.2 Functions on Traces

2.2.1 Summary

```
a_time
a_fabric
!
a_last_ping
a_rtt_estimate
```

2.2.2 Rules

```
– :
(a_time(t : arbiter_trace)(0 : num) = (0 : time)) ∧
(a_time t(SUC n) =
  let d = (case (t n) of A_DUR x → x || _ → 0) in
  d + a_time t n)
```

```
– :
(a_fabric t 0 = {}) ∧
(a_fabric t(SUC n) = case (t n) of A_FABRIC fs → fs || _ → a_fabric t n)
```

Rule version:

```

- :
(∀t.port_of_mac(t : arbiter_trace)0 = ∅) ∧
(∀t m.port_of_mac t(SUC m) =
  let oldmap = port_of_mac t m in
  case t m of
    A_DARK p1 → rrestrict oldmap(λp.¬(p = p1))
  || A_A2H(p2, A2H_MAC_GRANT mac) → oldmap ⊕ (mac ↦ p2)
  || _ → let pings_timed_out = λp.p ∈ rng(oldmap) ∧ F in
    rrestrict oldmap(λp.¬pings_timed_out p))

```

```

- :
(a_last_ping t id 0 = *) ∧
(a_last_ping t id(SUC m) = (case t m of
  A_A2H(p, A2H_PING id') → (case id' = id of T → ↑ m || F → a_last_ping t id m)
  || _ → a_last_ping t id m))

```

```

- :
(* rtt_estimate is calculated per port (arbiter-host connection) and id by keeping a record of the last
PING sent *)
(* N.B. PING and PONG messages are identified by pingid not by port *)

(a_rtt_estimate t p 0 = *) ∧
(a_rtt_estimate t p(SUC m) = (case (t m) of
  A_H2A(p', H2A_PONG id) → (if p' = p
    then (case (a_last_ping t id m) of ↑ m' → ↑(a_time t m - a_time t m') || * → *)
    else a_rtt_estimate t p m)
  || _ → a_rtt_estimate t p m))

```

2.3 Specification

2.3.1 Summary

grants_correctly_arbitered
starts_pinging
continues_pinging
pings_correctly_spaced

Rule version:

pingids_not_reused_too_soon
data_requests_get_granted
only_talk_to_ports_with_macs
one_mac_per_port
mac_requests_are_granted
one_port_per_mac
slots_not_wasted
arbiter_spec

2.3.2 Rules

– :
 grants_correctly_arbitered $t =$

$\forall n \text{ } psrc \text{ } mac.$
 $(t \ n = A_A2H(psrc, A2H_DATA_GRANT \ mac)) \implies$
let $rtt_est = a_rtt_estimate \ t \ psrc \ n$ **in**
case rtt_est **of** $* \rightarrow \mathbf{F} \parallel \uparrow rtt \rightarrow$
 $mac \in \mathbf{dom}((port_of_mac \ t \ n)) \wedge$
let $pdst = (port_of_mac \ t \ n)[mac]$ **in**
let $tn = a_time \ t \ n$ **in**
let $low_time = tn + \max(rtt - SLOP_TIME)0$ **in**
let $high_time =$
 $tn + rtt + TRANSMISSION_TIME + SLOP_TIME$ **in**
 $\exists low \ high. a_time \ t \ low \leq low_time \wedge$
 $high_time \leq a_time \ t \ high \wedge$
 $\forall n. low \leq n \wedge n \leq high \implies (psrc, pdst) \in a_fabric \ t \ n$

– :
 starts_pinging_ports($t : arbiter_trace$) =

$\forall p. \mathbf{mem} \ p \ ports \implies$
 $\exists n \ pingid. (t \ n = A_A2H(p, A2H_PING \ pingid)) \wedge$
 $a_time \ t \ n \leq UNCONNECTED_PING_REPEAT_TIME$

Rule version:

- :

continues_pinging $t =$

(* the arbiter repeatedly pings all ports, as long as time increases *)
 $(\forall n p.$
 $(\exists pingid.t n = A_A2H(p, A2H_PING pingid)) \wedge$
 $(\exists n'.n < n' \wedge$
 $(max CONNECTED_PING_REPEAT_TIME UNCONNECTED_PING_REPEAT_TIME) +$
 $TIMER_GRAININESS \leq a_time t n' - a_time t n) \implies$
 $(\exists n'.n < n' \wedge (\exists pingid.t n' = A_A2H(p, A2H_PING pingid))))$

