

Pattern Matching in a Typeless Language

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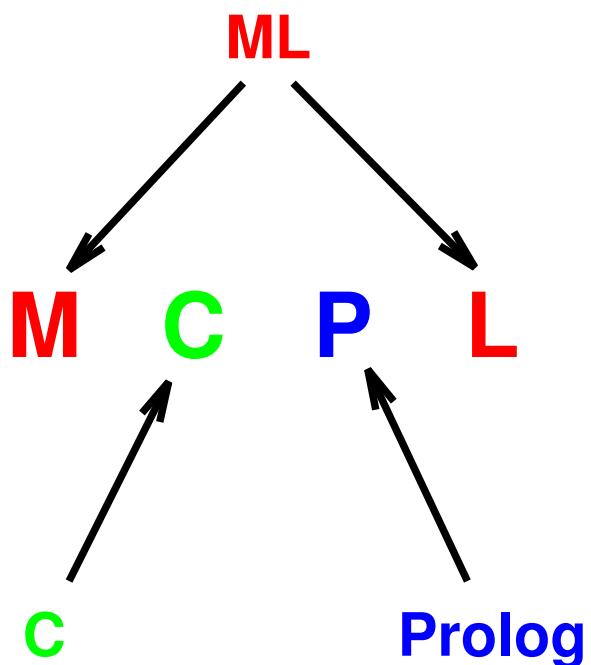
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New Museum Site
Pembroke Street
Cambridge, CB2 3QG

Contents of Talk

- Introduction
 - Types – static, dynamic, typeless
 - Language design philosophy
- Pattern Matching
 - Constants, ranges and variable binding
 - Structures
 - Relational operators and assignments
- Example Program fragments
 - Coins, Trees, Eval, Queens
 - Other Examples
- Conclusions

Origins of MCPL



FAQ

“It must be really difficult to construct a large system that is completely bug free in a typeless language?”

Yes

“It is really difficult to construct a large system that is completely bug free in any language.”

Type Checking

“It is well known that typechecking, while very useful, captures only a small part of what it means for a program to be correct; . . . ”

BL + JW
p.1812 JACM 1994

A Large Program

Another Large Program

$f(x);$

ML Puzzle

<insert>

```
fun f g g = g; f x x;
```

A Solution

```
datatype T = g; val x = g;
```

```
fun f g g = g; f x x;
```

Pathological

```
fun a f g = g f f;  
val b      = a o a;  
val c      = b o b;  
val d      = c o c;  
val e      = d o d;
```

Pathological

```
fun a f g = g f f;  
val b      = a o a;  
val c      = b o b;  
val d      = c o c;  
val e      = d o d;
```

When run under Moscow ML, this program generates 2,874,641 bytes of output on 42,297 lines.

PL/1

```
if (1 = 1b) then x = 1;  
else x = 2;
```

What does x now equal?

ML Fragments

```
fun f 0 = 1
| f n = n * f(n-1);

fun fib 0 = 1
| fib 1 = 1
| fib n = fib(n-1) + fib(n-2);

fun gcd(a, b) =
  if a=b then a
  else if a>b then gcd(a mod b, b)
            else gcd(a, b mod a);
```

Permutations

```
fun perm_prefix a = map (fn xs => a::xs);  
  
fun perm_iter(left,      []) = []  
| perm_iter(left, a::rest) =  
  perm_prefix a (perm(rev left@rest)) @  
  perm_iter(a::left, rest)  
  
and perm [] = [[]]  
| perm xs = perm_iter([], xs);  
  
perm[1,2,3];
```

Output

```
val it =  
  [[1, 2, 3], [1, 3, 2], [2, 1, 3],  
   [2, 3, 1], [3, 1, 2], [3, 2, 1]]  
  : int list list
```

Flatten

```
flat(      N, [N|E] , E) :- letter(N).
```

```
flat(n(L,R) ,      B, E) :- flat(L, B, M) ,  
                           flat(R, M, E).
```

```
letter(a).
```

```
letter(b).
```

```
letter(c).
```

```
letter(d).
```

```
?- flat(n(n(a,b),n(c,d)), R, []).
```

Output

R = [a, b, c, d]

Max Copy

```
mcopy(X, Y) :- mc(X, Y, 0, M, M).  
  
mc(x, x, N, N, _).  
  
mc(n(N,L,R), n(V,L1,R1), M0, M2, V) :-  
    N <= M0,  
    mc(L, L1, M0, M1, V),  
    mc(R, R1, M1, M2, V).  
  
mc(n(N,L,R), n(V,L1,R1), M0, M2, V) :-  
    N > M0,  
    mc(L, L1, N, M1, V),  
    mc(R, R1, M1, M2, V).  
  
try(X) :- write(X), nl,  
          mcopy(X, Y),  
          write(Y), nl.  
  
?- try( n(10,  
           n(15,n(12,x,n(13,x,x)),  
              n(17,x,x))  
         ),  
        n(11,n(16,n(10,x,x),x),x)  
      )  
     ).
```

Max Copy

Output

```
n(17,  
  n(17,n(17,x,n(17,x,x)),  
      n(17,x,x))  
  ),  
  n(17,n(17,n(17,x,x),x),x)  
)
```

Rotate

```
rotate([],[]).
```

```
rotate([X|Xs],Y) :- ap(Xs,[X],Y).
```

```
ap([],X,X).
```

```
ap([A|As],X,[A|R]) :- ap(As,X,R).
```

```
?- rotate([nice, to, see, you], R).
```

Output

```
R = [to, see, you, nice]
```

Translation

ML

```
fun f 0 = 1  
| f n = n * f(n-1);
```

MCPL

```
FUN f : 0 => 1  
      : n => n * f(n-1)
```

Translation

ML

```
fun fib 0 = 1
| fib 1 = 1
| fib n = fib(n-1) + fib(n-2);
```

MCPL

```
FUN fib : 0..1 => 1
      :      n => fib(n-1) + fib(n-2)
```

Translation

ML

```
fun gcd(a, b) =  
  if      a=b then a  
  else if a>b then gcd(a mod b, b)  
                else gcd(a, b mod a);
```

MCPL

```
FUN gcd  
: a,      =a => a  
: a, (<a)b => gcd(a MOD b, b)  
: a      b => gcd(a, b MOD a)
```

Translation?

