Databases

- (a) Define the notion of a *functional dependency*. [2 marks]
- (b) Consider the following "rule" for functional dependencies.

if
$$A \to B$$
 and $B, C \to D$, then $A, C \to D$.

Either prove this rule is correct, or present a counter-example showing that the rule is false. [4 marks]

(c) The union rule for functional dependencies states that if $F \models X \to Y$ and $F \models X \to Z$, then $F \models X \to Y \cup Z$ (this can also be written as $F \models X \to Y, Z$).

Prove this rule using only Armstrong's axioms. [4 marks]

- (d) Suppose that R(A, B, C) is a relational schema. Write a relational algebra query that evaluates to the empty set exactly when the functional dependency $B \to C$ holds on R. [4 marks]
- (e) The schema R(A, B, C, D, E) has the following functional dependencies.

$$\begin{array}{l} A \rightarrow B, C \\ C, D \rightarrow E \\ B \rightarrow D \\ E \rightarrow A \end{array}$$

Is D, E a candidate key for R? Explain your answer. [6 marks]