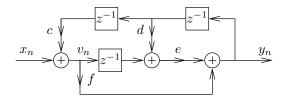
COMPUTER SCIENCE TRIPOS Part II – 2018 – Paper 9

6 Digital Signal Processing (MGK)

- (a) When converting a digital audio signal from one sampling frequency to another, it is common practice to use a low-pass filter. What is the purpose of this low-pass filter, and what cut-off frequency should it have if the change of sampling frequency is
 - (i) from 12 kHz to 48 kHz;
 - (ii) from 48 kHz to 12 kHz.

[4 marks]

(b) You are working on the firmware of a quadcopter drone. Your colleague, through trial and error, found that the following recursive filter nicely avoids unwanted oscillations in the control system:



- (i) What are the first three samples h_0, h_1, h_2 of the impulse response of this filter? [Note: All delay elements have been initialized to zero.] [6 marks]
- (ii) What is the z-transform H(z) = Y(z)/X(z) of the impulse response of this digital filter? [5 marks]
- (iii) The software development kit of your flight controller can only implement digital filters of the form

$$y_n = \sum_{k=0}^{3} b_k \cdot x_{n-k} - \sum_{l=1}^{3} a_l \cdot y_{n-l}.$$

What coefficient values a_l and b_k ($0 \le k \le 3$, $1 \le l \le 3$) will implement the same impulse response as your colleague's filter? [5 marks]