## 2005 Paper 10 Question 3

## Data Structures and Algorithms

(a) Briefly outline how a sequence of symbols can be encoded as a sequence of Huffman codes, and explain under what assumptions Huffman encoding generates optimally compact code.
(b) Estimate the number of bits needed to Huffman encode a random permutation of As, Bs and Cs, with each letter occurring one million times.
(c) Estimate the number of bits needed to Huffman encode a random permutation of As, Bs and Cs, where A occurs two million times and B and C each occur one million times.
(d) Estimate how many bits would be needed to encode the sequence in part (b) above using arithmetic coding. You may assume that $\log _{2} 3$ is about 1.6.
(e) Estimate, with justification, how many bits would be needed to encode the sequence in part ( $c$ ) above using arithmetic coding.