- :

pings_correctly_spaced $t =$

(* the interval between consecutive pings on a given port is determined by the arbiter's view of the status of the host on that port *)
 $(\forall n n' p pingid pingid'.$
 $n < n' \wedge$
 $(t n = A_A2H(p, A2H_PING pingid)) \wedge$
 $(t n' = A_A2H(p, A2H_PING pingid')) \wedge$
 $(\forall m.n < m \wedge m < n' \implies \neg \exists pingid''.t m = A_A2H(p, A2H_PING pingid'')) \implies$
let $port_connected_n = p \in \mathbf{rng}((port_of_mac t n))$ **in**
let $port_connected_n' = p \in \mathbf{rng}((port_of_mac t n'))$ **in**
let $port_connected_agree = (port_connected_n = port_connected_n')$ **in**
let $delta = (a_time t n' - a_time t n)$ **in**
if $port_connected_agree$ **then** (
 (* note that it may be possible to change connectedness twice between n and n' *)
let $ping_period = (\mathbf{if} port_connected_n$
 then $CONNECTED_PING_REPEAT_TIME$
 else $UNCONNECTED_PING_REPEAT_TIME)$ **in**
 $delta \in \mathbf{INTERVAL}(ping_period, ping_period + \mathbf{TIMER_GRAININESS})$
else $delta < (max CONNECTED_PING_REPEAT_TIME$
 $UNCONNECTED_PING_REPEAT_TIME)$
 $+ \mathbf{TIMER_GRAININESS})$

- :

pingids_not_reused_too_soon $t =$

(* the arbiter does not reuse pingids within MIN_PING_REUSE_TIME *)
 (* don't reuse pingids too much - in some long time interval, don't reuse the same ping id for the same port... *)

(* N.B. this doesn't notice whether the port has gone dark in the intervening time, or whether hosts disconnect and reconnect *)

$$\begin{aligned}
 & (\forall n \ p \ p' \ pingid \ n'. \\
 & \quad (t \ n = A_A2H(p, A2H_PING(pingid))) \wedge \\
 & \quad (t \ n' = A_A2H(p', A2H_PING(pingid))) \wedge \\
 & \quad (n' > n) \\
 & \quad \implies \\
 & \quad a_time \ t \ n' - a_time \ t \ n \geq MIN_PING_REUSE_TIME)
 \end{aligned}$$

— :
data_requests_get_granted $t =$

(* if the arbiter receives a request, it eventually sends a grant *)
 $\forall n \ p \ mac.$
 $(t \ n = A_H2A(p, H2A_DATA_REQUEST \ mac)) \wedge$
 $(mac \in \mathbf{dom}((port_of_mac \ t \ n)))$
 \implies
 $\exists m. m > n \wedge (t \ m = A_A2H(p, A2H_DATA_GRANT \ mac))$

— :
only_talk_to_ports_with_macs $t =$

(* the arbiter does not send anything (except mac-grants and pings) to ports with no assigned mac *)
 $(\forall n \ p \ msg.$
 $(t \ n = A_A2H(p, msg)) \wedge$
 $\neg(\exists mac. msg = A2H_MAC_GRANT \ mac) \wedge$
 $\neg(\exists pingid. msg = A2H_PING \ pingid)$
 \implies
 $p \in \mathbf{rng}((port_of_mac \ t \ n)))$

— :
one_mac_per_port($t : \text{arbiter_trace}$) =

(* the arbiter does not send two conflicting macs to the same port without a mac-request or a dark or a timeout on a series of pings inbetween *)

Rule version:

$$\begin{aligned}
& (\forall p. \forall n \text{ mac } n' \text{ mac}'. \\
& \quad (t \ n = \text{A_A2H}(p, \text{A2H_MAC_GRANT } \text{mac})) \wedge \\
& \quad (t \ n' = \text{A_A2H}(p, \text{A2H_MAC_GRANT } \text{mac}')) \wedge \\
& \quad (n < n') \wedge \\
& \quad \neg(\text{mac} = \text{mac}') \\
& \quad \implies \\
& \quad \exists n'' . n < n'' \wedge \\
& \quad \quad n'' < n' \wedge \\
& \quad \quad ((t \ n'' = \text{A_H2A}(p, \text{H2A_MAC_REQUEST})) \vee \\
& \quad \quad (t \ n'' = \text{A_DARK}(p))) \vee \\
& \quad \quad (* \text{ Placeholder for timeout on a series of pings between } n \text{ and } n'. *) \\
& \quad \mathbf{F}))
\end{aligned}$$

$$\begin{aligned}
- : \\
\text{mac_requests_are_granted}(t : \text{arbiter_trace}) = \\
(* \text{ if the arbiter receives a mac request, it eventually sends a grant } *) \\
(\forall n \ p. (t \ n = \text{A_H2A}(p, \text{H2A_MAC_REQUEST})) \implies \\
\quad \exists n' \ \text{mac}. n' > n \wedge \\
\quad (t \ n' = \text{A_A2H}(p, \text{A2H_MAC_GRANT } \text{mac})))
\end{aligned}$$