ML

```
fun gcd(a, b) =  
  if      a=b then a  
  else if a>b then gcd(a-b, b)  
                else gcd(a, b-a);
```

MCPL

```
FUN gcd  
: a,      =a => a  
: a, (<a)b => gcd(a-b, b)  
: a      b => gcd(a, b-a)
```

Coins

In how many ways can you form change for a given sum of money using coins of denominations, 50, 20, 10, 5, 2 and 1p?

50p 20p 10p 5p 2p 1p

Coins

ML

```
fun ways (s, [1] ) = 1
| ways (s, d::ds) =
  if d>s then ways(s, ds)
  else ways(s, ds) +
        ways(s-d, d::ds);

fun try s = ways(s, [50,20,10,5,2,1]);;

try 75;
```

MCPL

```
FUN ways
: s,      [ 1] => 1
: s, coins[>s] => ways(s, @coins!1)
: s, coins[ d] => ways(s, @coins!1) +
                    ways(s-d,  coins)

FUN try : s => ways(s, [50,20,10,5,2,1])

try 75
```

Coins

$$\sum_{s=0}^{\infty} W_s Z^s =$$

$$\frac{1}{(1-Z)(1-Z^2)(1-Z^5)(1-Z^{10})(1-Z^{20})(1-Z^{50})}$$

Eval

```
FUN lookup
: ?,          0 => RAISE E_Lookup
: v, [=v, val, ?] => val
: v, [ ?, ?, e] => lookup(v, e)

FUN eval
: [Id, v], e => lookup(v, e)
: [Num, k], ? => k
: [Mul, x, y], e => eval(x, e) * eval(y, e)
: [Div, x, y], e => eval(x, e) / eval(y, e)
: [Add, x, y], e => eval(x, e) + eval(y, e)
: [Sub, x, y], e => eval(x, e) - eval(y, e)
:                      => RAISE E_Eval
```

Lex

```
MANIFEST
  Id, Num, Mul, Div, Add, Sub, // Tokens
  Lparen, Rparen, Eof

STATIC strp, ch, token, lexval

FUN lex_init
: str => strp := str; rch()

FUN rch : => ch := %strp
           UNLESS ch=0 DO strp++

FUN lex : =>
  MATCH ch
  : 0          => token := Eof; RETURN
  : ',' | '\n' => rch(); lex(); RETURN
  : 'A'..'Z'   => lexval := ch
                    token := Id
  : '0'..'9'   => lexval := ch-'0'
                    token := Num
  : '('        => token := Lparen
  : ')'        => token := Rparen
  : '*'        => token := Mul
  : '/'        => token := Div
  : '+'        => token := Add
  : '-'        => token := Sub
  :             => RAISE E_syntax
  .
  rch()
```

Parser

```
FUN parse : str => lex_init str
          LET tree = nexp 0
          RETURN tree

FUN check : tok =>
  UNLESS token=tok RAISE E_Syntax
  lex()

FUN prim : => MATCH token
: Id|Num => LET a = mk2(token, lexval)
             lex()
             a
: Lparen => LET a = nexp 0
             check_for Rparen
             a
:           => RAISE E_syntax

FUN nexp : n => lex(); exp n

FUN exp : n =>
  LET a = prim()
  MATCH (token, n)
  : Mul, <2 => a := mk3(Mul, a, nexp 2)
  : Div, <2 => a := mk3(Div, a, nexp 2)
  : Add, <1 => a := mk3(Add, a, nexp 1)
  : Sub, <1 => a := mk3(Sub, a, nexp 1)
  :           => RETURN a
  . REPEAT
```

