

## 1994 Paper 4 Question 3

### Formal Languages and Automata

Explain what is meant by a *context-free* language. [5 marks]

Show that the union of two context-free languages (over the same alphabet  $\Sigma$ ) is again context-free. [5 marks]

Consider the language  $L$  over the alphabet  $\{a, b, c\}$  consisting of all strings of the form  $a^\ell b^m c^n$ , where  $\ell, m, n > 0$  and either  $\ell = m$  or  $m = n$ . Is  $L$  context-free? Is it a regular language? Justify your answers, stating carefully any well-known results that you use. [10 marks]