$$\begin{aligned}
- : \\
\text{one_port_per_mac } t = \\
(* \text{ the arbiter never assigns the same mac to more than one port } *) \\
(\forall n \ p \ \text{mac}. \\
(t \ n = \text{A_A2H}(p, \text{A2H_MAC_GRANT } \text{mac})) \wedge \\
\text{mac} \in \mathbf{dom}((\text{port_of_mac } t \ n)) \\
\implies ((\text{port_of_mac } t \ n[\text{mac}]) = p))
\end{aligned}$$

$$\begin{aligned}
- : \\
\text{slots_not_wasted} = \mathbf{T} \ (* \text{ performance concern: if you have any pending requests, grant at least one in} \\
\text{each slot - want to think about this, since the spec doesn't yet enforce the notion} \\
\text{of slot-based grant allocation } *)
\end{aligned}$$

```
– :  
arbiter_spec ports(t : arbiter_trace) =  
  
grants_correctly_arbitered t ∧  
starts_pinging ports t ∧  
continues_pinging t ∧  
pings_correctly_spaced t ∧  
pingids_not_reused_too_soon t ∧  
data_requests_get_granted t ∧  
only_talk_to_ports_with_macs t ∧  
one_mac_per_port t ∧  
mac_requests_are_granted t ∧  
one_port_per_mac t
```

Chapter 3

Hosts

3.1 Messages, Labels

3.1.1 Summary

h_lbl
type_abbrev_host_trace

3.1.2 Rules

```

- :
h_lbl =
  H_TAU
  | H_DUR of time
  | H_DARK
  | H_A2H of a2h_msg
  | H_H2A of h2a_msg
  | H_D2H of d2h_msg
  | H_H2D of h2d_msg
  | H_H2S of h2s_msg(* N.B. implementations will probably ignore the MAC FIXME do we want MAC here? *)
  | H_S2H of s2h_msg

```

```

- :
type_abbrev host_trace : num → h_lbl

```

3.2 Functions on Traces

3.2.1 Summary

<i>host_mac</i>	
<i>h_time</i>	
<i>mac_of_data</i>	
<i>pending_output</i>	
<i>h_wedged</i>	identifies when the dataplane should think that the host is wedged

3.2.2 Rules

```

- :
(host_mac t 0 = *) ∧
(host_mac t(SUC n) = (let mac = host_mac t n in
  case t n of
    H_TAU → mac
  || H_DUR d → mac
  || H_DARK → * (* already covered by H2D_WEDGED *)
  || H_A2H om → (case om of
    A2H_MAC_GRANT mac' → ↑ mac'
  || _x90 → mac)
  || H_H2A im → mac
  || H_D2H d2h_msg → (case d2h_msg of
    D2H_INVALIDATE_MY_MAC → *
  || _ → mac)
  || H_H2D h2d_msg → (case h2d_msg of
    H2D_WEDGED → *
  || _x89 → mac)
  || H_H2S _1 → mac
  || H_S2H _2 → mac
  ))

```

```

- :
(h_time t(0 : num) = (0 : time)) ∧
(h_time t(SUC n) = (let d = (case (t n) of H_DUR x → x || _ → 0) in
                        d + h_time t n))

```

```

- :
(mac_of_data t 0 = ARB) ∧
(mac_of_data t(SUC n) =
  case t n of (H_A2H(A2H_DATA_GRANT mac)) → mac || _ → mac_of_data t n)

```

```

- :
(pending_output(t : host_trace)mac 0 = []) ∧
(pending_output(t : host_trace)mac(SUC n) =
let pending_output = (pending_output t mac n) in
case t n of
  H_D2H(D2H_SEND(mac', data)) → if mac' = mac
    then pending_output ++ [data] else pending_output
  || H_H2S(H2S_DATA data) → if mac_of_data t n = mac
    then TL pending_output else pending_output
  || H_DARK → []
  || _ → pending_output)

```

```

- identifies when the dataplane should think that the host is wedged :
(h_wedged t 0 = F) ∧
(h_wedged t(SUC n) =
let wedged = h_wedged t n in
case t n of
  H_TAU → wedged
  || H_DUR _1 → wedged
  || H_DARK → wedged
  || H_A2H _2 → wedged (* receipt of messages unwedges *)
  || H_H2A _3 → wedged
  || H_D2H _4 → wedged
  || H_H2D h2d_msg → (case h2d_msg of
    H2D_RECV data → F (* i.e. the only way to reset wedged is to receive data *)
    || H2D_WEDGED → T)

