1997 Paper 7 Question 1

Specification and Verification I

The command REPEAT (E) S is executed by repeating S exactly n times, where n (assumed greater than zero) is the value of E in the initial state.

Devise a Floyd-Hoare style proof rule for establishing partial correctness specifications of the form $\{P\}$ REPEAT (E) S $\{Q\}$. [6 marks]

Justify the correctness of your rule informally.

[4 marks]

What verification conditions should REPEAT (E) generate?

[4 marks]

Prove

$$\{Y\geqslant 0\}\ Z:=0;\ \text{REPEAT}\ (Y)\ Z:=Z+X\ \{Z=X\times Y\}$$

[6 marks]