Main Program

```
MANIFEST // Exceptions
E_Syntax=100, E_Lookup, E_Eval, E_Space

STATIC spv, spp

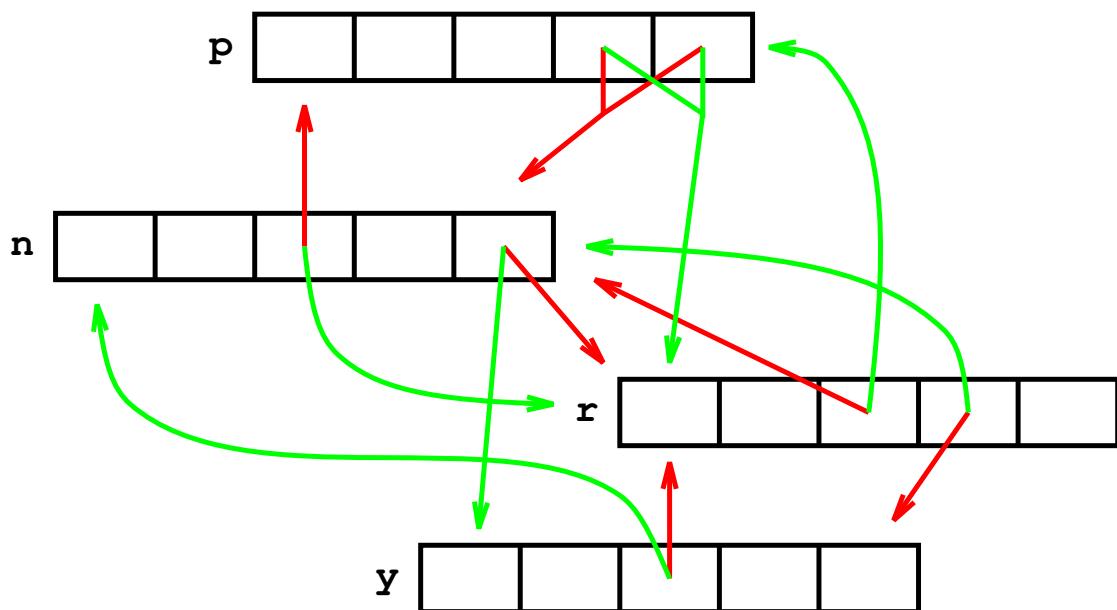
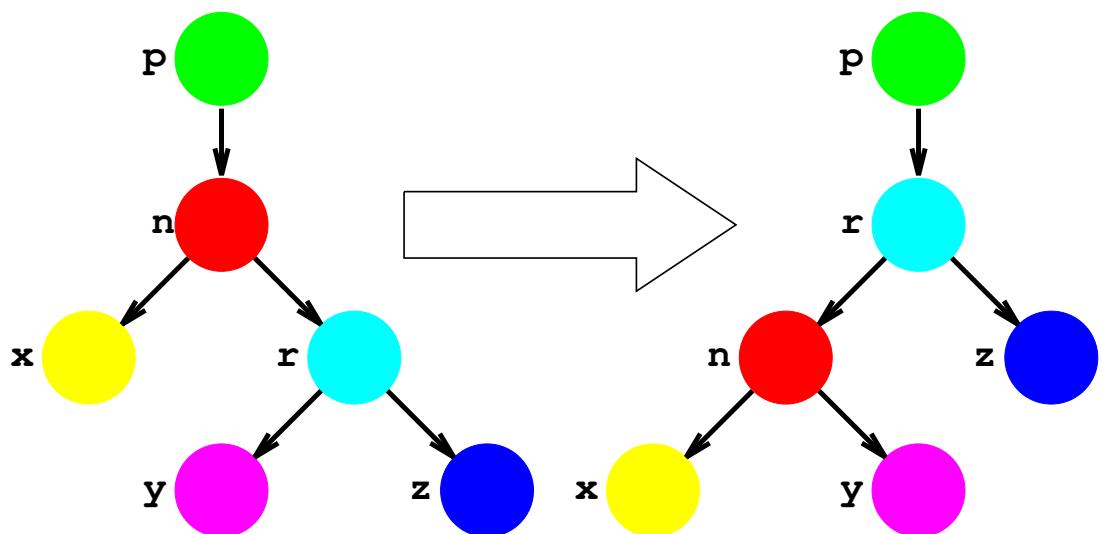
FUN mk2 : x, y => MATCH @spp!-2
  : <spv          => RAISE E_Space
  : p[:=x,:=y]    => spp := p; RETURN p

FUN mk3 : x, y, z => MATCH @spp!-3
  : <spv          => RAISE E_Space
  : p[:=x,:=y,:=z] => spp := p; RETURN p

FUN start :   =>
  spv := getvec 10_000
  spp := @ spv!10_000

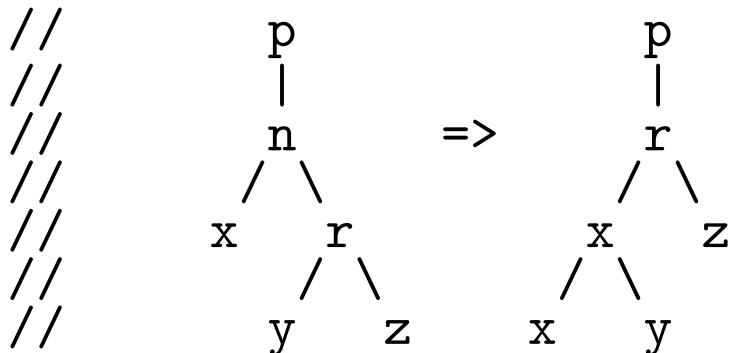
{ LET tree = parse "(3*A+4*B)/2"
  LET env  = [ 'A', 10, [ 'B', 11, 0 ] ]
  writef( "%d\n", eval(tree, env))
} HANDLE
  : E_Syntax      => writef "Syntax\n"
  : E_Lookup, v  => writef("Var %c\n", v)
  : E_Space       => writef "Space\n"
  : E_Eval        => writef "Eval\n"
  .
  freevec spacev
RETURN 0
```

Rotate Left



Rotate Left

// rotleft n promotes the right child



```
FUN rotleft
: n[key, val,
  p[?, ?, ?, pl, pr],
  x
  r[?, ?, rp, y[?, ?, yp, ?, ?], z],
 ] =>
```

```
IF p TEST n=pl THEN pl := r
                           ELSE pr := r
IF y DO yp := n
r, y, rp, p := y, n, p, l
```