```


\parallel H2D_LAM *mac* \rightarrow *wedged*)
 \parallel H_H2S_6 \rightarrow *wedged*
 \parallel H_S2H_7 \rightarrow *wedged*)

3.3 Specification

3.3.1 Summary

sends_onlyif_grant
only_sends_pending_output
replies_to_pings
sends_requests
responds_to_grants
asks_for_macs
notices_ping_absence
notices_dark
resends_requests
host_spec

3.3.2 Rules

– :

sends_onlyif_grant *t* =

(* if you send H2S_DATA then you must have previously received A2H_DATA_GRANT strictly within
 MAX_HOST_THINKING_TIME *)
 (* N.B. lack of symmetry with the above- no check for pending output *)
 (* $\exists!n'$ guarantees functional relation between H2S_DATA send and A2H_DATA_GRANT received *)

$\forall n \text{ data.}(t \ n = \text{H_H2S}(\text{H2S_DATA } \textit{data})) \implies$
 $\exists(*!*)n'.\exists \textit{mac}.n' < n \wedge$
 $(t \ n' = \text{H_A2H}(\text{A2H_DATA_GRANT } \textit{mac})) \wedge$
 $\text{h_time } t \ n - \text{h_time } t \ n' < \text{MAX_HOST_THINKING_TIME}$

– :

Rule version:

only_sends_pending_output $t =$

$\forall n \text{ data.}(t \ n = \text{H_H2S}(\text{H2S_DATA } \text{data})) \implies$
let $mac = \text{mac_of_data } t \ n$ **in**
 $\exists xs. \text{pending_output } t \ mac \ n = (\text{data} :: xs)$

– :

replies_to_pings($t : \text{host_trace}$) =

(* replies to pings strictly before MAX_HOST_THINKING_TIME elapses *)
 $\forall n \ \text{pingid.}(t \ n = \text{H_A2H}(\text{A2H_PING } \text{pingid})) \implies$
 $\exists m. n < m \wedge$
 $(t \ m = \text{H_H2A}(\text{H2A_PONG } \text{pingid})) \wedge$
 $\text{h_time } t \ m - \text{h_time } t \ n < \text{MAX_HOST_THINKING_TIME}$

– :

sends_requests($t : \text{host_trace}$) =

(* if you receive D2H_SEND, then you should send H2A_DATA_REQUEST *)
 $\forall n \ \text{mac } \text{data.}(t \ n = \text{H_D2H}(\text{D2H_SEND}(\text{mac}, \text{data}))) \implies$
 $\exists n'. n < n' \wedge (t \ n' = \text{H_H2A}(\text{H2A_DATA_REQUEST } \text{mac}))$

– :

responds_to_grants($t : \text{host_trace}$) =

(* if you receive A2H_DATA_GRANT then send H2S_DATA (signal the dataplane) strictly before MAX_HOST_THINKING_TIME *)

$(\forall n \ \text{mac.}(t \ n = \text{H_A2H}(\text{A2H_DATA_GRANT } \text{mac}))) \implies$
let $p = \text{pending_output } t \ \text{mac } n$ **in**
case p **of**
 $[\] \rightarrow \mathbf{T}$
 $\parallel \text{data} :: ps \rightarrow$
 $\exists n'. n < n' \wedge$
 $(t \ n' = \text{H_H2S}(\text{H2S_DATA } \text{data})) \wedge$
 $\text{h_time } t \ n' - \text{h_time } t \ n < \text{MAX_HOST_THINKING_TIME}$

Rule version:

– :

asks_for_macs(t : host_trace) =

(* if you do have a mac, don't ask for one, contrapositively: if you ask for a mac, you shouldn't have one *)

$\forall n.(t\ n = \text{H_H2A}(\text{H2A_MAC_REQUEST})) \implies (\text{host_mac } t\ n = *)$

– :

notices_ping_absence t =

$\forall n.$

$(\exists n'.n \leq n' \wedge \text{ARBITER_WRITEOFF_TIME} \leq \text{h_time } t\ n' - \text{h_time } t\ n \wedge$

$(\forall m.n \leq m \wedge m < n' \implies \neg \exists \text{pingid}.(t\ m = \text{H_A2H}(\text{A2H_PING } \text{pingid})))) \implies$

$\exists n'.n \leq n' \wedge$

(**let** $\text{delta} = \text{h_time } t\ n' - \text{h_time } t\ n$ **in**

$\text{delta} \in \text{INTERVAL}(\text{ARBITER_WRITEOFF_TIME},$

$\text{ARBITER_WRITEOFF_TIME} + \text{TIMER_GRAININESS})) \wedge$

$\text{h_wedged } t\ n'$

– :

notices_dark t =

(* if the line goes dark, send H2D_WEDGED strictly within MAX_HOST_THINKING_TIME *)

