## Databases

- (a) Define the operators of the core relational algebra. [5 marks]
- (b) Let R be a relation with schema  $(A_1, \ldots, A_n, B_1, \ldots, B_m)$  and S be a relation with schema  $(B_1, \ldots, B_m)$ . The quotient of R and S, written  $R \div S$ , is the set of tuples t over attributes  $(A_1, \ldots, A_n)$  such that for every tuple s in S, the tuple ts (i.e. the concatenation of tuples t and s) is a member of R. Define the quotient operator using the operators of the core relational algebra. [8 marks]
- (c) The core relational algebra can be extended with a duplicate elimination operator, and a grouping operator.
  - (*i*) Define carefully these two operators. [3 marks]
  - (*ii*) Assuming the grouping operator, show how the duplicate elimination operator is, in fact, unnecessary. [2 marks]
  - (*iii*) Can the grouping operator be used to define the projection operator? Justify your answer. [2 marks]