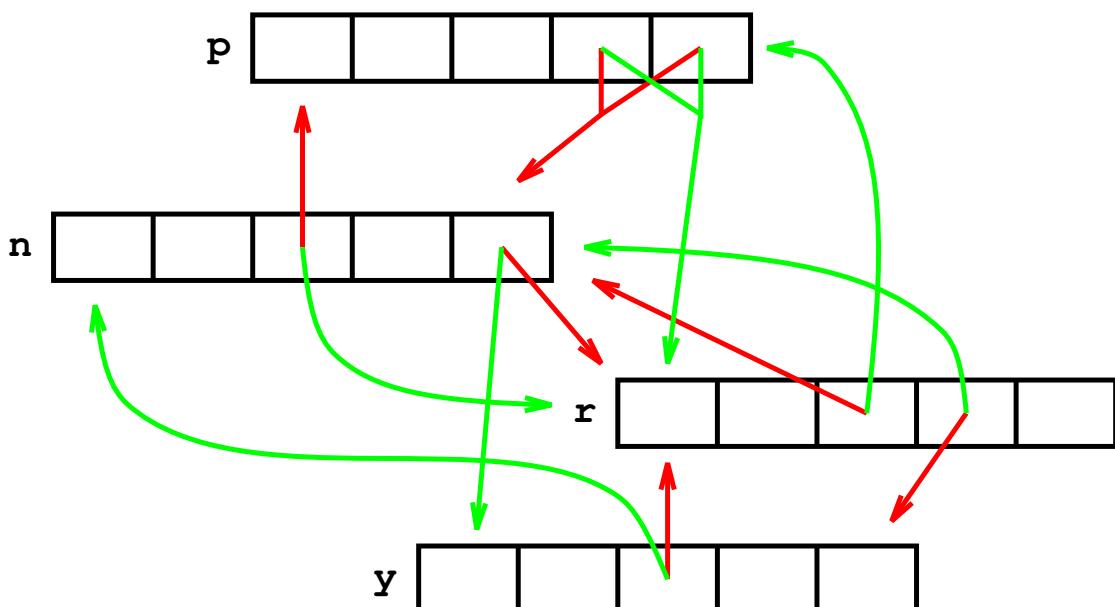
Rotate Left

```

FUN rotleft
: n[key, val,
  p[?, ?, ?, pl, pr],
  x
  r[?, ?, rp, y[?, ?, yp, ?, ?], z],
] =>

  IF p TEST n=pl THEN pl := r
    ELSE pr := r
  IF y DO yp := n
  r, y, rp, p := y, n, p, l

```



Splay

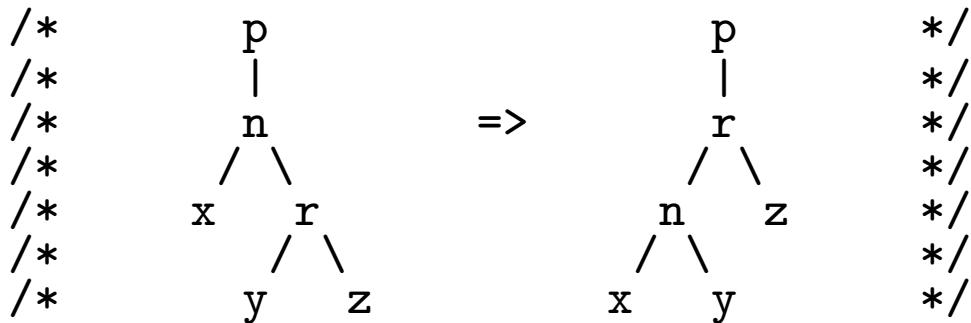
```

FUN splay : x => // Promote node x to the root
  MATCH x                                // Cases
    : [?, ?, , ] =>
      RETURN                                // no p
    : [?, ?, p[?, ?, , ] , ?, ?, ] =>
      rotright p // p
      // x \
    : [?, ?, p[?, ?, , ] , ?, ?, ] =>
      rotleft p // p
      // / x
    : [?, ?, p[?, ?, g[?, ?, ?, =p, ?] , =x, ?] , ?, ?, ] =>
      LET p'=p // g
      rotright g // p \
      rotright p' // x \
    : [?, ?, p[?, ?, g[?, ?, ?, =p, ?] , ?, =x] , ?, ?, ] =>
      LET g'=g // g
      rotleft p // p \
      rotright g' // / x
    : [?, ?, p[?, ?, g[?, ?, ?, ?, =p] , =x, ?] , ?, ?, ] =>
      LET g'=g // g
      rotright p // / p
      rotleft g' // x \
    : [?, ?, p[?, ?, g[?, ?, ?, ?, =p] , ?, =x] , ?, ?, ] =>
      LET p'=p // g
      rotleft g // / p
      rotleft p' // / x
  . REPEAT

```

Rotate Left

```
typedef
struct node { int key, val;
               struct node* parent;
               struct node* left;
               struct node* right;
} Node;
```



```
void rotleft(Node *n){
    Node *p = n->parent;
    Node *r = n->right;
    Node *y = r->left;

    if(p) if(n == p->left) p->left = r;
          else      p->right = r;

    if(y) y->parent = n;

    n->right  = y;
    r->left   = n;
    r->parent = p;
    n->parent = r;
}
```

Splay

```
void splay(Node **x){  
    for(;;){  
        Node *p = x->parent;  
        Node *g;  
        if(p==0) return; /* x is root */  
        g = p->parent;  
        if(g==0)  
            if(x == p->left) { rotright(p); /* p => x */  
                continue; /* x \ / p */  
            }  
            else { rotleft (p); /* p => x */  
                continue; /* / x p \ */  
            }  
  
        if(p == g->left)  
            if(x == p->left) { rotright(g); /* g => x */  
                rotright(p); /* p \ / p */  
                continue; /* x \ / g */  
            }  
            else { rotleft (p); /* g => x */  
                rotright(g); /* p \ / p g */  
                continue; /* / x / \ */  
            }  
  
        if(p == g->right)  
            if(x == p->left) { rotright(p); /* g => x */  
                rotleft (g); /* / p g p */  
                continue; /* x \ / \ */  
            }  
            else { rotleft (g); /* g => x */  
                rotleft (p); /* / p p \ */  
                continue; /* / x g \ */  
            }  
    }  
}
```