$\forall n.(t\ n = \text{H_DARK}) \implies$

$\exists n'.n < n' \wedge$

$(t\ n' = \text{H_H2D } \text{H2D_WEDGED}) \wedge$

$\text{h_time } t\ n' - \text{h_time } t\ n < \text{MAX_HOST_THINKING_TIME}$

– :

resends_requests t =

(* if you do not receive A2H_DATA_GRANT strictly before REQUEST_REISSUE_TIME after sending H2A_DATA_REQUEST, then resend H2A_DATA_REQUEST *)

Rule version:

$$\begin{aligned}
& \forall n \text{ mac}. (t \ n = \text{H_H2A}(\text{H2A_DATA_REQUEST } \text{mac})) \wedge \\
& (\forall n'. n < n' \wedge \text{h_time } t \ n' - \text{h_time } t \ n < \text{REQUEST_REISSUE_TIME} \implies \\
& \quad \neg(t \ n' = \text{H_A2H}(\text{A2H_DATA_GRANT } \text{mac}))) \implies \\
& \exists n'. n < n' \wedge \\
& \text{h_time } t \ n' - \text{h_time } t \ n \in \text{INTERVAL}(\text{REQUEST_REISSUE_TIME}, \\
& \quad \text{REQUEST_REISSUE_TIME} + \text{TIMER_GRAININESS}) \wedge \\
& (t \ n' = \text{H_H2A}(\text{H2A_DATA_REQUEST } \text{mac}))
\end{aligned}$$

— :

$$\begin{aligned}
& \text{host_spec}(t : \text{host_trace}) = \\
& \text{sends_onlyif_grant } t \wedge \\
& \text{only_sends_pending_output } t \wedge \\
& \text{replies_to_pings } t \wedge \\
& \text{sends_requests } t \wedge \\
& \text{responds_to_grants } t \wedge \\
& \text{asks_for_macs } t \wedge \\
& \text{notices_ping_absence } t \wedge \\
& \text{notices_dark } t \wedge \\
& \text{resends_requests } t
\end{aligned}$$

Rule version:

Chapter 4

Arbiter Channels

4.1 Messages, Labels

4.1.1 Summary

ca_msg
ca_lbl
type_abbrev_ca_trace

4.1.2 Rules

```
— :  
ca_msg =  
    CA_A2H of a2h_msg  
  | CA_H2A of h2a_msg
```

```
— :  
ca_lbl =  
    CA_TAU  
  | CA_DUR of time  
  | CA_A2C of time#a2h_msg  
  | CA_C2H of a2h_msg
```

```
| CA_H2C of time#h2a_msg
| CA_C2A of h2a_msg
```

```
– :
type_abbrev ca_trace : num → ca_lbl
```

4.2 Functions on Traces

4.2.1 Summary

ca_msgs channels start off empty

4.2.2 Rules

```
– channels start off empty :
(ca_msgs t 0 = []) ∧
(ca_msgs t (SUC n) = case t n of
  CA_TAU → ca_msgs t n
  || CA_DUR d →
    (let f(t', c) = (t' - d, c) in
     map f(ca_msgs t n))
  || CA_A2C(t1, m1) → (t1, CA_A2H m1) :: ca_msgs t n
  || CA_C2H m2 → REMOVE1(0, CA_A2H m2)(ca_msgs t n)
  || CA_H2C(t3, m3) → (t3, CA_H2A m3) :: ca_msgs t n
  || CA_C2A m4 → REMOVE1(0, CA_H2A m4)(ca_msgs t n))
```

4.3 Specification

4.3.1 Summary

arbiter_channel_spec

Rule version:

4.3.2 Rules

```

- :
arbitrator_channel_spec t =
 $\forall n.$  let  $ms = \text{ca\_msgs } t \ n$  in
  ( $\forall m.$  mem (0, CA_A2H  $m$ )  $ms = (t \ n = \text{CA\_C2H } m)$ )  $\wedge$ 
  ( $\forall m.$  mem (0, CA_H2A  $m$ )  $ms = (t \ n = \text{CA\_C2A } m)$ )

```


Rule version:

Chapter 5

Switches

5.1 Messages, Labels

5.1.1 Summary

s_lbl
type_abbrev_switch_trace

5.1.2 Rules

```
— :  
s_lbl =  
  S_TAU  
  | S_DUR of time  
  | S_FABRIC of fabric_state  
  | S_S2H of port#s2h_msg  
  | S_H2S of port#h2s_msg
```

```
— :  
type_abbrev switch_trace : num → s_lbl
```

