2005 Paper 4 Question 3

Data Structures and Algorithms

- (a) A closed hash table is one in which the overflow chains of key-value pairs are held within the table itself. Carefully describe how the closed hash table mechanism works for both insertion and lookup.
 [6 marks]
- (b) Assume that the initial probe is $p_0 = \text{Hash1}(\text{key}) \mod B$ and the secondary probes are $p_i, i = 1 \dots B 1$. Discuss the relative merits of the following schemes for choosing the secondary probes.
 - $(i) \quad p_i = (p_0 + i) \bmod B$
 - $(ii) p_i = (p_0 + 13 * i) \mod B$
 - $(iii) p_i = (p_0 + 13 * i + 17 * i * i) \mod B$
 - (iv) $p_i = (p_0 + \text{Hash2}(\text{key}) * i + 17 * i * i) \mod B$

You may assume that all the arithmetic is unsigned. [8 marks]

(c) Carefully describe a mechanism for deleting key–value pairs from a closed hash table. [6 marks]