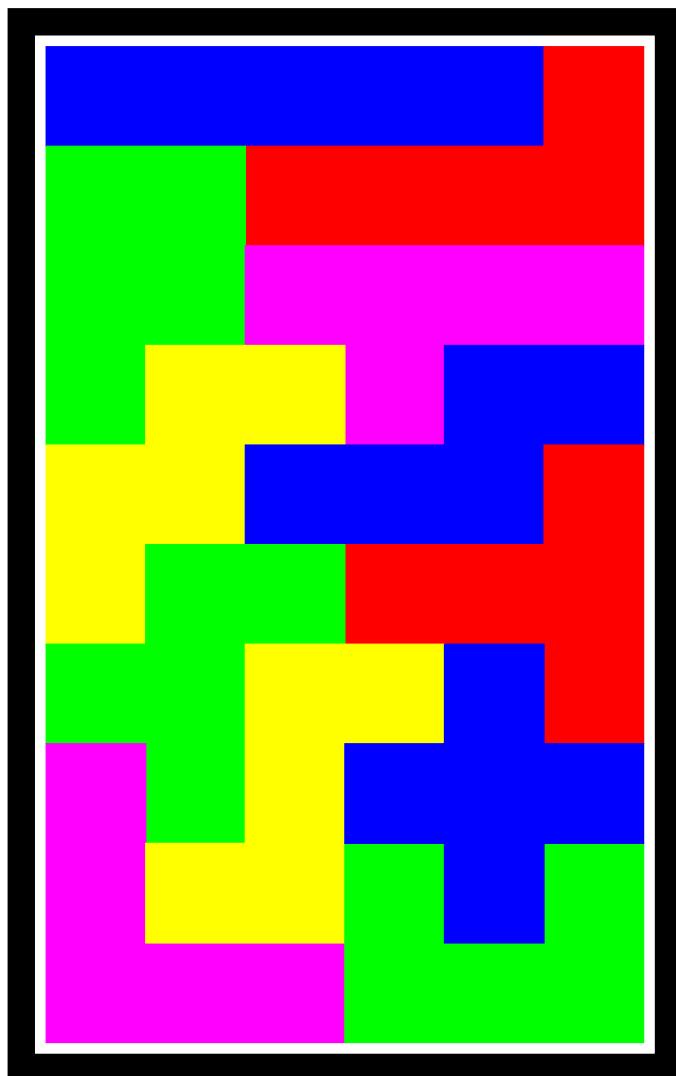
Pushterm

```
FUN pushterm: rel, x, y, z =>
  MATCH curts : [vm, vmax, t1, tp, tt, n] =>
    IF tp>tt RAISE(E_Space, "Too many terms\n")
    UNLESS TsVmax=1 DO abort 999
    EVERY curts : [?, <x :=x] =>
      : [?, <y :=y] =>
      : [?, <z :=z] =>
      .
    MATCH tp
    : [:=rel,:=x,:=y,:=z,np] => n++
                                tp := @np
```

Compact

```
FUN compact : [v, vmax, t1, tp, tt, n] =>
  LET p = tp          // Form histogram
  FOR i = 0 TO vmax DO v!i := 0
  FOR i = 1 TO n MATCH p
    : [rel, x, y, z, np] => (v!x)++
                                (v!y)++
                                (v!z)++
                                p := @np
    .
  LET newvmax = 2      // Form mapping
  v!0 := 0
  v!1 := 1
  v!2 := 2
  FOR i = 3 TO vmax MATCH v!i
    : 0 =>                  // Never used
    : 1 => v!i := 2          // Used once
    :   => v!i := ++newvmax // Multi used
    .
  p := tp              // Apply the mapping
  FOR i = 1 TO n MATCH p
    : [rel,x:=v!x,y:=v!y,z:=v!z,np] => p := @np
    .
  n := newvmax
```

Pentominoes



Pentominoes

```
STATIC board, count=0,  
    p1=0, p2=0, p3=0, p4=0, p5=0, p6=0,  
    p7=0, p8=0, p9=0, pA=0, pB=0, pC=0  
  
FUN try  
    : 12,                                ? => count++  
                                              pr board  
    : n,   [          ~=0,a1           ] => try(n,@a1)  
    : n, p[          a,a1,a2,a3,a4,  
            bz,by,bx, b,b1,b2,b3, ?,  
            ?,cy,cx, c,c1,c2, ?, ?,  
            ?, ?,dx, d,d1, ?, ?, ?,  
            ?, ?, ?, e           ] =>
```