5.2 Functions on Traces

5.2.1 Summary

switch_time
switch_fabric_state

5.2.2 Rules

```

- :
  (switch_time t(0 : num) = (0 : time)) ∧
  (switch_time t(SUC n) = (let d = (case (t(SUC n)) of S_DUR x → x
                                                    || _ → 0) in
                             d + switch_time t n))

```

```

- :
  (switch_fabric_state t 0 = {}) ∧
  (switch_fabric_state t(SUC n) = (
    case t n of
      S_FABRIC fs → fs
    || _ → switch_fabric_state t n
  ))

```

5.3 Specification

5.3.1 Summary

switch_spec

5.3.2 Rules

Rule version:

- :

switch_spec t =

(* Messages are only received if the fabric state is set appropriately. *)

$$(\forall n \text{ } psrc \text{ } data. (t \text{ } n = S_H2S(psrc, H2S_DATA \text{ } data)) \implies \\ \exists pdst. (psrc, pdst) \in (\text{switch_fabric_state } t \text{ } n)) \wedge$$

(* Messages are only sent if the fabric state is set appropriately. *)

$$(\forall n \text{ } pdst \text{ } data. (t \text{ } n = S_S2H(pdst, S2H_DATA \text{ } data)) \implies \\ \exists psrc. (psrc, pdst) \in (\text{switch_fabric_state } t \text{ } n)) \wedge$$

(* A message is sent only if it is received, and the fabric state stays constant for transmission time. *)

$$(\forall n' \text{ } psrc \text{ } pdst \text{ } data. \\ (t \text{ } n' = S_S2H(pdst, S2H_DATA \text{ } data)) \implies \\ \exists n. n < n' \wedge \\ (t \text{ } n = S_H2S(psrc, H2S_DATA \text{ } data)) \wedge (* \text{ Message received } \dots *) \\ (\text{switch_time } t \text{ } n' - \text{switch_time } t \text{ } n = \text{TRANSMISSION_TIME}) \wedge (* \\ \dots \text{TRANSMISSION_TIME} \\ \text{ago } *) \\ (\forall m. n < m \wedge m < n' \implies \neg \exists fs. t \text{ } m = S_FABRIC \text{ } fs) (* \text{ Fabric stays constant between receive} \\ \text{and send } *)$$

) \wedge

(* If a message is received, and the fabric state stays constant for transmission time, it is sent. *)

$$(\forall n \text{ } psrc \text{ } data. \\ (* \text{ Want to allow some Taus before the message has to be sent } *) \\ (t \text{ } n = S_H2S(psrc, H2S_DATA \text{ } data)) \wedge \\ (\exists n'. (\text{TRANSMISSION_TIME} = \text{switch_time } t(n + n') - \text{switch_time } t \text{ } n) \wedge \\ (\forall m. m < n' \implies \neg \exists fs. t(n + m) = S_FABRIC \text{ } fs)) \implies$$
(* N.B. could well be different n' , with preceding S_FABRIC change. *)
$$(\exists n' \text{ } pdst. (\text{TRANSMISSION_TIME} = \text{switch_time } t(n + n') - \text{switch_time } t \text{ } n) \wedge \\ (t(n + n') = S_S2H(pdst, S2H_DATA \text{ } data)))$$

)

Chapter 6

Switch Channels

6.1 Messages, Labels

6.1.1 Summary

cs_msg
cs_lbl
type_abbrev_cs_trace

6.1.2 Rules

```
— :  
cs_msg =  
    CS_S2H of s2h_msg  
  | CS_H2S of h2s_msg
```

```
— :  
cs_lbl =  
    CS_TAU  
  | CS_DUR of time  
  | CS_H2CS of time#h2s_msg  
  | CS_CS2S of h2s_msg
```

```
| CS_S2CS of time#s2h_msg  
| CS_CS2H of s2h_msg
```

```
– :  
type_abbrev cs_trace : num → cs_lbl
```

6.2 Specification

6.2.1 Rules

Chapter 7

Networks

7.1 Labels

7.1.1 Summary

n_lbl
type_abbrev_net_trace

7.1.2 Rules

```
- :
n_lbl =
  N_TAU
  | N_DUR of time
  | N_FABRIC of fabric_state
  | N_DARK of port
  | N_A2CA of port#a2h_msg#time
  | N_CA2H of port#a2h_msg
  | N_H2CA of port#h2a_msg#time
  | N_CA2A of port#h2a_msg
  | N_D2H of port#d2h_msg
  | N_H2D of port#h2d_msg
  | N_H2CS of port#h2s_msg#time
  | N_CS2S of port#h2s_msg
  | N_S2CS of port#s2h_msg#time
  | N_CS2H of port#s2h_msg
```

```

- :
type_abbrev net_trace : num → n_lbl

