## 1996 Paper 11 Question 4

## Compiler Construction

Describe a structure that could be used to represent the abstract syntax tree of the following  $\lambda$ -expression:

$$(\lambda a.(\lambda f.fa)(\lambda n.n + 1))3$$

Outline the definition of an evaluator function eval(expr, env) that could be used to evaluate a given expression expr represented in this way in the context of an environment given by env. Pay particular attention to the treatment of bound variables and the mechanism you use for function calls. [7 marks]

Is it possible with your implementation to give it a  $\lambda$ -expression which would cause eval to recurse to an unlimited depth? If so, give such a  $\lambda$ -expression; if not, explain why. [3 marks]

Is it possible with your implementation to give it a  $\lambda$ -expression that causes an environment chain of unlimited length to be created during the evaluation? If so, give a  $\lambda$ -expression that would cause this; if not, explain why it is not possible.

[3 marks]

In an erroneous implementation of eval the value of

$$(\lambda x.body)$$

is an object that does not incorporate the contextual environment, and whose call evaluates body in an environment derived from the environment of the call. Explain why such an implementation is wrong, giving an example  $\lambda$ -expression that would yield different results when evaluated by this implementation and yours. [7 marks]