Pentominoes

```
n++  
  
EVERY  
( 0, 0, 0, 0, 0 )  
  
: =a1,=a2,=a3,=a4,=p2 =>  
  a,a1, a2, a3, a4, p2 ALL:= n; try (n, @a1)  
  a,a1, a2, a3, a4, p2 ALL:= 0  
  
: =a1,=a2,=a3, =b,=p3 =>  
  a,a1, a2, a3, b, p3 ALL:= n; try (n, @a1)  
  a,a1, a2, a3, b, p3 ALL:= 0  
...  
  
: =b,=bx,=by,=bz,=p3 =>  
  a, b, bx, by, bz, p3 ALL:= n; try (n, @a1)  
  a, b, bx, by, bz, p3 ALL:= 0  
  
: =b,=bx,=by,=cy,=pC =>  
  a, b, bx, by, cy, pC ALL:= n; try (n, @a1)  
  a, b, bx, by, cy, pC ALL:= 0  
...  
  
: =b, =c, =d,=d1,=p3 =>  
  a, b, c, d, d1, p3 ALL:= n; try (n, @a1)  
  a, b, c, d, d1, p3 ALL:= 0  
  
: =b, =c, =d, =e,=p2 =>  
  a, b, c, d, e, p2 ALL:= n; try (n, @a1)  
  a, b, c, d, e, p2 ALL:= 0
```

Pentominoes

```
FUN pr : => writef("\nSolution no: %d", count)
FOR i = 0 TO 12*8-1 DO
{ LET n = board!i
LET ch = '*'
IF 0<=n<=12 DO
    ch := ".ABCDEFGHIJKLM" % n
UNLESS i MOD 8 DO newline()
writef(" %c", ch)
}
newline()

FUN start : =>
LET x = -1
board := [ x,x,x,x,x,x,x,x,
           x,0,0,0,0,0,0,x,
           x,x,x,x,x,x,x,x ] 

try(0, board)

writef("\nNumber of solutions: %d\n", count)
```

Eight Queens

```
GET "mcpl.h"

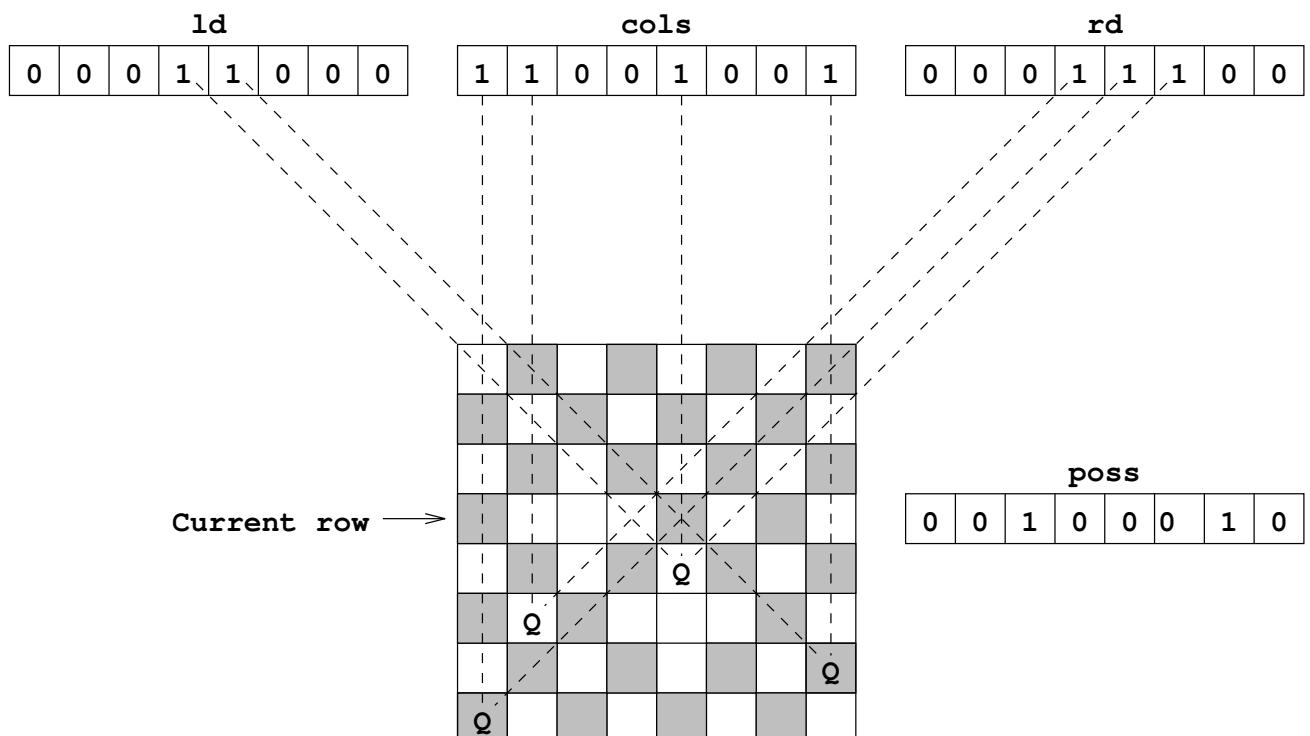
STATIC count, all

FUN try
: ?, =all, ? => count++

: ld, row, rd =>
  LET poss = ~(ld | row | rd) & all
  WHILE poss DO
    { LET bit = poss & -poss
      poss -:= bit
      try((ld|bit)<<1, row|bit, (rd|bit)>>1)
    }

FUN start : =>
  all := #b1111_1111
  count := 0
  try(0, 0, 0)
  writeln("Solutions: %d\n", count)
```

Eight Queens



Eight Queens

```
fun depthfirst(next, pred) x =
  let fun dfs []      = []
      | dfs(y::ys) =
          if pred y
          then y::dfs(next y @ ys)
          else dfs(next y @ ys)
  in dfs [x]
end;

fun notmem x []      = true
  | notmem x (y::ys) = if x=y
                        then false
                        else notmem x ys;

fun secr f y x = f(x, y);

fun upto(i, n) = if i>n
                  then []
                  else i :: upto (i+1, n);

fun filter f []      = []
  | filter f (x::xs) =
      if f x then x :: filter f xs
      else      filter f xs;
```

