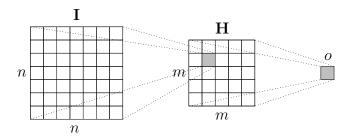
## COMPUTER SCIENCE TRIPOS Part IB - 2018 - Paper 6

## 2 Artificial Intelligence (SBH)

Evil Robot is updating his visual system. He has a single camera that produces an  $n \times n$  matrix I of pixel values. His visual system is arranged as follows:



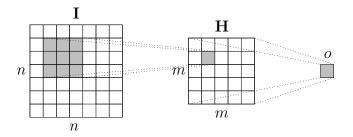
The input I is reduced to an  $m \times m$  matrix  $\mathbf{H}(\mathbf{I})$ . The elements  $H_{i,j}$  are

$$H_{i,j}(\mathbf{I}) = \sigma \left( \sum_{k=1}^{n} \sum_{l=1}^{n} w_{k,l}^{(i,j)} I_{k,l} + b^{(i,j)} \right)$$

where  $\sigma$  is an appropriate function, and  $w_{k,l}^{(i,j)}$  and  $b^{(i,j)}$  are the weights and bias for element (i,j). A single output  $o(\mathbf{H})$  is computed as

$$o(\mathbf{H}) = \sigma \left( \sum_{k=1}^{m} \sum_{l=1}^{m} w_{k,l} H_{k,l} + b \right).$$

- (a) If Evil Robot has a training example  $(\mathbf{I}', y')$  and is using an error  $E(\mathbf{w})$  where  $\mathbf{w}$  is a vector of all weights and biases available, derive an algorithm for computing  $\frac{\partial E}{\partial \mathbf{w}}$  for the example. [12 marks]
- (b) A modification to the system works as follows:



The mapping from **I** to **H** is replaced by an  $n' \times n'$  convolution kernel. This has a single set of parameters  $v_{k,l}$  and c used to compute every element of **H** as the weighted sum of a patch of elements in **I** 

$$H_{i,j}(\mathbf{I}) = \sigma \left( \sum_{k=1}^{n'} \sum_{l=1}^{n'} v_{k,l} I_{i+k-1,j+l-1} + c \right).$$

Provide a detailed description of how the algorithm derived in Part (a) must be updated to take account of this modification. [8 marks]

1