```

7.2 Functions on Net Traces

7.2.1 Summary

```

net_project_port
net_time
net_fabric
last_ping
net_rtt_estimate
net_mac
net_pending_output

```

pending output, presumably for a given port, per destination mac

7.2.2 Rules

```

- :
(* Most definitions are per port, so first project the trace onto the port before applying the relevant function. *)

```

```

net_project_port t p n = (case t n of
  N_TAU → N_TAU
  || N_DUR d → N_DUR d
  || N_FABRIC fs → N_TAU
  || N_DARK p' → (case p' = p of T → N_DARK p || F → N_TAU)
  || N_A2CA(p', a2h_msg, r) → (case p' = p of T → t n || F → N_TAU)
  || N_CA2H(p', a2h_msg) → (case p' = p of T → t n || F → N_TAU)
  || N_H2CA(p', h2a_msg, r) → (case p' = p of T → t n || F → N_TAU)
  || N_CA2A(p', h2a_msg) → (case p' = p of T → t n || F → N_TAU)
  || N_D2H(p', d2h_msg) → (case p' = p of T → t n || F → N_TAU)
  || N_H2D(p', h2d_msg) → (case p' = p of T → t n || F → N_TAU)
  || N_H2CS(p', h2s_msg, r) → (case p' = p of T → t n || F → N_TAU)
  || N_CS2S(p', h2s_msg) → (case p' = p of T → t n || F → N_TAU)

```

Rule version:

```

|| N_S2CS(p', s2h_msg, r) → (case p' = p of T → t n || F → N_TAU)
|| N_CS2H(p', s2h_msg) → (case p' = p of T → t n || F → N_TAU)

```

```

- :
(net_time t(0 : num) = (0 : time)) ∧
(net_time t(SUC n) = (
  let d = case t n of N_DUR x → x || _ → (0 : time) in
  d + net_time t n))

```

```

- :
(net_fabric t 0 = {}) ∧
(net_fabric t(SUC n) = case (t n) of N_FABRIC fs → fs || _ → net_fabric t n)

```

```

- :
(last_ping t id 0 = *) ∧
(last_ping t id(SUC m) = (case t m of
  N_A2CA(p, A2H_PING id', r) → (case id' = id of T → ↑ m || F → last_ping t id m)
  || _ → last_ping t id m))

```

```

- :
(* rtt_estimate is calculated per port (arbiter-host connection) and id by keeping a record of the last
PING sent *)

```

```

(net_rtt_estimate t 0 = *) ∧
(net_rtt_estimate t(SUC m) = (case (t m) of
  N_H2CA(p', H2A_PONG id, r) →
    (case (last_ping t id m) of ↑ m' → ↑(net_time t m - net_time t m') || * → *)
  || _ → net_rtt_estimate t m))

```

Rule version:

– :
 (* mac for a given port, according to messages sent by arbiter and host events
 D2H.INVALIDATE_MY_MAC and H2D_WEDGED *)

```
(net_mac t 0 = *) ∧
(net_mac t(SUC n) =
  (let mac = net_mac t n in
    case t n of
      N_DARK p' → * (* already covered by H2D_WEDGED *)
    || N_A2CA(p', a2h_msg, r) →
      (case a2h_msg of A2H_MAC_GRANT mac' → ↑ mac' || _x90 → mac)
    || N_D2H(p', d2h_msg) →
      (case d2h_msg of D2H_INVALIDATE_MY_MAC → * || _ → mac)
    || N_H2D(p', h2d_msg) → (case h2d_msg of H2D_WEDGED → * || _x89 → mac)
    || _1 → mac))
```

– **pending output, presumably for a given port, per destination mac :**

```
(net_pending_output t mac 0 = []) ∧
(net_pending_output t mac(SUC n) =
  (let oldq = (net_pending_output t mac n) in
    case (t n) of
      N_D2H(p, D2H_SEND(mac, data)) → oldq ++ [data]
      (* notion of pending output if host sends an arbitrary message? *)
    || N_H2CS(p, H2S_DATA data, r) → (case hd oldq = data of T → TL oldq || F → oldq)
    || N_DARK p → [] (* N_DARK clears pending output *)
    || _ → oldq))
```

7.3 Projections from Net Traces

7.3.1 Summary

n_to_a
arbiter_trace
n_to_h
host_trace
n_to_s
switch_trace
arbiter_channel_trace

Rule version:

