2004 Paper 9 Question 16

Topics in Concurrency

- (a) Describe the semantics of the modal μ -calculus. [4 marks]
- (b) Describe without proof the meaning of the following modal μ -calculus assertions:

(i)
$$\nu Z. \langle c \rangle Z$$
; [1 mark]

(ii)
$$\mu Z. \langle c \rangle Z$$
; [1 mark]

(iii)
$$\nu Z$$
. $(A \wedge ([c]F \vee \langle c \rangle Z))$ (here F means false); [2 marks]

(iv)
$$\mu Z$$
. $(B \vee (A \wedge \langle c \rangle Z))$; [2 marks]

(v)
$$\nu Z$$
. $(B \vee (A \wedge \langle c \rangle Z))$. [2 marks]

- (c) Consider the transition system consisting of two states p, q and two transitions $p \xrightarrow{c} q$ and $q \xrightarrow{c} p$.
 - (i) Does p satisfy μZ . ($[c]F \lor (\langle c \rangle T \land \langle c \rangle Z)$)?
 - (ii) Does p satisfy νZ . $([c]F \lor (\langle c \rangle T \land \langle c \rangle Z))$?

(Again, here F means false and T means true.) In this part you should justify your answers carefully. [8 marks]