Eight Queens

```
fun safequeen oldqs newq =
  let fun nodiag(i, []) = true
      | nodiag (i, q::qs) =
          abs(newq-q)<>i
          andalso
          nodiag(i+1,qs)

  in  notmem newq oldqs
      andalso
      nodiag(1,oldqs)
  end;

fun nextqueen n qs =
  map (secr op:: qs)
  (filter (safequeen qs) (upto(1,n)));

fun isfull n qs = length qs = n;

fun nqueens n =
  depthfirst (nextqueen n, isfull n) [];

length(nqueens 8);
```

Eight Queens

```
fun filter _ [] = []
| filter p (x::xs) =
  if p x then x :: filter p xs
  else      filter p xs;

fun free(x,y,z) =
  filter (fn(a,b,c) => x<>a andalso
          y<>b andalso
          z<>c);

fun try [] = 1
| try ([]::_) = 0
| try((sq::r)::s) = try(map(free sq)s)
  + try(r::s);
```

Eight Queens

```
try
[[(( 1,1, 8),( 2,2, 7),( 3,3, 6),( 4,4, 5),
  ( 5,5, 4),( 6,6, 3),( 7,7, 2),( 8,8, 1)
],
[(( 2,1, 9),( 3,2, 8),( 4,3, 7),( 5,4, 6),
  ( 6,5, 5),( 7,6, 4),( 8,7, 3),( 9,8, 2)
],
[(( 3,1,10),( 4,2, 9),( 5,3, 8),( 6,4, 7),
  ( 7,5, 6),( 8,6, 5),( 9,7, 4),(10,8, 3)
],
[(( 4,1,11),( 5,2,10),( 6,3, 9),( 7,4, 8),
  ( 8,5, 7),( 9,6, 6),(10,7, 5),(11,8, 4)
],
[(( 5,1,12),( 6,2,11),( 7,3,10),( 8,4, 9),
  ( 9,5, 8),(10,6, 7),(11,7, 6),(12,8, 5)
],
[(( 6,1,13),( 7,2,12),( 8,3,11),( 9,4,10),
  (10,5, 9),(11,6, 8),(12,7, 7),(13,8, 6)
],
[(( 7,1,14),( 8,2,13),( 9,3,12),(10,4,11),
  (11,5,10),(12,6, 9),(13,7, 8),(14,8, 7)
],
[(( 8,1,15),( 9,2,14),(10,3,13),(11,4,12),
  (12,5,11),(13,6,10),(14,7, 9),(15,8, 8)
]
];

```

Eight Queens

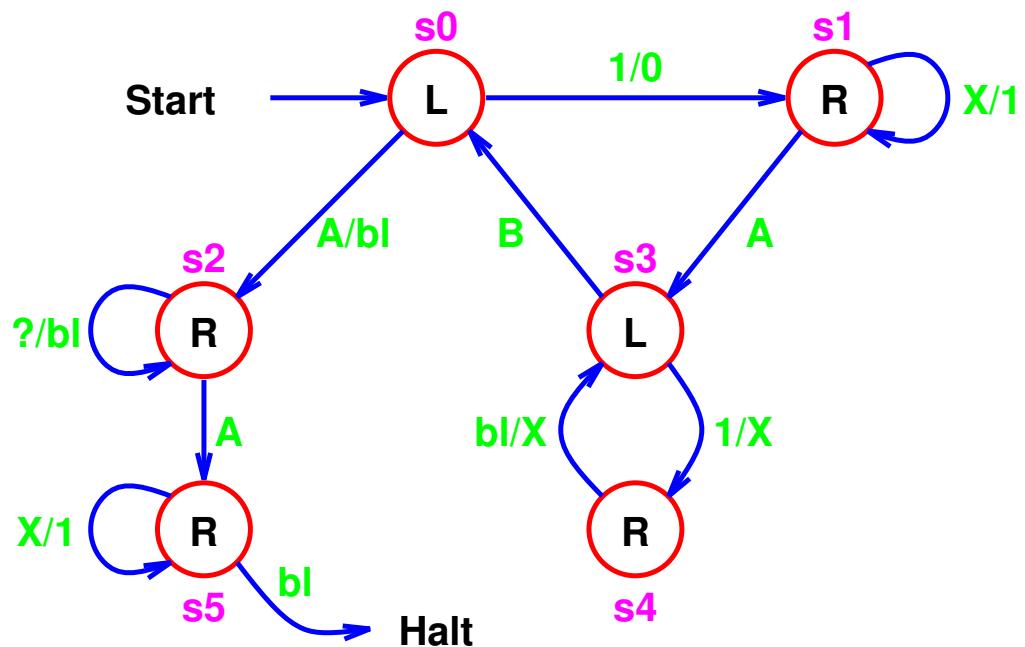
```
fun try 8 _ = 1
| try n qs = try_iter (n+1) 8 qs
```

```
and try_iter n 0 qs = 0
| try_iter n q qs =
  if ok q (q+1) (q-1) qs
  then try n (q::qs) +
       try_iter n (q-1) qs
  else try_iter n (q-1) qs
```

```
and ok a b c [] = true
| ok a b c (q::qs) =
  a<>q andalso
  b<>q andalso
  c<>q andalso
  ok a (b+1) (c-1) qs;
```

```
try 0 [] ;
```

