## 2001 Paper 11 Question 2

## Foundations of Programming

A graph consists of nine numbered vertices and 12 edges thus:


By inspection, it is clear that to get from vertex 0 to vertex 8 there are just six routes in which progress is always from a lower-numbered vertex to one with a higher number.

A programmer wishes to write a Java program to count the routes and begins with the following code:

```
public class Routes
    { private static final int[] first = {1,3,4,6,6,7,8,8};
        private static final int[] second = {2,4,5,0,7,0,0,0};
        private static int[] state = {-1,-1, -1,-1,-1,-1,-1,-1,+1};
        public static void main(String[] args)
            { System.out.println("There are " + tryit(0) + " routes");
            }
        private static int tryit(int vertex)
```

Together the first and second arrays form a data structure representing the graph. Explain and critically comment on these arrays.

Ultimately, element $v$ of the array state is intended to show the number of routes from vertex $v$ to vertex 8 . A value of -1 indicates that the number is not yet known. The method tryit (int vertex) returns the value of state[vertex], calculating and saving this value first if necessary. Supply an appropriate body for this method and explain its operation.