7.3.2 Rules

```

- :
n_to_a l = case l of
  N_TAU → A_TAU
  || N_DUR d → A_DUR d
  || N_FABRIC fs → A_FABRIC fs
  || N_DARK p1 → A_DARK p1
  || N_A2CA(p2, a2h_msg2, t2) → A_A2H(p2, a2h_msg2)
  || N_CA2H _3 → A_TAU
  || N_H2CA _4 → A_TAU
  || N_CA2A(p5, h2a_msg5) → A_H2A(p5, h2a_msg5)
  || N_D2H _6 → A_TAU
  || N_H2D _7 → A_TAU
  || N_H2CS _8 → A_TAU
  || N_CS2S _9 → A_TAU
  || N_S2CS _10 → A_TAU
  || N_CS2H _11 → A_TAU

```

```

- :
arbiter_trace(t : net_trace) = n_to_a o t

```

```

- :
n_to_h p l = case l of
  N_TAU → H_TAU
  || N_DUR dur → H_DUR dur
  || N_FABRIC _4 → H_TAU
  || N_DARK p8 → if p = p8 then H_DARK else H_TAU
  || N_A2CA _1 → H_TAU
  || N_CA2H(p1, m1) → if p = p1 then H_A2H m1 else H_TAU
  || N_H2CA(p2, m2, t2) → if p = p2 then H_H2A m2 else H_TAU
  || N_CA2A(p3, m3) → H_TAU
  || N_D2H(p4, m4) → if p = p4 then H_D2H m4 else H_TAU
  || N_H2D(p5, m5) → if p = p5 then H_H2D m5 else H_TAU
  || N_H2CS(p6, m6, t6) → if p = p6 then H_H2S m6 else H_TAU
  || N_CS2H(p7, m7) → if p = p7 then H_S2H m7 else H_TAU

```

Rule version:

```

|| N_CS2S _2 → H_TAU
|| N_S2CS _3 → H_TAU

```

```

- :
host_trace p(t : net_trace) = (n_to_h p) o t

```

```

- :
n_to_s l = case l of
  N_TAU → S_TAU
  || N_DUR d → S_DUR d
  || N_FABRIC fs → S_FABRIC fs
  || N_DARK p1 → S_TAU
  || N_A2CA _2 → S_TAU
  || N_CA2H _3 → S_TAU
  || N_H2CA _4 → S_TAU
  || N_CA2A _5 → S_TAU
  || N_D2H _6 → S_TAU
  || N_H2D _7 → S_TAU
  || N_H2CS _8 → S_TAU
  || N_CS2S(p9, h2s_msg) → S_H2S(p9, h2s_msg)
  || N_S2CS(p10, s2h_msg, t10) → S_S2H(p10, s2h_msg)
  || N_CS2H _11 → S_TAU

```

```

- :
switch_trace(t : net_trace) = n_to_s o t

```

```

- :
arbiter_channel_trace h(t : net_trace) = λn.case t n of
  N_DUR dur → CA_DUR dur
  || N_A2CA(h1, m1, t1) → if h = h1 then CA_A2C(t1, m1) else CA_TAU
  || N_CA2A(h2, m2) → if h = h2 then CA_C2A m2 else CA_TAU

```

Rule version:

```

|| N_H2CA(h3, m3, t3) → if h = h3 then CA_H2C(t3, m3) else CA_TAU
|| N_CA2H(h4, m4) → if h = h4 then CA_C2H m4 else CA_TAU
|| _ → CA_TAU

```

7.4 Specification

7.4.1 Summary

```

spec
example_trace
fromNum16
fromNum32

```

7.4.2 Rules

```

- :
spec ports(t : net_trace) =

arbiter_spec ports(arbiter_trace t) ∧
switch_spec(switch_trace t) ∧
(∀p. mem p ports ⇒
  host_spec(host_trace p t) ∧
  arbiter_channel_spec(arbiter_channel_trace p t))

```

```

- :
example_trace = [N_DUR(10 * USEC),
N_A2CA(n2w 0, A2H_PING(n2w 901), 84 * NSEC),
N_DUR(10 * USEC),
N_A2CA(n2w 0, A2H_PING(n2w 902), 84 * NSEC),
N_DUR(85 * NSEC),
N_CA2H(n2w 0, A2H_PING(n2w 902)),
N_H2CA(n2w 0, H2A_PONG(n2w 902), 84 * NSEC),
N_H2CA(n2w 0, H2A_MAC_REQUEST, 84 * NSEC),
N_DUR(85 * NSEC),
N_CA2A(n2w 0, H2A_PONG(n2w 902)),

```

Rule version:

```
N_DUR(80 * NSEC),  
N_CA2A(n2w 0, H2A_MAC_REQUEST),  
N_A2CA(n2w 0, A2H_MAC_GRANT(n2w 50), 84 * NSEC)]
```

```
— :  
fromNum16 = word16 $fromNum
```

```
— :  
fromNum32 = word32 $fromNum
```