A Turing Machine



Turing

```
fun str [] = ""
| str [x] = x
| str (x::xs) = x ^ " " ^ str xs;

fun pr (x, c, y) = output(std_out,
                           str x ^
                           "[" ^
                           c ^
                           "] " ^
                           str y ^
                           "\n");

fun tr s ch (x,y) =
  (pr (rev x, ch, y);
   s ch (x,y))
);

fun R c s (xs, y::ys) =
  tr s y (c::xs, ys)

| R c s (xs, []) =
  tr s " " (c::xs, []);

fun L c s (x::xs, ys) =
  tr s x (xs, c::ys)

| L c s ([] , ys) =
  tr s " " ([] , c::ys);

fun HALT c (x, y) = pr(rev x, c, y);
```

Turing

```
fun turing(lstr, ch, rstr) =
  s0 ch (rev(explode lstr), explode rstr)

and s0 "1" = R "0" s1
| s0 "A" = R " " s2
| s0 c = L c s0

and s1 "A" = L "A" s3
| s1 "X" = R "1" s1
| s1 c = R c s1

and s2 "A" = R "A" s5
| s2 _ = R " " s2

and s3 "B" = L "B" s0
| s3 "1" = R "X" s4
| s3 c = L c s3

and s4 " " = L "X" s3
| s4 c = R c s4

and s5 " " = HALT "A"
| s5 "X" = R "1" s5
| s5 c = R c s5;

turing("A11", "B", "111A");
```

Turing

```
STATIC ltape, ch, rtape

FUN right : c =>
  EVERY rtape
    :
      0 => rtape := mk2(0, ' ')
    :
      [link, k] => link, ltape, rtape, ch, k :=
        ltape, rtape, link, k, c
        pr()
      RETURN ch

FUN left : c =>
  EVERY ltape
    :
      0 => ltape := mk2(0, ' ')
    :
      [link, k] => link, rtape, ltape, ch, k :=
        rtape, ltape, link, k, c
        pr()
      RETURN ch

FUN halt : c => ch := c; pr()
```

Turing

```
FUN turing : init_state, lstr, char, rstr =>
  ltape, ch, rtape := 0, char, 0

  LET i = 0
  WHILE rstr%i DO i++
  WHILE i      DO rtape:=mk2(rtape, rstr%--i)
  WHILE lstr%i DO ltape:=mk2(ltape, lstr%i++)

  pr()
  init_state ch

FUN pr : =>
  prb ltape           // Print left tape
  writef("[%c]", ch) // Print the current ch
  prf rtape           // Print right tape
  newline()

FUN prb             // Print chars backwards
:      0 => RETURN
: [chs, ch] => prb chs; wrch ' ' ; wrch ch

FUN prf             // Print chars forwards
:      0 => RETURN
: [chs, ch] => wrch ch; wrch ' ' ; prf chs
```

Turing

```
FUN s0 : '1' => s1 (right '0')
    : 'A' => s2 (right ' ')
    : c   => s0 (left   c )

FUN s1 : 'A' => s3 (left   'A')
    : 'X' => s1 (right  '1')
    : c   => s1 (right  c )

FUN s2 : 'A' => s5 (right  'A')
    : ?   => s2 (right  ' ')

FUN s3 : 'B' => s0 (left   'B')
    : '1' => s4 (right  'X')
    : c   => s3 (left   c )

FUN s4 : ' ' => s3 (left   'X')
    : c   => s4 (right  c )

FUN s5 : ' ' =>      halt 'A'
    : 'X' => s5 (right  '1')
    : c   => s5 (right  c )
```

Turing

Call

```
turing(s0, "A11", 'B', "111A")
```

Output

```
A 1 1[B]1 1 1 A
A 1[1]B 1 1 1 A
A 1 0[B]1 1 1 A
A 1 0 B[1]1 1 A
A 1 0 B 1[1]1 A
A 1 0 B 1 1[1]A
A 1 0 B 1 1 1[A]
A 1 0 B 1 1[1]A
A 1 0 B 1 1 X[A]
A 1 0 B 1 1 X A[ ]
A 1 0 B 1 1 X[A]X
A 1 0 B 1 1[X]A X
A 1 0 B 1[1]X A X
A 1 0 B 1 X[X]A X
A 1 0 B 1 X X[A]X
A 1 0 B 1 X X A[X]
A 1 0 B 1 X X A X[ ]
A 1 0 B 1 X X A[X]X
A 1 0 B 1 X X[A]X X
A 1 0 B 1 X[X]A X X
A 1 0 B 1[X]X A X X
A 1 0 B[1]X X A X X
A 1 0 B X[X]X A X X
A 1 0 B X X[X]A X X
```

... lots of lines until ...

Turing

```
A 0 0[B]X X X A X X X X X X X  
A 0[0]B X X X A X X X X X X X  
A[0]0 B X X X A X X X X X X X  
[A]0 0 B X X X A X X X X X X X  
[0]0 B X X X A X X X X X X X  
[0]B X X X A X X X X X X X  
[B]X X X A X X X X X X X  
[X]X X A X X X X X X X  
[X]X A X X X X X X X  
[A]X X X X X X X  
A[X]X X X X X  
A 1[X]X X X X  
A 1 1[X]X X X  
A 1 1 1[X]X X  
A 1 1 1 1[X]X  
A 1 1 1 1 1[X]  
A 1 1 1 1 1 [ ]  
A 1 1 1 1 1 1[A]
```

I.e. 2 times 3 equals 6

Conclusions

- Typeless pattern matching is possible.
- It is readable and easy to understand.
- It is simple to implement and efficient.
- The MCPL compiler is small (35,268 bytes).
- It will compile itself in 0.4 seconds on a 200 MHz Pentium Pro.