## Algorithms

(a) How do insertions and deletions in a 2-3-4 tree retain the structure's perfect balance?
(b) Explain the structural relationship between 2-3-4 trees and red-black trees.
(c) Draw diagrams to illustrate left and right rotations at the root node of a binary search tree. Label the positions of all subtrees before and after the rotation.
[4 marks]
(d) Write pseudocode for a recursive function move_to_root ( $\mathrm{x}, \mathrm{k}$ ) which, given a binary search tree with root node $x$ and a key value $k$, uses a sequence of rotations to move the node with key value $k$ to the root of the tree and returns a pointer to the new root node.
[10 marks]

