## 2003 Paper 9 Question 9

## Database Theory

Assume a database with one relation parent consisting of pairs $(a, b)$ where $a$ is a parent of $b$.
(a) Write a Datalog query which gives the set of pairs $(x, y)$ such that $x$ and $y$ have a common ancestor $z$ and are the same number of generations from $z$.
(b) Write a query in Datalog with stratified negation which gives the set of pairs $(x, y)$ such that $x$ and $y$ have a common ancestor but not one from which they are the same number of generations distant. You may use the program you defined for part (a).
(c) Prove that the query defined in part (b) above cannot be expressed in Datalog without negation.
(d) For each of queries in parts $(a)$ and (b), give a bound on the running time to evaluate the query on a database with $n$ entries.
[4 marks]

